- 1.4: Does it ever make sense to say that one object is "twice as hot" as another? Does it matter whether one is referring to Celsius or kelvin temperatures? Explain.
 - It does not make sense to say that one object is "twice as hot" as another in the Celsius or Fahrenheit scale. These temperature scales are non-linear, though when talking about positive temperatures in these scales one could say "twice as hot" and still get their point across. Only in the linear scale, kelvin, does this statement make sense for all temperatures.
- 1.7: When the temperature of liquid mercury increases by one degree Celsius (or one kelvin), its volume increases by one part in 5500. The fractional increase in volume per unit change in temperature (when the pressure is held fixed) is called the thermal expansion coefficient, β ,

$$\beta \equiv \frac{\Delta V/V}{\Delta T},$$

where V is the volume and T is the temperature of the substance in question. For mercury, $\beta = 1/5500 \, \mathrm{K}^{-1}$.

- (a.) Get a mercury thermometer, estimate the size of the bulb at the bottom, and then estimate what the inside diameter of the tube has to be in order for the thermometer to work as required. Assume that the thermal expansion of the glass is negligible.
- (b.) The thermal expansion coefficient of water varies significantly with temperature. It is $7.5 \times 10^{-4} \,\mathrm{K^{-1}}$ at $100\,^{\circ}\mathrm{C}$, but decreases as the temperature is lowered until it becomes 0 at $4\,^{\circ}\mathrm{C}$. Below $4\,^{\circ}\mathrm{C}$ it is slightly negative, reaching a value of $-0.68 \times 10^{-4} \,\mathrm{K^{-1}}$ at $0\,^{\circ}\mathrm{C}$. This behavior is related to the fact that ise is les dense than water. With this behavior in mind, imagine the process of a lake freezing over, and discuss in some detail how this process would be different if the thermal expansion coefficient of water were always positive.

1.9: What is the volume of one mole of air, at room temperature and 1 atm pressure?

The volume of air, which we shall assume is an ideal gas, is given by the ideal gas

$$V = \frac{nRT}{P}.$$

From the problem statement, $n=1\,\text{mol}$, $T=293\,\text{K}$, $R=8.31\,\text{J}\,\text{mol}^{-1}\,\text{K}^{-1}$, and $P=1.013\times 10^5\,\text{Pa}$. Then,

$$V = \frac{1 \,\text{mol} \times 293 \,\text{K} \times 8.31 \,\text{J} \,\text{mol}^{-1} \,\text{K}^{-1}}{1.013 \times 10^5 \,\text{Pa}} = 0.0240 \,\text{m}^3.$$

1.10: Estimate the number of air molecules in an average-sized room.

law to be

Suppose the average sized room is a cube with side lengths 5 meters. We then take standard temperature and pressure: $T = 293 \,\mathrm{K}$, and $P = 1.013 \times 10^5 \,\mathrm{Pa}$. The number of molecules in an ideal gas is given by

$$N = \frac{PV}{kT},$$

where $V = 125 \,\mathrm{m}^3$, and $k = 1.381 \times 10^{-23} \,\mathrm{J \, K^{-1}}$. Then

$$N = \frac{1.013 \times 10^5 \,\mathrm{Pa} \times 125 \,\mathrm{m}^3}{1.381 \times 10^{-23} \,\mathrm{J \, K}^{-1} 293 \,\mathrm{K}} = 3.13 \times 10^{27}$$

1.11: Rooms A and B are the same size and are connected by an open door. Room A, however, is warmer. Which room contains the greater mass of air? Explain carefully.

Rooms A and B have the same mass of air. If we consider the rooms before room A was heated, perhaps that morning before sunrise, then they are in equilibrium and thus have the same mass of air. Then, the sun rose. Room A is heated and yet it's volume remains unchanged. Thus, the pressure rises in room A. Room A may exchange a higher energy gas particle with room B as the two come back into thermal equilibrium. However, in doing so, room A will be at a lower pressure and thus room B will be more likely to "send over" a gas particle. Thus the two rooms will maintain an equilibrium in molecule count.

1.17: Even at low density, real gases don't quite obey the ideal gas law. A systematic way to account for deviations from ideal behavior is the virial expansion,

$$PV = nRT \left(1 + \frac{B(T)}{V/n} + \frac{C(T)}{(V/n)^2} + \cdots \right),$$

where the functions B(T), C(T), and so on are called the virial coefficients. When the density of the gas is fairly low, so that the volume per mole is large, each term in the series is much smaller than the one before. In many situations it's sufficient to omit the third term and concentrate on the second, whose coefficient B(T) is called the second virial coefficient. Here are some measured values of the second virial coefficient for nitrogen N_2 :

T [K]	$B \left[\text{cm}^3 \text{mol}^{-1} \right]$
100	-160
200	-35
300	-4.2
400	9.0
500	16.9
600	21.3

(a.) For each temperature in the table, compute the second term in the virial equation, B(T)/(V/n), for nitrogen at atmospheric pressure. Discuss the validity of the ideal gas law under these conditions.

For nitrogen at atmospheric pressure, the volume of gas is given by

$$V = \frac{nRT}{P},$$

where R is a universal gas constant, T is given, $P = 1.013 \times 10^5$ Pa, and the n term, being present in both numerator and denominator, divides out in the calculation of C from B.

T [K]	B/(V/n)
100	-19504
200	-2133
300	-170
400	274
500	412
600	434

(b.) Think about the forces between molecules, and explain why we might expect B(T) to be negative at low temperatures but positive at high temperatures.

1.18: Calculate the rms speed of a nitrogen molecule at room temperature.

The rms speed of a nitrogen gas molecule, (N_2) , at some temperature is given by

$$v_{\rm rms} = \sqrt{\frac{3kT}{m}},$$

where $m = 4.65 \times 10^{-26} \,\text{kg}$. Then,

$$v_{\rm rms} = \sqrt{\frac{3 \times 1.381 \times 10^{-23} \,\mathrm{J \, K^{-1}} \times 293 \,\mathrm{K}}{4.65 \times 10^{-26} \,\mathrm{kg}}} = 511 \,\mathrm{m \, s^{-1}}.$$

1.19: Suppose you have a gas containing hydrogen molecules and oxygen molecules in thermal equilibrium. Which molecules are moving faster, on average? By what factor?

The ratio of rms velocities between the oxygen molecules, (O_2) , and hydrogen molecules, (H_2) , is given by

$$v_{\rm rms,O_2}^2 m_{\rm O_2} = v_{\rm rms,H_2}^2 m_{\rm H_2} \Rightarrow \frac{v_{\rm rms,O_2}}{v_{\rm rms,H_2}} = \sqrt{\frac{m_{\rm H_2}}{m_{\rm O_2}}}.$$

Substituting the masses of both molecules we find

$$\frac{v_{\rm rms,O_2}}{v_{\rm rms,H_2}} = 1.022 \times 10^{-14}.$$

That is, the oxygen molecules are moving, on average, many orders of magnitude slower than the hydrogen molecules.

1.23: Calculate the total thermal energy in a liter of helium at room temperature and atmospheric pressure. Then repeat the calculation for a liter of air.

The total thermal energy of an ideal gas is given by

$$U = Nf\frac{1}{2}kT,$$

where NkT can be found via the ideal gas law as

$$NkT = PV$$
.

One liter is equivalent to $1 \times 10^{-3} \,\mathrm{m}^3$, which is V. A helium molecule, (H₂), is a diatomic molecule and thus has 3 translational degrees of freedom and two rotational: f = 5. Thus, the total thermal energy stored in this system is given by

$$U = \frac{PVf}{2} = \frac{1.013 \times 10^5 \, \mathrm{Pa} \times 1 \times 10^{-3} \, \mathrm{m}^3 \times 5}{2} = 253.25 \, \mathrm{J}.$$