Phys 361: Introduction to Array Assignment

Problem 1: Basic calculation with an array.

For the function $y = x^2 - e^{0.5x} + x$, calculate the value of y for the following values of x using an row array for x with the following elements: -3, -2, -1, 0, 1, 2, 3.

```
x = -3:3;

y = x.^2 - exp(1).^(0.5 .* x) + x

y = 1 \times 7

5.7769   1.6321  -0.6065  -1.0000  0.3513  3.2817  7.5183
```

Problem 2: Defining functions.

Exploring Built-in Functions for Arrays and Matrices

Many, dare I say most, built-in functions have no problem working with arrays and matrices. Depending on the function, it might act element-by-element or on the whole array. Below are a few examples. Run the code and replace the "What does.." line with some a short description of what the function does. Try to figure it out without looking at the help.

Declaring and shaping arrays:

What does linspace do?

Linspace creates a row vector starting at the first argument, ending at the second argument, with the number of entries specified by the third argument.

```
array1 = linspace(1,20,200)

array1 = 1×200
1.0000 1.0955 1.1910 1.2864 1.3819 1.4774 1.5729 1.6683 · · ·
```

What does length do?

Length returns the number of entries in an array.

```
length(array1)
ans = 200
```

What does rand do?

rand generates an $m \times n$ matrix of random numbers.

```
randmat=rand(4,6)
randmat = 4 \times 6
    0.8147
               0.6324
                          0.9575
                                    0.9572
                                               0.4218
                                                          0.6557
    0.9058
               0.0975
                          0.9649
                                    0.4854
                                               0.9157
                                                          0.0357
    0.1270
               0.2785
                          0.1576
                                    0.8003
                                               0.7922
                                                          0.8491
    0.9134
               0.5469
                          0.9706
                                    0.1419
                                               0.9595
                                                          0.9340
```

What does size do?

size returns the shape of an $m \times n$ array as a vector of two numbers $[m \ n]$.

size(randmat)

ans =
$$1 \times 2$$
4 6

What does reshape do?

Reshape takes input of an $m \times n$ array and returns a new $a \times b$ array. Reshape will preserve entries wherever possible.

reshape(randmat, 8,3)

```
ans = 8 \times 3
    0.8147
               0.9575
                          0.4218
    0.9058
               0.9649
                          0.9157
                          0.7922
    0.1270
               0.1576
    0.9134
               0.9706
                          0.9595
    0.6324
               0.9572
                          0.6557
    0.0975
               0.4854
                          0.0357
               0.8003
    0.2785
                          0.8491
    0.5469
               0.1419
                          0.9340
```

What does diag do?

diag creates an appropriately sized matrix with entries specified by a vector argument.

diagval=[10:-2:4]

diagval =
$$1 \times 4$$

10 8 6 4

newdiagmat=diag(diagval)

```
newdiagmat = 4 \times 4
                              0
     10
              0
                      0
              8
      0
                      0
                              0
      0
              0
                      6
                              0
      0
              0
                      0
                              4
```

What does zero do?

zeros creates an $m \times n$ array with all 0 entrys.

zeros(3,2)

What does ones do?

ones creates an $m \times n$ array with all 1 entrys.

ones(3,2)

ans =
$$3 \times 2$$

1 1

1 1

1 1

What does eye do?

eye creates an identity matrix of size n.

```
eye(3)

ans = 3x3

1  0  0

0  1  0

0  0  1
```

Basic Statistics:

How does mean work?

mean returns the average of the passed array. Mean defaults to taking the mean of each column and returning a row vector. This seems to disagree with the comments but looking at the output the row vector is 3 entries long and the matrix is a 2 by 3 matrix.

```
newrando=rand(2,3)
                         %Generate a test matrix
newrando = 2 \times 3
   0.6787
             0.7431
                       0.6555
   0.7577
             0.3922
                       0.1712
mean(newrando)
                         %Defualts to taking the mean of row
ans = 1 \times 3
                       0.4133
   0.7182
             0.5677
                         %Mean of rows
mean(newrando,1)
ans = 1 \times 3
   0.7182
                       0.4133
             0.5677
mean(newrando,2)
                         %Mean of columns
ans = 2 \times 1
   0.6924
   0.4404
mean(mean(newrando)) %Doing it twice will give you the mean of all values
```

ans = 0.5664

How does max work? (Note: min is a function that works in a similar way.)

max returns the maximum value of an array and the index of that value.

```
randarray=rand(1,6)'
```

```
randarray = 6×1
0.7060
0.0318
0.2769
0.0462
0.0971
0.8235
```

ans=max(randarray)

```
ans = 0.8235
```

[d,n]=max(randarray) %Optional output format

```
d = 0.8235
n = 6
```

What does sum do?

sum returns the sum of all numbers in an array. If the array is a matrix then sum returns the sum of columns in the matrix.

sum(newrando)

```
ans = 1x3
1.4365 1.1354 0.8267
```

sum(randarray)

ans = 1.9816

What does sort do?

sort sorts the entries of an array. The default behavior is to sort the entries least to greatest.

sort(randarray)

ans = 6×1 0.0318 0.0462 0.0971 0.2769 0.7060 0.8235

What does median do?

median returns the median of a list of numbers.

median(randarray)

ans = 0.1870

What does std do?

std returns the standard deviation of a list of numbers.

std(randarray)

```
ans = 0.3497
```

Advanced: What does det do?

det returns the determinant of a matrix.

```
squaremat=rand(3,3)

squaremat = 3×3
    0.6948    0.0344    0.7655
    0.3171    0.4387    0.7952
    0.9502    0.3816    0.1869

det(squaremat)
```

```
ans = -0.3564
```

Advanced: What do dot and cross do?

dot and cross return the dot and cross product of vectors respectively.

```
a=[1 2 3];
b=[3 4 5];
dot(a,b)
ans = 26
cross(a,b)
```

```
ans = 1 \times 3
-2 4 -2
```

Advanced: What does inv do?

inv returns the inversion of a matrix.

```
inv(squaremat)

ans = 3×3
     0.6213     -0.8015     0.8655
     -1.9539     1.6767     0.8692
     0.8303     0.6521     -0.8247

inv(squaremat)*squaremat

ans = 3×3
```

```
ans = 3×3
1.0000 0.0000 0.0000
0 1.0000 -0.0000
0 0 1.0000
```

Note: There are many more useful functions than than what is included here. A pdf of useful functions can be found on the Canvas webpage.

Optional Advanced Exercises:

Exercise 1: Explore table arrays

Use the Help window or doc table to learn how to use the table command. Look up information on at least 4 elementary particles (name, charge, mass, spin, etc.)

Follow the example in the documentation and make a table containing the information you gathered.

```
% define the properties of four elementary particles as vectors
% electron-neutrino, muon-neutrino, tau-neutrino, sterile-neutrino (hypothetical)
% name = ["\nu_{\text{e}}" "\nu_{\mu}" "\nu_{\text{s}}" "\nu_{\text{s}}"]
name = ["electron-neutrino", "muon-neutrino", "tau-neutrino", "sterile-neutrino"];
% charge in units of the elementary charge e
charge = zeros(1,4);
% mass in units of eV/c^2
% since neutrino mass is not well measured mass is reported as the maximum theoretical
% the sterile neutrino is not well constrained so it will be random, for fun
mass = [1.0, 0.17, 18.2, 1*10.^(rand*15)];
spin = ones(1,4).*(1/2);
% define the variable names
var_names = ["flavour", "charge", "mass", "spin"]

var_names = 1×4 string
```

```
"flavour" "charge" "mass" "spin"

% define the table
neutrino_table = table(name', charge', mass', spin', 'VariableNames', var_names)
```

 $neutrino_table = 4 \times 4 table$

	flavour	charge	mass	spin
1	"electron-neutrino"	0	1	0.5000
2	"muon-neutrino"	0	0.1700	0.5000
3	"tau-neutrino"	0	18.2000	0.5000
4	"sterile-neutrino"	0	3.2910e+08	0.5000

Exercise 2: Explore the cell data type

The cell data type allows you to collect lists of any type of data. For example, you can create a cell of data that contains both numbers and strings. Look up the documentation on cell and cell2table (or watch the short video on Canvas). Define a cell data type for elementary particles, storing the name, mass, charge, and spin for each partile. Next write some code to display the information in a table.

```
% neutrino cell defined such that columns refer to a particular neutrino
neutrino_cell = {
    "electron-neutrino", "muon-neutrino", "tau-neutrino", "sterile-neutrino";
    1, 1, 1;
    1.0, 0.17, 18.2, 1*10.^(rand*15);
    1/2, 1/2, 1/2};
```

cell2table(neutrino_cell, 'RowNames', var_names)

ans = 4×4 table

	neutrino_cell1	neutrino_cell2	neutrino_cell3	neutrino_cell4
1 flavour	"electron-neutrino"	"muon-neutrino"	"tau-neutrino"	"sterile-neutrino"
2 charge	"1"	"1"	"1"	"1"
3 mass	"1"	"0.17"	"18.2"	"13.7345"
4 spin	"0.5"	"0.5"	"0.5"	"0.5"

Exercise 3: Explore the structure data type

The stucture data type is another useful way to store data. Look up the documentation on structures and cell2struct. Define a structure data type for elementary particles, storing the name, mass, charge, and spin for each partile. Demonstrate your structure works as intended with some output.

```
neutrino_struct.name = name'
neutrino struct = struct with fields:
     name: [4×1 string]
   charge: [4×1 double]
     mass: [4×1 double]
     spin: [4×1 double]
neutrino_struct.charge = charge'
neutrino_struct = struct with fields:
     name: [4×1 string]
   charge: [4×1 double]
     mass: [4×1 double]
     spin: [4×1 double]
neutrino_struct.mass = mass'
neutrino_struct = struct with fields:
     name: [4×1 string]
   charge: [4×1 double]
     mass: [4×1 double]
     spin: [4×1 double]
neutrino_struct.spin = spin'
neutrino struct = struct with fields:
     name: [4×1 string]
   charge: [4×1 double]
     mass: [4×1 double]
     spin: [4×1 double]
struct2table(neutrino_struct)
```

$ans = 4 \times 4 table$

	name	charge	mass	spin
1	"electron-neutrino"	0	1	0.5000
2	"muon-neutrino"	0	0.1700	0.5000

	name	charge	mass	spin
3	"tau-neutrino"	0	18.2000	0.5000
4	"sterile-neutrino"	0	3.2910e+08	0.5000