

addNode()

This function first checks if the node is in the graph already. Therefore, addNode() has a complexity of $O(n)$.

addEdge()

This function checks if both nodes are in the graph and their locations in the same loop. Therefore, the complexity of addEdge() is $O(n)$.

dijkstra()

dijkstra() performs the following actions:

- Checks if both nodes exist. $O(n)$
- Obtains the source node. $O(n)$
- Loops until queue is empty. $O(n)$
 - Determines which index has the lowest cost. $O(n)$
 - Add or update children. $O(n)$
 - Check if a child is visited. $O(n)$
 - Check if a child is in the queue. $O(n)$
- Construct the output path. $O(n)$

One list stands out as being deep.

- Loops until queue is empty. $O(n)$
 - Determines which index has the lowest cost. $O(n)$
 - Add or update children. $O(n)$
 - Check if a child is visited. $O(n)$
 - Check if a child is in the queue. $O(n)$

As the loop is 3 levels deep, this means dijkstra() has a complexity of $O(n^3)$.

prim()

prim() is also 3 loops deep as it is directly based off of dijkstra(). Therefore, it also has a complexity of $O(n^3)$.