- 1. Let Y be the set of all living people, and let the binary relation be "is married to" (assuming monogamy throughout society).
 - (a) Identify the meaning of cases (1) through (4) as found in slide 5/14.
 - Case (1). (xRy, yRx). x is married to y and y is married to x.
 - Case (2). (xRy, not yRx). x is married to y and y is not married to x.
 - Case (3). (not xRy, yRx). x is not married to y and y is married to x.
 - Case (4). (not xRy, not yRx). x is not married to y and y is not married to x.
 - (b) For each property p1 through p9, as found in slide 6/14, state whether or not the property is satisfied and why.
 - p1. Reflexive. x is married to x. This is not satisfied; society does not recognize marriage to the self.
 - p2. Irreflexive. x is not married to x. This is satisfied; society does not recognize marriage to the self.
 - p3. Symmetric. If x is married to y then y is married to x. This is satisfied; two people are mutually in marriage to one another.
 - p4. Asymmetric. If x is married to y then y is not married to x. This is not satisfied; two people are mutually in marriage to one another as a pair.
 - p5. Antisymmetric. If x is married to y and y is married to x then x is y. This is not satisfied; a marriage exists between two unique people.
 - p6. Transitive. If x is married to y and z is married to x then x is married to z. This is not satisfied; a person cannot be married to two people so person x cannot be married to both y and z by assumption of monogamy.
 - p7. Negatively transitive. If x is not married to y and y is not married to z then x is not married to z. This is not satisfied; if x were married to z it could still be said that x is not married to y and y is not married to z.
 - p8. Connected. x is married to y and y is married to x for all people x and y. This is not satisfied; there are people who are not married.
 - p9. Weakly connected. If x and y are different people then x is married to y or y is married to x. This is not satisfied; there are people who are not married.

2. Show that asymmetry (p4) and negative transitivity (p7) imply transitivity (p6).

the properties asymmetry and negative transitivity.

Proof. Let Y be some set and R be some binary operation on Y. Suppose R has