Assignment 0

Work Summary:

I completed all the tasks shown below.

Task 1:

In your terminal, run: conda info

Result:

I performed this task on my Windows PC. This was before I configured Anaconda to my liking, but hopefully shows what you were looking for.

```
(base) C:\Users\Gundam>conda info
    active environment : base
   active env location : D:\anaconda3
            shell level : 1
user config file : C:\Users\Gundam\.condarc
populated config files : C:\Users\Gundam\.condarc
          conda version : 23.7.2
   conda-build version : 3.26.0
         python version : 3.11.4.final.0
      virtual packages : __archspec=1=x86_64
                           __cuda=12.2=0
                             _win=0=0
      base environment : D:\anaconda3 (writable)
     conda av data dir : D:\anaconda3\etc\conda
 conda av metadata url : None
           channel URLs : https://repo.anaconda.com/pkgs/main/win-64
                           https://repo.anaconda.com/pkgs/main/noarch
https://repo.anaconda.com/pkgs/r/win-64
                           https://repo.anaconda.com/pkgs/r/noarch
                           https://repo.anaconda.com/pkgs/msys2/win-64
                           https://repo.anaconda.com/pkgs/msys2/noarch
          package cache : D:\anaconda3\pkgs
      envs directories : D:\anaconda3\envs
                           C:\Users\Gundam\.conda\envs
                           C:\Users\Gundam\AppData\Local\conda\conda\envs
               platform : win-64
             user-agent: conda/23.7.2 requests/2.31.0 CPython/3.11.4 Windows/10 Windows/10.0.19045
          administrator : True
             netrc file : None
           offline mode : False
base) C:\Users\Gundam>
```

Task 2:

- $1. \ Run \ \textbf{all} \ of the \ python \ commands \ in \ the \ table \ "Linear \ Algebra \ Equivalents"$
- 2. *Perform this task in IPython/Jupyter and paste the results into my report

Jupyter Notebook:

There were so many commands in that section.

Task 2

September 12, 2023

```
[143]: import numpy as np
      from scipy import io, integrate, linalg, signal
      from scipy.sparse.linalg import cg, eigs
      a = np.array((1,1,23,21,23,123,12))
  [5]: np.ndim(a)
  [5]: 1
  [8]: np.size(a)
  [8]: 7
  [9]: a.shape
  [9]: (7,)
 [10]: np.block([[a,a],[a,a]])
 [10]: array([[ 1,
                     1, 23, 21, 23, 123, 12,
                                                   1,
                                                      1, 23, 21,
                                                                     23, 123,
               12],
             [ 1,
                     1, 23, 21, 23, 123, 12,
                                                  1, 1, 23, 21, 23, 123,
               12]])
 [11]: a[-1]
 [11]: 12
 [28]: B = np.array((1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16)).reshape((4,4))
 [28]: array([[ 1, 2,
                       3, 4],
             [5, 6, 7, 8],
             [ 9, 10, 11, 12],
             [13, 14, 15, 16]])
 [29]: B[1,1]
```

```
[29]: 6
[26]: B[-3:]
[26]: array([[5, 6, 7, 8],
             [ 9, 10, 11, 12],
             [13, 14, 15, 16]])
[27]: B[0:3,1:2]
[27]: array([[ 2],
             [6],
             [10]])
[31]: B[np.ix_([1,2,3],[0,2])]
[31]: array([[ 5, 7],
             [9, 11],
             [13, 15]])
[33]: C = np.random.rand(21,21)
[34]: C[2:21:2,:]
[34]: array([[0.50795545, 0.48936508, 0.54067876, 0.3877504, 0.80515658,
              0.09005673, 0.7860626, 0.78982655, 0.06836634, 0.07917667,
              0.54096591, 0.63693553, 0.11297633, 0.22294527, 0.68505408,
              0.03129167, 0.64712718, 0.65773018, 0.04004832, 0.19742811,
              0.66979499],
             [0.36540886, 0.85378718, 0.33451775, 0.70047621, 0.86586032,
              0.94262554, 0.17621397, 0.13278768, 0.27242085, 0.63859063,
              0.69569402, 0.59574855, 0.11666465, 0.39917953, 0.92778887,
              0.24767024, 0.89866584, 0.53402894, 0.44943926, 0.12791323,
              0.04244098],
             [0.3156326, 0.25628462, 0.57912897, 0.2885751, 0.72893306,
              0.7482645 , 0.12890675, 0.76897558, 0.644847 , 0.17760294,
              0.615192 , 0.23460024, 0.54182636, 0.24070467, 0.41319899,
              0.25978578, 0.22849712, 0.06512782, 0.80682495, 0.54597361,
              0.75766397],
             [0.04832052, 0.43765049, 0.31369769, 0.53767639, 0.67677963,
              0.00610449, 0.15507278, 0.1168632, 0.12087029, 0.89153942,
              0.49992397, 0.35936763, 0.32153875, 0.56689468, 0.21077418,
              0.64822014, 0.38455403, 0.77736567, 0.52788009, 0.77798752,
              0.675173547.
             [0.25932408, 0.22168514, 0.98573892, 0.53340685, 0.46022071,
              0.80362839, 0.44997946, 0.44523415, 0.83118348, 0.48272407,
              0.08545704, 0.39027295, 0.70768485, 0.45499212, 0.42929322,
              0.21836007, 0.6137215, 0.09078424, 0.06465765, 0.86069554,
```

```
[0.38259821, 0.8134914, 0.56900485, 0.83573219, 0.80576633,
              0.06502091, 0.13705673, 0.39074202, 0.13382944, 0.78657798,
              0.18562449, 0.51465965, 0.83759434, 0.25976978, 0.68537889,
              0.50675771, 0.81652188, 0.84394796, 0.62765541, 0.77699853,
              0.04896942],
             [0.18892511, 0.09578368, 0.51885701, 0.16234459, 0.70087325,
              0.44716754, 0.66323531, 0.14955779, 0.02719985, 0.06699379,
              0.35640079, 0.19507003, 0.66281473, 0.77415986, 0.83173451,
              0.52912313, 0.33085883, 0.92503473, 0.6700173, 0.71896037,
              0.2112904 ].
             [0.76127489, 0.05859464, 0.02737959, 0.24182748, 0.66490087,
              0.1380581 , 0.09028234, 0.97205854, 0.58328348, 0.78524923,
              0.09932692, 0.95116439, 0.92136103, 0.68790983, 0.28094438,
              0.46263586, 0.86330351, 0.34751444, 0.38661191, 0.22994917,
              0.75824505],
             [0.97160582, 0.21003744, 0.06975635, 0.46236794, 0.94414214,
              0.72099979, 0.62184149, 0.63313746, 0.10901849, 0.64110355,
              0.25723196, 0.93792264, 0.00844011, 0.57442003, 0.18453634,
              0.06088297, 0.59450565, 0.45279661, 0.94871528, 0.23382246,
              0.56501549],
             [0.35903316, 0.56371838, 0.27109753, 0.09264331, 0.19383362,
              0.16165441, 0.13867873, 0.96635108, 0.53393402, 0.64520554,
              0.69629756, 0.40287136, 0.48388163, 0.88754486, 0.39644624,
              0.75021415, 0.85506252, 0.43879764, 0.2276983, 0.55798028,
              0.4500788211)
[35]: C[::2,:]
[35]: array([[0.66765167, 0.70327315, 0.71019957, 0.61384896, 0.07877105,
              0.0948342 , 0.38565003, 0.93872098, 0.10146884, 0.535532
              0.8972091 , 0.13652558, 0.84987938, 0.26354035, 0.37128465,
              0.08154511, 0.60327041, 0.88705769, 0.16169807, 0.58512215,
              0.04572998],
             [0.50795545, 0.48936508, 0.54067876, 0.3877504, 0.80515658,
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              0.54096591, 0.63693553, 0.11297633, 0.22294527, 0.68505408,
              0.03129167, 0.64712718, 0.65773018, 0.04004832, 0.19742811,
              0.66979499],
             [0.36540886, 0.85378718, 0.33451775, 0.70047621, 0.86586032,
              0.94262554, 0.17621397, 0.13278768, 0.27242085, 0.63859063,
              0.69569402, 0.59574855, 0.11666465, 0.39917953, 0.92778887,
              0.24767024, 0.89866584, 0.53402894, 0.44943926, 0.12791323,
              0.04244098],
             [0.3156326, 0.25628462, 0.57912897, 0.2885751, 0.72893306,
              0.7482645 , 0.12890675 , 0.76897558 , 0.644847 , 0.17760294 ,
              0.615192 , 0.23460024, 0.54182636, 0.24070467, 0.41319899,
```

0.92471019],

```
0.75766397],
             [0.04832052, 0.43765049, 0.31369769, 0.53767639, 0.67677963,
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             0.49992397, 0.35936763, 0.32153875, 0.56689468, 0.21077418,
             0.64822014, 0.38455403, 0.77736567, 0.52788009, 0.77798752,
             0.67517354],
             [0.25932408, 0.22168514, 0.98573892, 0.53340685, 0.46022071,
             0.80362839, 0.44997946, 0.44523415, 0.83118348, 0.48272407,
             0.08545704, 0.39027295, 0.70768485, 0.45499212, 0.42929322,
             0.21836007, 0.6137215, 0.09078424, 0.06465765, 0.86069554,
             0.92471019],
             [0.38259821, 0.8134914, 0.56900485, 0.83573219, 0.80576633,
             0.06502091, 0.13705673, 0.39074202, 0.13382944, 0.78657798,
             0.18562449, 0.51465965, 0.83759434, 0.25976978, 0.68537889,
             0.50675771, 0.81652188, 0.84394796, 0.62765541, 0.77699853,
             0.04896942],
             [0.18892511, 0.09578368, 0.51885701, 0.16234459, 0.70087325,
             0.44716754, 0.66323531, 0.14955779, 0.02719985, 0.06699379,
             0.35640079, 0.19507003, 0.66281473, 0.77415986, 0.83173451,
             0.52912313, 0.33085883, 0.92503473, 0.6700173, 0.71896037,
             0.2112904 ].
             [0.76127489, 0.05859464, 0.02737959, 0.24182748, 0.66490087,
             0.1380581 , 0.09028234, 0.97205854, 0.58328348, 0.78524923,
             0.09932692, 0.95116439, 0.92136103, 0.68790983, 0.28094438,
             0.46263586, 0.86330351, 0.34751444, 0.38661191, 0.22994917,
             0.75824505].
             [0.97160582, 0.21003744, 0.06975635, 0.46236794, 0.94414214,
             0.72099979, 0.62184149, 0.63313746, 0.10901849, 0.64110355,
             0.25723196, 0.93792264, 0.00844011, 0.57442003, 0.18453634,
             0.06088297, 0.59450565, 0.45279661, 0.94871528, 0.23382246,
             0.56501549],
             [0.35903316, 0.56371838, 0.27109753, 0.09264331, 0.19383362,
             0.16165441, 0.13867873, 0.96635108, 0.53393402, 0.64520554,
             0.69629756, 0.40287136, 0.48388163, 0.88754486, 0.39644624,
             0.75021415, 0.85506252, 0.43879764, 0.2276983, 0.55798028,
             0.45007882]])
[36]: B[np.r_[:len(B),0]]
[36]: array([[1, 2, 3, 4],
             [5, 6, 7, 8],
             [ 9, 10, 11, 12],
             [13, 14, 15, 16],
             [1, 2, 3, 4]
[37]: B.transpose()
```

0.25978578, 0.22849712, 0.06512782, 0.80682495, 0.54597361,

```
[37]: array([[ 1, 5, 9, 13],
             [2, 6, 10, 14],
             [3, 7, 11, 15],
             [4, 8, 12, 16]])
[38]: B.conj().T
[38]: array([[ 1, 5, 9, 13],
             [2, 6, 10, 14],
             [3, 7, 11, 15],
             [4, 8, 12, 16]])
[40]: B @ B
[40]: array([[ 90, 100, 110, 120],
             [202, 228, 254, 280],
             [314, 356, 398, 440],
             [426, 484, 542, 600]])
[41]: B * B
[41]: array([[ 1,
                    4,
                          9, 16],
                        49, 64],
             [ 25,
                   36,
             [81, 100, 121, 144],
             [169, 196, 225, 256]])
[42]: B / B
[42]: array([[1., 1., 1., 1.],
             [1., 1., 1., 1.],
             [1., 1., 1., 1.],
             [1., 1., 1., 1.]])
[43]: B **3
[43]: array([[
                 1,
                       8,
                            27,
                                  64],
             [ 125, 216, 343, 512],
             [729, 1000, 1331, 1728],
             [2197, 2744, 3375, 4096]], dtype=int32)
[45]: (B > 4)
[45]: array([[False, False, False, False],
             [ True,
                     True,
                             True,
                                    True],
             [ True,
                     True,
                           True,
                                    True],
             [ True,
                     True, True,
                                    True]])
[46]: np.nonzero(B > 4)
```

```
[46]: (array([1, 1, 1, 1, 2, 2, 2, 2, 3, 3, 3, 3], dtype=int64),
       array([0, 1, 2, 3, 0, 1, 2, 3, 0, 1, 2, 3], dtype=int64))
[47]: C[:, np.nonzero(a > 8)[0]]
[47]: array([[0.71019957, 0.61384896, 0.07877105, 0.0948342, 0.38565003],
             [0.99964595, 0.83588417, 0.73720922, 0.36751443, 0.95219909],
             [0.54067876, 0.3877504, 0.80515658, 0.09005673, 0.7860626],
             [0.49694401, 0.73623091, 0.33167801, 0.56177818, 0.4154183],
             [0.33451775, 0.70047621, 0.86586032, 0.94262554, 0.17621397],
             [0.68216186, 0.87984085, 0.87529541, 0.72252974, 0.94559731],
             [0.57912897, 0.2885751, 0.72893306, 0.7482645, 0.12890675],
             [0.38643026, 0.6155913, 0.27644926, 0.69047203, 0.5766595],
             [0.31369769, 0.53767639, 0.67677963, 0.00610449, 0.15507278],
             [0.06468991, 0.97739081, 0.34953018, 0.66689364, 0.5662745],
             [0.98573892, 0.53340685, 0.46022071, 0.80362839, 0.44997946],
             [0.19539218, 0.95886336, 0.18287204, 0.9723965, 0.2306296],
             [0.56900485, 0.83573219, 0.80576633, 0.06502091, 0.13705673],
             [0.33839171, 0.77048957, 0.66956242, 0.81707666, 0.73450392],
             [0.51885701, 0.16234459, 0.70087325, 0.44716754, 0.66323531],
             [0.85061293, 0.46462982, 0.20948858, 0.61939412, 0.84629468],
             [0.02737959, 0.24182748, 0.66490087, 0.1380581, 0.09028234],
             [0.44813288, 0.2777773, 0.71652776, 0.60497513, 0.81186188],
             [0.06975635, 0.46236794, 0.94414214, 0.72099979, 0.62184149],
             [0.89612215, 0.40789089, 0.4485911, 0.33195765, 0.52459968],
             [0.27109753, 0.09264331, 0.19383362, 0.16165441, 0.13867873]])
[50]: C[:, C[:,0].T > 0.5]
[50]: array([[0.66765167, 0.71019957, 0.93872098, 0.13652558, 0.60327041,
              0.16169807],
             [0.01974482, 0.99964595, 0.62909784, 0.49422326, 0.30861164,
              0.33333274],
             [0.50795545, 0.54067876, 0.78982655, 0.63693553, 0.64712718,
              0.04004832],
             [0.42763192, 0.49694401, 0.11997263, 0.83028259, 0.72595403,
              0.87682461],
             [0.36540886, 0.33451775, 0.13278768, 0.59574855, 0.89866584,
              0.44943926],
             [0.18569337, 0.68216186, 0.24469452, 0.17996015, 0.46018781,
              0.3036383],
             [0.3156326, 0.57912897, 0.76897558, 0.23460024, 0.22849712,
              0.80682495],
             [0.85058719, 0.38643026, 0.95571536, 0.51630769, 0.09872904,
              0.87184936],
             [0.04832052, 0.31369769, 0.1168632, 0.35936763, 0.38455403,
              0.52788009],
```

```
0.28118054],
            [0.25932408, 0.98573892, 0.44523415, 0.39027295, 0.6137215,
             0.06465765],
            [0.81778012, 0.19539218, 0.04414333, 0.38248309, 0.77151403,
             0.44774193],
            [0.38259821, 0.56900485, 0.39074202, 0.51465965, 0.81652188,
             0.62765541],
            [0.32219784, 0.33839171, 0.92032249, 0.45106637, 0.39143511,
             0.18588854],
            [0.18892511, 0.51885701, 0.14955779, 0.19507003, 0.33085883,
             0.6700173],
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             0.8552289],
            [0.76127489, 0.02737959, 0.97205854, 0.95116439, 0.86330351,
             0.38661191],
            [0.23316187, 0.44813288, 0.73425247, 0.36153839, 0.70215769,
             0.87752115],
            [0.97160582, 0.06975635, 0.63313746, 0.93792264, 0.59450565,
             0.94871528],
            [0.21990272, 0.89612215, 0.20298869, 0.690036 , 0.7212259 ,
             0.7863145],
            [0.35903316, 0.27109753, 0.96635108, 0.40287136, 0.85506252,
             0.2276983 11)
[51]: C*(C[:,0].T > 0.5)
[51]: array([[0.66765167, 0.
                              , 0.71019957, 0. , 0.
                 , 0. , 0.93872098, 0. , 0. , 0. , 0. , 0.
             0.
             0.
                     , 0.60327041, 0. , 0.16169807, 0.
             0.
                     ],
            [0.01974482, 0. , 0.99964595, 0. , 0. 
0. , 0. , 0.62909784, 0. , 0.
                                                   , 0.
                      , 0.49422326, 0. , 0.
             0.
                     , 0.30861164, 0. , 0.33333274, 0.
             0.
             0.
                     ],
            [0.50795545, 0. , 0.54067876, 0. , 0.
                    , 0. , 0.78982655, 0.
                                                      , 0.
                     , 0.63693553, 0. , 0. , 0.
                      , 0.64712718, 0. , 0.04004832, 0.
             0.
             0.
                      ],
            [0.42763192, 0. , 0.49694401, 0. , 0. 
0. , 0. , 0.11997263, 0. , 0.
                     , 0.83028259, 0. , 0. , 0.
             0.
                     , 0.72595403, 0. , 0.87682461, 0.
             0.
                      ],
             0.
```

[0.28662007, 0.06468991, 0.7311157, 0.7281835, 0.78800516,

```
[0.36540886, 0. , 0.33451775, 0. , 0. 
0. , 0. , 0.13278768, 0. , 0. 
0. , 0.59574855, 0. , 0. , 0.
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0. ],
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0. , 0. , 0.24469452, 0. , 0. 
0. , 0.17996015, 0. , 0. , 0. 
0. , 0.46018781, 0. , 0.3036383 , 0.
 0. ],
[0.3156326 , 0. , 0.57912897, 0. , 0. 
0. , 0. , 0.76897558, 0. , 0.
            , 0.23460024, 0. , 0. , 0.
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 0. , 0.22849712, 0. , 0.80682495, 0. 
0. ],
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0. , 0. , 0.95571536, 0. , 0.
            0.
 Ο.
             ],
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0. , 0. , 0.1168632 , 0. , 0. 
0. , 0.35936763, 0. , 0. , 0.
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0. , 0. , 0.44523415, 0. , 0. 
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0. , 0.6137215 , 0. , 0.06465765, 0.
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0. , 0. , 0.04414333, 0. , 0.
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 0.
 0.
0.
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0. , 0. , 0.39074202, 0. , 0. 
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0. , 0.81652188, 0. , 0.62765541, 0.
 0.
             ],
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0. , 0. , 0.92032249, 0. , 0.
```

```
0. , 0.45106637, 0. , 0. , 0. 
0. , 0.39143511, 0. , 0.18588854, 0.
                           ],
                [0.18892511, 0. , 0.51885701, 0. , 0. 
0. , 0. , 0.14955779, 0. , 0. 
0. , 0.19507003, 0. , 0. , 0.
                            , 0.33085883, 0. , 0.6700173 , 0.
                 0.
                 0.
                            ],
               [0.18886701, 0. , 0.85061293, 0. , 0. 
0. , 0. , 0.24704175, 0. , 0. 
0. , 0.18121727, 0. , 0. , 0. 
0. , 0.40706745, 0. , 0.8552289 , 0.
                0.
                            ],
               [0.76127489, 0. , 0.02737959, 0. , 0. 
0. , 0. , 0. , 0.97205854, 0. , 0.
                           , 0.95116439, 0. , 0. , 0. , 0. , 0. , 0. , 0.38661191, 0.
                 0.
                 0.
                0. ],
                [0.23316187, 0. , 0.44813288, 0. , 0. 
0. , 0. , 0. , 0.73425247, 0. , 0.
                           , 0.36153839, 0. , 0. , 0. , 0. , 0. , 0.70215769, 0. , 0.87752115, 0.
                 0.
                 0.
                 0.
                           ],
               [0.97160582, 0. , 0.06975635, 0. , 0. 
0. , 0. , 0.63313746, 0. , 0. 
0. , 0.93792264, 0. , 0. , 0.
                            , 0.59450565, 0. , 0.94871528, 0.
                0.
                 0.
                           ],
               [0.21990272, 0. , 0.89612215, 0. , 0. 
0. , 0. , 0.20298869, 0. , 0. 
0. , 0.690036 , 0. , 0. , 0.
                            , 0.7212259 , 0. , 0.7863145 , 0.
                0.
                0.
                           ],
               [0.35903316, 0. , 0.27109753, 0. , 0. 
0. , 0. , 0.96635108, 0. , 0. 
0. , 0.40287136, 0. , 0. , 0. 
0. , 0.85506252, 0. , 0.2276983 , 0.
                0.
0.
                         ]])
[53]: G = C.copy()
       G[:] = 3
       G
3., 3., 3., 3., 3.],
                3., 3., 3., 3., 3.],
```

```
3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.],
    3., 3., 3., 3., 3.]])
[55]: C[1,:].copy()
[55]: array([0.01974482, 0.64398191, 0.99964595, 0.83588417, 0.73720922,
    0.36751443, 0.95219909, 0.62909784, 0.55998114, 0.47259722,
    0.42441957, 0.49422326, 0.44192151, 0.92646357, 0.8736134 ,
    0.48038851, 0.30861164, 0.58253552, 0.33333274, 0.42675823,
    0.59618863])
```

[56]: C.flatten()

```
[56]: array([0.66765167, 0.70327315, 0.71019957, 0.61384896, 0.07877105,
             0.0948342 , 0.38565003, 0.93872098, 0.10146884, 0.535532
            0.8972091, 0.13652558, 0.84987938, 0.26354035, 0.37128465,
            0.08154511, 0.60327041, 0.88705769, 0.16169807, 0.58512215,
             0.04572998, 0.01974482, 0.64398191, 0.99964595, 0.83588417,
             0.73720922, 0.36751443, 0.95219909, 0.62909784, 0.55998114,
            0.47259722, 0.42441957, 0.49422326, 0.44192151, 0.92646357,
            0.8736134 , 0.48038851, 0.30861164, 0.58253552, 0.33333274,
             0.42675823, 0.59618863, 0.50795545, 0.48936508, 0.54067876,
            0.3877504, 0.80515658, 0.09005673, 0.7860626, 0.78982655,
            0.06836634, 0.07917667, 0.54096591, 0.63693553, 0.11297633,
            0.22294527, 0.68505408, 0.03129167, 0.64712718, 0.65773018,
             0.04004832, 0.19742811, 0.66979499, 0.42763192, 0.8077131,
             0.49694401, 0.73623091, 0.33167801, 0.56177818, 0.4154183
            0.11997263, 0.32594569, 0.3462954, 0.09437829, 0.83028259,
            0.81123039, 0.46139246, 0.99435563, 0.14300766, 0.72595403,
            0.80833704, 0.87682461, 0.93907868, 0.88110827, 0.36540886,
            0.85378718, 0.33451775, 0.70047621, 0.86586032, 0.94262554,
            0.17621397, 0.13278768, 0.27242085, 0.63859063, 0.69569402,
             0.59574855, 0.11666465, 0.39917953, 0.92778887, 0.24767024,
             0.89866584, 0.53402894, 0.44943926, 0.12791323, 0.04244098,
            0.18569337, 0.71869917, 0.68216186, 0.87984085, 0.87529541,
             0.72252974, 0.94559731, 0.24469452, 0.09083119, 0.12253008,
            0.68240709, 0.17996015, 0.21773992, 0.75203189, 0.72815613,
            0.16790109, 0.46018781, 0.18516958, 0.3036383, 0.86488328,
            0.77023496, 0.3156326, 0.25628462, 0.57912897, 0.2885751,
             0.72893306, 0.7482645 , 0.12890675, 0.76897558, 0.644847
             0.17760294, 0.615192 , 0.23460024, 0.54182636, 0.24070467,
            0.41319899, 0.25978578, 0.22849712, 0.06512782, 0.80682495,
            0.54597361, 0.75766397, 0.85058719, 0.67581048, 0.38643026,
            0.6155913 , 0.27644926 , 0.69047203 , 0.5766595 , 0.95571536 ,
            0.7403472 , 0.71837528, 0.8632412 , 0.51630769, 0.06620236,
            0.75975391, 0.01020282, 0.12728421, 0.09872904, 0.27054806,
             0.87184936, 0.60308585, 0.19036307, 0.04832052, 0.43765049,
             0.31369769, 0.53767639, 0.67677963, 0.00610449, 0.15507278,
            0.1168632 , 0.12087029, 0.89153942, 0.49992397, 0.35936763,
            0.32153875, 0.56689468, 0.21077418, 0.64822014, 0.38455403,
            0.77736567, 0.52788009, 0.77798752, 0.67517354, 0.28662007,
            0.74725434, 0.06468991, 0.97739081, 0.34953018, 0.66689364,
            0.5662745 , 0.7311157 , 0.97803475 , 0.32666199 , 0.50720416 ,
             0.7281835 , 0.19606144, 0.40465897, 0.27577268, 0.81512318,
            0.78800516, 0.60529236, 0.28118054, 0.32507877, 0.68342808,
            0.25932408, 0.22168514, 0.98573892, 0.53340685, 0.46022071,
            0.80362839, 0.44997946, 0.44523415, 0.83118348, 0.48272407,
             0.08545704, 0.39027295, 0.70768485, 0.45499212, 0.42929322,
```

```
0.21836007, 0.6137215, 0.09078424, 0.06465765, 0.86069554,
0.92471019, 0.81778012, 0.365743 , 0.19539218, 0.95886336,
0.18287204, 0.9723965, 0.2306296, 0.04414333, 0.76730757,
0.17145096, 0.13484781, 0.38248309, 0.0022059, 0.79333267,
0.27530156, 0.62944613, 0.77151403, 0.2463938, 0.44774193,
0.39905209, 0.24168986, 0.38259821, 0.8134914, 0.56900485,
0.83573219, 0.80576633, 0.06502091, 0.13705673, 0.39074202,
0.13382944, 0.78657798, 0.18562449, 0.51465965, 0.83759434,
0.25976978, 0.68537889, 0.50675771, 0.81652188, 0.84394796,
0.62765541, 0.77699853, 0.04896942, 0.32219784, 0.96809382,
0.33839171, 0.77048957, 0.66956242, 0.81707666, 0.73450392,
0.92032249, 0.3047297, 0.15896727, 0.65920102, 0.45106637,
0.40984918, 0.74634819, 0.44347315, 0.98183026, 0.39143511,
0.07967018, 0.18588854, 0.5539278, 0.88165363, 0.18892511,
0.09578368, 0.51885701, 0.16234459, 0.70087325, 0.44716754,
0.66323531, 0.14955779, 0.02719985, 0.06699379, 0.35640079,
0.19507003, 0.66281473, 0.77415986, 0.83173451, 0.52912313,
0.33085883, 0.92503473, 0.6700173 , 0.71896037, 0.2112904 ,
0.18886701, 0.0810226, 0.85061293, 0.46462982, 0.20948858,
0.61939412, 0.84629468, 0.24704175, 0.38971302, 0.98760284,
0.82928162, 0.18121727, 0.87199287, 0.76147414, 0.95421424,
0.81432047, 0.40706745, 0.68306045, 0.8552289, 0.21845963,
0.56201457, 0.76127489, 0.05859464, 0.02737959, 0.24182748,
0.66490087, 0.1380581, 0.09028234, 0.97205854, 0.58328348,
0.78524923, 0.09932692, 0.95116439, 0.92136103, 0.68790983,
0.28094438, 0.46263586, 0.86330351, 0.34751444, 0.38661191,
0.22994917, 0.75824505, 0.23316187, 0.63123325, 0.44813288,
0.2777773 , 0.71652776, 0.60497513, 0.81186188, 0.73425247,
0.30213704, 0.71567392, 0.29041554, 0.36153839, 0.40539386,
0.88064201, 0.41436388, 0.71116361, 0.70215769, 0.45861722,
0.87752115, 0.61539366, 0.78548926, 0.97160582, 0.21003744,
0.06975635, 0.46236794, 0.94414214, 0.72099979, 0.62184149,
0.63313746, 0.10901849, 0.64110355, 0.25723196, 0.93792264,
0.00844011, 0.57442003, 0.18453634, 0.06088297, 0.59450565,
0.45279661, 0.94871528, 0.23382246, 0.56501549, 0.21990272,
0.11380696, 0.89612215, 0.40789089, 0.4485911, 0.33195765,
0.52459968, 0.20298869, 0.52611763, 0.0957067, 0.81560728,
0.690036 , 0.9484254 , 0.28968705, 0.07277301, 0.48230064,
0.7212259 , 0.04632913, 0.7863145 , 0.10389162, 0.17197998,
0.35903316, 0.56371838, 0.27109753, 0.09264331, 0.19383362,
0.16165441, 0.13867873, 0.96635108, 0.53393402, 0.64520554,
0.69629756, 0.40287136, 0.48388163, 0.88754486, 0.39644624,
0.75021415, 0.85506252, 0.43879764, 0.2276983, 0.55798028,
0.45007882])
```

[58]: np.arange(1,11)

```
[58]: array([ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10])
[59]: np.arange(10)
[59]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
[60]: np.arange(1,11)[:, np.newaxis]
[60]: array([[ 1],
             [2],
             [3],
             [4],
             [5],
             [ 6],
             [7],
             [8],
             [ 9],
             [10]])
[61]: np.zeros((3,4,5))
[61]: array([[[0., 0., 0., 0., 0.],
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]
             [[0., 0., 0., 0., 0.],
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]
             [[0., 0., 0., 0., 0.],
              [0., 0., 0., 0., 0.],
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]]])
[62]: np.ones((3,4))
[62]: array([[1., 1., 1., 1.],
             [1., 1., 1., 1.],
             [1., 1., 1., 1.]])
[63]: np.eye(3)
[63]: array([[1., 0., 0.],
             [0., 1., 0.],
             [0., 0., 1.]])
```

```
[64]: np.diag(a)
                            Ο,
                                            Ο,
[64]: array([[
                      0,
                                 0,
                                                  0],
                 1,
                                       Ο,
              Ο,
                       1,
                            Ο,
                                 Ο,
                                       0,
                                            0,
                                                  0],
                           23,
              0,
                      0,
                                 0,
                                            0,
                                                  0],
                                       Ο,
              0,
                      Ο,
                            0,
                                21,
                                       0,
                                            0,
                                                  0],
              Ο,
                 0,
                            0,
                                  0,
                                      23,
                                            0,
                                                  0],
                                 Ο,
              Ο,
                            0,
                                       0, 123,
                                                  0],
                 0,
              [ 0,
                       0,
                            0,
                                 0,
                                       0,
                                            0,
                                                 12]])
[66]: np.diag(a,1)
                                                       0],
[66]: array([[
                            0,
                                 Ο,
                                       Ο,
                                            Ο,
                                                  0,
                       1,
              Ο,
                 0,
                      0,
                                 0,
                                            Ο,
                                                  0,
                                                       0],
                            1,
              [
                 Ο,
                      0,
                            0,
                                23,
                                       Ο,
                                            0,
                                                  0,
                                                       0],
              0,
                      Ο,
                            Ο,
                                 Ο,
                                      21,
                                            Ο,
                                                  0,
                                                       0],
                                                       0],
              0,
                 0,
                      0,
                            0,
                                 0,
                                       Ο,
                                           23,
              0,
                      0,
                            0,
                                 0,
                                       0,
                                            0, 123,
                                                       0],
              0,
                      0,
                            0,
                                 0,
                                       0,
                                            0,
                                                  0,
                                                      12],
              [ 0,
                       0,
                            0,
                                 0,
                                       0,
                                            0,
                                                  0,
                                                       0]])
[69]: np.random.rand(2,3)
[69]: array([[0.64637182, 0.05697136, 0.76095196],
              [0.98705373, 0.51300603, 0.19795049]])
[70]: np.linspace(1,3,4)
[70]: array([1.
                         , 1.66666667, 2.333333333, 3.
                                                                ])
[71]: np.mgrid[0:9.,0:6.]
[71]: array([[[0., 0., 0., 0., 0., 0.],
               [1., 1., 1., 1., 1., 1.]
               [2., 2., 2., 2., 2., 2.]
               [3., 3., 3., 3., 3., 3.]
               [4., 4., 4., 4., 4., 4., 4.]
               [5., 5., 5., 5., 5., 5.]
               [6., 6., 6., 6., 6., 6.]
               [7., 7., 7., 7., 7., 7.]
               [8., 8., 8., 8., 8., 8.]
              [[0., 1., 2., 3., 4., 5.],
               [0., 1., 2., 3., 4., 5.],
               [0., 1., 2., 3., 4., 5.],
               [0., 1., 2., 3., 4., 5.],
               [0., 1., 2., 3., 4., 5.],
               [0., 1., 2., 3., 4., 5.],
```

```
[0., 1., 2., 3., 4., 5.],
              [0., 1., 2., 3., 4., 5.],
              [0., 1., 2., 3., 4., 5.]])
[73]: np.ogrid[0:9.,0:6.]
[73]: [array([[0.],
              [1.],
              [2.],
              [3.],
              [4.],
              [5.],
              [6.],
              [7.],
              [8.]]),
       array([[0., 1., 2., 3., 4., 5.]])]
[74]:
      np.meshgrid([1,2,4],[2,4,5])
[74]: [array([[1, 2, 4],
              [1, 2, 4],
              [1, 2, 4]]),
       array([[2, 2, 2],
              [4, 4, 4],
              [5, 5, 5]])]
[75]: np.ix_([1,2,4],[2,4,5])
[75]: (array([[1],
              [2],
              [4]]),
       array([[2, 4, 5]]))
[77]: np.tile(np.arange(3), (4, 5))
[77]: array([[0, 1, 2, 0, 1, 2, 0, 1, 2, 0, 1, 2, 0, 1, 2],
             [0, 1, 2, 0, 1, 2, 0, 1, 2, 0, 1, 2, 0, 1, 2],
             [0, 1, 2, 0, 1, 2, 0, 1, 2, 0, 1, 2, 0, 1, 2],
             [0, 1, 2, 0, 1, 2, 0, 1, 2, 0, 1, 2, 0, 1, 2]])
[83]: np.concatenate((np.arange(10).reshape(2,5),np.arange(10,20).reshape(2,5)), 1)
[83]: array([[ 0, 1, 2, 3, 4, 10, 11, 12, 13, 14],
             [5, 6, 7, 8, 9, 15, 16, 17, 18, 19]])
[84]: np.concatenate((np.arange(10),np.arange(10,20)))
```

```
[84]: array([ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16,
            17, 18, 19])
[85]: a.max()
[85]: 123
[86]: np.maximum(a, a**2)
[86]: array([
                           529,
                                  441,
                                        529, 15129,
                                                      144])
                1,
                      1,
[87]: np.sqrt(B @ B)
                                    , 10.48808848, 10.95445115],
[87]: array([[ 9.48683298, 10.
            [14.2126704, 15.09966887, 15.93737745, 16.73320053],
            [17.72004515, 18.86796226, 19.94993734, 20.97617696],
                                    , 23.28089345, 24.49489743]])
            [20.63976744, 22.
[88]: np.logical_and(C>0.5, C<0.75)
[88]: array([[ True, True, True, True, False, False, False, False, False,
              True, False, False, False, False, False,
                                                            True, False,
             False, True, False],
            [False, True, False, False, True, False, False,
                                                            True,
             False, False, False, False, False, False, False,
             False, False, True],
            [ True, False, True, False, False, False, False, False,
             False,
                    True, True, False, False, True, False,
                                                            True,
             False, False, True],
            [False, False, False, True, False, True, False, False, False,
             False, False, False, False, False, False,
                                                            True, False,
             False, False, False],
            [False, False, False, True, False, False, False, False,
                    True, True, False, False, False, False,
             False, False, False],
            [False, True, True, False, False, True, False, False, False,
             False, True, False, False, False, True, False, False, False,
             False, False, False],
            [False, False, True, False, True, True, False, False,
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             False,
                    True, False],
                    True, False, True, False, True, False, True,
              True, False, True, False, False, False, False, False, False,
             False, True, False],
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             False, False, False, True, False, True, False, False,
              True, False, True],
            [False, True, False, False, False, True, True, False,
```

```
False, False,
                         True],
            [False, False, False,
                                True, False, False, False, False,
            False, False, False,
                                 True, False, False, False,
                                                           True, False,
            False, False, False],
            [False, False, False, False, False, False, False, False,
            False, False, False, False, False, True, False, False,
            False, False, False],
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            False, True, False],
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            False, False, True, False, False,
                                                    True, False, False,
             True, True, False],
            [False, False, False, False, True, False, False, False,
            False, False, False, False, False, False, False,
            False, False, True],
            [False, False, False, True, False, False, False,
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            False, False, False],
            [False, True, False, False, True, True, False,
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                                                           True, False,
            False, True, False],
            [False, False, False, False, True,
                                                   True,
                                                           True, False,
             True, False, False, True, False, False,
                                                           True, False,
            False, False, True],
            [False, False, False, False, False, True, False,
                                                                 True,
            False, False, True, False, False, False, False,
                                                           True, False,
            False, False, False],
                    True, False, False, False, False, False,
            [False,
             True,
                    True, False, False, False, False, False, False,
            False,
                    True, False]])
[90]: np.logical_or(C < 0.1, C > 0.9)
[90]: array([[False, False, False, False, True, False, True, False,
            False, False, False, False, False, True, False, False,
            False, False, True],
            [ True, False, True, False, False, False, True, False, False,
            False, False, False, True, False, False, False, False,
            False, False, False],
            [False, False, False, False, True, False, False, True,
             True, False, False, False, False, True, False, False,
             True, False, False],
```

False, True, True, False, False, False, False, False,

```
[False, False, False, False, False, False, False, False,
       True, False, False, False,
                                 True, False, False, False,
       True, False],
[False, False, False, False,
                                  True, False, False, False,
False, False, False, False,
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              False, False, False]])
[95]: J = np.arange(0,256, dtype='int')
      K = np.arange(0,256, dtype='int') + 1
      K & J
[95]: array([ 0,
                     Ο,
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                                                          8,
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                                          4,
                                               6,
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             220, 222, 192, 224, 224, 226, 224, 228, 228, 230, 224, 232, 232,
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             240, 248, 248, 250, 248, 252, 252, 254,
[96]: K | J
[96]: array([
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                          3,
                                7,
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                                          7,
                                               7,
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            235, 239, 237, 239, 239, 255, 241, 243, 243, 247, 245, 247, 247,
            255, 249, 251, 251, 255, 253, 255, 255, 511])
[97]: np.linalg.inv(C)
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                                        1.19052311, 0.36627422, -0.98524635,
                                        0.01110087, 0.43544334, 0.11230539,
             -0.02013484,
                           1.01620187,
              0.22619511,
                           0.9034426 , 0.61301652 , -1.67652619 , -0.08237231 ,
             -1.32202516],
             [ 0.12292603, -0.38321704,
                                        0.94855221,
                                                     0.41142747, 0.90124711,
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                                       1.04675666,
                                                    0.5158068 , -0.70814768,
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                                                     0.45502567, -0.08797323,
                           0.84124406, 1.64729373, -2.1421718, 0.13604767,
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             -1.55460387,
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 0.81906622],
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 0.27005525],
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               0.86045482],
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              -0.0124584, 0.17526749, -0.83980816, -0.15569322, 0.54685071,
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              -0.63841267],
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               0.34440348],
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               1.15755296],
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              -0.17310167, 0.3535176, -0.79146824, 0.08852253, -0.44038546,
               0.02003731, 0.36367269, 0.51419792, -0.48040908, -0.08655192,
              -0.56380545]])
[101]: np.linalg.pinv(B)
[101]: array([[-0.285, -0.145, -0.005, 0.135],
             [-0.1075, -0.0525, 0.0025, 0.0575],
             [0.07, 0.04, 0.01, -0.02],
             [0.2475, 0.1325, 0.0175, -0.0975]])
[103]: np.linalg.matrix_rank(B)
[103]: 2
[108]: np.linalg.solve(B, B[2,:])
[108]: array([-6.75, 4.25, 3.75, -1.])
[109]: np.linalg.svd(B)
[109]: SVDResult(U=array([[-0.13472212, -0.82574206, 0.38124745, -0.39325613],
             [-0.3407577, -0.4288172, -0.21521411, 0.80850658],
             [-0.54679327, -0.03189234, -0.71331411, -0.43724476],
             [-0.75282884, 0.36503251, 0.54728078, 0.02199431]])
      S=array([3.86226568e+01, 2.07132307e+00, 7.60977226e-16, 3.86063773e-16]),
      Vh=array([[-0.4284124 , -0.47437252, -0.52033264, -0.56629275],
             [0.71865348, 0.27380781, -0.17103786, -0.61588352],
```

```
[0.28255951, -0.72647617, 0.6052738, -0.16135714],
             [-0.46921223, 0.41500889, 0.57761893, -0.52341558]]))
[120]: np.linalg.cholesky(np.array((2,-1,0,-1,2,-1,0,-1,2)).reshape(3,3))
[120]: array([[ 1.41421356, 0.
                                     , 0.
                                                  ],
             [-0.70710678, 1.22474487, 0.
                                                  ],
             ΓΟ.
                         , -0.81649658, 1.15470054]])
[126]: D, V = np.linalg.eig(B)
      print(D)
      print(V)
      [ 3.62093727e+01 -2.20937271e+00 2.80575969e-16 -8.29646454e-16]
      [[-0.15115432 -0.72704996 -0.01128698 -0.250341 ]
       [-0.34923733 -0.28320876 0.42321091 0.69689908]
       [-0.54732033 \quad 0.16063243 \quad -0.81256087 \quad -0.64277516]
       [-0.74540333 0.60447363 0.40063694 0.19621708]]
[150]: D, V = linalg.eig(B, np.random.rand(B.shape[0], B.shape[1]))
      print(D)
      print(V)
      [-5.13011045e+01+0.j 1.02614934e+01+0.j 4.69505866e-15+0.j
        1.56664418e-15+0.j]
      [-0.03516474 -0.0116871 0.17440125 -0.82536462]
       [-0.61764839 -0.72494302 0.73434214 0.36712246]
       [ 0.08302458 -0.00273762 -0.54769518  0.03037323]]
[151]: D,V = eigs(B, k=3)
      print(D)
      print(V)
      [ 3.62093727e+01+0.j -2.20937271e+00+0.j 2.80575969e-16+0.j
       -8.29646454e-16+0.j]
      [[-0.15115432 -0.72704996 -0.01128698 -0.250341 ]
       [-0.34923733 -0.28320876 0.42321091 0.69689908]
       [-0.54732033  0.16063243  -0.81256087  -0.64277516]
       [-0.74540333  0.60447363  0.40063694  0.19621708]]
[134]: Q,R = np.linalg.qr(B)
      print(Q,R)
      [[-0.06019293 -0.83449195 -0.19896747 -0.51030574]
       [-0.30096463 -0.45762462 0.6456494
                                            0.53210606]
       [-0.54173634 -0.08075729 -0.69439639 0.4667051 ]
       [-0.78250805 0.29611005 0.24771446 -0.48850542]] [[-1.66132477e+01
      -1.82986497e+01 -1.99840516e+01 -2.16694536e+01]
       [ 0.00000000e+00 -1.07676380e+00 -2.15352761e+00 -3.23029141e+00]
```

```
[ 0.0000000e+00
                    0.00000000e+00 0.00000000e+00 -1.57441779e-15]]
[144]: P,L,U = linalg.lu(B)
     print(P)
     print(L)
     print(U)
     [[0. 1. 0. 0.]
      [0. 0. 0. 1.]
      [0. 0. 1. 0.]
      [1. 0. 0. 0.]]
                                              ]
     [[ 1.
                 0.
                           0.
                                     0.
      [ 0.07692308 1.
                                              ]
                           0.
                                     0.
      [ 0.69230769  0.33333333  1.
                                     0.
                                              1
      1.
                                              ]]
     [[ 1.30000000e+01 1.40000000e+01 1.50000000e+01 1.60000000e+01]
      [ 0.0000000e+00
                    9.23076923e-01 1.84615385e+00 2.76923077e+00]
      [152]: cg
[152]: <function scipy.sparse.linalg._isolve.iterative.cg(A, b, x0=None, tol=1e-05,
     maxiter=None, M=None, callback=None, atol=None)>
[153]: np.fft.fft(a)
[153]: array([ 204.
                                  , -63.02531912+106.960705j
                        +0.j
           -106.00067557 -34.22782984j,
                                     70.52599469 -71.46057129j,
             70.52599469 +71.46057129j, -106.00067557 +34.22782984j,
            -63.02531912-106.960705j ])
[154]: np.fft.ifft(a)
                                , -9.00361702-15.28010071j,
[154]: array([ 29.14285714 +0.j
           -15.14295365 +4.88968998j, 10.0751421 +10.20865304j,
            10.0751421 -10.20865304j, -15.14295365 -4.88968998j,
            -9.00361702+15.28010071j])
[155]: np.sort(a)
               1, 12, 21, 23, 23, 123])
[155]: array([ 1,
[156]: np.sort(B,axis=1)
[156]: array([[ 1, 2,
                   3, 4],
           [5, 6, 7, 8],
           [ 9, 10, 11, 12],
```

```
[13, 14, 15, 16]])
[158]: I = np.argsort(B[:,0])
       b = B[I,:]
       print(b)
      [[1 2 3 4]
       [5 6 7 8]
       [ 9 10 11 12]
       [13 14 15 16]]
[160]: linalg.lstsq(B, np.random.rand(B.shape[0]))
[160]: (array([0.00211429, 0.00845879, 0.01480329, 0.02114778]),
       array([], dtype=float64),
       array([3.86226568e+01, 2.07132307e+00, 7.60977226e-16, 3.86063773e-16]))
[163]: signal.resample(a, int(np.ceil(len(a)/2)))
[163]: array([-19.1502842 , 28.86856302, 16.86418387, 89.98896588])
[164]: np.unique(a)
[164]: array([ 1, 12, 21, 23, 123])
[165]: a.squeeze()
```

[165]: array([1, 1, 23, 21, 23, 123, 12])

[]:

Task 3:

 $Run\ the\ following\ script\ in\ IPython\ and\ paste\ the\ figure\ created\ by\ the\ script\ into\ your\ report$

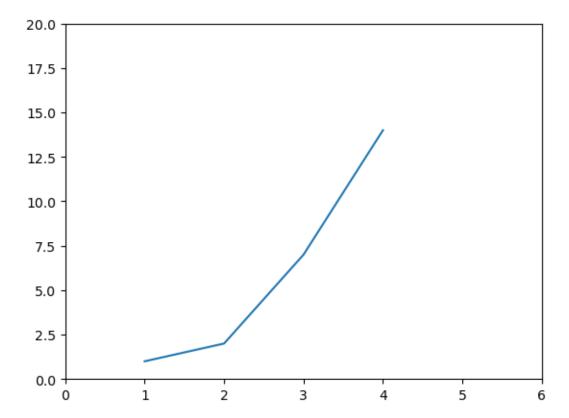
```
import matplotlib.pyplot as plt
plt.plot([1,2,3,4], [1,2,7,14])
plt.axis([0, 6, 0, 20])
plt.show()
```

Jupyter Notebook:

Task_3

September 12, 2023

```
[2]: import matplotlib.pyplot as plt
plt.plot([1,2,3,4], [1,2,7,14])
plt.axis([0, 6, 0, 20])
plt.show()
```



[]:

Task 4:

Use Matplotlib to create a figure of your choice in IPython. Paste your code and figure into your report

Jupyter Notebook:

$Task_4$

September 12, 2023

```
[9]: import matplotlib.pyplot as plt
import numpy as np

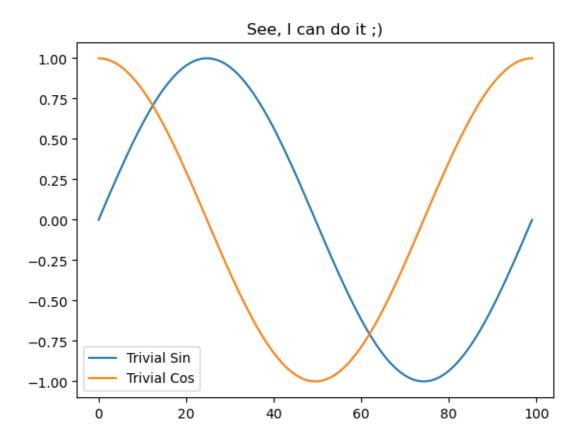
vals_1 = np.sin(np.linspace(0,np.pi*2, 100))
vals_2 = np.cos(np.linspace(0,np.pi*2, 100))

plt.plot(vals_1, label = "Trivial Sin")
plt.plot(vals_2, label = "Trivial Cos")

plt.title("See, I can do it ;)")

plt.legend()

plt.show()
```



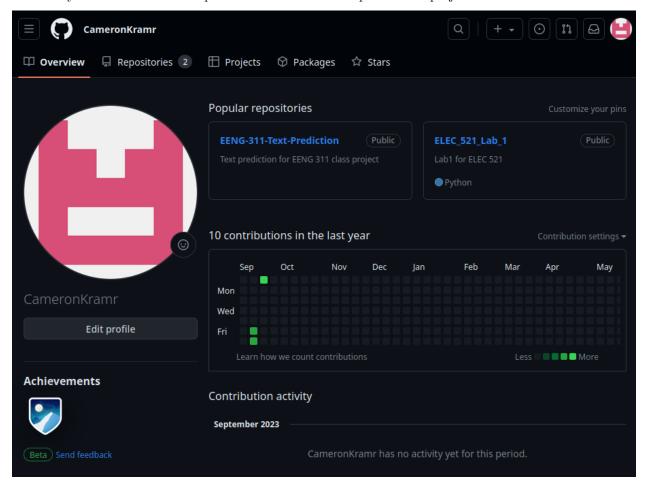
[]:

Task 5:

Paste your VCS account into your report

Result:

Here is my Github account as requested. This was before I pushed this project to Github.



Task 6:

Start a new project in PyCharm. Commit and push your project to VCS as a public project and share a link of your project in your report

Result:

I did not use PyCharm to make the repository. Find link to the repository for this task here. There, you will find all of the Jupyter notebooks as well as the build and Markdown files used to generate this report. Instead of PyCharm, I used the CLI interface for GIT.