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Thermodynamic limits of hydrologic cycling within the Earth system: concepts, estimates and implications

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iscussion Paper

Discussion Pape

Discussion Paper

Discussion Paper

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

|d | ►|

•

Back Close

Full Screen / Esc

Printer-friendly Version



The hydrologic cycle results from the combination of energy conversions and atmospheric transport, and the laws of thermodynamics set limits to both. Here, we apply thermodynamics to derive the limits of the strength of hydrologic cycling within the Earth system and the properties and processes that shape these limits. We set up simple models to derive analytical expressions of the limits of evaporation and precipitation in relation to vertical and horizontal differences in solar radiative forcing. These limits result from a fundamental trade-off by which a greater evaporation rate reduces the temperature gradient and thus the driver for atmospheric motion that exchanges moistened air from the surface with the drier air aloft. The limits on hydrologic cycling thus reflect the strong interaction between the hydrologic flux, motion, and the driving gradient. Despite the simplicity of the models, they yield estimates for the limits of hydrologic cycling that are within the observed magnitude, suggesting that the global hydrologic cycle operates near its maximum strength. We close with a discussion of how thermodynamic limits can provide a better characterization of the interaction of vegetation and human activity with hydrologic cycling.

1 Introduction

The global hydrologic cycle plays a critical role in the Earth system (Chahine, 1992). The phase transitions of water between its liquid to gaseous form involve substantial amounts of energy, so that the fluxes of evaporation and precipitation strongly affect heating and cooling rates at the surface and within the atmosphere. These differences in heating and cooling form the basic drivers from which atmospheric motion is generated. Atmospheric motion, in turn, plays a vital role in transporting moisture from the places at which water evaporates to where it condenses. Hence, the hydrologic cycle shapes energy balances and interacts strongly with atmospheric motion and transport.

HESSD

Discussion Paper

Discussion Paper

Discussion

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables

. .

Figures

< 4

•

Back

Full Screen / Esc

Printer-friendly Version



Figures

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



In this study we ask about the fundamental factors that limit the strength of hydrologic cycling within the Earth system. To establish such limits, we combine thermodynamics with a holistic view of how hydrologic cycling takes place within the Earth system. Thermodynamics describes general rules for the constraints, directions, and limits as-5 sociated with energy conversions. A general result of thermodynamics is the Carnot limit, which describes the maximum rate by which a heating difference can be converted into mechanical work. This mechanical work is needed to maintain atmospheric motion, and motion is needed to maintain the ability to transport moisture. Several studies indicate that the atmospheric circulation operates near its thermodynamic limit (Paltridge, 1975, 1978; Lorenz et al., 2001; Kleidon et al., 2003, 2006), so that we can infer the strength of the associated heat and moisture transport by atmospheric motion from the assumption of maximum thermodynamic efficiency. The limit of hydrologic cycling that we explore here results from the general trade-off by which stronger hydrologic cycling involves more energy associated with phase transitions, so that less energy is available to drive atmospheric transport. By doing so, we do not need to look at the thermodynamics of atmospheric processes involved in hydrologic cycling in detail, as done by several previous studies on the thermodynamics of hydrologic cycling (Renno and Ingersoll, 1996; Pauluis and Held, 2002a,b; Konings et al., 2012). We rather start with the assumption of the Carnot limit in the context of the Earth system and estimate the maximum strength of the hydrologic cycle as a result of the trade-off between energy being used for phase transitions and for the generation of atmospheric transport.

To explore the interplay between phase transitions and moisture transport in more detail, we consider a thought experiment in which we vary the magnitude of evaporation and consider its consequences in the context of the processes shown in Fig. 1. In this thought experiment, the surface is heated by absorption of solar radiation, terrestrial radiation is exchanged between the surface and the atmosphere, and the atmosphere cools by the emission of terrestrial radiation into space. The evaporation of water removes latent heat from the surface (arrow "A"), and this heat is released within the

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

HESSD

A. Kleidon and M. Renner

Abstract

References

Title Page

Back

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I ◀ ▶I

Back Close
Full Screen / Esc

Printer-friendly Version

Interactive Discussion



atmosphere when it condenses. From the differential heating between the surface and the atmosphere, atmospheric motion is generated and transports sensible as well as latent heat (arrow "B") from the heated surface to the cooler atmosphere.

When we now consider a case in which more water is evaporated at the surface (i.e. 5 we strengthen arrow "A"), this would in steady state be accompanied by a greater rate of precipitation, which at first sight would seem to imply a greater strength of hydrologic cycling. This greater strength, however, is associated with more evaporative cooling at the surface and more condensational heating in the atmosphere, so that the heating difference between the surface and the atmosphere would be reduced. Since motion is generated out of heating differences, this reduced heating difference should result in less motion and a lower ability to transport moisture (i.e. a weaker arrow "B") from the locations at which water evaporates to the locations at which it condenses. This transport is essential to maintain hydrologic cycling, as it is through atmospheric transport that the moistened air near the surface is replaced by drier air from above, and the condensed moisture that is removed by precipitation from the atmosphere is replaced by the moistened air from the surface. Hence, the increased transport of latent heat with a stronger hydrologic cycle and the reduced ability to transport due to the reduced heating difference should result in a trade-off that sets an upper limit on the strength of the hydrologic cycle. The limit to transport is then determined by thermodynamics, specifically the Carnot limit. The combination of this limit with the energy and transport requirements for hydrologic cycling then yields the maximum possible strength of hydrologic cycling within the Earth system.

The goal of this paper is to establish this maximum strength of hydrologic cycling from the thermodynamic constraints by which motion, and hence moisture transport, can be generated within the Earth system from its external forcing. We derive this limit from very simple energy balance models similar to those that were used to explore a related, proposed thermodynamic principle of Maximum Entropy Production (Lorenz et al., 2001; Kleidon, 2004), although we do not invoke this principle here. By using

observations, we can then show that the current hydrologic cycle appears to operate near this limit.

In the following section, we first provide a brief introduction to thermodynamics, thermodynamic limits, and describe an overview of how we apply thermodynamics to the combined roles of energy balances and atmospheric transport for hydrologic fluxes. In Sect. 3, we set up two simple models to derive analytic expressions for the maximum strength of hydrologic cycling that are related to vertical convection and large-scale horizontal atmospheric transport. We identify the main sensitivities of these limits, derive global estimates, and compare these to observations. Our estimates are certainly strong simplifications and only consider first-order effects, so that we discuss the limitations of our models and the estimates, and compare our approach to previous work in Sect. 5. We then describe how this approach can provide a framework to better understand and characterize the effects of vegetation activity and human alterations on hydrologic cycling. We close with a brief summary and conclusion.

2 Thermodynamics of hydrologic cycling within the Earth system

The derivation of the maximum strength of hydrologic cycling requires some background on the relevant constraints on the processes that are shown in Fig. 1, particularly by the conservation of energy, and how thermodynamics sets limits to these processes. In the following, we first briefly describe the laws of thermodynamics and how thermodynamic limits emerge from these laws. We describe how heating gradients are generated within the Earth system from the solar radiative forcing that can be used to derive work, how this work is used to generate atmospheric motion, and how motion results in the transport of sensible heat. We then describe how hydrologic cycling is embedded in these processes. The application of thermodynamic limits to this description is then performed in the following section. A summary of the variables used in the formulations is shown in Table 1.

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

→

Back Close

Full Screen / Esc

Printer-friendly Version



Thermodynamics is a physical theory that describes the rules for energy conversions. For a complete accounting of these energy conversions, we consider a system with a well-defined boundary through which heat, mass and other physical properties are exchanged. The thermodynamic state of the system is characterized at least by its internal energy, U, and its entropy, S, which measures the dispersal of energy within the system.

The first law of thermodynamics describes that the change in internal energy of the system equals the net addition or removal of heat by exchange with the surroundings, and the net work done by (or on) the system. If we express these changes through time, the first law is expressed as:

$$\frac{\mathrm{d}U}{\mathrm{d}t} = J_{\mathrm{net}} - G + D \tag{1}$$

where J_{net} is the net heat flux through the system boundary, G = dW/dt is the rate by which work is done by the system on its surroundings (or the physical power) to generate other forms of energy (e.g. potential or kinetic energy), and D is the dissipative heating that results from the conversions of other forms of energy back into heat within the system, for instance by friction.

The second law of thermodynamics requires that during energy conversions, energy is increasingly dispersed. This requirement is accounted for by the entropy budget of the system, which balances the changes in entropy of the system with the entropy produced by processes within the system, σ , with the entropy that is exchanged when energy (or mass) is exchanged with the surroundings, $J_{s,net}$:

$$\frac{\mathrm{d}S}{\mathrm{d}t} = \sigma - J_{\mathrm{s,net}} \tag{2}$$

The second law requires that $\sigma \ge 0$.

Discussion Paper

Discussion Pape

Discussion Paper

Printer-friendly Version

Interactive Discussion



HESSD 10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

References

Figures

Back

Full Screen / Esc

Figures

Back

Full Screen / Esc

Interactive Discussion



A system is in a steady state when its internal energy as well as its entropy do not change in the mean, that is, dU/dt = 0 and dS/dt = 0. It is in a state of thermodynamic equilibrium when the entropy of the system has reached its maximum value. In this state, $\sigma = J_{s, net} = 0$. A state of disequilibrium can be maintained if the system maintains 5 a net exchange of entropy, $J_{s,net} \ge 0$, which allows for entropy production within the system. Such a disequilibrium is maintained by entropy exchange. The most relevant form of entropy exchange in this study is the exchange of heat that takes place at different temperatures. When heat is added to a hot reservoir with a temperature T_h at a rate $J_{\rm in}$, the entropy of the system increases by $J_{\rm in}/T_{\rm h}$. When a cold reservoir with a temperature T_c within the same system is cooled at a rate J_{out} , the entropy of the system decreases by $J_{\rm out}/T_{\rm c}$. The net entropy exchange by the system then is $J_{\rm s, net} = J_{\rm out}/T_{\rm c} - J_{\rm in}/T_{\rm h}$, which is greater than zero even if $J_{\rm in} = J_{\rm out}$ and the system does not gain or lose energy. Hence, entropy exchange with the surroundings is essential to maintain a state of thermodynamic disequilibrium and dissipative activity, such as motion or hydrologic cycling, within the system.

Work can be performed by the system from this net entropy exchange to generate, for instance, kinetic energy. When work is performed through time, it is described by the physical term power. The maximum rate at which work can be performed is known as the Carnot limit, which follows directly from the combination of the first and second law. If we consider a system with heat exchange fluxes J_{in} and J_{out} and that performs work at a rate G, then the first law states $J_{in} = J_{out} + G$. When J_{in} is added at a temperature $T_{\rm h}$ and $J_{\rm out}$ is removed at a temperature $T_{\rm c}$, then the second law requires that $J_{\rm s,net}$ = $J_{\rm in}/T_{\rm h} - J_{\rm out}/T_{\rm c} \ge 0$. The Carnot limit follows from the best case where the entropy exchange is zero, $J_{s,net} = 0$, yielding the expression:

$$G_{\text{max}} = J_{\text{in}} \cdot \frac{T_{\text{h}} - T_{\text{c}}}{T_{\text{h}}}$$
 (3)

In the case of the atmosphere, this work is performed within the system, so that in steady state the work performed equals the free energy dissipated, $G_{max} = D$. If this

10, 3187–3236, 2013

HESSD

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Introduction **Abstract**

References

Printer-friendly Version

dissipation occurs at the temperature of the cold reservoir, this results in entropy production within the system, which is given by $\sigma = D/T_{\rm c} = G_{\rm max}/T_{\rm c} = J_{\rm in}(T_{\rm h}-T_{\rm c})/(T_{\rm h}T_{\rm c}) = J_{\rm s,net}$. Note that the Carnot limit does not require any particular knowledge about the mechanisms and steps by which this work is actually being derived from the heating gradient.

2.2 Energy and entropy balances of the Earth system

Heating gradients in the Earth system are generated from differential absorption of solar radiation. We consider the two dominant gradients that are formed from solar radiation, which are shown schematically in Fig. 2. Solar radiation is predominantly absorbed at the surface, which results in a vertical heating gradient between the surface and the atmosphere (Fig. 2a). Since more solar radiation is absorbed in the tropics than at the poles due to the orientation of surfaces towards the incoming radiation, a large-scale horizontal gradient is formed between the tropics and the poles (Fig. 2b). These heating gradients are described by the respective energy balances, which we formulate in the following, based on the simple models of Kleidon (2004). These balances are considered in simplified form and in a steady state for simplicity, and set the basis for the following derivation of thermodynamic limits to hydrologic cycling.

2.2.1 Vertical heating gradient

Solar radiation is mostly absorbed at the surface, resulting in surface heating, while this heat is emitted mostly from the atmosphere in form of terrestrial radiation. This forms a vertical gradient in heating between the surface and the atmosphere (Fig. 2a) which forms the driving gradient for convective motion and local, vertical transport of moisture.

The difference in heating and cooling between the surface and the atmosphere is described by the energy balances of the surface and the atmosphere respectively. The following variables use the indices "s" and "a" to refer to the surface and atmosphere.

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables

▶I

Figures

- 4

Back

Class

Full Screen / Esc

Printer-friendly Version



$$0 = J_{\text{in.s}} - J_{\text{s.a}} - J_{\text{c}} \tag{4}$$

The energy balance for the atmosphere consists of the cooling by the emission of radiation into space, $J_{\text{out,a}}$, the heating due to radiative exchange with the surface, $J_{\text{s,a}}$, and the convective heat flux, J_{c} :

$$0 = -J_{\text{out.a}} + J_{\text{s.a}} + J_{\text{c}} \tag{5}$$

Taken together, these energy balances yield the global radiative energy balance of the system:

$$0 = J_{\text{in,s}} - J_{\text{out,a}} \tag{6}$$

The entropy balance of the system in steady state is composed of the import of heat $J_{\text{in,s}}$ by absorption of solar radiation at the temperature T_{s} of the surface, the export of $J_{\text{out,a}} = J_{\text{in,s}}$ by emission of terrestrial radiation from the atmosphere to space at a temperature T_{a} , and the total production of entropy σ_{c} within the system:

$$0 = \sigma_{\rm c} + \frac{J_{\rm in,s}}{T_{\rm s}} - \frac{J_{\rm out,a}}{T_{\rm a}} \tag{7}$$

Hence, the total entropy production is given by

$$\sigma_{\rm c} = J_{\rm in,s} \cdot \left(\frac{1}{T_{\rm a}} - \frac{1}{T_{\rm s}}\right) \tag{8}$$

This entropy production consists of entropy production by radiative exchange, $\sigma_{\rm s,a}$, by the sensible heat flux, $\sigma_{\rm sh}$, and by irreversible processes associated with hydrologic cycling, $\sigma_{\rm lh}$, so that

$$\sigma_{\rm c} = \sigma_{\rm s,a} + \sigma_{\rm sh} + \sigma_{\rm lh} \tag{9}$$

as is detailed further below.

iscussion Pa

10

10, 3187-3236, 2013

Thermodynamic limits of hydrologic cycling

HESSD

A. Kleidon and M. Renner

Title Page

Discus

H





Abstract



Introduction

References

Figures

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



The large-scale temperature gradient in the horizontal is described by the energy balances of the tropical and extratropical (or polar) regions. The indices "t" and "p" in the following variables refer to the tropical and polar regions. The energy balance of the tropical regions is described by the absorption of solar radiation, $J_{\text{in,t}}$, the emission of terrestrial radiation into space, $J_{\text{out,t}}$, and the large-scale transport of sensible and latent heat from the tropics to the polar regions, J_{is} :

$$0 = J_{\text{in,t}} - J_{\text{out,t}} - J_{\text{ls}} \tag{10}$$

The energy balance of the polar regions is described equivalently by absorption of solar radiation, $J_{\text{in,p}}$ (with $J_{\text{in,p}} < J_{\text{in,t}}$), the emission of terrestrial radiation, $J_{\text{out,p}}$, and the heating by the heat transport from the tropical regions, J_{is} :

$$0 = J_{\text{in,p}} - J_{\text{out,p}} + J_{|s}$$
 (11)

Taken together, both energy balances yield the global radiative energy balance:

$$0 = J_{in,t} + J_{in,p} - J_{out,t} - J_{out,p}$$
 (12)

The entropy balance of the system is composed of the import of heat when solar radiation, $J_{\text{in,t}}$ and $J_{\text{in,p}}$, is absorbed at the respective temperatures, the export of heat when it is emitted as terrestrial radiation, $J_{\text{out,t}}$ and $J_{\text{out,p}}$, and the entropy production within the system, σ_{is} :

$$0 = \sigma_{ls} + \frac{J_{in,t} - J_{out,t}}{T_t} + \frac{J_{in,p} - J_{out,p}}{T_p}$$
 (13)

iscussion D

Discussio

Discussi

Discussion I

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Abstract

Title Page

Conclusions References

Tables Figures

I∢

■ •

Back Close

Full Screen / Esc

Printer-friendly Version



$$\sigma_{\rm ls} = J_{\rm ls} \cdot \left(\frac{1}{T_{\rm p}} - \frac{1}{T_{\rm t}}\right) \tag{14}$$

using Eqs. (10) and (11). As above (Eq. 8), the entropy production consists of frictional dissipation of large-scale motion and hydrologic processes:

with the contributions, $\sigma_{\rm sh}$ and $\sigma_{\rm lh}$, described further below.

Atmospheric motion

Mechanical power is derived from the two heating gradients formulated above. This power results in atmospheric motion and is associated with the formation of a momentum gradient. This power results from a buoyancy force that is generated from radiative heating of air, which lowers its density, but as we will see in the following, we do not need to consider a specific form of this buoyancy force. We describe the generation of motion in general, using the temperature T_h to refer to the heated region (surface or tropics) and T_c for the temperature of the cooled region (atmosphere or extratropics). For the two heating gradients discussed above, $T_h = T_s$ and $T_c = T_a$ for the vertical heating gradient, and $T_h = T_t$ and $T_c = T_p$ for the large-scale horizontal gradient.

The momentum associated with atmospheric motion reflects the balance of momentum generation by buoyancy, F_h , and dissipation by friction, F_f . This is expressed by the momentum balance for motion of air with a velocity v:

$$0 = F_b - F_f = F_b - C_d \rho v^2$$
 (16)

where C_d is a drag coefficient that characterizes the strength of friction, which is typically turbulent. When Eq. (16) is multiplied by the velocity, we obtain the balance equation for the kinetic energy associated with motion:

$$0 = G - D = G - C_{d}\rho v^{3}$$
 (17)

Back

Printer-friendly Version

Interactive Discussion



10, 3187–3236, 2013

Title Page

Abstract Introduction References

Figures

HESSD

Thermodynamic

limits of hydrologic

cycling

A. Kleidon and M. Renner

Full Screen / Esc

$$V = \left(\frac{G_{\text{max}}}{C_{\text{d}}\rho}\right)^{1/3} \tag{18}$$

The exchange velocity, in turn, describes the transport of sensible heat, J_{sh} , between the heated reservoir with temperature T_h and the cooled reservoir with temperature T_c :

$$J_{\rm sh} = c_p \rho v (T_{\rm h} - T_{\rm c}) \tag{19}$$

where c_{ρ} is the specific heat capacity of air, and ρ is the air density.

The motion that is generated from the heating gradient and the associated heat flux follow the direction imposed by the second law. This heat flux is directed to transport heat from the warm reservoir to the cold reservoir. The extent by which this increases the entropy within the system is characterized by the rate at which entropy is being produced by atmospheric motion, $\sigma_{\rm sh}$:

$$\sigma_{\rm sh} = J_{\rm sh} \cdot \left(\frac{1}{T_{\rm c}} - \frac{1}{T_{\rm h}}\right) = \frac{G_{\rm max}}{T_{\rm c}} \tag{20}$$

since power equals frictional dissipation, G = D, in steady state. Hence, atmospheric motion at the maximum power limit is approximately equivalent with producing entropy at the maximum possible rate (with an equivalence given if the kinetic energy is entirely dissipated at the cold temperature, T_c).

HESSD

10, 3187-3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

onclusions References

Tables Figures

l∢ ⊳l

Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Hydrologic cycling involves the phase transitions from liquid to gaseous during evaporation and the reverse during condensation. A state of maximum entropy and thermodynamic equilibrium is reached for an open water surface when the overlying air reaches saturation. The distance to thermodynamic equilibrium can thus be characterized by the relative humidity, r, of the air. To maintain evaporation, condensation, and precipitation in steady state, and thus hydrologic cycling, air needs to be continuously dehumidified by the atmosphere (Pauluis and Held 2002a, b). This is mostly achieved by lifting of vapor by vertical motion.

We consider the formulation of hydrologic cycling in a general way, with cycling of moisture from a heated reservoir which evaporates at a temperature $T_{\rm h}$ to a cooled reservoir at which moisture condenses at a temperature $T_{\rm c}$ (as above, with the application to the two gradients given by $T_{\rm h} = T_{\rm s}$ and $T_{\rm c} = T_{\rm a}$ for the vertical heating gradient and $T_{\rm h} = T_{\rm t}$ and $T_{\rm c} = T_{\rm p}$ for the large-scale horizontal gradient). The water cycle is assumed to operate in a steady state within the system, in which evaporation E balances precipitation E so that the total amount of water vapor within the atmosphere does not change:

$$0 = E - P \tag{21}$$

The evaporative flux from the surface balances the overall moisture transport between the two reservoirs, which transports the moistened air from the heated reservoir with a specific humidity of $q_{\rm h}$ and replaces it with the drier air from the cooled reservoir with a specific humidity of $q_{\rm c}$. Hence, the latent heat flux, $J_{\rm lh}$, can be written as:

$$J_{\rm lh} = \lambda E = \lambda \rho v (q_{\rm h} - q_{\rm c}) \tag{22}$$

If we further assume that air had sufficient time to reach saturation when water evaporates from the heated reservoir (or when it condenses at the cooled reservoir), we

HESSD

10, 3187-3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

I₫

Figures

▼ ...

Back Close

Full Screen / Esc

Printer-friendly Version



can approximate $q_h \approx q_{sat}(T_h)$ and $q_c \approx q_{sat}(T_c)$. With the linearization of the saturation vapor pressure (see Appendix), we obtain for the latent heat flux:

$$J_{\rm lh} = c_p \rho v \frac{s}{v} (T_{\rm h} - T_{\rm c}) \tag{23}$$

where $\gamma = c_p p/(0.622\lambda) \approx 65 \, \text{Pa}$ is the psychrometric constant, and s is the slope of the saturation vapor pressure curve, as described by Eq. (A5).

The process of converting heat during evaporation at the heated reservoir and condensation at the cooled reservoir results in entropy production, σ_{lh} , associated with hydrologic cycling:

$$\sigma_{\rm lh} = J_{\rm lh} \cdot \left(\frac{1}{T_{\rm c}} - \frac{1}{T_{\rm h}}\right) \tag{24}$$

This entropy production captures several processes related to hydrologic cycling. It includes additional generation of atmospheric motion (and subsequent frictional dissipation) due to the greater buoyancy of moistened air compared to dry air and due to the release of latent heat at an atmospheric temperature that is typically above the radiative temperature of the atmosphere (both of these effects are not explicitly considered here further for sake of simplicity). In addition, this entropy production includes the work done in lifting water from the surface to the level at which it precipitates, which then results in frictional dissipation of falling raindrops (Pauluis et al., 2000), and it includes diffusive losses of water vapor (Goody, 2000).

In the case of vertical convection, the entropy production, σ_{lh} , would in the ideal case be associated entirely with work that converts energy into additional kinetic energy (thus contribute a term G_{lh} to the G in Eq. (17), with the total power then being related to generate moist convection), and into the work G_{lift} that is associated with the lifting of water to the height at which it precipitates. The entropy would then be produced when the generated additional kinetic energy and potential energy is dissipated. We would

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

l∢ ≽l

→

Back Close

Full Screen / Esc

Printer-friendly Version



$$G_{\rm lh} + G_{\rm lift} = J_{\rm lh} \frac{T_{\rm h} - T_{\rm c}}{T_{\rm h}} = D_{\rm lh} = \sigma_{\rm lh} T_{\rm c}$$

$$(25)$$

The power that is associated with lifting water at a rate E over a height difference Δz at which it precipitates is given by

$$_{5} G_{\text{lift}} = Eg\Delta z \tag{26}$$

where q is the gravitational acceleration, and the height of lifting is approximated by

$$\Delta z = (T_{\rm h} - T_{\rm c})/\Gamma \tag{27}$$

where Γ is the adiabatic lapse rate.

In the case of large-scale horizontal transport, moisture is transported horizontally and does not necessarily involve lifting. Hence, in the ideal case the energy involved in the latent heat flux would be converted into kinetic energy and $G_{lift} = 0$.

Maximum strength of hydrologic cycling

In this section we derive expressions and values for the maximum strength of hydrologic cycling from the set of energy- and entropy balances of the previous section. While these formulations are highly simplified, the description of the two dominant radiative gradients is "complete" in the sense that energy and mass is being conserved and the second law of thermodynamics is being fulfilled.

Maximum power limit 3.1

The energy balances provide the basis to determine the temperatures and the respective temperature differences. For the net emission of terrestrial radiation, we use a linearized approximation for terrestrial radiation as detailed in the Appendix. For given **HESSD**

10, 3187-3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

References

Figures

Back

Printer-friendly Version









fluxes of insolation $(J_{\text{in,s}}, J_{\text{in,t}}, \text{ and } J_{\text{in,p}})$ and a given radiative "conductivity" k_r , this set of energy balances is in principle determined, except for the strength of convective motion. Motion is unconstrained because the value of the strength of turbulent friction, C_{d} , or, equivalently, the exchange velocity v (which are directly related by Eq. 18) is unknown. In this context it is important to note that the Carnot limit (Eq. 3) does not determine the strength of motion because the convective heat flux that drives the "engine", $J_{\text{in}} = J_c$ while constrained, is not determined by the energy balances. The case of no motion ($J_{\text{in}} = 0$ in Eq. 3) is a solution to the energy balance in steady state, but the energy balances are also solved by values greater than zero ($J_{\text{in}} > 0$). The second law further constrains the value of J_{in} to values that maintain a temperature gradient that directs the heat fluxes from the heated region to the cooled region.

The additional constraint to motion comes from the contrasting effects of the heat flux $J_{\rm in}$ on the power that can be derived from this heat flux which results in a maximum power state (Fig. 3). At small values of $J_{\rm in}$, the power first increases with $J_{\rm in}$. However, with greater values of $J_{\rm in}$, heat is transported from the heated to the cooled reservoir at a faster rate, so that the difference in temperatures must decrease. This reduction in the temperature difference reduces the efficiency of generating power out of $J_{\rm in}$, so that a state of maximum power is achieved at an intermediate value of the heat flux $J_{\rm in}$ and temperature difference, $T_{\rm h}-T_{\rm c}$. We use this maximum power state to derive the exchange velocity ν , which then represents the limit by which motion can be generated. Since a maximum in power corresponds to a maximum in turbulent dissipation, the turbulent exchange through the surface boundary layer should also be maximized in this state. Hence, the maximum strength of hydrologic cycling is derived from the assumption that the vapor transport by atmospheric motion limits hydrologic cycling.

3.2 Maximum strength of hydrologic cycling by vertical convection

To derive an analytic expression for the maximum strength of hydrologic cycling that is driven by vertical convection, we start at the Carnot limit for convective motion. Here, the sensible heat flux acts as the heat flux from which motion is generated ($J_{in} = J_{sh,c}$ in

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Abstract Introduction

Title Page

Conclusions References

Id bl

Figures

→

Back Close

Full Screen / Esc

Printer-friendly Version



Eq. 3), and the temperature difference $T_h - T_c$ is described by the temperature difference between the surface and the atmosphere, $T_s - T_a$:

$$G_{\rm c} = J_{\rm sh,c} \cdot \frac{T_{\rm s} - T_{\rm a}}{T_{\rm s}} \tag{28}$$

With the linearized expression for the radiative exchange flux $J_{s,a}$, we can express the temperature difference by the energy balances, Eqs. (4) and (5), and the expressions for the turbulent heat fluxes, Eqs. (19) and (22), as:

$$T_{s} - T_{a} = \frac{J_{\text{in,s}}}{k_{r} + c_{D}\rho v(1 + s/\gamma)}$$
(29)

With this expression for the temperature difference and the expression for the sensible heat flux, Eq. (19), the power can be expressed as:

$$I_{0} G_{c} = \frac{c_{\rho}\rho v}{T_{s} \left(k_{r} + c_{\rho}\rho v(1 + s/\gamma)\right)^{2}} J_{\text{in,s}}^{2}$$
(30)

This expression has a maximum for an optimum value for the vertical exchange velocity. The trade-off between heat flux and driving gradient as well as the maximum in power is shown in Fig. 4. For this figure, values of $J_{\rm in,s}=168\,{\rm W\,m^{-2}}$, $k_{\rm r}=5.4\,{\rm W\,m^{-2}\,K^{-1}}$, $c_{\rm p}\rho=1200\,{\rm J\,K^{-1}\,m^{-3}}$ and $s=124\,{\rm Pa\,K^{-1}}$ were used (with a mean temperature of $T=288\,{\rm K}$). It shows how the driving temperature gradient is the largest with no motion. In such a state, the difference in heating would be entirely dissipated by radiative exchange, as shown by the ratio $J_{\rm s,a}\approx J_{\rm in,s}$ in Fig. 4b. When more of the solar radiative heating is transported by convective heat transport to the cold reservoir (i.e. a greater ratio of $J_{\rm c}/J_{\rm in,s}$), then this is associated with a lower value of the temperature difference. Hence, this trade-off between the convective heat flux and the temperature difference shape the maximum power state shown in Fig. 4b.

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introdu

nclusions References

Tables Figures

[4 ▶]

→

Back Close

Full Screen / Esc

Printer-friendly Version



$$v_{\text{opt}} = \frac{\gamma}{s + v} \frac{k_{\text{r}}}{C_{\text{o}} \rho} \tag{31}$$

The associated optimum turbulent heat fluxes, $J_{sh,c,opt}$ and $J_{lh,c,opt}$, are given by

$$J_{\text{sh,c,opt}} = \frac{\gamma}{s + v} \frac{J_{\text{in,s}}}{2} \tag{32}$$

and

$$J_{\text{lh,c,opt}} = \frac{s}{s + v} \frac{J_{\text{in,s}}}{2} \tag{33}$$

The optimum latent heat flux, $J_{\text{lh,c,opt}}$, corresponds to the evaporative mass flux of water at the surface, and the flux of precipitation of vapor within the atmosphere. Hence, we derive the maximum strength of evaporation, $E_{\text{c,max}}$, that is permitted by convective motion from Eq. (33) by

$$E_{c,\text{max}} = \frac{J_{\text{lh,c,opt}}}{\lambda} = \frac{s}{s + v} \frac{J_{\text{in,s}}}{2\lambda} = P_{c,\text{max}}$$
(34)

Noting that the net emission of radiation from the surface, $J_{s,a}$, is also $J_{in,s}/2$ at this maximum power state, we can express $E_{c,max}$ in terms of the net surface radiation, $J_{net} = J_{in,s} - J_{in,s}/2 = J_{in,s}/2$:

$$E_{c,\text{max}} = \frac{s}{s + v} \frac{J_{\text{net}}}{\lambda}$$
 (35)

HESSD

10, 3187-3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

onclusions References

Tables Figures

I∢ ≻I

•

Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Furthermore, we can characterize the state of the atmospheric vapor content in terms of its distance to thermodynamic equilibrium. The relative humidity of the surface air, r_c , that drives surface evaporation is in the context of the formulations here given by

$$r_{\rm c} = \frac{e_{\rm sat}(T_{\rm a})}{e_{\rm sat}(T_{\rm s})} \tag{36}$$

Using the linearizations for q_{sat} and the approximation $1/(1-x) \approx 1-x$, this expression can be reformulated as

$$r_{\rm c} \approx 1 - \frac{s}{e_{\rm sat}(T_{\rm a})} \frac{J_{\rm in,s}}{2k_{\rm r}} \tag{37}$$

Since the emission of terrestrial radiation is constrained by the global energy balance, $T_{\rm a}$ as well as $e_{\rm sat}(T_{\rm a})$ should be relatively fixed properties within the system, so that the dominant effect on r is the decrease in r with an increase in $J_{\rm in.s.}$.

In summary, we note that the maximum strength of hydrologic cycling, in terms of its fluxes (cf. Eq. 34) as well as its state of disequilibrium (cf. Eq. 37), is directly related to the absorption of solar radiation, $J_{\text{in,s}}$, which represents the heat input that generates the driving temperature gradient between the Earth's surface and the atmosphere.

3.3 Maximum strength of hydrologic cycling by the large-scale circulation

The maximum strength of hydrologic cycling by the large-scale circulation is derived equivalently. We start with the expression of the Carnot limit, applied to the large-scale horizontal difference in insolation:

$$G_{\rm ls} = J_{\rm sh,ls} \cdot \frac{T_{\rm t} - T_{\rm p}}{T_{\rm t}} \tag{38}$$

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I∢ ►I

■ •

Back Close
Full Screen / Esc

Printer-friendly Version



We solve for the temperature difference, $T_t - T_p$, using Eqs. (10) and (11), use the expressions for the turbulent heat fluxes, Eqs. (19) and (22), and obtain:

$$T_{t} - T_{p} = \frac{J_{\text{in},t} - J_{\text{in},p}}{k_{r} + 2c_{p}\rho v(1 + s/\gamma)}$$
(39)

The power G_{ls} associated with large-scale generation of motion is then given by:

As in the case of vertical convection, this expression has a maximum for an optimum value for the horizontal exchange velocity, v. This maximum is illustrated in Fig. 5. We used values of $J_{\text{in,t}} = 288 \,\text{W}\,\text{m}^{-2}$, $J_{\text{in,p}} = 192 \,\text{W}\,\text{m}^{-2}$, which roughly correspond to the mean solar absorption in the tropics (latitudes < 30°), which is about 20 % above the global mean absorption of solar radiation of 240 Wm⁻², and the extratropics, which is about 20% below the global mean. For the other parameters, we used values representative of the mean mid-troposphere, with a temperature of $T = 266 \,\mathrm{K}$ and pressure of 500 hPa, yielding $k_r = 4.3 \,\mathrm{W \, m^{-2} \, K^{-1}}$, $c_p \rho = 657 \,\mathrm{J \, K^{-1} \, m^{-3}}$, $\gamma = 32 \,\mathrm{Pa \, K^{-1}}$ and $s = 26 \,\mathrm{Pa}\,\mathrm{K}^{-1}$. The shape of the relationships are practically identical with those shown in Fig. 4, yet the interpretation is somewhat different. Here, it is not the absorbed solar radiation from the surface, $J_{in.s}$ that is transported by convective motion to the atmospheric cold reservoir, but rather the difference in absorbed solar radiation, $J_{\text{in.t}} - J_{\text{in.p.}}$ which is transported by horizontal motion to the cold, extratropical reservoir. Also, the relative proportion of transported sensible and latent heat are different, which is due to the lower value of s due to the lower, assumed temperature at which the value of s was calculated.

The analytic expressions associated with the maximum power state, $G_{ls,max}$, are derived as above from the condition $dG_{ls}/dv = 0$. This yields an expression for the

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

References

Figures

Full Screen / Esc

$$v_{\text{opt}} = \frac{\gamma}{s + \gamma} \frac{k_{\text{r}}}{2c_{n}\rho} \tag{41}$$

The associated optimum large-scale transport of sensible and latent heat, $J_{\text{sh,ls,opt}}$ and $J_{\text{lh.ls.opt}}$, are given by

$$J_{\text{sh,ls,opt}} = \frac{\gamma}{S+V} \frac{(J_{\text{in,t}} - J_{\text{in,p}})}{4}$$
 (42)

and

$$J_{\text{lh,ls,opt}} = \frac{s}{s + v} \frac{(J_{\text{in,t}} - J_{\text{in,p}})}{4} \tag{43}$$

Again, we convert the latent heat flux to a mass flux associated with evaporation and precipitation due to large-scale motion:

10
$$E_{ls,max} = \frac{J_{lh,ls,opt}}{\lambda} = \frac{S}{S+V} \frac{(J_{in,t} - J_{in,p})}{4\lambda} = P_{ls,max}$$
 (44)

The relative humidity, $r_{\rm is}$, of the air that would drive evaporation in the tropics is given by:

$$r_{\rm ls} = \frac{e_{\rm sat}(T_{\rm p})}{e_{\rm sat}(T_{\rm t})} \tag{45}$$

or, using the equivalent approximations as above,

$$r_{\rm ls} \approx 1 - \frac{s}{e_{\rm sat}(T_{\rm p})} \frac{J_{\rm in,t} - J_{\rm in,p}}{4k_{\rm r}}$$
 (46)

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

References

Tables Figures

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Discussion Paper

Discussion Paper

Discussion Paper

Discussion Paper











As in the case of vertical convection, we note that the maximum strength of largescale hydrologic cycling is directly related to the heat input that generates the driving gradient, which in this case is given by the magnitude of differential solar radiative heating, $J_{\text{in.t}} - J_{\text{in.p}}$. Since $J_{\text{in.s}}$ is generally greater than $(J_{\text{in.t}} - J_{\text{in.p}})/2$, we would expect convective cycling to play a more dominant role in cycling water than large-scale

Global estimates

transport.

The expressions for optimum evaporative fluxes associated with maximum power are now used to derive the maximum strength of the hydrologic cycle that are associated with the two dominant gradients in solar radiative heating and associated properties. The numerical values of these estimates should be seen as estimates of the order of magnitude because, obviously, guite a number of simplifications were made and many specifics are not included in the estimates. Some analysis on the importance of different factors that shape these estimates, in particular to those that shape the values of the involved power, are further explored in the context of sensitivities in the next section.

We used the above values of the mean absorption of solar radiation at the surface, $J_{\text{in.s}} = 168 \,\text{W}\,\text{m}^{-2}$, and the difference in absorption of solar radiation between the tropics and the extratropics, $J_{\text{in.t}} = 288 \,\text{W}\,\text{m}^{-2}$ and $J_{\text{in.p}} = 192 \,\text{W}\,\text{m}^{-2}$. The separation between tropics and extratropics is done at a latitude of 30°, so that the associated areas are of the same size. These values were already used in the examples shown in Figs. 4 and 5. The values associated with the maximum power states are shown in Table 2 and these values are compared to corresponding estimates based on observations in Table 3.

In the following comparison, we compare the estimates associated with vertical solar heating gradient with global mean characteristics, and the estimates associated with the large-scale horizontal gradient to mean atmospheric transport characteristics.

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract

References

Figures

Back

Full Screen / Esc

Printer-friendly Version



Back

Printer-friendly Version

Interactive Discussion



We first compare the estimated partitioning of fluxes in the surface energy balance to the estimates of Kiehl and Trenberth (1997). Our estimates are of similar magnitude as observed. The magnitude of turbulent fluxes is, however, too small by 15 W m⁻², and the partitioning between sensible and latent heat is biased towards the sensible heat flux. Both aspects result in a bias in the latent heat flux that is 21 W m⁻² lower than what is estimated from observations. Hence, when we compare the corresponding mean strength of the hydrologic cycle in terms of mean global evaporation to estimates of Oki and Kanae (2006), our estimate is of similar magnitude, but about 26 % too low. As we will see in the sensitivities below, these biases can be understood in terms of the simple treatment of terrestrial radiation and by not accounting for temporal variations.

The estimated heat fluxes associated with the large-scale horizontal difference in solar irradiation are compared to values of poleward heat and moisture transport. Masuda (1988) estimated from satellite radiative data that the peak hemispheric heat transport is about 5.9 PW (1 PW = 10^{15} W). We use the total heat transport rather than just the part associated with atmospheric transport, because we do not resolve the oceanic contribution. However, Trenberth and Caron (2001) estimate that the atmosphere transports the vast majority of this heat. When the value of 5.9 PW is divided by surface area, this value corresponds to a mean heat transport per unit surface area of 23 W m⁻². Our estimate of 24 W m⁻² is very close to this number. The contribution to this heat transport by water vapor was estimated by Oki et al. (1995). They estimated the peak in large-scale hemispheric moisture transport to be about $25 \times 10^{12} \,\mathrm{m}^3 \,\mathrm{a}^{-1}$. This flux corresponds to a transport of latent heat of about 2 PW per hemisphere, or about 8 W m⁻². Our estimate of 11 W m⁻² is in the same range, but somewhat higher.

The estimated values for the power associated with large-scale motion is compared to the generation rate of kinetic energy, which is typically in the order of 2Wm⁻² (Lorenz, 1955; Peixoto and Oort, 1992). Our estimate of 1.1 W m⁻² is about half of the observed value. This low value can be explained by the comparatively large value of k, used here, which was derived from the linearization of blackbody radiation. A comparable model which used an empirical parameterization of net terrestrial radiation

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Abstract References

Title Page

Figures

Full Screen / Esc

(Kleidon, 2010) with a smaller slope yielded a generation rate comparable to the observed magnitude. Since k_r does not enter the estimates for the optimum heat flux directly, the optimum heat flux, the partitioning into sensible and latent heat transport, and the strength of large-scale hydrologic cycling should be relatively unaffected by this bias. The power involved in lifting moisture which is subsequently dissipated by falling raindrops has been estimated by Pauluis et al. (2000) to be up to 2–4 W m⁻² in the tropics. Our global estimate of 0.35 W m⁻² is quite a bit lower, but as it represents a global average, it does not correspond to an upper bound on this number so that these numbers are not directly comparable.

In summary, our extremely simple estimates that are based on the assumption of maximum power associated with atmospheric transport estimate the observed magnitudes of heat and moisture transport within the climate system very well. This suggests that the global hydrologic cycle can indeed be understood as a cycle that operates close to the limit of maximum strength.

4 Sensitivities

The maximum strength of hydrologic cycling is inferred here from the assumption of maximum power regarding moisture transport. The comparison with observations shows that these estimates are quite reasonable in their magnitude, but are sometimes lower than what is observed. The tradeoff that results in the maximum power limit is a fundamental consequence of the second law in combination with energy balance constraints in steady state, so that the existence of this limit should not be a concern. The particular optimum state that is associated with this limit depends, however, on the particular formulations that describe the relationship between heat flux, the energy balance constraints, on the assumption of steady state conditions, and on the use of global mean averages rather than spatially and temporally explicit values. Hence, it is important to understand the factors that affect these maximum power states and what these imply for the estimated maximum strength of hydrologic cycling.

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

l∢ ≯l

■ •

Back Close

Full Screen / Esc

Printer-friendly Version



The most important factor in these estimates is the magnitude of the solar radiative forcing. The magnitude of the forcing enters directly into the estimates for the maximum power (Eqs. 30 and 40) as well as the expressions for the optimum evaporation rate (Eqs. 34 and 44). The magnitude of these forcings vary spatially and temporally on Earth, so we first look at the sensitivity of these expressions to the two solar radiative heating differences, $J_{in.s}$ and $(J_{in.t} - J_{in.p})$ (Fig. 6).

The sensitivity to the vertical solar radiative heating difference, $J_{\rm in.s.}$, is shown in Fig. 6a, b. The sensitivity was calculated in a slightly different way as in the maximum power examples of the previous section, because with the wide range of variation in $J_{\text{in.s}}$ it can no longer be assumed that k_r and s are unaffected. These values were calculated for the radiative temperature that is associated with the particular radiative forcing. We find that at the limit of low and high values of $J_{in.s}$, the power as well as the heat fluxes vary roughly linearly with the forcing. At these two extremes, variations in the forcing in either space or time would average out when using mean values because of this linearity. It is rather in the middle range of the sensitivity at values of $J_{\text{in,s}} \approx 200$ – 400 W m⁻² where the relationships are non-linear, and variations do not average out. In this range, an averaging of variations would likely result in an underestimation of the latent heat flux, J_{lh} , and the associated values of G_{lh} and G_{lift} .

The sensitivity to the magnitude of the large-scale horizontal forcing is shown in Fig. 6c, d. In these sensitivities, the mean solar radiation was fixed to a value of 240 W m⁻², the value of k_r was derived from the mean forcing, and the value of s from the temperature T_t . The sensitivities for this forcing are much more linear, although we note that G_{ls} shows a slight quadratic dependence on $J_{in,t}$ - $J_{in,p}$, and J_{sh} saturates at high values of $J_{\text{in t}} - J_{\text{in p}}$. When variations are averaged, we would expect that the power is underestimated, and we may also expect a slight underestimation of the latent heat flux.

In the estimates, we assumed that the atmosphere is fully absorbing. In the natural atmosphere, this is often not the case, and the absorptivity of the atmosphere depends on many factors, in particular on cloud cover and the concentration of greenhouse

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page **Abstract**

References

Figures

Back

Full Screen / Esc

Printer-friendly Version

gases (such as water vapor and carbon dioxide). When the atmosphere is not a black-body, but partially transparent, then a given rate of radiative exchange between the surface and the atmosphere is accomplished by a greater temperature difference, and this corresponds to a smaller value of $k_{\rm r}$. We can thus approximate the sensitivity of our estimates to the strength of the atmospheric greenhouse by the sensitivity to the value of $k_{\rm r}$ (Fig. 7).

In the sensitivity to $J_{\rm in,s}$ (Fig. 7a, b), we note that the value of the optimum convective heat flux $J_{\rm c}$ is not affected by the value of $k_{\rm r}$, but that the power as well as the partitioning between sensible and latent heat are strongly affected. A low value of $k_{\rm r}$ results in higher surface temperatures, a greater temperature difference between the surface and the atmosphere, and hence in a greater overall value of the maximum power, $G_{\rm c}$, as well as a shift in the partitioning towards a greater value of the latent heat flux. The same line of reasoning applies to the sensitivity to $J_{\rm in,t}-J_{\rm in,p}$ that is shown in Fig. 7c, d. What this implies for the averaging of variations is that the overall magnitude of the optimum convective heat fluxes is quite robust, but that the estimates for the associated evaporative flux as well as the power involved is rather sensitive to the radiative properties of the atmosphere.

These sensitivities are computed assuming steady state conditions in which the simulated temperatures are in steady state with the energy fluxes. When the solar radiative forcing varies during the day (or through seasons), then the energy balances are typically not in a steady state. What this averaging over such variations in solar radiation imply for our estimates, we may consider two extreme cases for the sake of simplicity. In the first case, we assume a heat reservoir which absorbs solar radiation with a large heat capacity, such as a water surface. For this case we can assume a large thermal inertia so that the averaging should not play a role. For the second case we consider a heat reservoir which absorbs solar radiation with a very small heat capacity, such as a forest canopy. In this case, we can assume that the steady state between radiative fluxes and energy balances is established fast. Hence, the above considerations of the biases due to temporal variations in the solar radiative forcing would only apply when

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

l∢ ≯l

- ◆

Back Close

Full Screen / Esc

Printer-friendly Version



the thermal inertia of the absorbing surface is relatively small compared to the time scale by which the solar forcing varies.

To sum up, the sensitivities we performed here suggest that spatial and temporal averaging could result in an underestimation of the latent heat flux. These biases are, however, not of a substantial magnitude, because the deviations from linear relationships are not that large. Nevertheless, such averaging could result in an underestimation of the the strength of hydrologic cycling. Furthermore, we found that radiative properties of the atmosphere that would affect the strength of radiative exchange play an important role in shaping the strength of hydrologic cycling as well.

5 Discussion

5.1 Limitations

The estimates derived here on the maximum strength of the hydrologic cycle are, of course, subject to several limitations. Some of these limitations regarding the use of global mean values have already been discussed above in the context of the sensitivities, where we specifically identified the importance of radiative transfer characteristics. Other notable limitations are that we did not consider land explicitly, we did not include interactions with cloud cover into the model which would affect the radiative properties of the atmosphere, and the two forcing gradients were treated in isolation, although they would likely affect each other. We also did not link the turbulent dissipation of kinetic energy with the turbulent transport of moisture at the interface between the surface and the atmosphere. Since dissipation of kinetic energy equals the generation of kinetic energy in steady state, a state of maximum power associated with atmospheric motion would likely also be associated with maximum dissipation near the surface and hence maximum turbulent moisture transport within the boundary layer. We did not consider this link explicitly here.

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

▶I

Back Close

Full Screen / Esc

Printer-friendly Version



These aspects could be addressed in future work. The addition of extra details would make the models necessarily more complicated and would likely require some empirical parameters. It would also potentially provide a wider range of predictions that could be tested with observations. The estimates developed here can in fact be seen as the simplest possible estimate of the maximum strength of the hydrologic cycle. It contains a minimum representation of the physics, in terms of the energy balances that describe the driving gradients and which explicitly consider the first and second law of thermodynamics. This formulation has practically no empirical parameters, except for the use of observed values for the solar forcing and typical mean temperatures used to determine s and k_r . From this perspective it is quite remarkable how close our estimates are to the observed strength of the hydrologic cycle. The sensitivities also revealed that the associated optimum heat fluxes are quite robust, although the maximum power limit as well as the partitioning between sensible and latent heat can be quite sensitive.

Overall, there are clearly many aspects that could be improved and that could refine our estimates of the maximum strength. The fact that our simple estimates are, nevertheless, in the same order of magnitude as the observed hydrologic cycle suggests that we captured the relevant, first-order processes very well. Furthermore, it implies that the natural hydrologic cycle on Earth would seem to operate near its maximum strength.

5.2 Relation to previous work

Our results build on and extend earlier work on the thermodynamics of hydrologic cycling. Thermodynamics has been used, for instance, to explain the intensity of hurricanes (Emanuel, 1999), or to describe hydrologic cycling in the context of vertical convection as a dehumidifier (Pauluis and Held, 2002a,b; Pauluis, 2011). Konings et al. (2012) recently explored the thermodynamics of the diurnal growth of a moist atmospheric boundary layer. These studies also used the Carnot limit to describe the strength of cycling, but they provided a more detailed treatment of the different steps involved in the thermodynamic cycle that generates the work within the atmosphere.

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Abstract Introduction

Title Page

Conclusions References

Figures

Back Close

Full Screen / Esc

Printer-friendly Version



Here, we did not consider these individual steps, but rather started with the Carnot limit and treated atmospheric dynamics like a "black box" engine. We then looked at the combination of this limit with the energy balances that shape the driving gradient for the heat engine. By doing so, we do not need to describe the details of the "black box" that is constrained by the Carnot limit. What we show here is that the magnitude of the heat flux through the "engine" is substantial, it affects the magnitude of the driving gradient in steady state, and thereby sets the maximum power limit. This is in contrast to previous studies, who used a prescribed temperature difference as forcing. In this sense, our work complements previous approaches on the thermodynamics of the hydrologic cycle.

The strong interaction between the heat flux and the driving gradient that we found here relates very closely to studies that employed the proposed principle of Maximum Entropy Production (MEP, Paltridge, 1975; Ozawa et al., 2003; Kleidon et al., 2010). The MEP principle states that thermodynamic systems organize into states in which they produce entropy at the maximum possible rate. This principle was previously applied to poleward atmospheric heat transport and could reproduce temperature profiles on Earth (Paltridge, 1975, 1978), empirical values for turbulent dissipation (Kleidon et al., 2003, 2006), and the climate characteristics of other planets (Lorenz et al., 2001). It was applied to vertical exchange of radiation and heat within the atmosphere (Ozawa and Ohmura, 1997; Lorenz and Mckay, 2003; Kleidon, 2004) to determine vertical fluxes and resulting temperature profiles. The models developed here are very similar to those used in these studies, although the latent heat flux was not explicitly considered before and the interpretation of the limit is different. Here, we merely applied the Carnot limit to the heat flux and considered the depleted temperature gradient that is associated with a greater heat flux. This combination of the Carnot limit with the trade-off between flux and gradient resulted in a maximum power state. In steady state, power equals dissipation, and a maximum power state corresponds to a state of maximum dissipation. As already mentioned at the end of Sect. 2.3, if this dissipation occurs at the temperature of the cold sink, the maximum power state used here corresponds to

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

l∢ ≯l

- - -

Back Close

Full Screen / Esc

Printer-friendly Version



Discussion

Back

a state of maximum entropy production. Since kinetic energy is typically not dissipated exclusively at the cold sink, it implies that the maximum power state would be close, but somewhat below the MEP state in terms of its entropy production. While the values associated with both states are very similar, the assumption of a maximum power is 5 easier to interpret in terms of classical mechanics. Hence, the results obtained from MEP may be more appropriately phrased as a Carnot limit in which the assumption of a fixed, unaffected temperature difference is being relaxed.

At a more general level, our work demonstrates how tightly linked the hydrologic cycle is to the functioning of the whole Earth system and its forcing. The maximum strength of hydrologic cycling is in first order directly proportional to the magnitude of differences in absorption of solar radiation. This is reflected in the estimates for maximum evaporation rates (Eqs. 34 and 44), which are proportional to the surface absorption of solar radiation and the difference in solar radiation between the tropics and the poles. These differences in solar radiative heating result directly from the planetary forcing and are of critical importance because these differences act as the thermodynamic driver that maintains a system away from a state of thermodynamic equilibrium. This disequilibrium can be expressed by the relative humidity. Our approximations for the relative humidity shows that the extent of disequilibrium is directly proportional to the magnitude of this forcing (Eqs. 37 and 46).

The tight linkage of the maximum strength of hydrologic cycling to the solar forcing represents the one side of the interplay between the hydrologic cycle and the Earth system. The other side is represented by the strong effect that the latent heat flux has on the magnitude of its driving gradient. It is this interaction between the heat flux and the driver which shapes the maximum power limit. The maximum power limit, in turn, results practically in an insensitivity of the total heat fluxes to changes in radiative properties of the atmosphere, as shown by the sensitivities to k, in Fig. 7. This insensitivity of heat fluxes to changes in k_r is consistent with the observation that atmospheric heat transport is indeed insensitive to such changes and depends primarily on solar radiative forcing, albedo, and planetary geometry (Stone, 1978). Here, the optimum heat

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Abstract

Title Page

References

Figures

Full Screen / Esc

Printer-friendly Version

fluxes depend solely on the difference in solar absorption, $J_{\text{in,t}} - J_{\text{in,p}}$, which reflect the same properties as those stated by Stone (1978), but in addition it explicitly makes use of the assumption that atmospheric motion operates at its thermodynamic limit. This interplay between a state of thermodynamic disequilibrium associated with hydrologic cycling, the maximum power limit, and strong interactions is consistent with the broad picture of how disequilibrium is generated within the Earth system in general and how Earth system processes follow and accelerate the direction of the second law (Kleidon, 2012).

The insight that the hydrologic cycle appears to operate near its maximum strength is non-trivial. Any engineer would agree that reaching the Carnot limit for an engine is a formidable, if not nearly impossible challenge. This necessarily raises the question of how the natural processes of the hydrologic cycle are organized such that they are able to operate close to this limit. We may get a clue to the answer from a recent approach to understand thermodynamic limits associated with river systems (Kleidon et al., 2013). In this paper we looked at the energetics of water and sediment transport in catchments and suggested that it is through structure formation that river systems can deplete their driving gradient of continental topography at the fastest possible rate. Applied to moisture transport within the atmosphere, this would suggest that the maximum power limit is achieved by the spatial, and possibly temporal, organization of moist convection. Clearly, these aspects would need to be explored further in future work.

5.3 Implications

These insights emphasize the need to take a thermodynamic as well as a holistic Earth system perspective when we want to understand the functioning of the hydrologic cycle, how it is affected by biotic and human activity, and how the hydrologic cycle changes in response to altered forcing. We first note that an aspect of change can result from two different aspects: it can either lead to a hydrologic flux to operate closer to (or further from) the maximum strength, or it can change the maximum strength itself. To illustrate this distinction with common terminology, the first aspect

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Abstract Introduction

Conclusions References

Tables Figures

Title Page

I**4** ►I

Back Close

Full Screen / Esc

Printer-friendly Version



corresponds to a change that would affect the actual evaporation rate, while the latter aspect corresponds to a change in the potential evaporation rate (which corresponds to the maximum strength, as shown above).

We illustrate these different aspects of change in terms of vegetation effects on hy-5 drologic cycling. We first note that vegetation strongly affects the fluxes of water from the soil into the atmosphere over land. Soil water is taken up by the root system of the vegetation, it is then transported by the vascular system to the canopy, where it is transpired into the atmosphere. These flows of water are represented in Fig. 8 by the arrows "A". The effect of this biotic "plumbing system" is typically to enhance evapotranspiration rates on land because the ability of a bare soil is typically very low to sustain high evaporation rates during dry episodes. This enhanced ability of the vegetated surface to evaporate water would seem to represent an aspect that would make the evaporative flux on land to operate closer to the maximum strength. An example of vegetation that alters the maximum strength is the effect of vegetation on the radiative properties of the surface (arrow "B" in Fig. 8). Vegetated surfaces generally have a lower surface albedo, which results in a higher absorption of incident solar radiation. Because absorbed solar radiation is a key factor in shaping the maximum strength estimates, the lowering of the surface albedo corresponds to a greater capacity to evaporate water. The effect of this albedo change can be illustrated by sensitivity simulations with a coupled climate-vegetation model (Kleidon, 2006), in which the conditions of a "Desert World" with no vegetation present were simulated. Compared to this "Desert World" state, the mean latent heat flux on land increased by 26.8 W m⁻² while net solar radiation increased by 9.6 W m⁻². What this seems to imply is that the resulting change in hydrologic cycling can be attributed to a 9.6/26.8 ≈ 36% increase in the capacity to cycle water while the remaining increase is an enhancement of the actual evaporation rate without a change in the maximum strength. At the same time it is important to note that this increase by vegetation activity comes at an energetic cost of creating and maintaining biomass, which is derived from photosynthesis. It is this vegetation activity that builds and maintains the "plumbing system" as well as the other effects described

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

•

Back Close
Full Screen / Esc

Printer-friendly Version



above that shape the effects on hydrologic cycling. Ultimately, one would also need to consider whether these effects would enhance, or reduce, the ability of vegetation to perform photosynthesis as it is through photosynthesis that vegetation activity is being maintained.

We can also apply this line of reasoning to human activity, which requires freshwater for a variety of reasons, including drinking water, sanitation, irrigation, and industrial uses. This freshwater is taken out, and eventually returned, to the natural hydrologic cycle (represented by arrow "C" in Fig. 8). The largest fraction of freshwater use is associated with irrigation of croplands (Oki and Kanae, 2006), with different sources of where the water from irrigation comes from (diversion of river flow, groundwater or desalination of seawater, with the latter two sources associated with energy needs in the process). In the context here, irrigated croplands result in two different types of change (represented by arrow "D"). First, more water is made available for evaporation, so that evaporation could operate closer to its limit. Second, cropland is associated with land cover change from its natural state. The change in land cover would likely impact the maximum strength for water cycling. If the natural state was forested, the change to cropland would likely be associated with an increase in the surface albedo, which would reduce the maximum strength limit. If the irrigated cropland is located in a desert region, the surface albedo is likely to decrease, which would potentially increase the maximum strength limit. Hence, it is not directly clear whether human activities would tend to reduce or enhance the strength of hydrologic cycling as well as its limit. In this context it is important to recognize that hydrologic fluxes do not operate in the context of a static, natural limit (which the concept of a "planetary boundary" Rockström et al., 2009 would suggest), but that the limits are in principle affected by human activity as well.

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

■ Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



We derived the thermodynamic limits of global hydrologic cycling from a simple representation of the hydrologic cycle within the Earth system that can be seen to represent the minimum amount of required physics. This minimum representation includes the energy balances that form the driving gradient for motion, which is needed to transport moisture, and serve as the source (or sink) of energy for the phase transitions associated with hydrologic cycling as well as the first and second law of thermodynamics, which yield the limits to motion and transport. The combined need for energy for evaporation and for atmospheric transport then established the limit to the strength of the hydrologic cycle. This limit results from the strong interaction between hydrologic fluxes with the heating gradient that drives atmospheric transport. When we used observed values for the forcing, we obtained estimates for the maximum strength of hydrologic cycling that are close to the observed state of the hydrologic cycle. We conclude that the natural hydrologic cycle within the Earth system appears to operate near its maximum, thermodynamic strength.

Our work is only a first demonstration of the utility of a thermodynamic view, as well as a holistic view on the hydrologic cycle within the Earth system. The thermodynamic view emphasizes the role of a thermodynamic driver that is needed to generate dynamics associated with hydrologic cycling and its associated disequilibrium. The holistic view includes the interactions of hydrologic cycling with other Earth system processes and which links hydrologic processes to the ultimate drivers of planetary dynamics. In future work, this view should be developed further. The use of spatially and temporally explicit datasets of climatic forcing would allow for a much more detailed comparison of the maximum strength predictions with observations. The effects of vegetation activity and, more generally, global change on the hydrologic cycle could be analyzed in terms of their effects on the maximum strength, as outlined in the discussion. The establishment of such maximum strength limits of hydrologic processes and their sensitivity to

HESSD

Discussion Paper

Discussion Paper

Discussion

10, 3187-3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I⊀ ≯I

→

Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



change should help us to better understand and predict how the hydrologic cycle has changed in the past, and how it is likely to change in the future.

Appendix A

Linear approximations

We derive simple, linearized approximations for terrestrial radiation and for the saturation vapor pressure that are used in the models. These approximations allow us to derive very simple, analytical solutions for the limits and this facilitates the evaluation of the first order dynamics that shape these limits. We should nevertheless recognize that these models cannot be highly precise, and serve the purpose to illustrate the limits as well as to provide a first order estimate of the magnitude of the limits.

To obtain a linearized expression for net emission of longwave radiation, we do a Taylor expansion to first order of the Stefan–Boltzmann law:

$$J_{I}(T) \approx \sigma T_{0}^{4} + \left(\frac{d}{dT} \left(\sigma T^{4}\right)\right)_{T=T_{0}} \cdot (T - T_{0})$$
(A1)

with a reference temperature T_0 , $\sigma = 5.67 \times 10^{-8} \,\mathrm{W m}^{-2} \,\mathrm{K}^{-4}$ being the Stefan–Boltzmann constant, and a slope that will be abbreviated by k_r in the following:

$$k_{\rm r} = \left(\frac{\rm d}{{\rm d}T}\left(\sigma T^4\right)\right)_{T=T_0} = 4\sigma \cdot T_0^3$$
 (A2)

With this linearization, the net radiative exchange between a warm reservoir at temperature $T_{\rm h}$ and a cool reservoir at a temperature $T_{\rm c}$ is then given by

$$J_{h,c} = J_I(T_h) - J_I(T_c) = k_r \cdot (T_h - T_c)$$
(A3)

assuming that both emit like black bodies, that is, that their emissivities are $\epsilon=1$.

iscussion Pa

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

nclusions References

Tables Figures

[4 ▶]

Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



$$e_{\text{sat}}(T) = e_0 \cdot \exp[19.83 - 5417 \,\text{K/T}]$$
 (A4)

with a value of $e_0 = 6.11 \,\text{hPa}$ and T in units of K. We obtain a linearized expression by a Taylor expansion around a reference temperature T_0 :

$$e_{\text{sat}}(T) \approx e_{\text{sat}}(T_0) + \left(\frac{de_{\text{sat}}}{dT}\right)_{T=T_0} \cdot (T - T_0)$$
 (A5)

Here, the slope of the vapor pressure curve, evaluated at the reference temperature T_0 , will be abbreviated by s:

$$s = \left(\frac{de_{sat}}{dT}\right)_{T=T_0} = \frac{s_0}{T_0^2} \cdot \exp\left[19.83 - 5417/T_0\right]$$
 (A6)

with $s_0 = e_0 \cdot 5417$ K. With this linearization, the difference in saturation vapor pressure, $\Delta e_{\rm sat}$ between two air masses with temperatures $T_{\rm h}$ and $T_{\rm c}$ is then simply linear in the associated temperature difference:

$$\Delta e_{\text{sat}} = s \cdot (T_{\text{h}} - T_{\text{c}}) \tag{A7}$$

Acknowledgements. The ideas for this paper originated from the preparation for the "Biogeophysics and Earth System Science" (BESS) summer school. AK acknowledges financial support from the Helmholtz Alliance "Planetary Evolution and Life". This research contributes to the "Catchments As Organized Systems (CAOS)" research group funded by the German Science Foundation (DFG).

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HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract

Introduction

Conclusior

References

Tables

Figures

I∢

►I

■



Back



Full Screen / Esc.

Printer-friendly Version



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Discussion Paper

Discussion Paper

Discussion Paper

Discussion Paper

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Abstract Introduction

Conclusions References

Tables

Title Page

Id bl

Figures

•

Back Close

Full Screen / Esc

Printer-friendly Version



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10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

l∢ ⊳l

4 ▶

Full Screen / Esc

Back

Printer-friendly Version

Interactive Discussion



3224

Discussion Paper

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20

HESSD

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

- ◆

Back Close

Full Screen / Esc

Printer-friendly Version



Table 1. Variables used in this study.

Symbol	Variable
$\overline{c_p}$	specific heat capacity of air
$oldsymbol{\mathcal{C}}_{p}$	drag coefficient
D	dissipation
Δz	height at which condensation occurs
F	force
Γ	adiabatic lapse rate
g	gravitational acceleration
J	heat flux
$J_{\mathtt{s}}$	entropy flux
J_{lh}	latent heat flux
J_{sh}	sensible heat flux
Ε	evaporation
Р	precipitation
λ	latent heat of vaporization
G	power, or generation rate of free energy
q	specific humidity
ρ	air density
S	slope of water vapor saturation curve
S	entropy
σ	entropy production
Τ	temperature
U	internal energy
V	exchange velocity

10, 3187-3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

▶I

Close

Full Screen / Esc

Back

Printer-friendly Version



Table 2. Global estimates of the maximum strength of the hydrologic cycle due to the vertical solar heating gradient ("convection", $J_{\text{in,s}}$) and due to the large-scale horizontal solar heating gradient ("large-scale", $(J_{\text{in,t}} - J_{\text{in,p}})/2$). The estimates represent the values associated with the maximum power states shown in Figs. 4 and 5. The optimum latent heat flux associated with a maximum power state is then converted to a corresponding water flux per unit area.

property	convective	large-scale
driving gradient (observed)	168 W m ⁻²	48 W m ⁻²
max. power (dry convection)	1.7 W m ⁻²	0.6 W m ⁻²
max. power (moist convection)	4.8 W m ⁻²	0.5 W m ⁻²
max. power (lifting)	0.35 W m ⁻²	-
terrestrial radiation	81 W m ⁻²	24 W m ⁻²
sensible heat	$30 \text{W} \text{m}^{-2}$	$13 \mathrm{W m^{-2}}$
latent heat	$57 \mathrm{W m^{-2}}$	$11 \text{W} \text{m}^{-2}$
max. evaporation	2.0mm d^{-1}	$0.4 \text{mm} \text{d}^{-1}$

10, 3187-3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

l≼ ⊳l

•

Back Close

Full Screen / Esc

Printer-friendly Version



Table 3. Comparison of the maximum strength estimates of hydrologic cycling derived here from the assumption of maximum power associated with atmospheric transport with observation-based estimates.

property	estimated	observed	sources
net terrestrial radiation	81 W m ⁻²	66 W m ⁻²	Kiehl and Trenberth (1997)
sensible heat flux	$30 \text{W} \text{m}^{-2}$	$24 \mathrm{W m^{-2}}$	Kiehl and Trenberth (1997)
latent heat flux	$57 \mathrm{W m^{-2}}$	$78{\rm Wm^{-2}}$	Kiehl and Trenberth (1997)
evaporation/precipitation	2.0mm d^{-1}	2.7mm d^{-1}	Oki and Kanae (2006)
poleward heat transport	24W m^{-2}	23W m^{-2}	Masuda (1988)
large-scale moisture transport	11 W m ⁻²	8 W m ⁻²	Oki et al. (1995)
large-scale generation of kinetic energy	1.1 W m ⁻²	2 W m ⁻²	Peixoto and Oort (1992)
frictional dissipation of raindrops	0.35 W m ⁻²	$< 2-4 \mathrm{Wm}^{-2}$	Pauluis et al. (2000)

10, 3187-3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I∢ ≯I

•

Close

Full Screen / Esc

Back

Printer-friendly Version



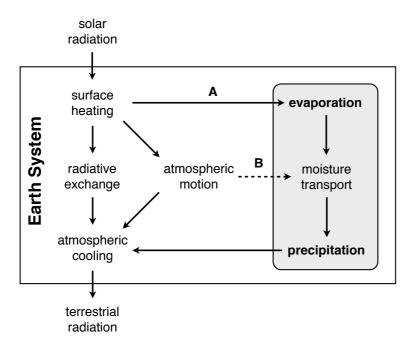


Fig. 1. Schematic diagram to illustrate the primary factors that limit the strength of hydrologic cycling within the Earth system. The arrows indicate the flow of energy, from the incoming solar radiation at the top of the diagram which results mostly in the heating of the Earth's surface, to the emission of terrestrial radiation, mostly from the atmosphere, to space at the bottom. Hydrologic cycling is embedded in these energy transfers (shown by the grey box) as it removes heat where water evaporates (arrow "A") and releases that heat when it condenses and results in precipitation. The differences in heating between the surface and the atmosphere generates atmospheric motion, which plays a critical role in transporting moisture from the locations at which water evaporates to the locations at which it condenses (as indicated by the dashed arrow, "B"). The limit to hydrologic cycling results from the tradeoff between paths "A" and "B", because the associated flows of energy are subject to energy conservation.

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

l⊀ ≻l

→

Back Close

Full Screen / Esc

Printer-friendly Version



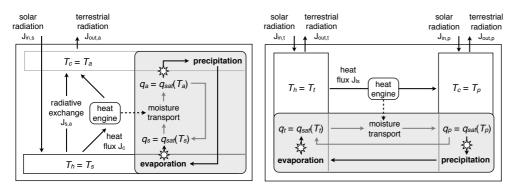


Fig. 2. Simple representation of hydrologic cycling resulting from (left) vertical differences and (right) large-scale horizontal differences in solar radiative heating. The first heating difference shown in (left) results from surface heating due to the absorption of solar radiation (lower box, with temperature $T_{\rm s}$) and radiative cooling of the atmosphere (upper box, with temperature $T_{\rm a}$). The second heating difference (right) results from the greater insolation in the tropical regions (left box, with temperature $T_{\rm t}$) compared to the extratropics (right box, with temperature $T_{\rm p}$). These heating differences serve as the hot and cold reservoirs (with temperatures $T_{\rm h}$ and $T_{\rm c}$) for heat engines from which work can be derived to fuel atmospheric motion. Within the grey areas, grey arrows the grey areas show the hydrologic cycle and how it is associated with the energy balances. The stars (*) symbolize the phase transitions of water between its liquid and vapor state. Grey arrows indicate mass fluxes of water vapor, while black arrows indicate fluxes of liquid water.

10, 3187–3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Figures

I∢ ►I

■ Back Close

Full Screen / Esc

Printer-friendly Version



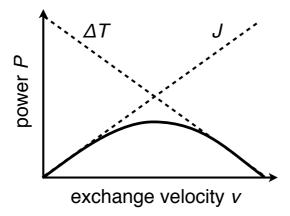


Fig. 3. Illustration of the maximum power limit to motion resulting from the depletion of the driving temperature difference, ΔT , by the resulting transport of heat, J. The Carnot limit to the power of a heat engine (solid line) is given by the product of the heat flux and the driving temperature difference (dashed lines). In the atmosphere, this work is used to generate motion and is reflected in a certain velocity ν by which heat is transported by convection. The resulting heat flux increases with ν , but depletes the driving temperature difference.

10, 3187-3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables

I⊀ ≯I

Figures

Back Close

Full Screen / Esc

Printer-friendly Version



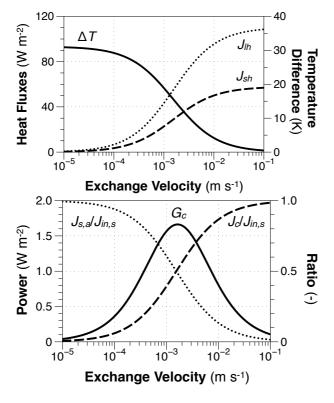


Fig. 4. Trade-off involved in setting the maximum strength in hydrologic cycling due to vertical solar heating differences. **(a)** Sensible (dashed line, $J_{\rm sh}$) and latent (dotted line, $J_{\rm lh}$) heat flux as well as the temperature difference (solid line, $\Delta T = T_{\rm s} - T_{\rm a}$) as a function of exchange velocity v. **(b)** Power (solid line, $G_{\rm c}$) as well as the ratio of radiative cooling (dotted line, $J_{\rm s,a}$) and cooling by convective heat fluxes (dashed line, $J_{\rm c}$) in relation to the rate of heating by absorption of solar radiation, $J_{\rm in.s}$.

10, 3187-3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

onclusions References

Tables Figures

||4|| ►||

▼ ...

Full Screen / Esc

Back

Printer-friendly Version



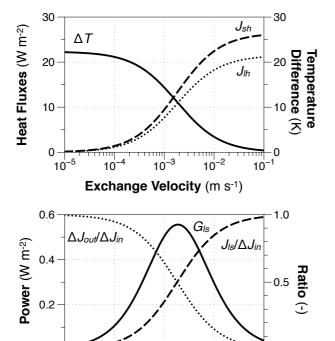


Fig. 5. Same as Fig. 4, but for the large-scale horizontal difference in solar radiative heating. **(a)** Sensible (dashed line, $J_{\rm sh}$) and latent (dotted line, $J_{\rm lh}$) heat flux as well as the temperature difference (solid line, $\Delta T = T_{\rm t} - T_{\rm p}$) as a function of exchange velocity v. **(b)** Power (solid line, $G_{\rm ls}$) as well as the ratio of the difference in radiative cooling (dotted line, $\Delta J_{\rm out} = (J_{\rm out,t} - J_{\rm out,t})/2$) and cooling by convective heat fluxes (dashed line, $J_{\rm ls}$) in relation to the difference in solar radiation, $\Delta J_{\rm in} = (J_{\rm in,t} - J_{\rm in,p})/2$.

10 -3

Exchange Velocity (m s-1)

10 -5

10 -4

10 -2

HESSD

10, 3187-3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Tables Figures

l∢ ⊳l

■ Back Close

Full Screen / Esc

Printer-friendly Version



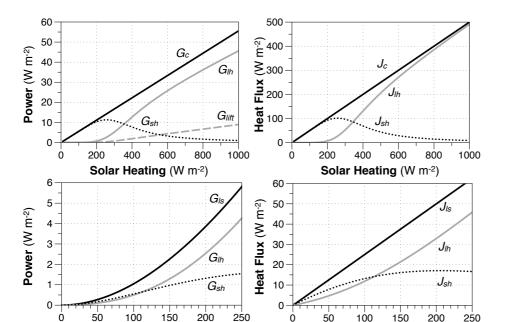


Fig. 6. Sensitivity of the maximum power state associated with the vertical ($J_{\text{in,s}}$, top row) and the large-scale horizontal ($J_{\text{in,t}} - J_{\text{in,p}}$, bottom row) solar radiation difference to the magnitude of the difference. The left plots show the sensitivity of the power associated with the sensible heat flux (G_{sh} , dotted line), the latent heat flux (G_{lh} , grey line), the power involved in lifting (G_{lift} , dashed grey line), and the sum of all (G_{c} , solid line). The plots on the right show the sensible heat flux (J_{sh} , dotted line), the latent heat flux (J_{lh} , grey line), and the total turbulent heat fluxes (J_{c} , solid line). The global mean values of the present day are about $J_{\text{in,s}} = 170 \, \text{W m}^{-2}$ and $J_{\text{in,t}} - J_{\text{in,p}} = 96 \, \text{W m}^{-2}$ (although different values for k_{r} and s were used in Figs. 4 and 5.)

Solar Heating (W m⁻²)

Solar Heating (W m⁻²)

HESSD

10, 3187-3236, 2013

Thermodynamic limits of hydrologic cycling

A. Kleidon and M. Renner

Title Page

Abstract Introduction

Conclusions References

Figures

•

Full Screen / Esc

Back

Printer-friendly Version





Back Full Screen / Esc

Abstract

Conclusions

Tables

Printer-friendly Version

HESSD

10, 3187–3236, 2013

Thermodynamic

limits of hydrologic

cycling

A. Kleidon and M. Renner

Title Page

Introduction

References

Figures



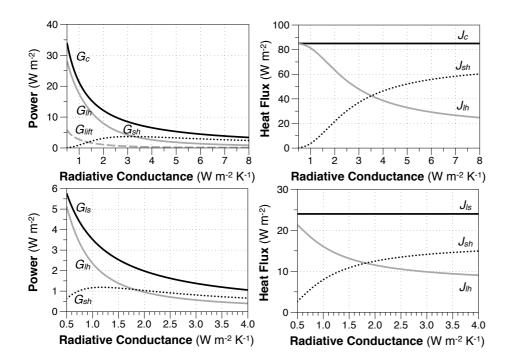


Fig. 7. Same as Fig. 6, but showing the sensitivity to the radiative conductance, k_r .



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Interactive Discussion



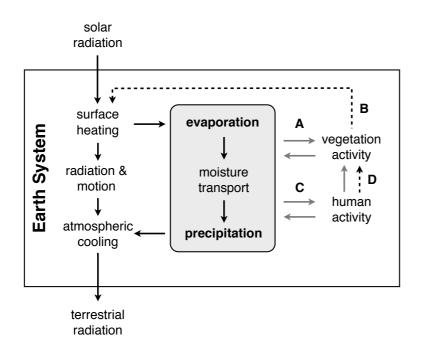


Fig. 8. Conceptual diagram to illustrate interactions between vegetation and human activity with the strength of hydrologic cycling within an Earth system context, which is based on Fig. 1. Grey arrows "A" and "C" reflect the fluxes of water associated with vegetation and human activity, which affect how close hydrologic fluxes operate to the maximum that is set mostly by the radiative forcing. The dashed arrow "B" describes the effects of vegetation on the radiative forcing which alters the maximum strength limit and thereby the capacity of the Earth system to cycle water. Human activity can also affect this limit through vegetation changes, e.g. by land cover change (arrow "D").

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Figures

References