

## Stats326 - Assignment3

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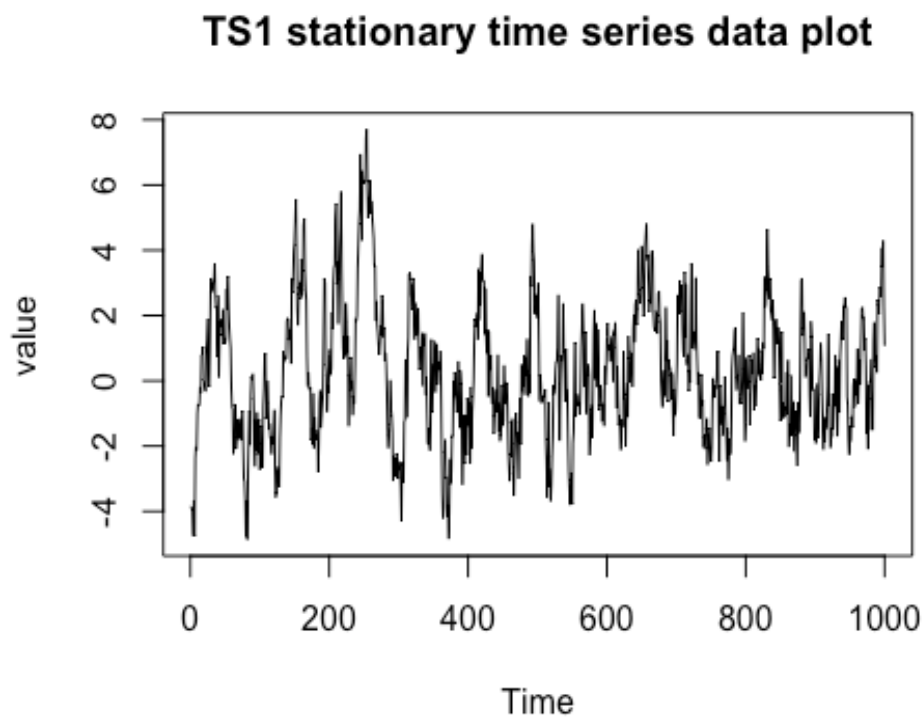
29 Jan 2018

```
library(readr)

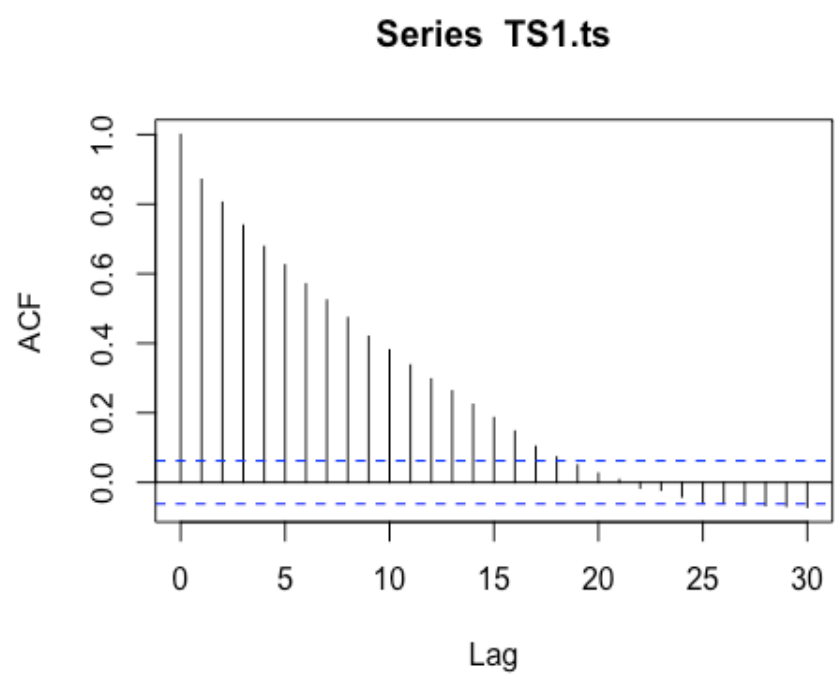
some_data = read.table("A3Data.txt", header = T)
```

Question 1

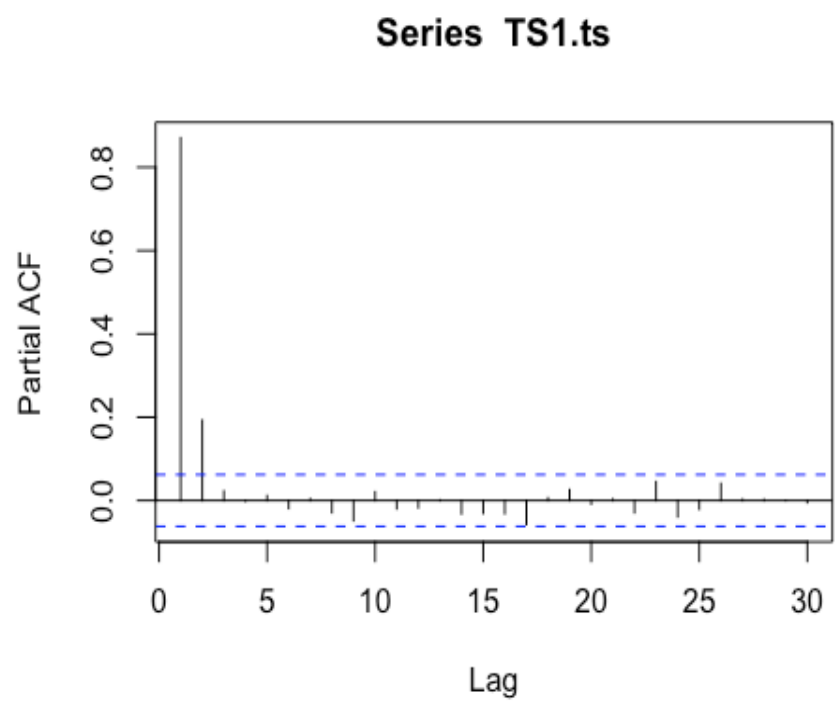
```
TS1.ts = ts(some_data$TS1, frequency = 1, start=1)
plot.ts(TS1.ts,main="TS1 stationary time series data plot", xlab="Time",ylab=
"value")
```



```
acf(TS1.ts)
```

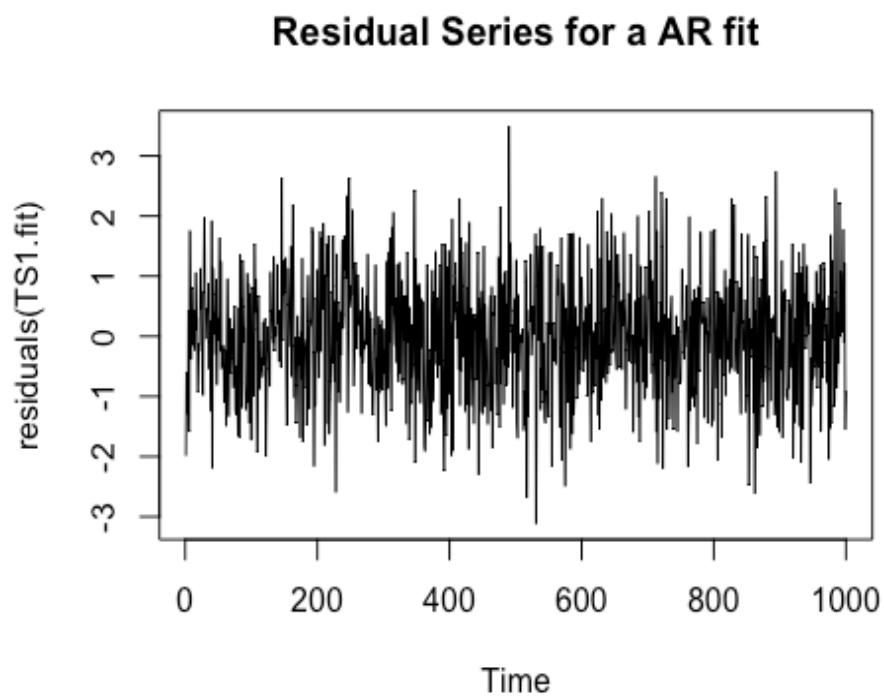


```
pacf(TS1.ts)
```



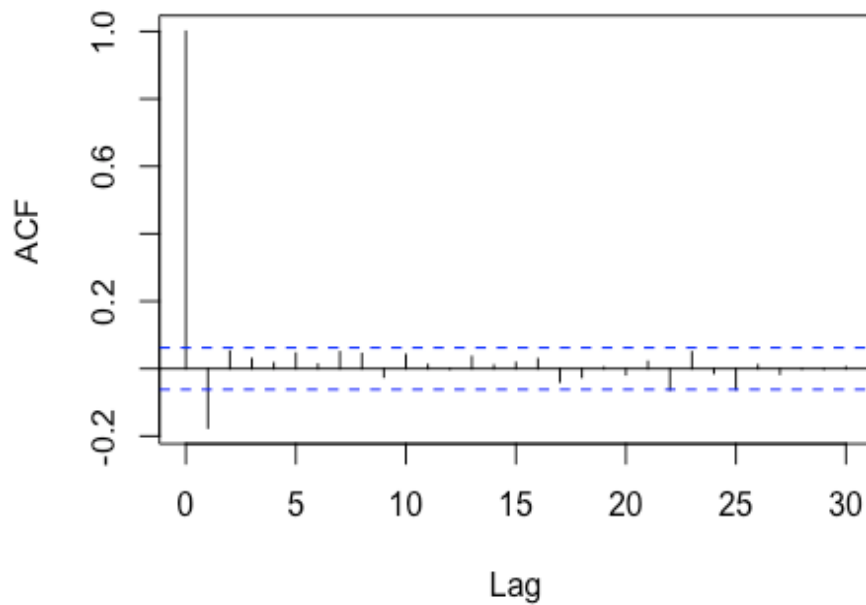
```
TS1.fit = arima(TS1.ts, order=c(1,0,0))  
TS1.fit
```

```
##  
## Call:  
## arima(x = TS1.ts, order = c(1, 0, 0))  
##  
## Coefficients:  
##          ar1  intercept  
##      0.8736    0.2481  
## s.e. 0.0154    0.2469  
##  
## sigma^2 estimated as 0.988:  log likelihood = -1413.61,  aic = 2833.22  
plot.ts(residuals(TS1.fit), main= "Residual Series for a AR fit")
```



```
acf(residuals(TS1.fit))
```

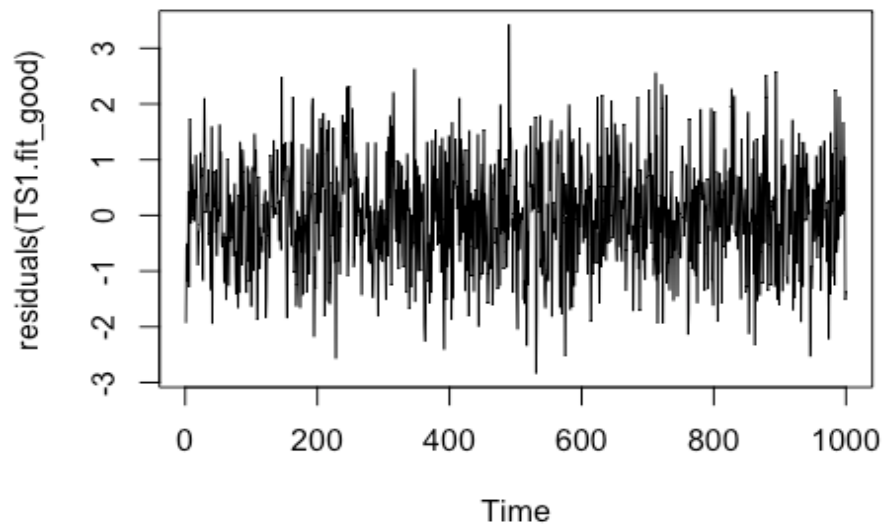
### Series residuals(TS1.fit)



```
TS1.fit_good = arima(TS1.ts, order=c(1,0,1))
TS1.fit_good

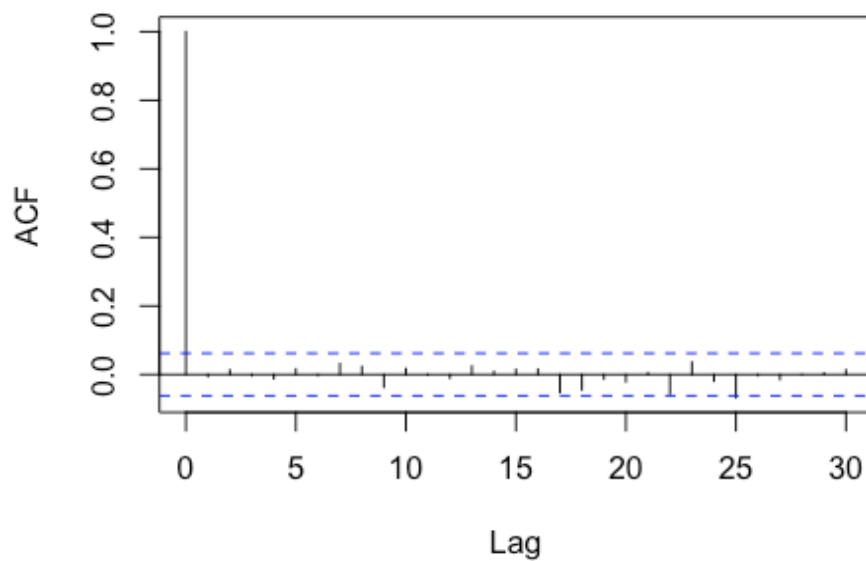
##
## Call:
## arima(x = TS1.ts, order = c(1, 0, 1))
##
## Coefficients:
##      ar1      ma1  intercept
##    0.9265 -0.2295    0.2323
## s.e. 0.0135  0.0343    0.3191
##
## sigma^2 estimated as 0.9481:  log likelihood = -1393.05,  aic = 2794.1
plot.ts(residuals(TS1.fit_good), main= "Residual Series for a ARMA fit")
```

**Residual Series for a ARMA fit**



```
acf(residuals(TS1.fit_good))
```

**Series residuals(TS1.fit\_good)**



(Q1d)

Initial comments - After plotting the time series we could easily see it is a stationary univariate time series with perhaps a slight pattern of sorts but also had lots of white noise. However once we reviewed the acf and pacf plots we could comfortably see an exponential

decay in the acf and the pacf showing a cut off at lag(1), we knew we would need to fit a sort of AR(1) model.

Initial Equation:  $y_t = \rho y_{t-1} + \epsilon_t$  where  $\epsilon_t \sim \text{wn}$

(Q1e)

Estimated equation:  $y_t = 0.8736 * y_{t-1} + 0.0154$

(Q1f) Comment on Residuals - After fitting the AR(1) model, you can clearly see the residuals mainly showing white noise with no other pattern clearly being seen and the variance is normally distributed around 0 or 0 mean.

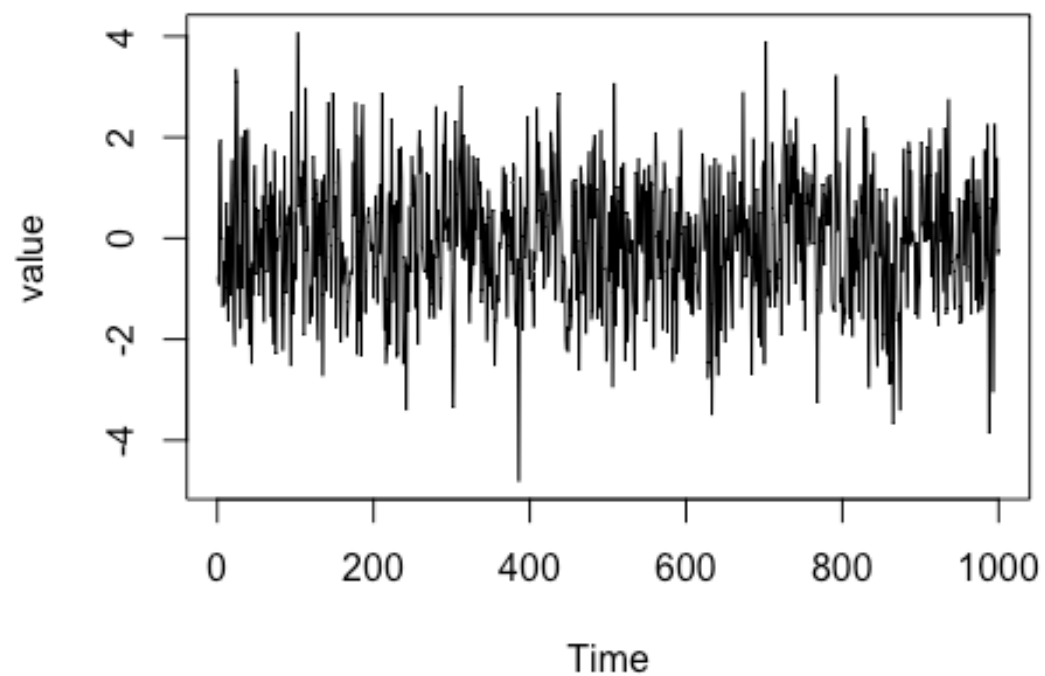
(Q1g) Comment on ACF - The new ACF with the fitted model shows no decay anymore but slight negative autocorrelation at lag 1, this may be fixed by adding a MA to the model.

(Q1h) New Model - After I saw a slight negative autocorrelation on the acf residuals of the first model, I decided to add in a moving average feature to a new model, which gave me a significantly lower AIC from 2833.22 - 2794.1. This is a far better model.

Question 2

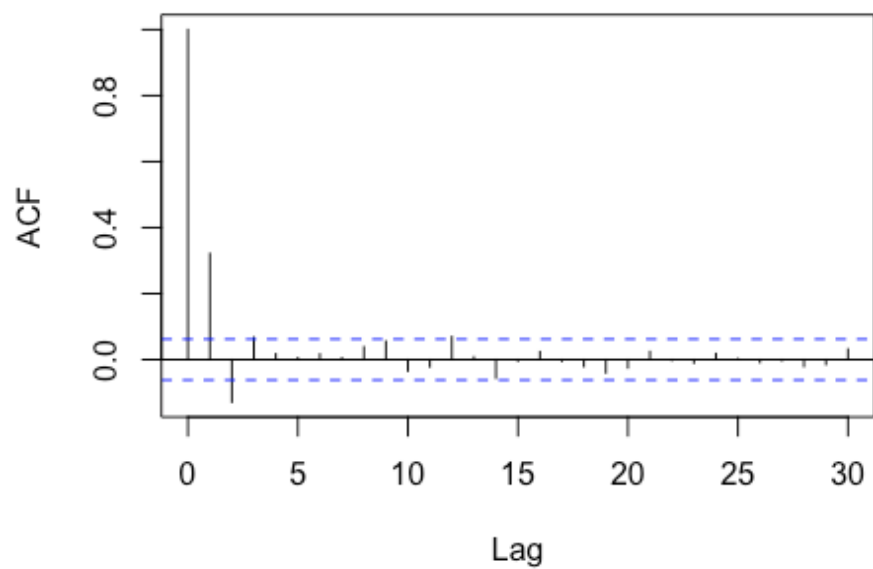
```
TS2.ts = ts(some_data$TS2, frequency = 1, start=1)
plot.ts(TS2.ts, main="TS2 stationary time series data plot", xlab="Time", ylab="value")
```

**TS2 stationary time series data plot**

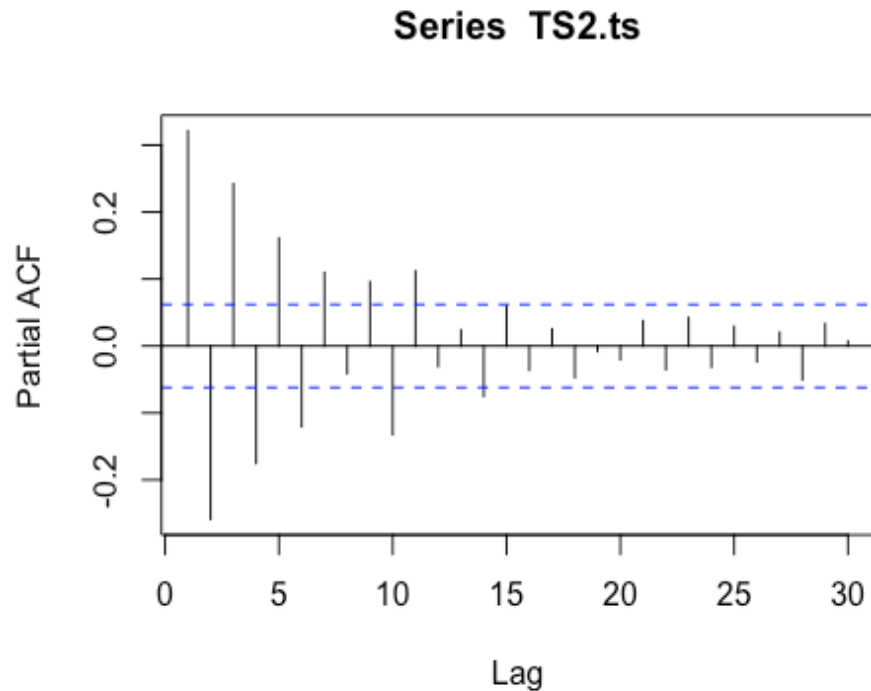


```
acf(TS2.ts)
```

**Series TS2.ts**



```
pacf(TS2.ts)
```

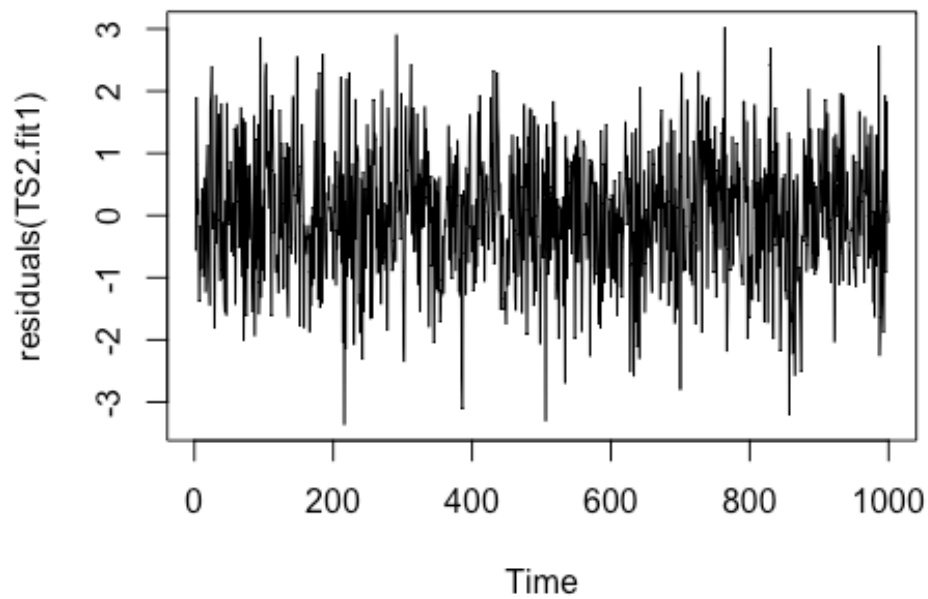


```
TS2.fit1 = arima(TS2.ts, order=c(0,0,2))
TS2.fit1

##
## Call:
## arima(x = TS2.ts, order = c(0, 0, 2))
##
## Coefficients:
##          ma1          ma2  intercept
##      0.6434  -0.2563   -0.0709
## s.e.  0.0290   0.0286    0.0461
##
## sigma^2 estimated as 1.103:  log likelihood = -1468.9,  aic = 2945.8
plot.ts(residuals(TS2.fit1), main= "Residual Series for a MA fit2")
```

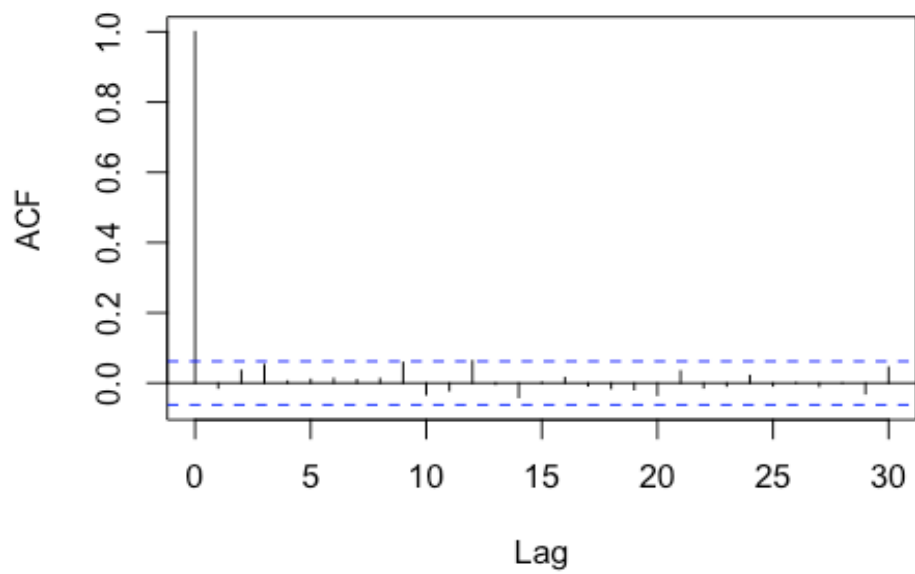


**Residual Series for a MA fit2**



```
acf(residuals(TS2.fit1))
```

**Series residuals(TS2.fit1)**



(Q2d)

The initial plots for TS2 showed plenty of white noise, with the pacf plot showing plenty of decay or persistence and the acf plot cutting off at lag(2), therefore my first model was going to be a moving average cut off at lag(2) so MA(2).

Initial Equation –  $y_t = \epsilon_t + \alpha_1 * \epsilon_{t-1} + \alpha_2 * \epsilon_{t-2}$  where  $\epsilon_t$  is a white noise series

(Q2e) Fitted Equation –  $y_t = \epsilon_t + 0.6434 * 0.0290 - 0.2563 * 0.0286$

(Q2f) The residuals plot from my model show a constant variance with a mean of 0, only appearing to show white noise it seems. (Q2g) The acf plot looks much better with no more lags showing the model is a good fit.

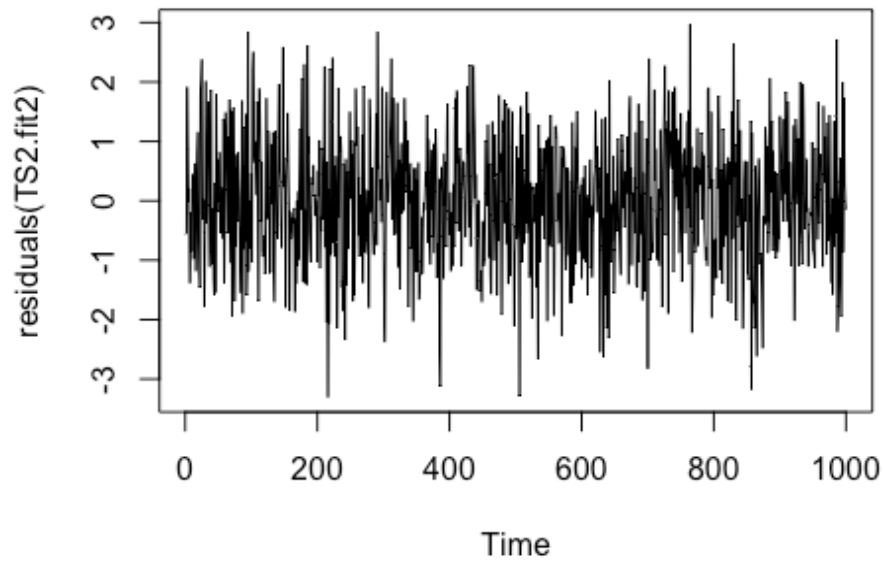
(Q2h) I tried a ARMA(1,2) model thinking there may have been decay in the acf and pacf that I may have missed and or the AIC of this model is a little bit better than my original model of 2945.8 vs 2945.4 of the ARMA model.

```
TS2.fit2 = arima(TS2.ts, order=c(1,0,2))
TS2.fit2

##
## Call:
## arima(x = TS2.ts, order = c(1, 0, 2))
##
## Coefficients:
##          ar1          ma1          ma2  intercept
##       -0.1630    0.7916   -0.1276   -0.0710
## s.e.    0.1021    0.1012    0.0899    0.0475
##
## sigma^2 estimated as 1.101:  log likelihood = -1467.7,  aic = 2945.4

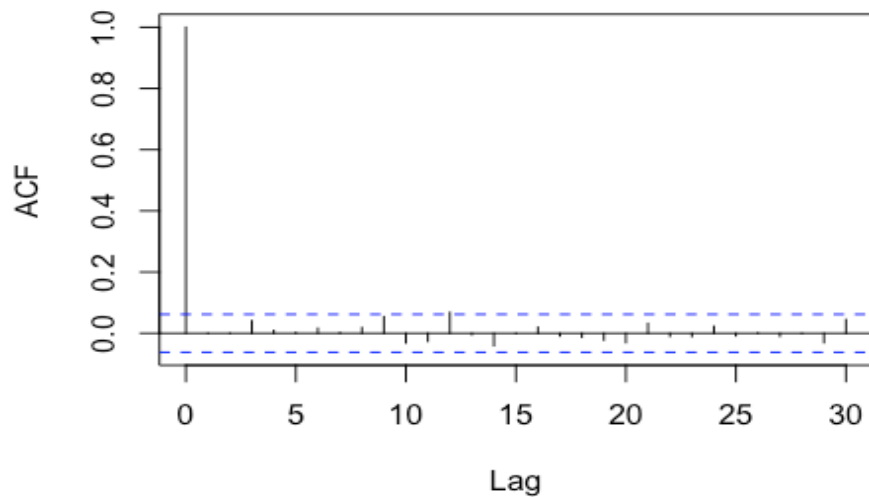
plot.ts(residuals(TS2.fit2), main= "Residual Series for a MA fit2")
```

### Residual Series for a MA fit2



```
acf(residuals(TS2.fit2))
```

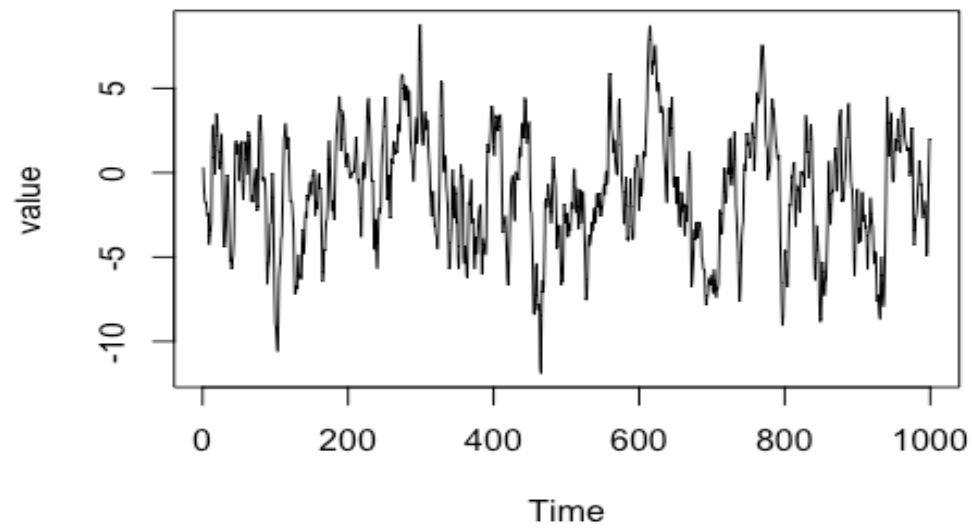
### Series residuals(TS2.fit2)



### Question 3

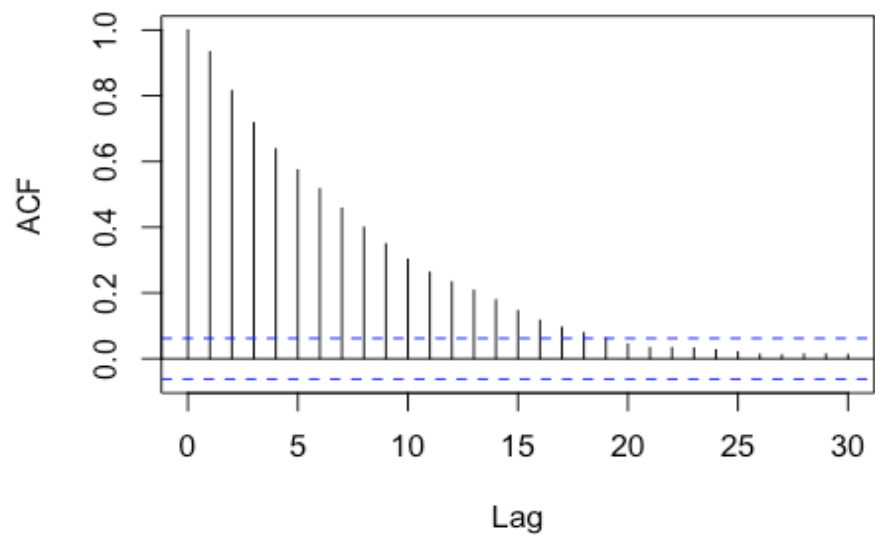
```
TS3.ts = ts(some_data$TS3, frequency = 1, start=1)
plot.ts(TS3.ts, main="TS3 stationary time series data plot", xlab="Time", ylab="value")
```

**TS3 stationary time series data plot**

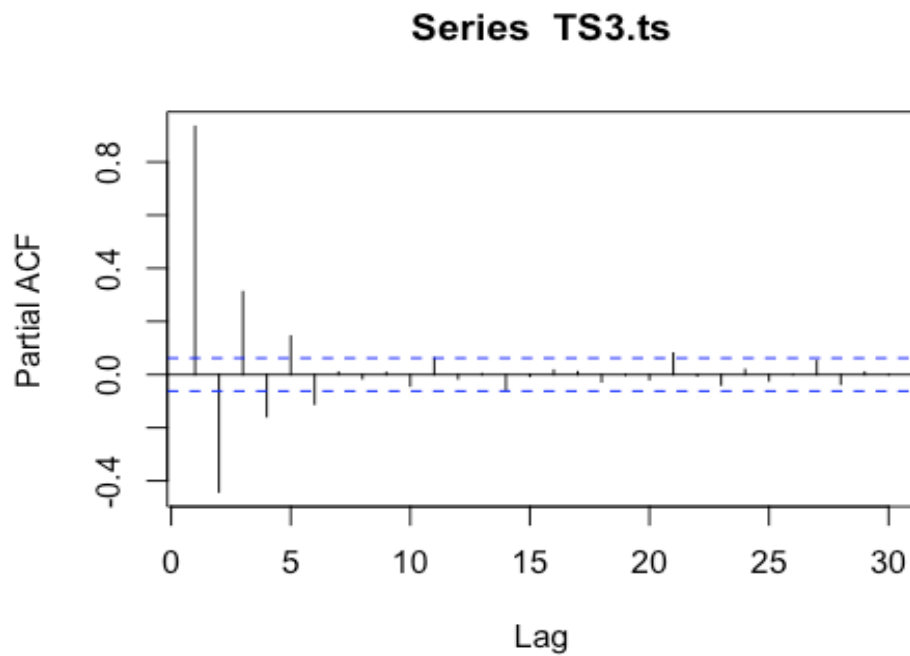


```
acf(TS3.ts)
```

**Series TS3.ts**



```
pacf(TS3.ts)
```



```
TS3.fitARMA = arima(TS3.ts, order=c(1,0,1))
```

```
TS3.fitARMA
```

```
##
```

```
## Call:
```

```
## arima(x = TS3.ts, order = c(1, 0, 1))
```

```
##
```

```
## Coefficients:
```

```
##          ar1      ma1  intercept
```

```
##      0.8717  0.7136   -1.0092
```

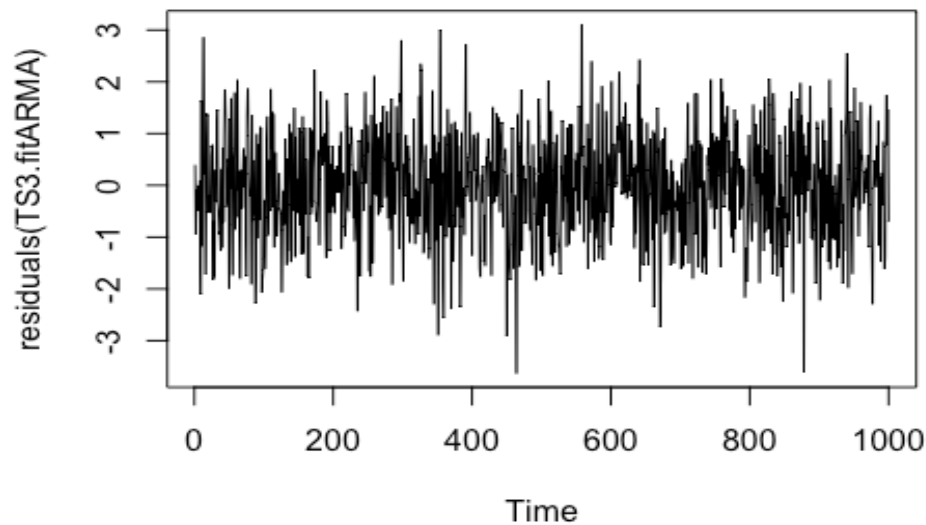
```
## s.e.  0.0158  0.0228    0.4241
```

```
##
```

```
## sigma^2 estimated as 1.022:  log likelihood = -1431.3,  aic = 2870.61
```

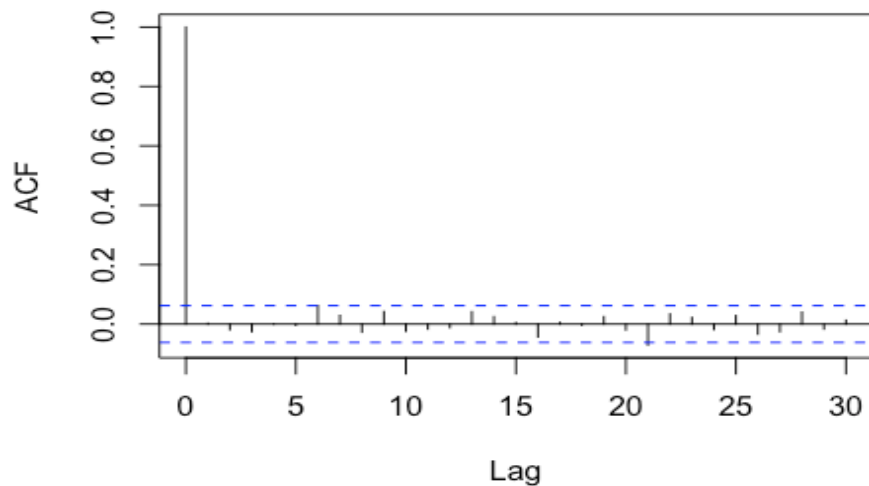
```
plot.ts(residuals(TS3.fitARMA), main= "Residual Series for a ARMA fit on TS3  
data")
```

### Residual Series for a ARMA fit on TS3 data



```
acf(residuals(TS3.fitARMA))
```

### Series residuals(TS3.fitARMA)



(Q3d)

The initial plots for TS3 showed plenty of white noise, with the pacf plot showing plenty of decay or persistence and the acf plot also showing decay, therefore my initial model was going to be fitting a ARMA model with p and q being of value 1.

Initial Equation – ARMA(1,1) is:  $y_t = p_1 * y_{t-1} + \epsilon_t + \alpha_1 * \epsilon_{t-1}$  where  $\epsilon_t \sim WN$

(Q3e)

Fitted Equation –  $y_t = 0.8717 * y_{t-1} + \epsilon_t + 0.7136 * 0.0228$

(Q3f)

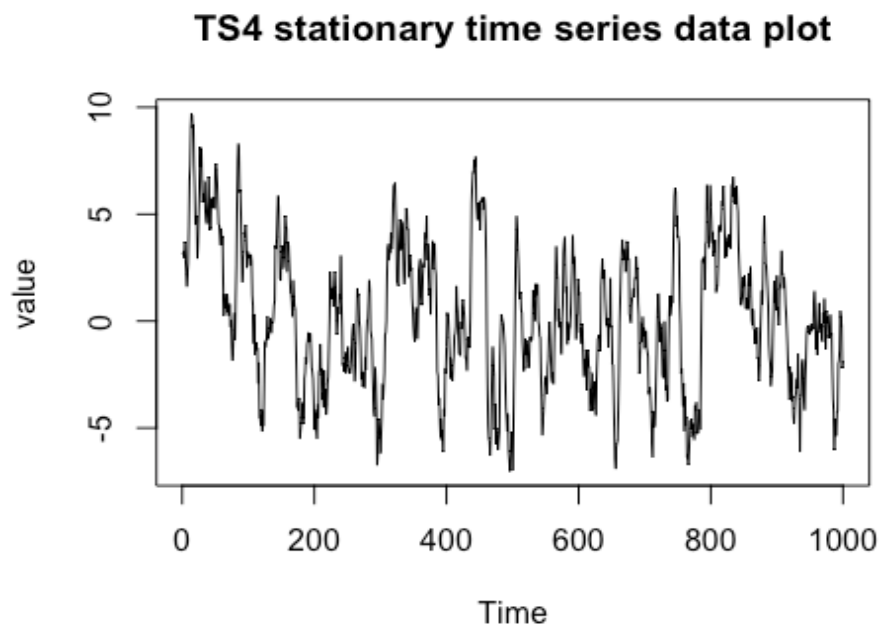
The residuals plot from my model show a constant variance with a mean of 0, only appearing to show white noise it seems. (Q3g) The acf plot looks much better with no more lags showing the model is a good fit.

(Q3h)

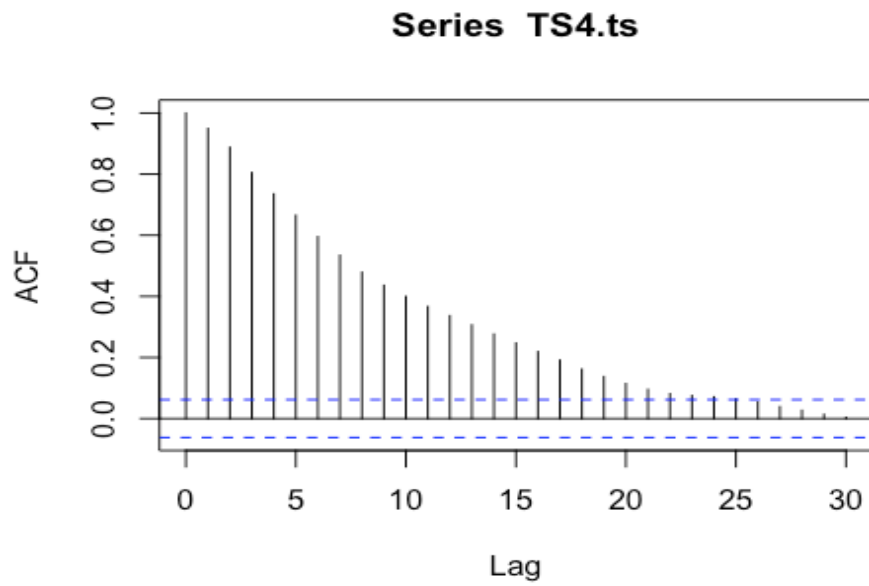
I tried add an extra AR and AM term to the above model separately but finding that the AIC for both models were higher then my original above, I rejected both of them.

Question 4

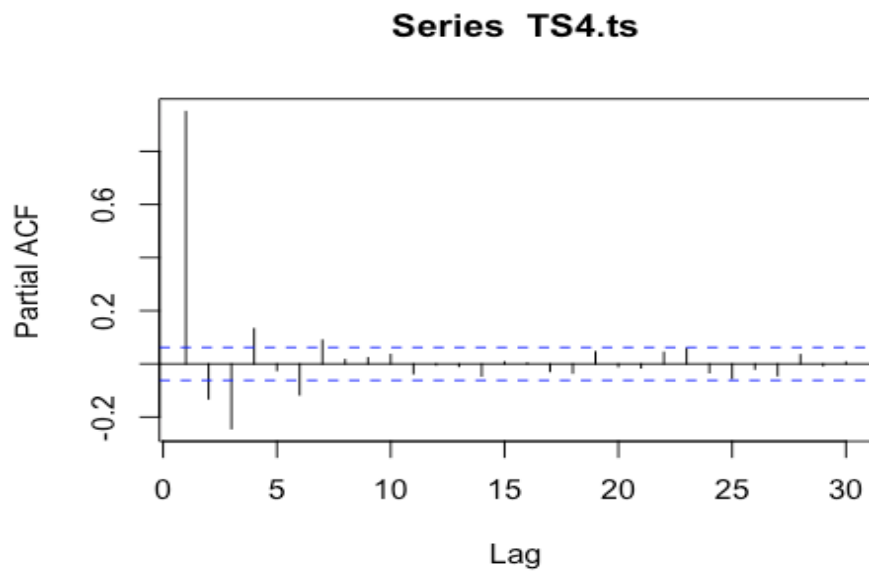
```
TS4.ts = ts(some_data$TS4, frequency = 1, start=1)
plot.ts(TS4.ts, main="TS4 stationary time series data plot", xlab="Time", ylab="value")
```



```
acf(TS4.ts)
```



```
pacf(TS4.ts)
```

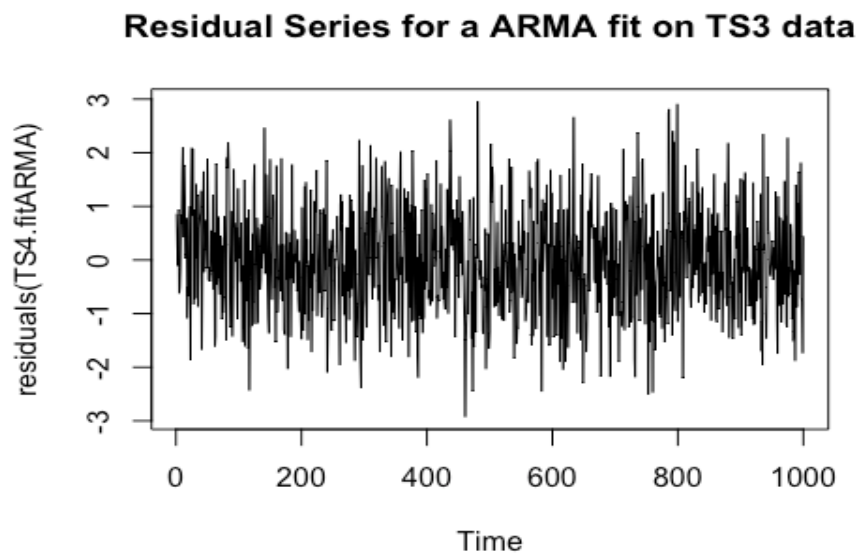


```
TS4.fitARMA = arima(TS4.ts, order=c(3,0,1))
TS4.fitARMA

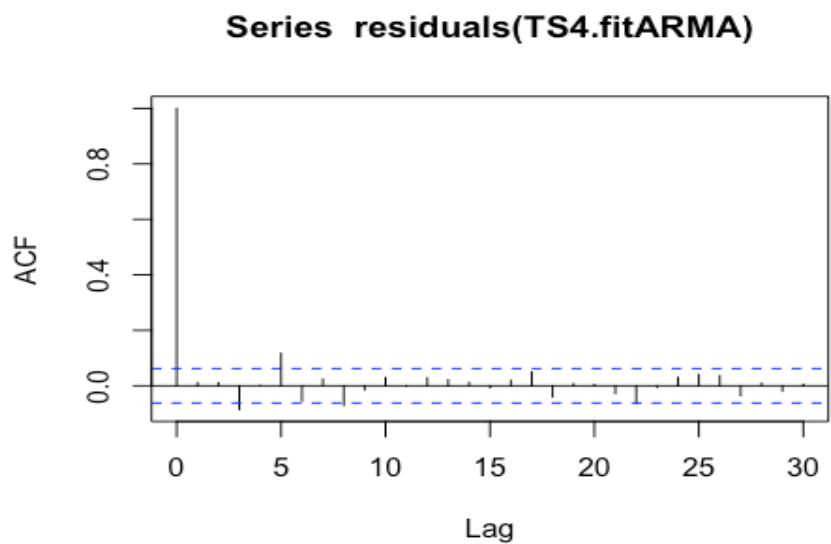
##
## Call:
## arima(x = TS4.ts, order = c(3, 0, 1))
##
## Coefficients:
##          ar1          ar2          ar3          ma1  intercept
```



```
##      0.7392  0.4725 -0.3009  0.3252    0.2243
## s.e. 0.0732  0.0746  0.0303  0.0732    0.4619
##
## sigma^2 estimated as 0.9828:  log likelihood = -1411.57,  aic = 2835.14
plot.ts(residuals(TS4.fitARMA), main= "Residual Series for a ARMA fit on TS3
data")
```



```
acf(residuals(TS4.fitARMA))
```



(Q4d)

The initial plots for TS4 showed plenty of white noise, with the acf plot showing strong decay and the pacf plot showing perhaps some decay or persistence and a cutoff at lag(3), therefore my initial model was going to be fitting an ARMA model with p and q being of value 3 and 1.

Initial Equation - ARMA(3,1) is:  $y_t = p_1 * y_{t-1} + p_2 * y_{t-2} + p_3 * y_{t-3} + \epsilon_t + \alpha_1 * \epsilon_{t-1}$  where  $\epsilon_t \sim WN$   
(Q4e)

Fitted Equation -  $y_t = 0.7392 * y_{t-1} + 0.4725 * y_{t-2} - 0.3009 * y_{t-3} + \epsilon_t + 0.3252 * \epsilon_{t-1}$   
(Q4f)

The residuals plot from my model show a constant variance with a mean of 0, only appearing to show white noise it seems. (Q4g) The acf plot looks much better but still has a few lag issues at 3 and 5.

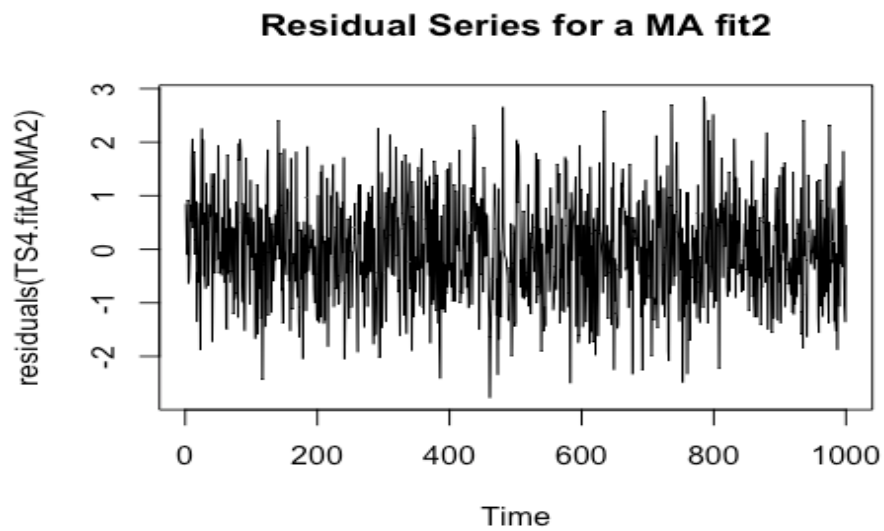
(Q4h)

I tried adding another AR and MA term so my model was ARMA(4,2) the AIC of this model is better than my original model of 2835.14 - 2813.61 as below, also the residuals look much better when looking at the acf and all the lags are not significant any more.

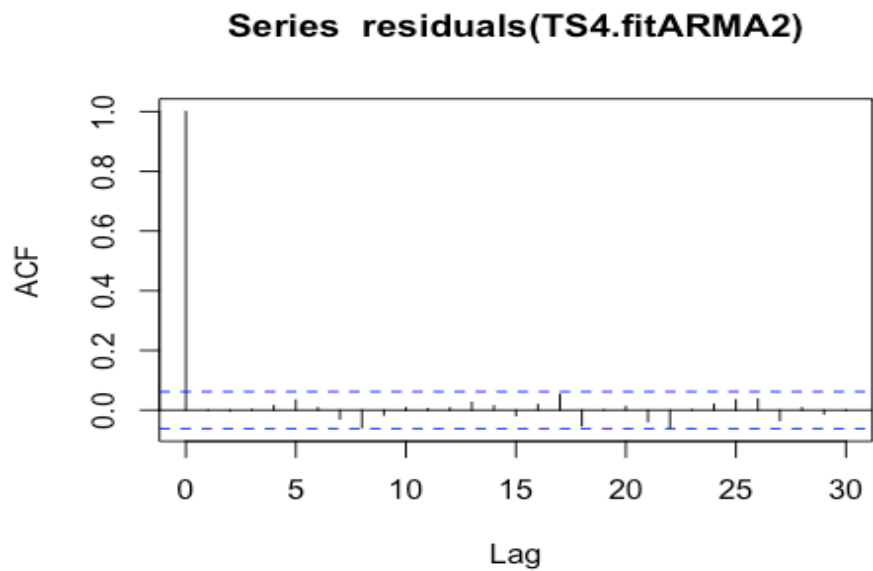
```
TS4.fitARMA2 = arima(TS4.ts, order=c(4,0,2))
TS4.fitARMA2

##
## Call:
## arima(x = TS4.ts, order = c(4, 0, 2))
##
## Coefficients:
##          ar1      ar2      ar3      ar4      ma1      ma2  intercept
##          0.1542  0.5590  0.2802 -0.1498  0.9347  0.578   0.2286
## s.e.      0.1359  0.1346  0.0855  0.0623  0.1312  0.067   0.4919
##
## sigma^2 estimated as 0.9579:  log likelihood = -1398.8,  aic = 2813.61

plot.ts(residuals(TS4.fitARMA2), main= "Residual Series for a MA fit2")
```



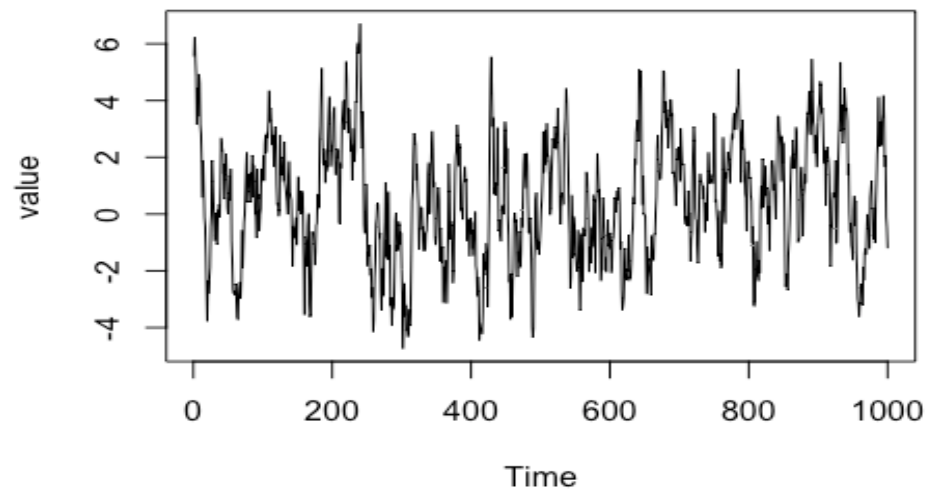
```
acf(residuals(TS4.fitARMA2))
```



Question 5

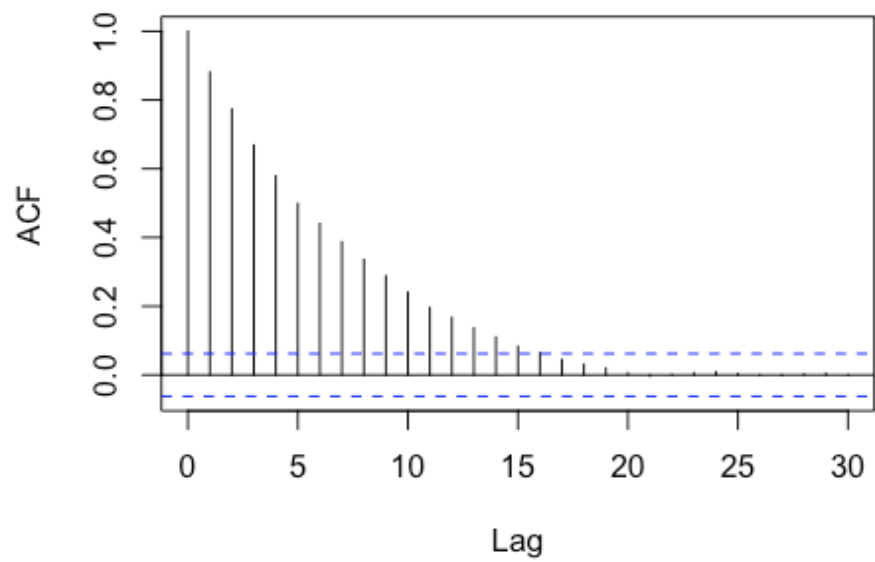
```
TS5.ts = ts(some_data$TS5, frequency = 1, start=1)
plot.ts(TS5.ts, main="TS5 stationary time series data plot", xlab="Time", ylab="value")
```

**TS5 stationary time series data plot**

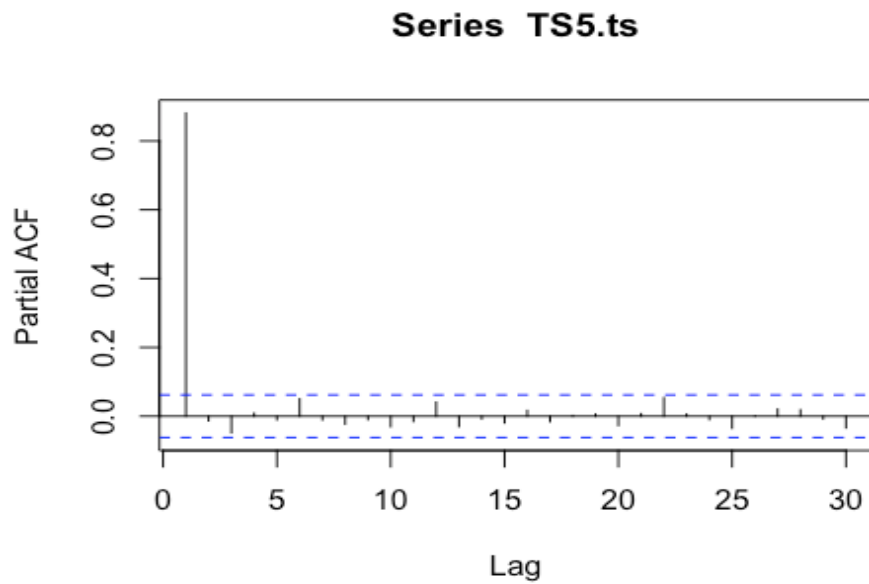


```
acf(TS5.ts)
```

**Series TS5.ts**



```
pacf(TS5.ts)
```

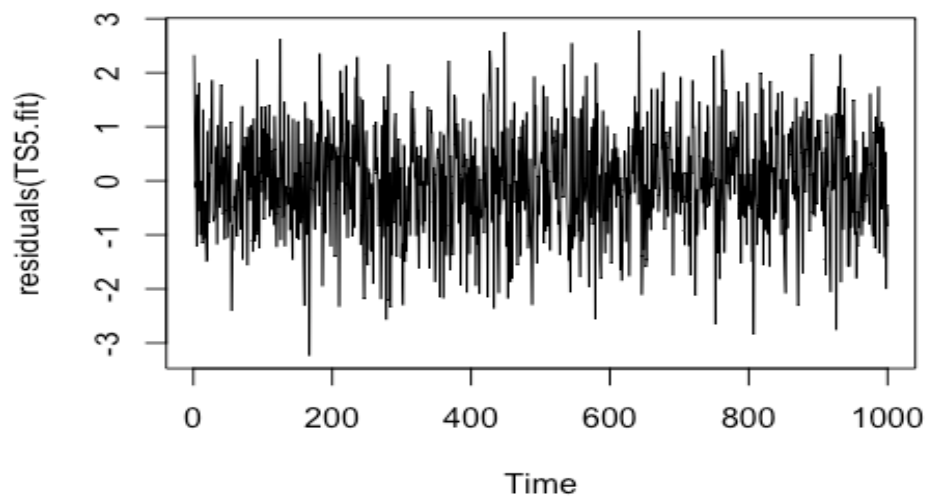


```
TS5.fit = arima(TS5.ts, order=c(1,0,0))
TS5.fit

##
## Call:
## arima(x = TS5.ts, order = c(1, 0, 0))
##
## Coefficients:
##          ar1  intercept
##          0.8861    0.5293
## s.e.    0.0147    0.2716
##
## sigma^2 estimated as 0.9723:  log likelihood = -1405.68,  aic = 2817.36

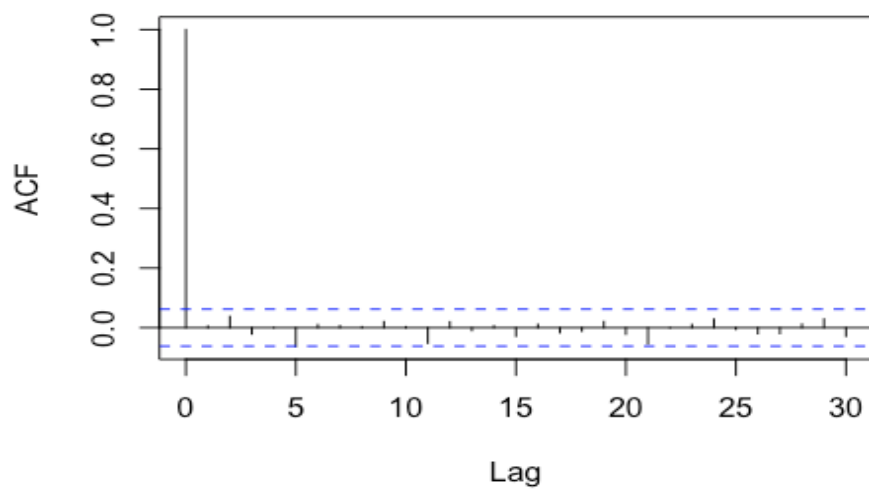
plot.ts(residuals(TS5.fit), main= "Residual Series for a ARMA fit on TS3 data")
```

**Residual Series for a ARMA fit on TS3 data**



```
acf(residuals(TS5.fit))
```

**Series residuals(TS5.fit)**



(Q5d)

The initial plots for TS5 showed plenty of white noise, with the acf plot showing strong decay and the pacf plot showing no persistence and a cutoff at lag(1), therefore my initial model was going to be fitting an AR(1) model.

Initial Equation -  $y_t = \rho y_{t-1} + \epsilon_t$  where  $\epsilon_t \sim \text{wn}$

(Q5e)

Fitted Equation –  $y_t = 0.8861 * y_{t-1} + 0.0147$

(Q5f)

The residuals plot from my model show a constant variance with a mean of 0, only appearing to show white noise it seems. (Q5g) The acf plot of the residuals looks fine.

(Q5h)

I did not really know how to improve this model, I tried adding a moving average term to see if it would reduce the AIC but it was higher. I think my original is the best final model.