

1) 1.1

y = 3	x = 3	result
3	9	3

result = 27

Algorithm output = 27

1.2 It will be executed 1 time

1.3 The algorithm will calculate x^y

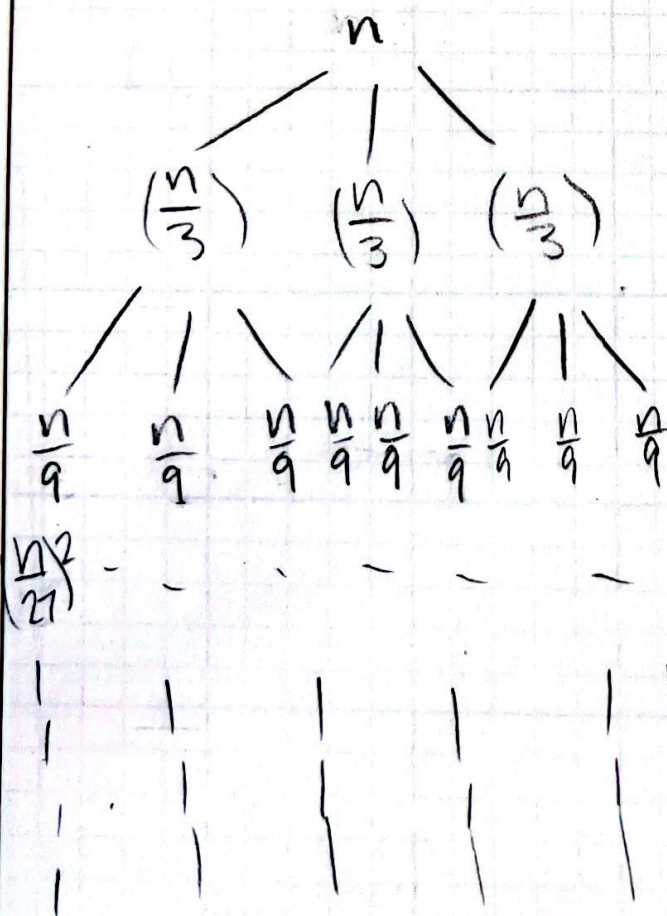
$$2) \quad T(n) = 2(T(n/3)) + n$$

$$T(n) = 2T\left(\frac{n}{3}\right) + n$$

$$T(n) = n^2 + \frac{n^2}{3} + \frac{n^2}{9} + \frac{n^2}{27} + \dots$$

logn times

$$T(n) = O(n)$$



1) Total no. of recursion is 3

2) Input size to each recursive execution is 1

3) $T(n) = n + \frac{n}{3} + \frac{n}{9} + \frac{n}{27} + \dots - \log n \text{ times}$

4) Total work: $\frac{n}{3}$

2.2

$$T(n) = -3$$

3) 3.1)

$$T(n) = 2T\left(\frac{n}{2}\right) + n \log n$$

$$T(n) = aT\left(\frac{n}{b}\right) + f(n)$$

$$a = 2 \quad b = 2$$

$$n^{\log_b a} = n^{\log_2 2} = n^1 = n$$

Case 2

$$\Theta(f(n) \log n) = \underline{\Theta(n \log^2 n)}$$

3.2

Master's Theorem can't be applied because $f(n)$ is less than $n^{\log_b a}$ but by a non-polynomial difference.

4)

5	1	2	7	9	3	7	8	4
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5	1	2	3	9	7	7	8	4
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5	1	2	3	4	7	7	8	9
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4	1	2	3	5	7	7	8	9
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1	2	3	4	5	7	7	8	9
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