Assignment 2

Math 351

Upload the .tex source and the .pdf output containing your solutions to the following exercises on Polylearn on or before Sunday.

Exercise 1. Reproduce the type on this page and below this sentence.

Every mathematical statement, such as $\sum_{n=1}^{\infty} 1/n^2 = \pi^2/6$, should be part of a sentence. Even equations need punctuation!

The notation $\lim f(x) = L$ means that for every $\varepsilon > 0$ there is a $\delta > 0$ such that $|x-a| < \delta$ implies $|f(x)-L| < \varepsilon$. An incorrect way to typeset this

$$\forall (\varepsilon > 0) \exists (\delta > 0) \ni (|x - a| < \delta \implies |f(x) - L| < \varepsilon).$$

The symbols \forall , \exists , \Rightarrow , and \implies should be used only in the context of the mathematical subject of formal logic and should not replace the words "for all", "there exists", and "such that", and "implies".

One of your instructor's favorite mathematical statements is

$$n! \sim \sqrt{2\pi n} \left(\frac{n}{e}\right)^n$$

otherwise known as Stirling's formula. As an example, 100! is approximately equal to $\sqrt{200\pi}(100/e)^{100} \approx 9.32 \times 10^{157}$.

The following is true:

$$\left| \int_{1}^{a} \frac{\sin x}{x} \, dx \right| \le \int_{1}^{a} \left| \frac{\sin x}{x} \right| \, dx$$
$$\le \int_{1}^{a} \frac{1}{x} \, dx$$
$$= \ln a.$$

After first simplifying using the exponential and the natural log functions, L'Hôpital's rule can be used to evaluate $\lim_{x\to 2^-} (4-x)^{1/(2-x)}$. Take $\mathbf{x}, \mathbf{y} \in \mathbb{R}^n$. The inner product of \mathbf{x} and \mathbf{y} is defined by $\langle \mathbf{x}, \mathbf{y} \rangle = \mathbf{x}^{\mathsf{T}} \mathbf{y}$.

It follows that

$$\langle \mathbf{x}, \mathbf{x} \rangle = \mathbf{x}^{\mathsf{T}} \mathbf{x} = \|\mathbf{x}\|^2,$$

which is a non-negative real number.

Exercise 2. Please share your top three (or bottom three, how would I know?) mathematical statements, being sure to use full English sentences and proper punctuation.

An assignment which does this in an interesting way or makes amusing use of mathematical type setting will earn the coveted $\mbox{\sc in}\mbox{\sc TEXer}$ of the week distinction.