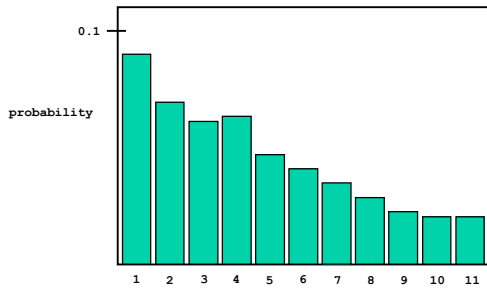


Distribution of Integer Values



- many small values means better compression

Recap: Taking Differences

armadillo	127	312	678	946	...
alligator	34	68	131	241	268 312 414 490 ...
dog	12	29	41	87	111 143 189 234 267 312 333 378 ...

- idea: use efficient coding for docIDs, frequencies, and positions in index
- first, take differences, then encode those smaller numbers:
- example: encode alligator list, first produce differences:
 - if postings only contain docID:
(34) (68) (131) (241) ... becomes (34) (34) (43) (110) ...
 - if postings with docID and frequency:
(34,1) (68,3) (131,1) (241,2) ... becomes (34,1) (34,3) (43,1) (110,2) ...
 - if postings with docID, frequency, and positions:
(34,1,29) (68,3,9,46,98) (131,1,46) (241,2,45,131) ...
becomes (34,1,29) (34,3,9,37,52) (43,1,46) (110,2,45,86) ...
 - afterwards, do encoding with one of many possible methods

Recap: var-byte Compression

- simple byte-oriented method for encoding data
- encode number as follows:
 - if < 128 , use one byte (highest bit set to 0)
 - if $< 128 * 128 = 16384$, use two bytes (first has highest bit 1, the other 0)
 - if $< 128^3$, then use three bytes, and so on ...
- examples: $14169 = 110 * 128 + 89 = \boxed{1101110} \boxed{01011001}$
 $33549 = 2 * 128 * 128 + 6 * 128 + 13 = \boxed{10000010} \boxed{10000110} \boxed{00001101}$
- example for a list of 4 docIDs: after taking differences
 (34) (178) (291) (453) ... becomes (34) (144) (113) (162)
- this is then encoded using six bytes total:
 - 34 = $\boxed{00100010}$
 - 144 = $\boxed{10000001} \boxed{00010000}$
 - 113 = $\boxed{01110001}$
 - 162 = $\boxed{10000001} \boxed{00100010}$
- not a great encoding, but fast and reasonably OK
- implement using char array and char* pointers in C/C++

Rice Coding:

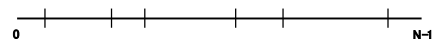
- consider the average or median of the numbers (i.e., the gaps)
- simplified example for a list of 4 docIDs: after taking differences
 (34) (178) (291) (453) ... becomes (34) (144) (113) (162)
- so average is $g = (34 + 144 + 113 + 162) / 4 = 113.33$
- Rice coding: round this to smaller power of two: $b = 64$ (6 bits)
- then for each number x , encode $x-1$ as
 $(x-1)/b$ in unary followed by $(x-1) \bmod b$ binary (6 bits)
 - $33 = 0 * 64 + 33 = 0 \quad 100001$
 - $143 = 2 * 64 + 15 = 110 \quad 001111$
 - $112 = 1 * 64 + 48 = 10 \quad 110000$
 - $161 = 2 * 64 + 33 = 110 \quad 100001$
- note: there are no zeros to encode (might as well deduct 1 everywhere)
- simple to implement (bitwise operations)
- better compression than var-byte, but slightly slower

Golomb Coding:

- example for a list of 4 docIDs: after taking differences
 (34) (178) (291) (453) ... becomes (34) (144) (113) (162)
- so average is $g = (34 + 144 + 113 + 162) / 4 = 113.33$
- Golomb coding: choose $b \sim 0.69 * g = 78$ (usually not a power of 2)
- then for each number x , encode $x-1$ as
 $(x-1)/b$ in unary followed by $(x-1) \bmod b$ in binary (6 or 7 bits)
- need fixed encoding of number 0 to 77 using 6 or 7 bits
- if $(x-1) \bmod b < 50$: use 6 bits else: use 7 bits
- e.g., $50 = 110010 \ 0$ and $64 = 110010 \ 1$
 - $33 = 0 * 78 + 33 = 0 \quad 100001$
 - $143 = 1 * 78 + 65 = 10 \quad 1100111$
 - $112 = 1 * 78 + 34 = 10 \quad 100010$
 - $161 = 2 * 78 + 5 = 110 \quad 000101$
- optimal for random gaps (dart board, random page ordering)

Rice and Golomb Coding:

- uses parameters b – either global or local
- local (once for each inverted list) vs. global (entire index)
- local more appropriate for large index structures
- but does not exploit clustering within a list
- compare: random docIDs vs. alpha-sorted vs. pages in book
 - random docIDs: no structure in gaps, global is as good as local
 - pages in book: local better since some words only in certain chapters
 - assigning docIDs alphabetically by URL is more like case of a book
- instead of storing b , we could use N (# of docs) and f_t :
 $g = (N - f_t) / (f_t + 1)$
- idea: e.g., 6 docIDs divide 0 to $N-1$ into 7 intervals



Gamma and Delta Coding:

- no parameters such as b: each number coded by itself
- simplified example for a list of 4 docIDs: after taking differences (34) (178) (291) (453) ... becomes (34) (144) (113) (162)
- imagine each number as binary with leading 1: 34 = 100010
- then for each number x, encode x-1 as $1 + \text{floor}(\log(x))$ in unary followed by $\text{floor}(\log(x))$ bits
- thus, 1 = 0 and 5 = 110 01
- 33 = 111110 00001
- 143 = 11111110 0001111
- 112 = 1111110 110000
- 161 = 11111110 0100001
- note: good compression for small values, e.g., frequencies
- bad for large numbers, and fairly slow
- Delta coding: Gamma code; then gamma the unary part

Simple9 (S9) Coding: (Anh/Moffat 2004)

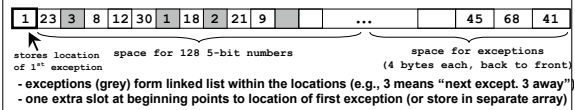
- idea: produce a word-aligned code – basic unit 32 bits
- try to pack several numbers into one word (32 bits)
- each word is split into 4 control bits and 28 data bits
- what can we store in 28 bits?
 - 1 28-bit number
 - 2 14-bit numbers
 - 3 9-bit numbers (1 bit wasted)
 - 4 7-bit numbers
 - 5 5-bit numbers (3 bits wasted)
 - 7 4-bit numbers
 - 9 3-bit numbers (1 bit wasted)
 - 14 2-bit numbers
 - 28 1-bit numbers
- then use other 4 bits to store which of these 9 cases is used (assumption for simplicity: all numbers that we encounter need at most 28 bits)

Simple9 (S9) Coding: (continued)

- store and retrieve numbers using fixed bit masks
- algorithm:
 - do the next 28 numbers fit into one bit each?
 - if yes: use that case
 - if no: do the next 14 numbers fit into 2 bits each?
 - if yes: use that case
 - if no: do the next 9 numbers fit into 3 bits each?
 - ... and so on ...
- fast decoding: only one if-decision for every 32 bits
- compare to varbyte: one or more decisions per number
- decent compression: can use < 1 byte for small numbers
- related techniques: relate10 and carryover12
- Simple16 (S16): contains several optimizations over S9

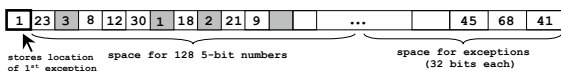
PFOR-DELTA: (Heman 2005)

- idea: compress/decompress many values at a time (e.g., 128)
- how many bits per number?
 - different choice for each number? (decoding slow due to branches)
 - or one size fits all? (bad compression)
- good compromise: choose size such that 90% fit, code the other 10% as exceptions
- suppose in next 128 numbers, 90% are < 32: choose b=5
- allocate 128 x 5 bits, plus space for exceptions
- exceptions stored at end as ints (using 4 bytes each)
- example: b=5 and sequence 23, 41, 8, 12, 30, 68, 18, 45, 21, 9, ...



PFOR-DELTA: (ctd.)

- there may sometimes be "forced exceptions":
 - in example: if there are more than 2^b consecutive numbers < 2^b , then encode the 2^b -th number as exception so we can keep a simple linked list structure
- very simple and fast decoding
 - first, copy the 128 b-bit numbers into integer array (very fast per element)
 - then traverse linked list and patch the exceptions (slower per element)
 - if we keep exceptions < 10%, this will be extremely fast
 - first phase: unroll loops for best performance – hardcode for each b
- note: always uncompress next 128 posts into temp array
 - do not uncompress entire list into one long array: slower since out of cache
- simple effective improvement: do not use 32 bits / except
 - use maximum among next 128 numbers to choose number of bits
 - 10-20% better compression with basically same speed (if done properly)



Some Experimental Numbers

- results from Witten/Moffat/Bell book
- includes golomb, gamma, delta, but not others above
- data with "locality": books, or web pages sorted by URL
 - word occurrences not uniform within a book, but often clustered in one part
- in this case, interpolative better
- see book for details

Table 3.1 Statistics of document collections.

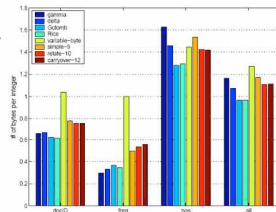
		Collection			
		Bole	GNUlib	Comcast	TREC
Documents	N	31,101	64,343	261,829	741,864
Number of terms	F	884,894	2,570,305	22,805,520	333,338,738
Distinct terms	n	8,965	48,488	36,680	535,346
Index pointers	f	701,412	2,226,300	12,878,418	134,954,414
Total size (Mbytes)		4.33	14.05	131.86	2070.29

Table 3.2 Compression of inverted files in bits per pointer.

Method	Bits per pointer			
	Bole	GNUlib	Comcast	TREC
Global methods				
Unary	382	389	487	1918
Binary	19.00	18.00	18.00	20.00
Bernoulli	5.96	5.98	5.96	6.03
γ	6.35	5.98	4.25	6.38
Observed frequency	5.96	4.02	4.25	5.97
Local methods				
Bernoulli	6.88	6.18	5.40	5.94
Hyperbolic	5.75	5.18	4.85	5.88
Shrunk Bernoulli	5.65	4.70	4.20	5.44
Batched frequency	5.98	4.84	4.02	5.41
Interpolative	5.28	5.08	3.87	5.18

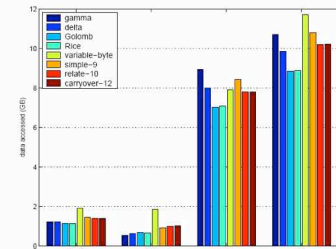
Some Newer Experimental Numbers

- by Xiaohui Long, 2006
- includes golomb, rice, gamma, delta, S9 and its variants
- lists weighted by frequency in queries
 - not total index size, but size of compressed data fetched per query
 - but also tracks index size reasonably well
- bytes per compressed integer in list
- var-byte bad for frequency
 - always at least one byte
- S9 and variants much better
- but not as good as others



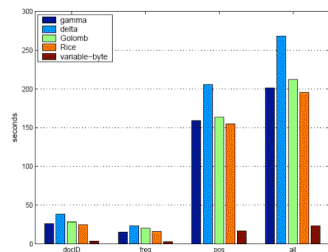
Some Experimental Numbers (ctd.)

- another perspective: index data access in GB / 1000 queries
- note: position data much larger than docID and frequency
 - reason: several positions/posting, and larger numbers on average
- relative differences in cost smaller if we have positions



Some Experimental Numbers (ctd.)

- CPU cost for uncompressed (Xiaohui Long, 2006)
- cost per 1000 queries on 8 million pages (not fully optimized)
- var-byte MUCH faster than the others
- later: other newer techniques (S9, PFORDELTA, etc.) also fast



Hacking up Rice Coding:

- can we implement Rice coding much faster than known?
- note similarity to PFORDELTA: unary part == exception
- more bits for binary part == fewer exceptions
- idea: when compressing 128 integers:
 - store 128 binary parts followed by 128 unary parts
 - during decompression, first retrieve the 128 binary parts
 - use same bit-copy routines as in PFORDELTA
 - then apply unary parts to patch things up
 - of course, more exceptions as in PFORDELTA
- second idea: process 8 bits of the unary data at once
 - switch statement with 256 cases and 2000 lines of code - but fast!

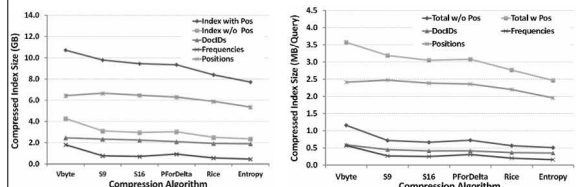
Experimental Setup:

- set of 7.4 million web pages
- Excite query trace from 1999

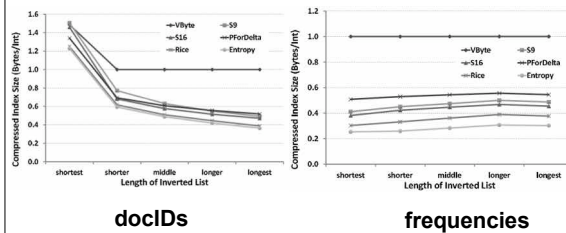
Trace	Queries	Unique Queries	Query Length	List Length
Excite	1,500,005	536,239	2.59	220,331
AOL(time)	1,861,054	536,239	2.75	208,426
AOL(user)	1,920,154	536,239	2.80	204,663

- remove duplicate queries (to take result caching into account)
- select 1000 consecutive queries, run in main memory
- 3.2 Ghz Pentium 4, gcc compiler, ...
- used var-byte for very short lists

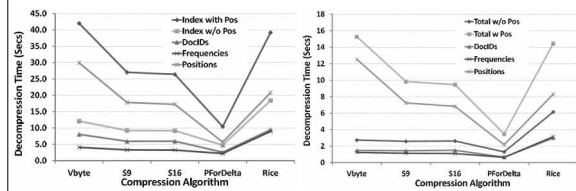
Compressed Size:



Bytes per Integer:



Decompression Times:



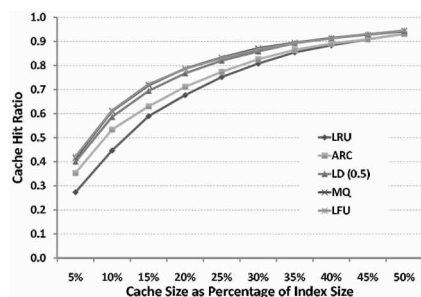
Decompression Speeds: (millions of integers / second)

Algorithm	Total w/o Pos	Total w Pos	DocID	Freq	Pos
VByte	416.32	183.66	381.90	457.56	132.86
S9	439.49	285.27	391.73	500.51	230.04
S16	433.78	296.53	376.92	510.86	243.76
PForDelta	868.70	803.11	855.79	882.01	763.67
Rice	185.39	194.20	190.44	180.59	200.72

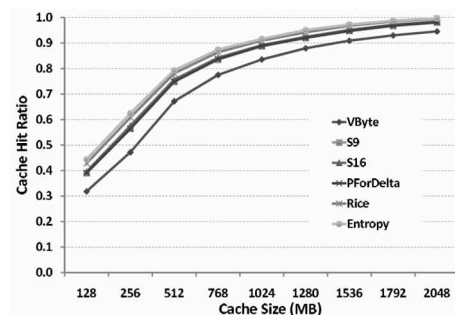
Index Caching - Algorithms

- study of replacement policies for list caching
- most common algorithm: LRU (Least Recently Used)
- alternative: LFU (Least Frequently Used)
- discussion: LRU vs. LFU
 - LRU good for changing hot items, LFU for more static
 - out of cache, out of mind ?
- Landlord: generalization of weighted caching
 - analyzed for weighted caching (Cao/Irani/Young)
 - modification: give longer leases to repeat tenants
- Multi-Queue (MQ) (Zhou/Philbin/Li 2001)
- Adaptive Replacement Policy (Megiddo/Modha 2003)

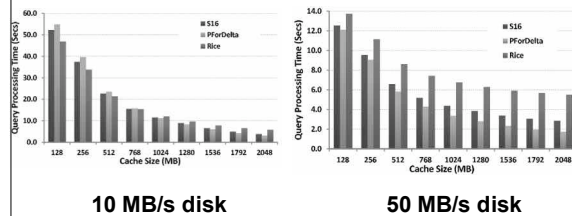
Comparison of Caching Policies:



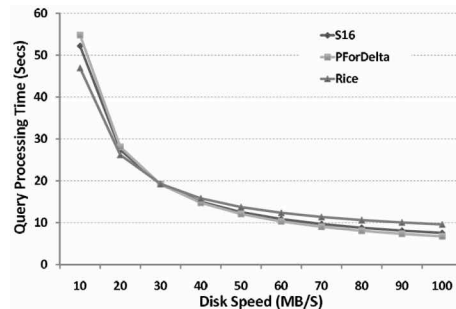
Impact of Compression:



Total Cost for Fixed Disk Speed:



Effect of Disk Speed:



Conclusions

- Great differences in speed and compression
- Old story: var-byte is not as good in compression, but much faster and thus used in practice
- New story (last 2-3 years): there are other techniques that are faster and also compress much better
- Decompression speeds: GBs per second !
- Bit- versus byte-alignment is not the issue
- But you need to be able to use fixed masks and avoid branch mispredicts (simple ideas, long code)
- LRU not a good caching policy
- Compression has caching consequences ...
- Better compression gives higher cache hit ratio

Index Compression in Google (1998)

- see paper for details
- forward barrel: postings during sorting, before final index constructed
- inverted barrels: inverted index structure: 27 bits / docID, 5 bits / freq
- plus extra context data about each hit (each occurrence)
- was replaced by newer technique ...

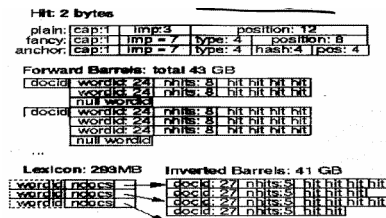


Figure 3. Forward and Reverse Indexes and the Lexicon