# **Project 3**

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## Find a Way

The main idea is to increase the link on node 1, but not increases the too much on others, and because need to increase both hub and authority, thus an edge link into node 1 and an edge link out from node 1 is necessary.

Ways:

1. Add edge out from node 1 (ex. 1→4)
2. Add edge link to node 1 (ex. 3→1)

Note that the 2 edges add should not be occur on the same node.

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
|  | Before | | | After | | |
|  | Hub | Authority | PageRank | Hub | Authority | PageRank |
| graph\_1.txt | 0.2 | 0 | 0.025 | 0.5 | 0.25 | 0.101 |
| graph\_2.txt | 0.2 | 0.2 | 0.2 | 0.357 | 0.357 | 0.278 |
| graph\_3.txt | 0.191 | 0.191 | 0.173 | 0.322 | 0.262 | 0.224 |

The below shows the graph after process, the graph on the left is the original and the graph on the right is the graph after adding edges:

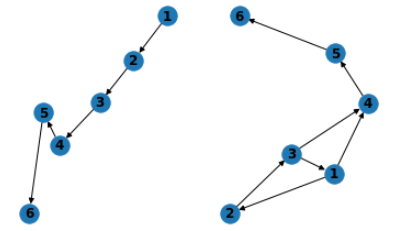


Figure 1：Graph 1 before and after process

一張含有 滑雪, 設備 的圖片

自動產生的描述一張含有 滑雪 的圖片

自動產生的描述

Figure 2: Graph 2 before and after process Figure 3: Graph 3 before and after process

## Algorithm Description

### PageRank

1. Initialize PageRank of each node with , where n is the number of nodes.
2. Update PageRank of each node by the formula , where d is the damping factor, ei,j is an edge that link to vj from vi, PR(vi) is the PageRank of vi, and Outdegree(vi) is the out degree of vi. The damping factor is set to 0.1.
3. Repeat Step 2 until the PageRank converges.

### HITS

1. Initialize authority and hub of each node with 1.
2. For each node,
   1. update authority by the sum of hub of its parents.
   2. update hub the sum of authority of its children.
3. Normalize the authority and hub.
4. Repeat Step 2 and Step 3 until converges.

### SimRank

1. Initialize SimRank as identity matrix. This indicates that .
2. Update the SimRank matrix by formula

where C is the decay factor, set as 0.7, and I(a) represent the parents of a.

1. Repeat Step 2 by 30 iterations.

## Result Analysis and Discussion

### PageRank

PageRank is a way of measuring the importance of a node. To simplify the analysis, only the maximum value and corresponding node will be recorded. The table below shows the results under different damping factor

|  |  |  |  |
| --- | --- | --- | --- |
| Graph | d | maximum value | corresponding node |
| graph\_1.txt | 0.1 | 0.379 | 6 |
| 0.125 | 0.353 | 6 |
| 0.15 | 0.332 | 6 |
| graph\_2.txt | 0.1 | 0.2 | all |
| 0.125 | 0.2 | all |
| 0.15 | 0.2 | all |
| graph\_3.txt | 0.1 | 0.327 | 2,3 |
| 0.125 | 0.326 | 2,3 |
| 0.15 | 0.324 | 2,3 |

Analysis and discussion:

1. According to the result of graph 1, the closer the node to the leaf, the more important the node is.
2. According to the result of graph 2, the PageRank of the nodes in a circle will be equal, which is interpretable.
3. According to the result of graph 3, the more the link of a node, the more important the node is.
4. According to the result of graph 1 and graph 3, with increasing the damping factor, the range of the PageRank will be decreased. Thus, PageRank between nodes will be more balance.

### HITS

HITS is the way to measure the hubs and authorities of a graph. The idea of hubs and authorities can be used to rank the importance of nodes in a graph or network. To simplify the analysis, only the maximum value and the corresponding node will be recorded. The table below shows the results:

|  |  |  |  |
| --- | --- | --- | --- |
| Graph | Hub/Authority | maximum value | corresponding node |
| graph\_1.txt | Hub | 0.2 | all except 6 |
| Authority | 0.2 | all except 1 |
| graph\_1.txt | Hub | 0.2 | all |
| Authority | 0.2 | all |
| graph\_1.txt | Hub | 0.309 | 2,3 |
| Authority | 0.309 | 2,3 |

Analysis and discussion:

1. According to the result of graph 1, the value of hub and authority are respect to the indegree and outdegree of the node. Similar to the result in graph 2 and graph 3

### SimRank

SimRank is a measure of the similarity of two objects in a graph or network. It is based on the idea that two objects are similar if they are related to similar parents in a directed graph. To simplify the analysis, only the maximum value (except 1 as 1 occur during the common nodes pair) and the corresponding nodes pair will be recorded. The table below shows the results under different decay factor:

|  |  |  |  |
| --- | --- | --- | --- |
| Graph | C | maximum value except 1 | corresponding nodes pair |
| graph\_1.txt | 0.7 | 0 | (a,b) where a and b are distinct nodes |
| 0.8 | 0 | (a,b) where a and b are distinct nodes |
| 0.9 | 0 | (a,b) where a and b are distinct nodes |
| graph\_2.txt | 0.7 | 0 | (a,b) where a and b are distinct nodes |
| 0.8 | 0 | (a,b) where a and b are distinct nodes |
| 0.9 | 0 | (a,b) where a and b are distinct nodes |
| graph\_3.txt | 0.7 | 0.538 | (1,3) and (2,4) |
| 0.8 | 0.667 | (1,3) and (2,4) |
| 0.9 | 0.818 | (1,3) and (2,4) |

Analysis and discussion:

1. According to the result of graph 1 and graph 2, there is not similar node pairs exists in these two graphs as every node are unique, there is no exists two nodes with similar parents.
2. According to the result of graph 3, node 1 is similar to node 3 as they have common parent node 2, similar for node 2 and node 4.
3. According to the result of graph 3, by increasing the decay factor, the SimRank of the similar pairs will be increased. It indicates that the decay factor controls the value of the SimRank.

## Effectiveness Analysis