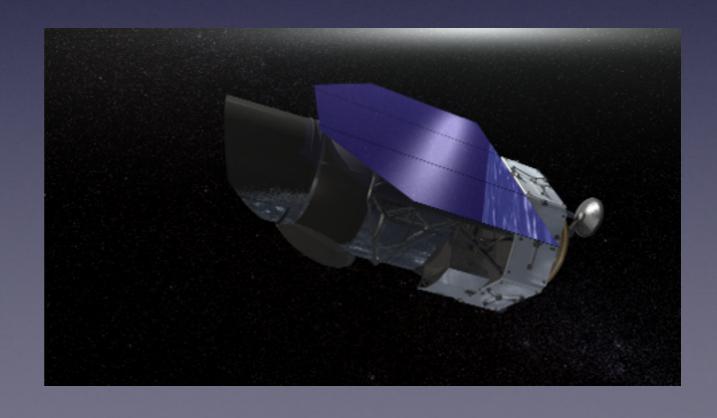
## Hierarchical Bayesian Models for SN la in the Optical and NIR



SN la NIR Meeting U. Pittsburgh 12 April 2018 Kaisey Mandel
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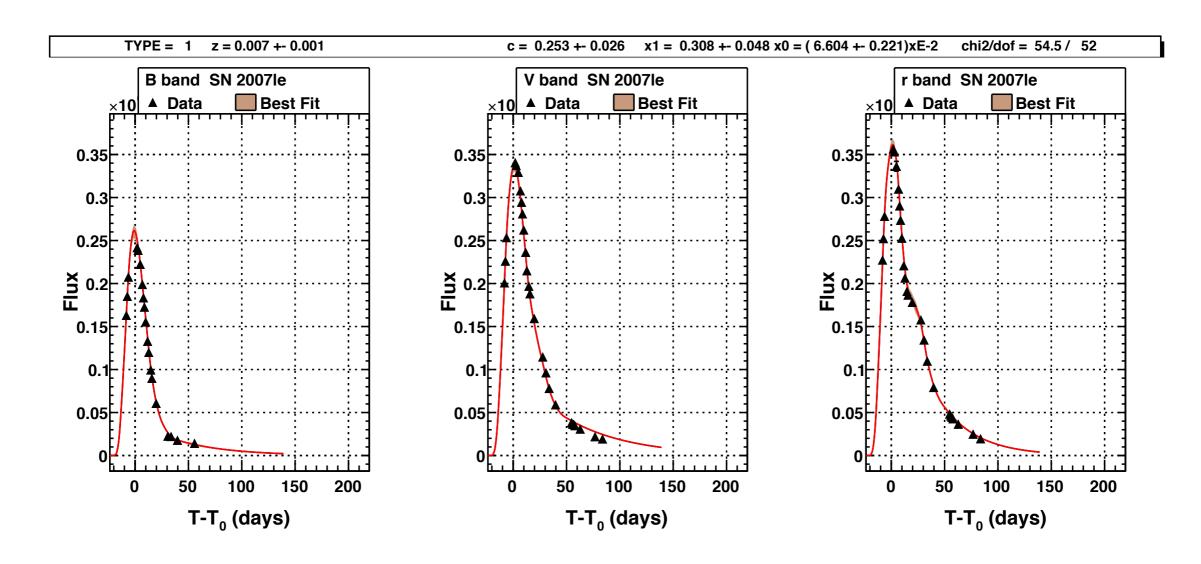
### Outline

- Simple-BayeSN: (Mandel, Scolnic, Shariff, Foley & Kirshner 2017)
  - A statistical model for the SN la colour-magnitude relation (with intrinsic variation and dust effects)
  - Implications for Optical and NIR
- BayeSN Optical+NIR LC model (Mandel et al. 2011)

### Current State of Play

- Current optical surveys are now limited by systematic uncertainties, e.g. photometric calibration error and modeling error, rather than "statistical" (number of supernovae).
- Conventional analysis method (SALT2) does not distinguish between different physical effects of intrinsic SN variations and extrinsic host galaxy dust extinction/reddening
- Scolnic et al. 2014: a different colour/mag modeling interpretation of the Hubble Diagram scatter results in a 4% systematic shift in w
- Confounding of host galaxy dust extinction/reddening with intrinsic SN la optical color variations systematically limits the accuracy and precision of SN la distances & cosmological constraints

### Conventional Approach



- SALT2 continuous light curve model fit to irregularly samples, noisy optical data (SN2007le, BVR, CfA4)
- Estimates peak apparent magnitude  $m_B$ , peak apparent color c = (B-V), and light curve shape x

#### Conventional Tripp Formula

Abs Mag = 
$$m_B - \mu = M_0 + \alpha \cdot x + \beta \cdot c$$

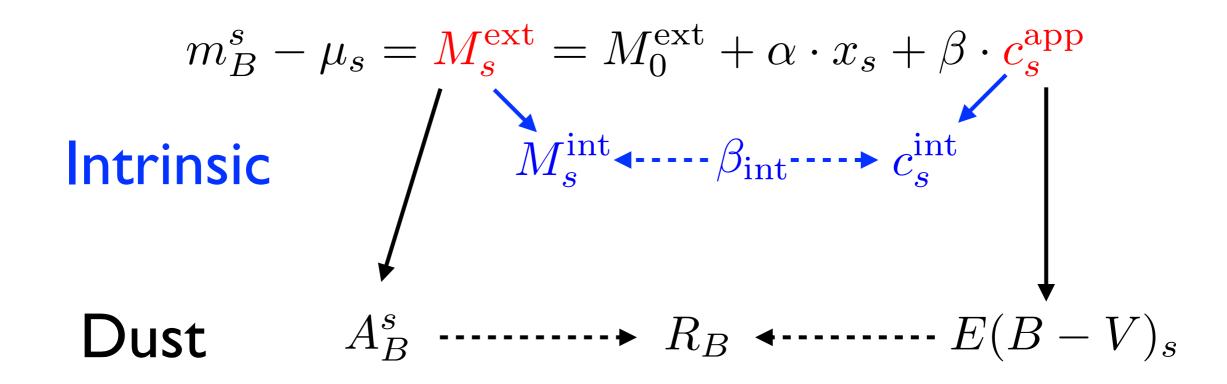
- A Simplistic Linear Model for Absolute Magnitude with width-luminosity  $(\alpha)$  and color-luminosity trends  $(\beta)$
- Typically find  $\beta \approx [\Delta Mag \text{ in B } / \Delta Color \text{ B-V}] \approx 3$ Unusually low  $\beta$  compared to normal MW interstellar dust c.f.  $R_B \approx 4.1 \ (R_V = R_B - I \approx 3.1)$ .
- $\bullet$  Problem: Regresses dust-extinguished magnitude  $M_s^{\rm ext}$  vs dust-reddened apparent color  $c_s^{\rm app}$

$$m_B^s - \mu_s = M_s^{\text{ext}} = M_0^{\text{ext}} + \alpha \cdot x_s + \beta \cdot c_s^{\text{app}}$$

- Does not distinguish between intrinsic SN la variations and host galaxy dust (only one β for all color-mag effects)
- Realistically, SN la magnitudes and colors contain both intrinsic SN la variations and host galaxy dust effects

$$M_s^{\text{ext}} = M_s^{\text{int}} + A_B^s$$
  $c_s^{\text{app}} = c_s^{\text{int}} + E(B - V)_s$ 

# Problem with Conventional Tripp Formula



Two Color-Mag effects (intrinsic  $\beta_{int}$ , dust  $R_B$ ), one  $\beta$  Slope parameter!

### Words (and Notation) Matter!

"Intrinsic": Latent parameters of SN in absence of host galaxy dust

- ullet Intrinsic Abs. Mag:  $\,M_s^{
  m int}$
- Intrinsic Color:  $c_s^{
  m int}$

Effects of Host Galaxy Dust for each SN (only positive!)

- Reddening  $E_s \equiv E(B-V)_s$
- Extinction (dimming)

$$A_B^s = R_B \times E(B - V)_s$$

"Dusty": Latent parameters of SN including effects of host galaxy dust

- Extinguished Abs. Mag  $\,M_s^{
  m ext} = M_s^{
  m int} \,+\,A_B^s\,$
- Apparent Color  $c_s^{\mathrm{app}} = c_s^{\mathrm{int}} + E(B-V)_s$

Two Physically distinct correlations cannot be captured with one  $\beta$  color-mag relation!

$$M_s^{\mathrm{int}} \sim c_s^{\mathrm{int}}$$
  
 $A_B^s \sim E(B-V)_s$ 

## What about the host galaxy dust?

### Dust Absorption vs. Wavelength of Light

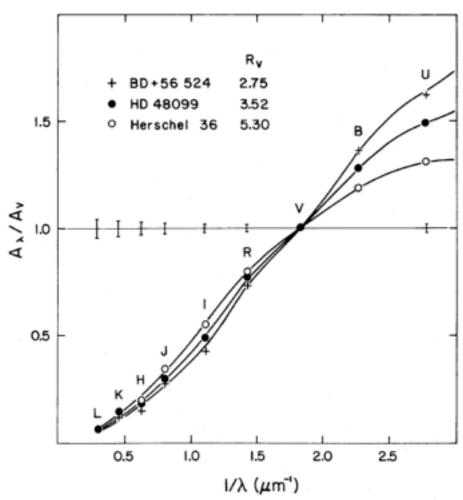
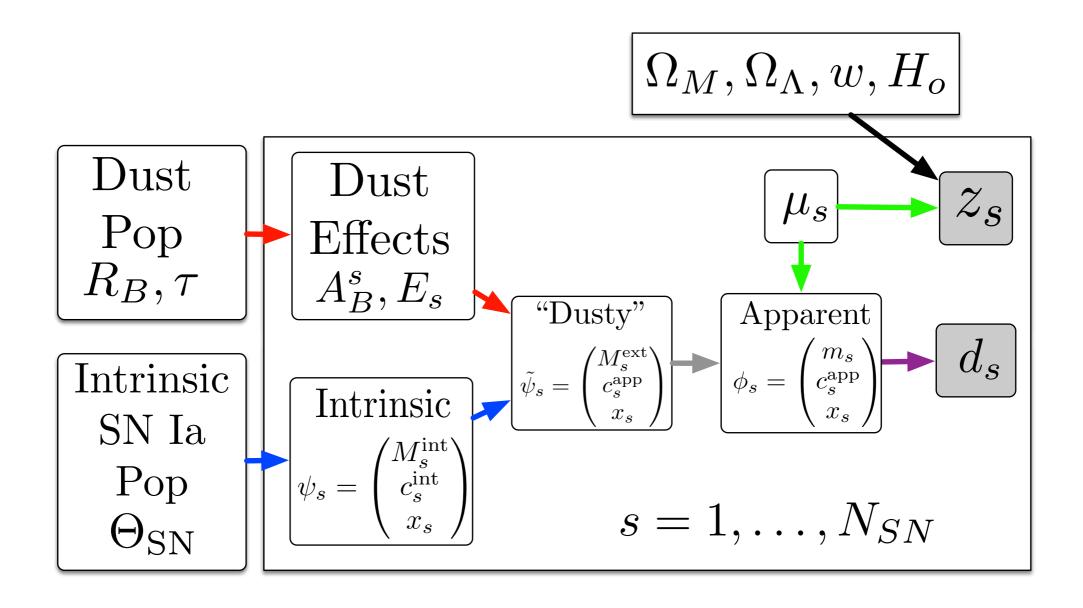


Fig. 3.—Comparison between the mean optical/NIR  $R_{\nu}$ -dependent extinction law from eqs. (2) and (3) and three lines of sight with largely separated  $R_{\nu}$  values. The wavelength position of the various broad-band filters from which the data were obtained are labeled (see Table 3). The "error" bars represent the computed standard deviation of the data about the best fit of  $A(\lambda)/A(V)$  vs.  $R_{\nu}^{-1}$  with  $a(x) + b(x)/R_{\nu}$  where  $x \equiv \lambda^{-1}$ . The effect of varying  $R_{\nu}$  on the shape of the extinction curves is quite apparent, particularly at the shorter wavelengths.

- Absorption of light (dimming)
   depends on λ, causing reddening
- Interstellar lines of sight to SN in different galaxies can pass through different random amounts of dust
- Key Parameters of Interstellar Dust (different for each SN)
  - A<sub>B</sub> ~ Amount of Dust Absorption (dimming)
  - $R_B = A_B/E(B-V) \sim Wavelength$ Dependence of Dust Absorption
- Don't really know a priori which SN are unaffected by dust; must model probabilistically

#### My Approach (Mandel+09, 11, 14, 17):

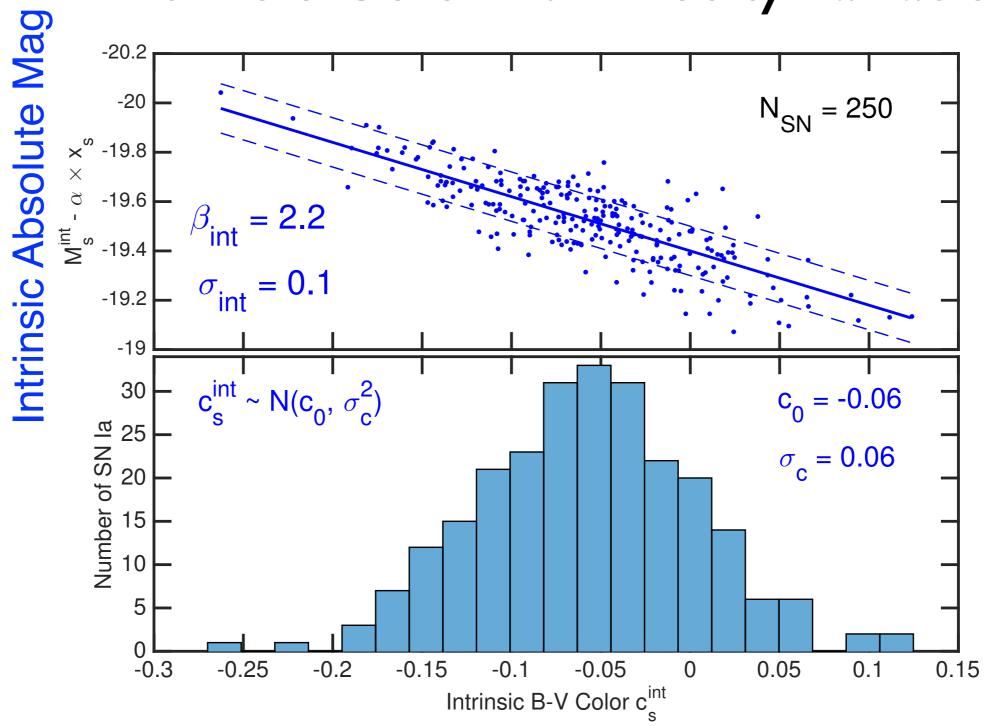
Hierarchical Bayesian / Probabilistic Generative Model



Observed SN la Data = Sum of latent random effects: intrinsic variation, dust, measurement error (Simple-BayeSN)

## Understanding the Probabilistic Generative Model via Forward Simulation

#### Intrinsic Color-Luminosity Variations



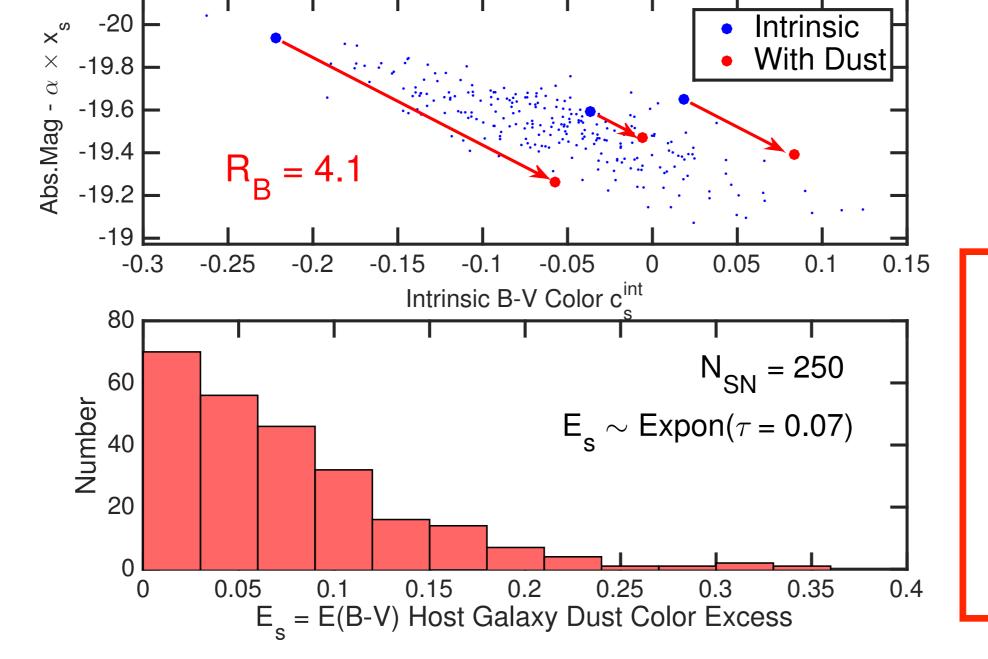
Intrinsic Color

#### Host Galaxy Dust Effects:

Reddening:  $c_s^{app} = c_s^{int} + E(B - V)_s$ 

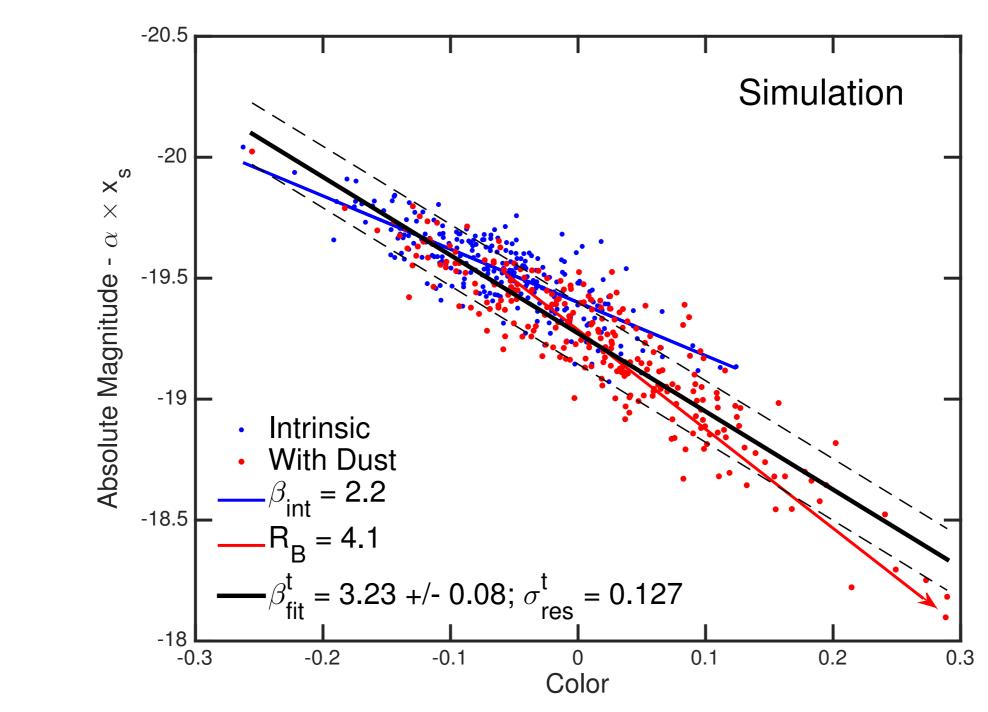
Extinction:  $M_s^{\text{ext}} = M_s^{\text{int}} + A_B^s$ 

**Dust Law:**  $R_B = R_V + 1 = A_B/E(B - V)$ 



Dust
Extinction &
Reddening
are Only
Positive!
(E<sub>s</sub> > 0)

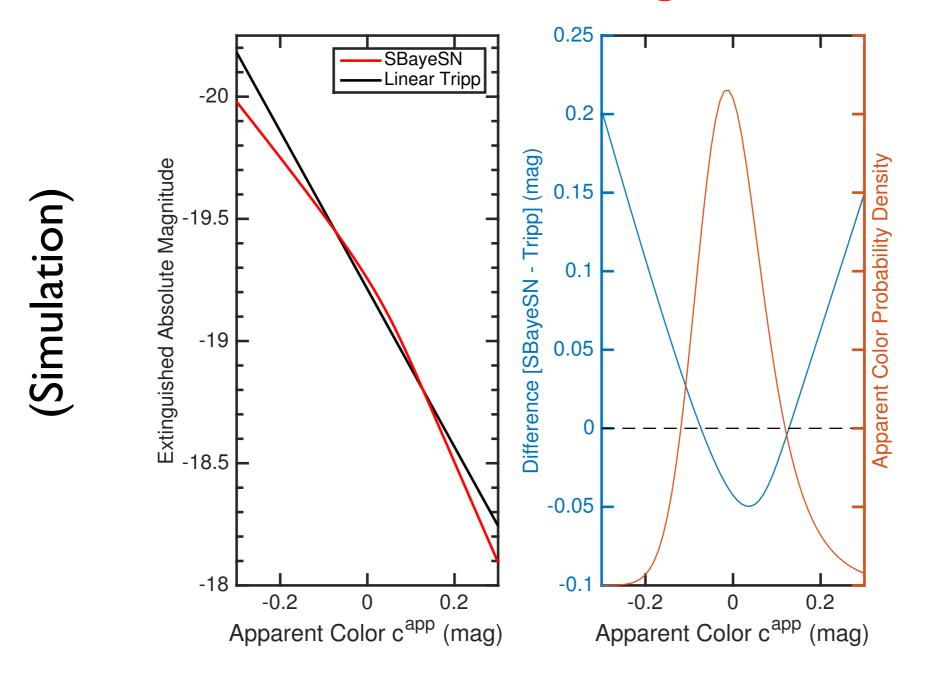
#### SN la Color-Mag Distribution (intrinsic vs dusty)



(Black: Conventional Tripp Fit)

$$m_B^s - \mu_s = M_B^{\text{ext}} = M_0^{\text{ext}} + \alpha \cdot x_s + \beta \cdot c_s^{\text{app}}$$

# Effective "Dusty" Color-Magnitude Distribution is a Convolution of the Intrinsic & Dust Distributions: Effective Color-Mag Trend is a Curve!



Model Predicts
Positive Distance
Bias for Linear
Tripp Fit
in the tails of
apparent color
distribution

Tripp Fit is a linear approx. to curve near mean apparent color

#### Inverse Problem: Statistical inference with SN la

- SN la cosmology inference based on empirical relations
- Statistical models for SN la are learned from the data
- Several Sources of Randomness & Uncertainty
  - I. Photometric (Measurement) & LC Fitting errors
  - 2. "Intrinsic Variation" = Population Distribution of SN la
  - 3. Random Peculiar Velocities in Hubble Flow
  - 4. Host Galaxy Dust: extinction and reddening.
- Observed Distributions are convolutions of these effects
- How to incorporate this all into a coherent statistical model? (How to "de-convolve"?) - Hierarchical Bayes!

### Advantages of Hierarchical Models

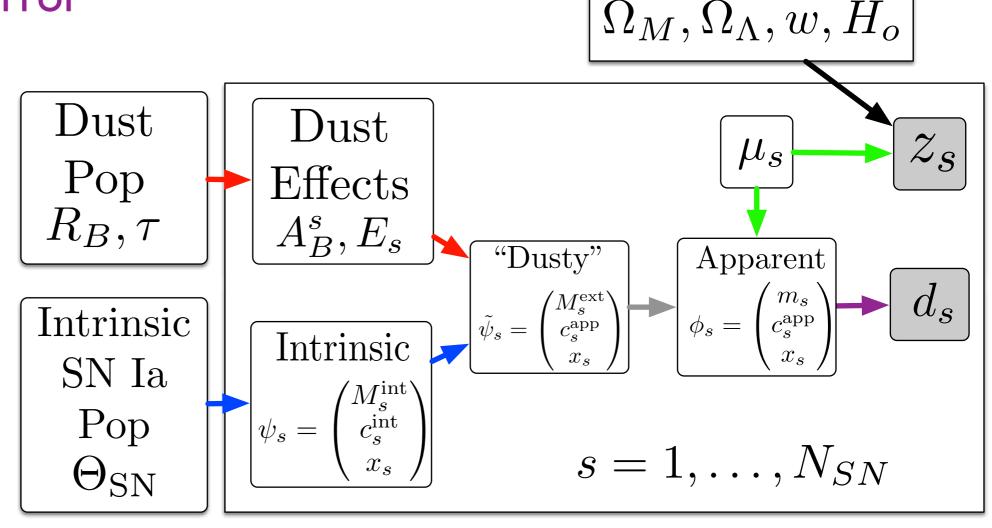
- Incorporate multiple sources of randomness & uncertainty underlying the observed data
- Express structured probability models adapted to conceptual / physical data-generating forward process
- Hierarchically Model (Physical) Populations and Individuals simultaneously: e.g. intrinsic SN Ia properties and Dust Reddening/Absorption
- Inference = probabilistically de-convolves multiple latent effects underlying data
- Full Posterior probability distribution = Global, coherent quantification of uncertainties at individual and population levels

#### Directed Acyclic Graph for SN la Inference with Hierarchical Bayesian Model (Simple-BayeSN) (Mandel et al. 2016)

- Intrinsic Variation of SN la
- Dust Extinction & Reddening
- Peculiar Velocities
- Measurement Error

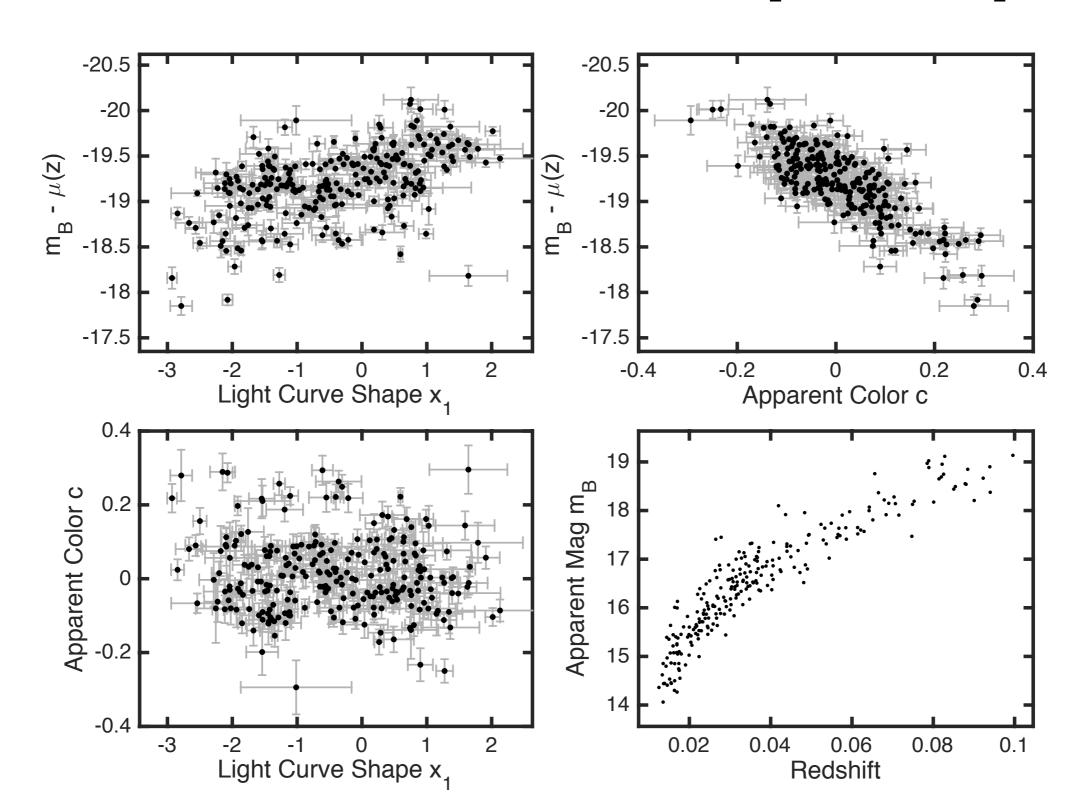
Global Joint
Posterior
Probability
Density
Conditional
on all SN
Data

Probabilistic
Graphical Model



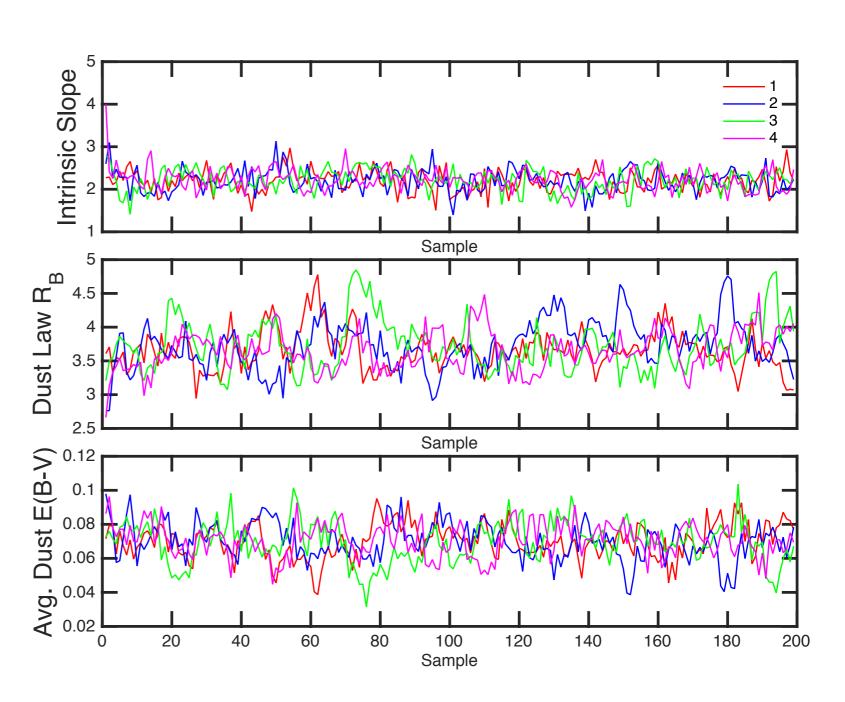
#### The Data:

Optical LC fits for 248 nearby (low-z < 0.1) SN Ia (CfA, CSP) cross-calibrated with Pan-STARRS [Scolnic+15]



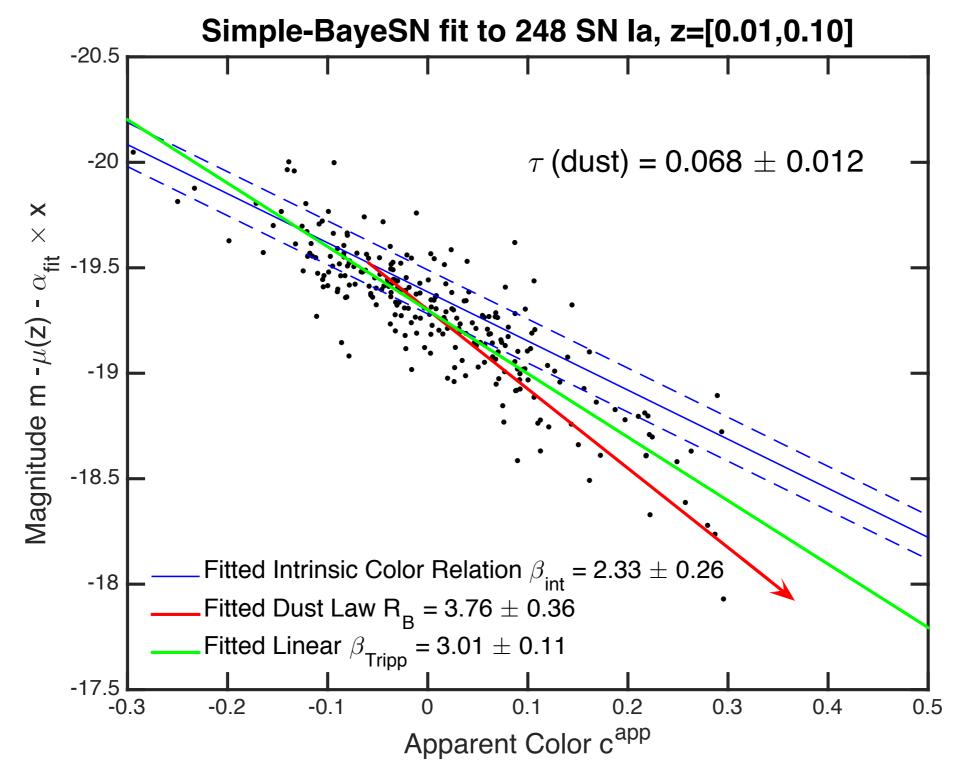
## Bayesian Posterior Inference & Statistical Computation

- Estimate Intrinsic
   Relation, Dust Law,
   Dust Population, etc.
- Gibbs Sampling utilizes conditionals of full posterior to update MCMC steps
- Explore joint posterior probability of all parameters



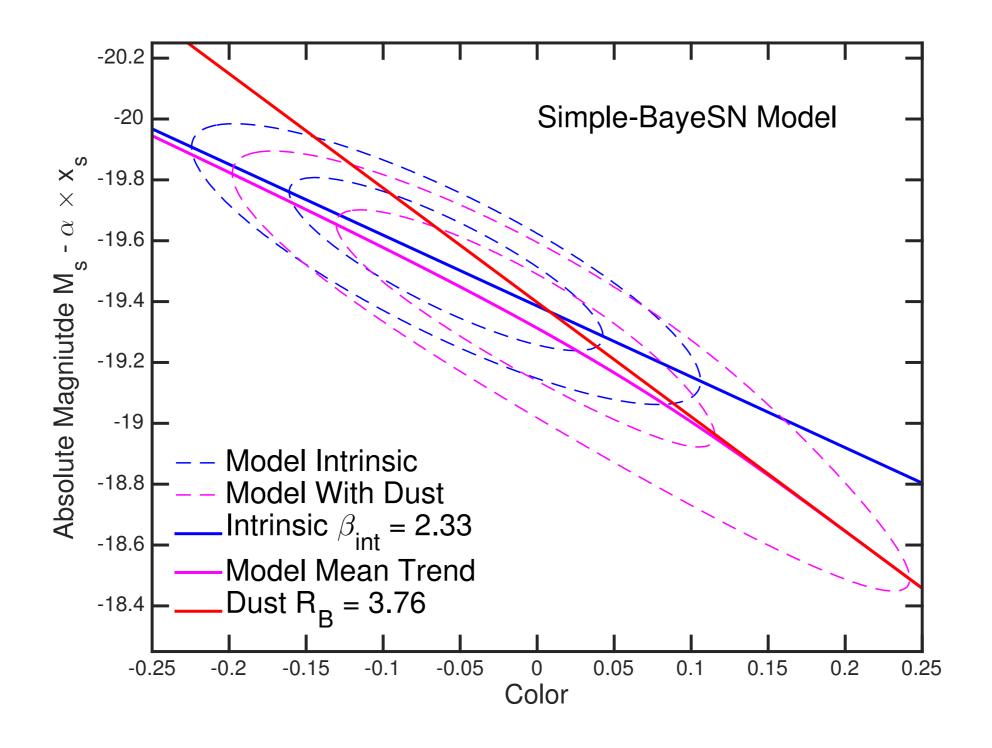
Four Parallel MCMC Chains

#### Results: Discerning Dust vs. Intrinsic Variations



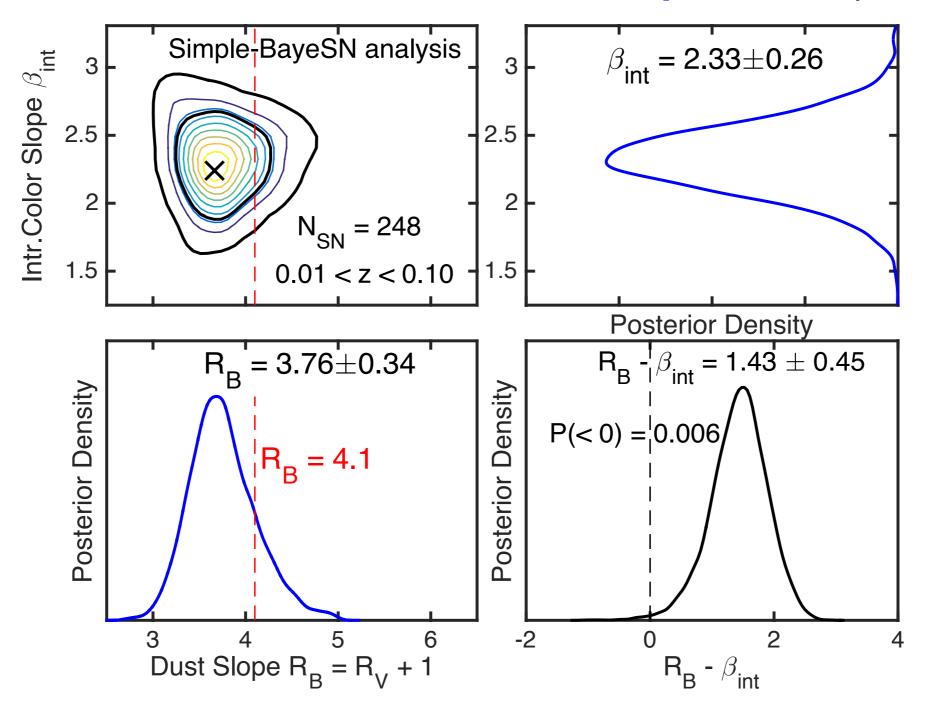
Intrinsic Color-Magnitude Slope  $\neq$  Dust Reddening Vector! (Color-Magnitude Effects NOT described by a single slope  $\beta$ !)

#### Effective Colour-Mag Distribution



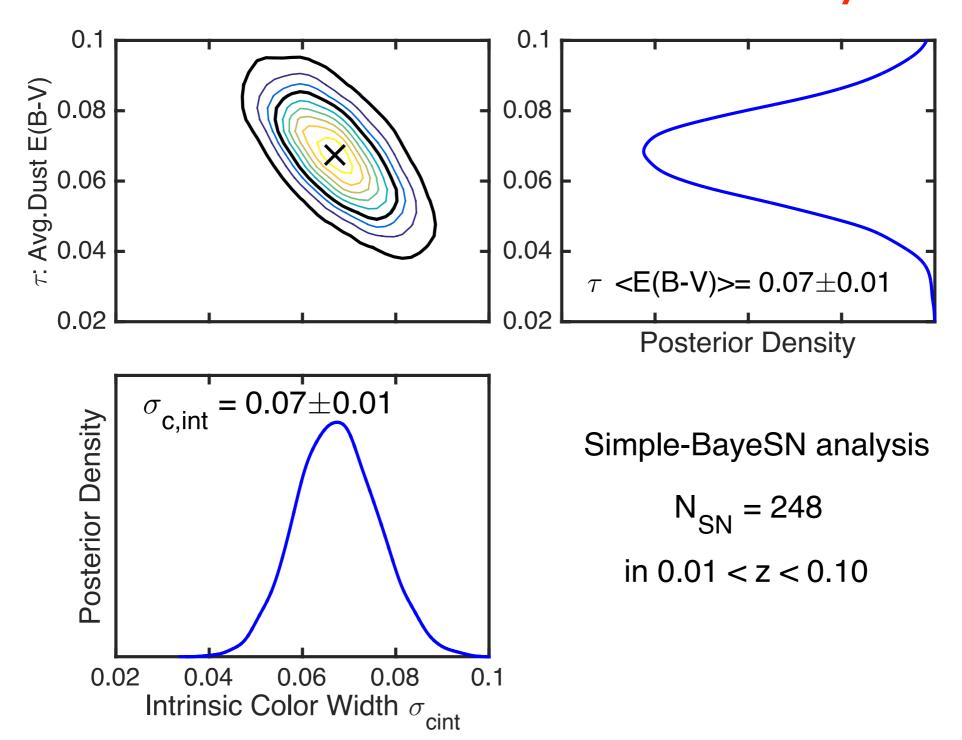
Nonlinear Mean Apparent Colour-Magnitude Relation

## Results: Inferring Dust Extinction/Reddening ( $R_B$ ) vs. Intrinsic Color-Luminosity Trend ( $\beta_{int}$ )



Dust Reddening Vector consistent with Milky Way dust  $(R_V = 3.1)$ ! Intrinsic Color-Magnitude Slope  $\neq$  Dust Reddening Vector!

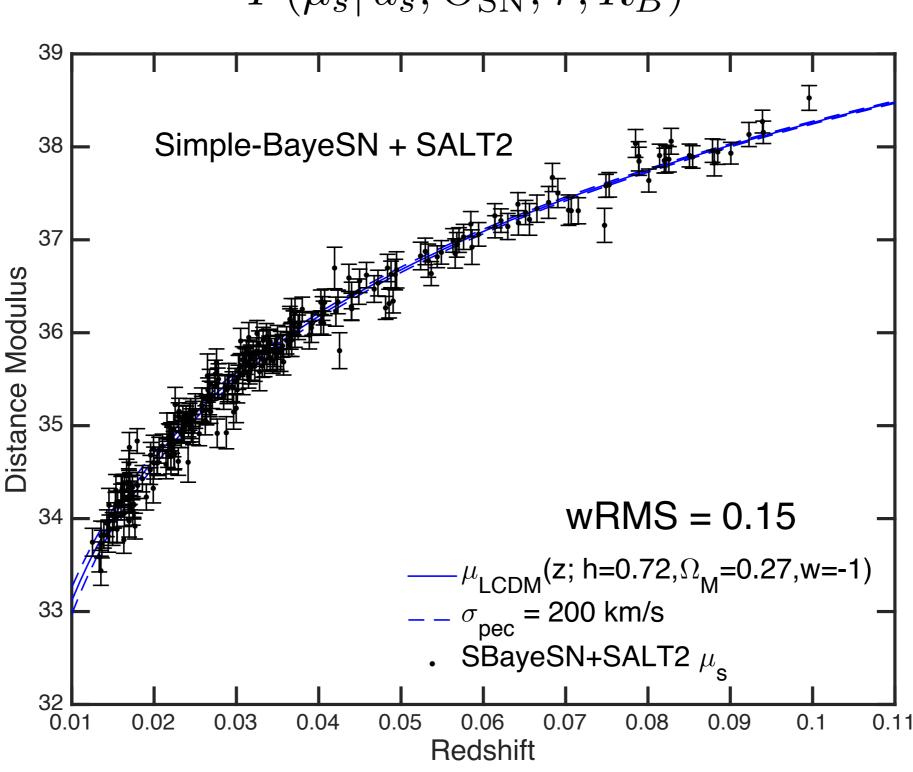
## Results: Inferring Population Distributions of SN la Intrinsic Color vs Host Galaxy Dust



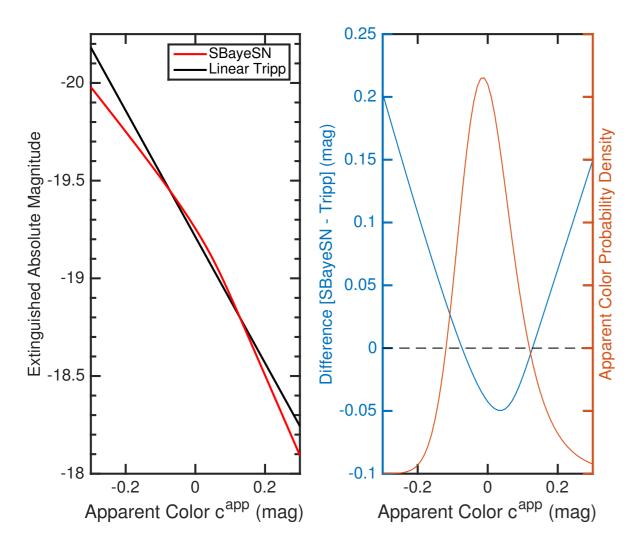
Roughly Equal Contributions to Total Apparent Color Variance

# Hubble Diagram: Use Trained Model Hyperparameters to Predict Photometric Distances based on SN Ia Light Curve Data:

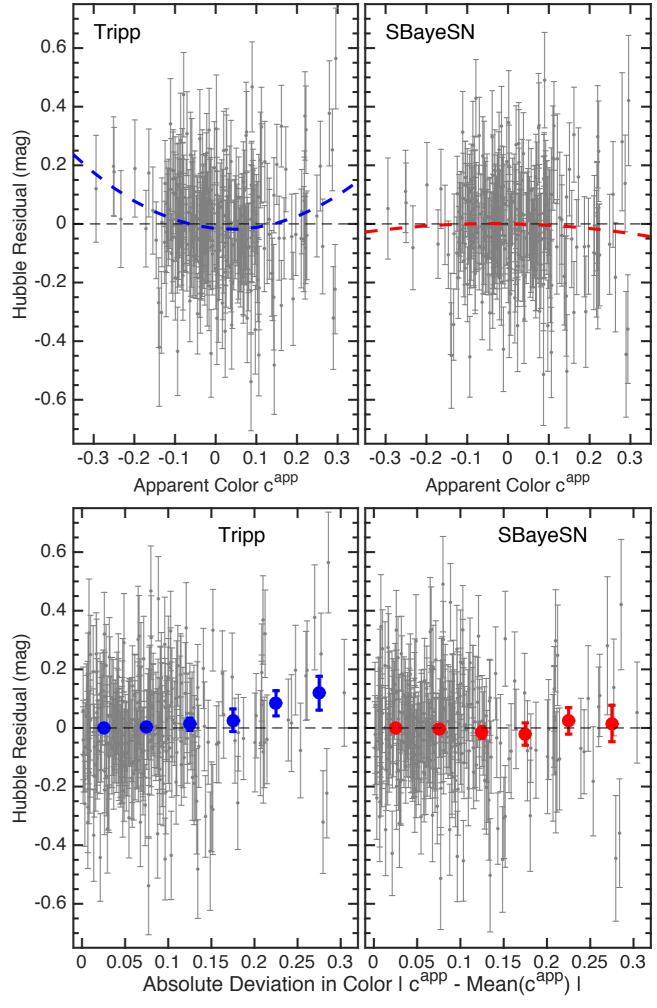
$$P(\mu_s | d_s, \hat{\Theta}_{SN}, \hat{\tau}, \hat{R}_B)$$



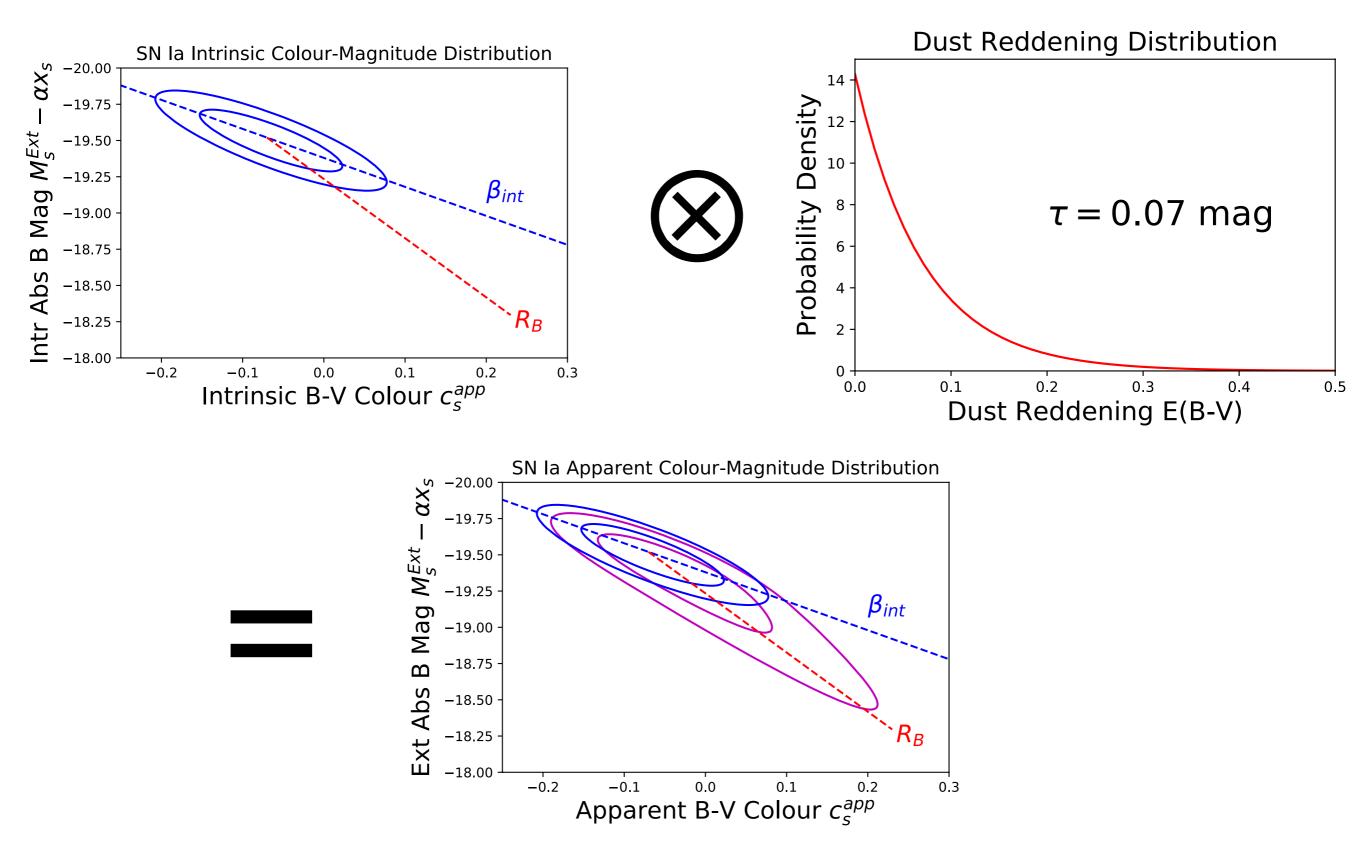
#### Hubble Residuals



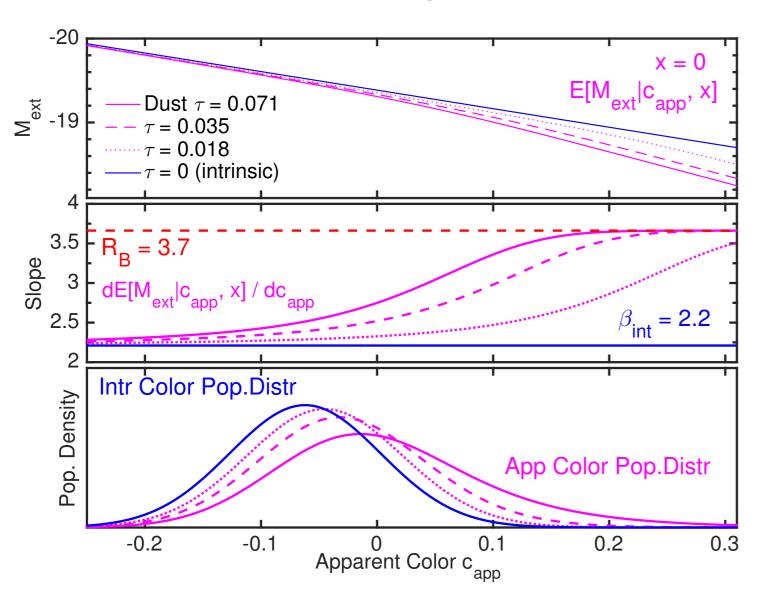
Simple-BayeSN
Corrects ~ 0.1 mag bias
in tails of SN Ia
color distribution
relative to Linear Tripp fit



#### Main Effect of Model



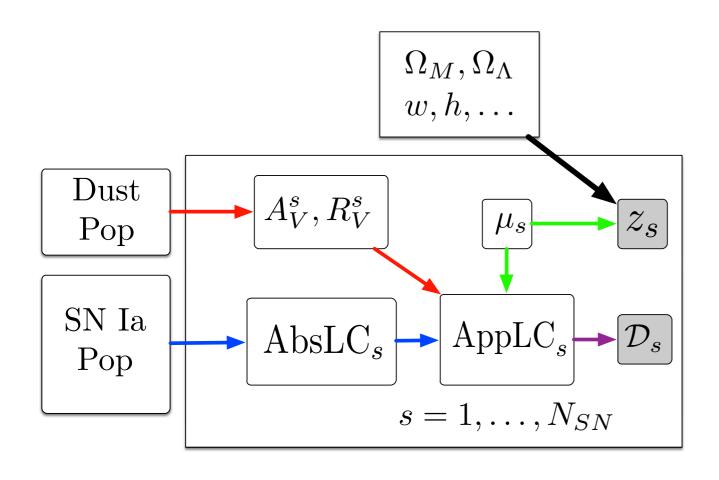
# Implications for / Advantages of NIR change effective $\tau$ = Avg. Dust



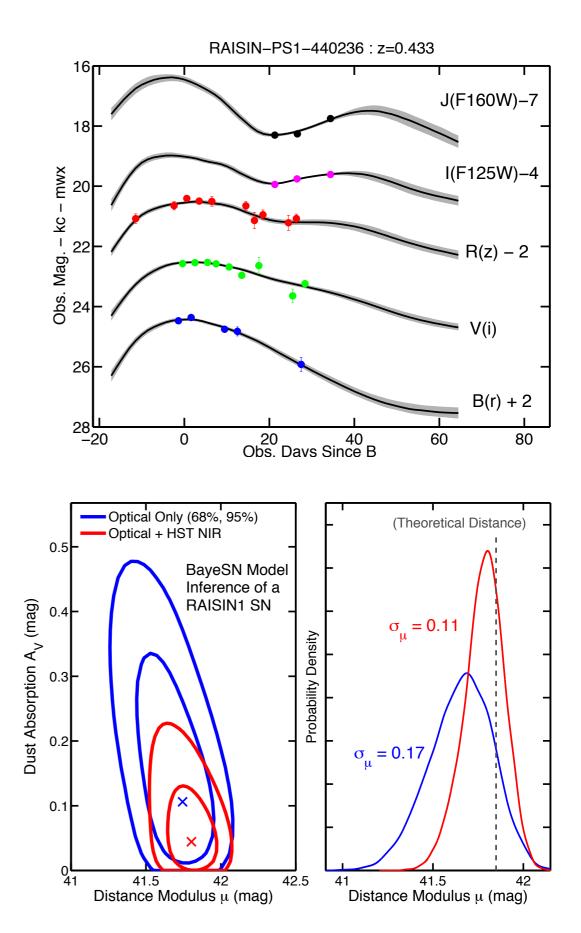
Using M<sub>NIR</sub> for standard candle, would expect a significant suppression of effect

For any combination of  $M_F$  and  $c_{F-G}$ , effect depends on relative colour-mag slopes and dispersions of intrinsic vs. dust components

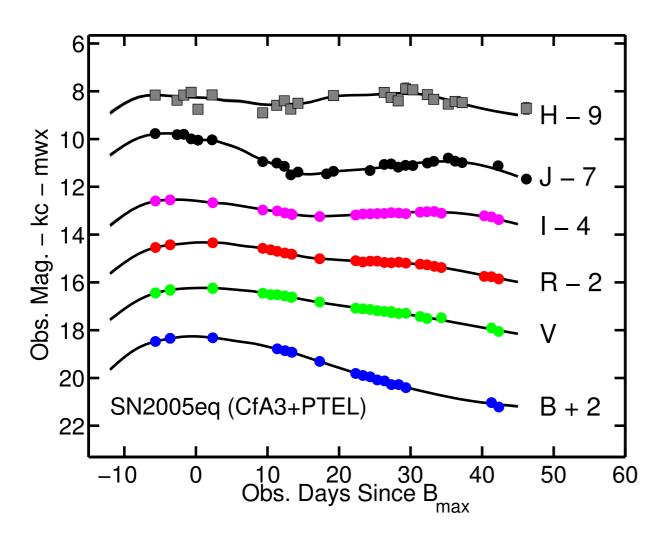
# BayeSN: Optical+NIR LC model



Mandel, Narayan & Kirshner 2011



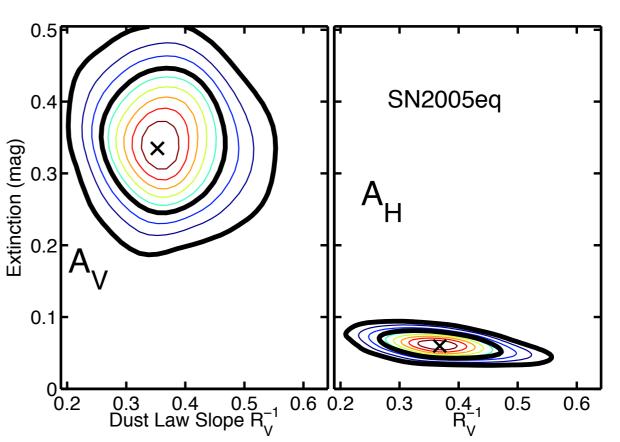
#### Optical+NIR Hierarchical Model Inference



PTEL+CfA3 Light-curves (Moderate Extinction)

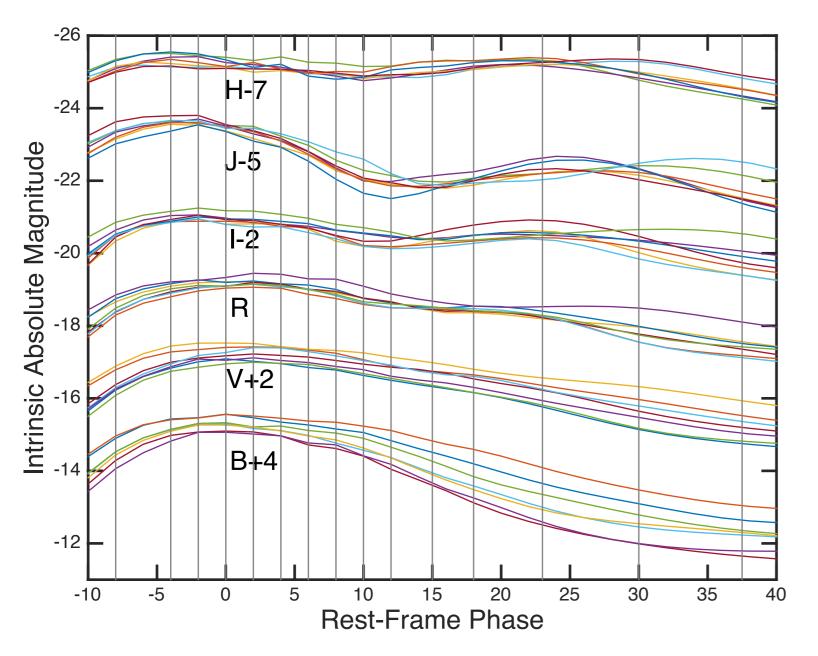
Mandel, Narayan & Kirshner (2011)

#### Marginal Posterior of Dust



#### BayeSN: Modeling SN Ia Light curves: Learning the population distribution of LCs

#### Beyond one parameter: a "non-parametric" approach

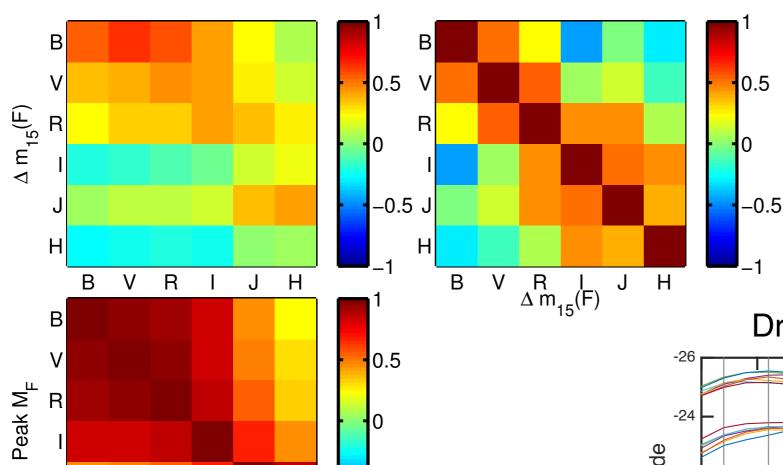


Mandel, Narayan & Kirshner 2011

- Many Local Parameters
   describing intrinsic absolute
   magnitude and shape of LC
   over short time segments at
   each rest-frame λ-filter
- Goal: Learn from the data the (non-stationary) Covariance Structure of SN Ia intrinsic absolute light curves over multiple λ-filters and phases t
- Models Gaussian Process joint intrinsic distribution of LCs (over t and λ-filter)

#### BayeSN Light Curve Population Analysis

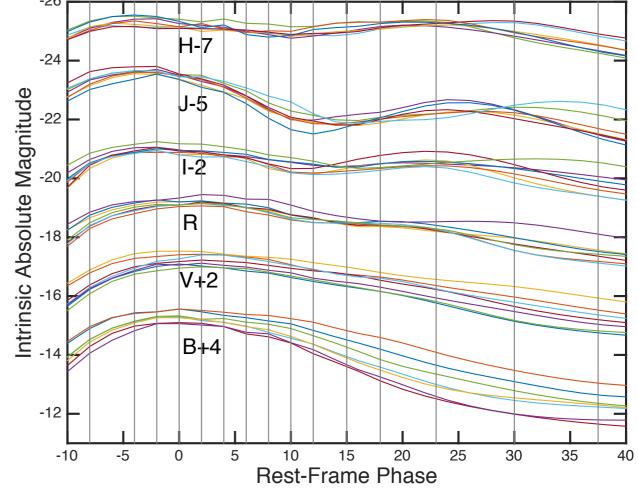
Mandel, Narayan & Kirshner 2011



-0.5

Learning the Intrinsic Covariance of SN Ia LC Population

Draws from Population Distribution



Correlation Map for Luminosities and LC Decline Rates

Peak M<sub>E</sub>

Н

Η