

9



Our fundamental unit of text analysis is the document term matrix.



Our fundamental unit of text analysis is the document term matrix.

This is a set of stacked vectors, with each entry in each vector representing the 'amount' of a particular term.



Our fundamental unit of text analysis is the document term matrix.

This is a set of stacked vectors, with each entry in each vector representing the 'amount' of a particular term.

This is could be (re-)weighted in some way (e.g. tfidf).



Our fundamental unit of text analysis is the document term matrix.

This is a set of stacked vectors, with each entry in each vector representing the 'amount' of a particular term.

This is could be (re-)weighted in some way (e.g. tfidf).

now cover some fundamental statistical properties of text

9



Our fundamental unit of text analysis is the document term matrix.

This is a set of stacked vectors, with each entry in each vector representing the 'amount' of a particular term.

This is could be (re-)weighted in some way (e.g. tfidf).

now cover some fundamental statistical properties of text

and think about how to compare documents,



Our fundamental unit of text analysis is the document term matrix.

This is a set of stacked vectors, with each entry in each vector representing the 'amount' of a particular term.

This is could be (re-)weighted in some way (e.g. tfidf).

now cover some fundamental statistical properties of text

and think about how to compare documents, and summarize their content.

• collect raw text in machine readable/electronic form. Decide what constitutes a document.

- collect raw text in machine readable/electronic form. Decide what constitutes a document.
- 2 strip away 'superfluous' material: HTML tags, capitalization, punctuation, stop words etc.

- collect raw text in machine readable/electronic form. Decide what constitutes a document.
- Strip away 'superfluous' material: HTML tags, capitalization, punctuation, stop words etc.
- 3 cut document up into useful elementary pieces: tokenization.

- collect raw text in machine readable/electronic form. Decide what constitutes a document.
- Strip away 'superfluous' material: HTML tags, capitalization, punctuation, stop words etc.
- 3 cut document up into useful elementary pieces: tokenization.
- add descriptive annotations that preserve context: tagging.

- collect raw text in machine readable/electronic form. Decide what constitutes a document.
- Strip away 'superfluous' material: HTML tags, capitalization, punctuation, stop words etc.
- 3 cut document up into useful elementary pieces: tokenization.
- add descriptive annotations that preserve context: tagging.
- map tokens back to common form: lemmatization, stemming.

- collect raw text in machine readable/electronic form. Decide what constitutes a document.
- Strip away 'superfluous' material: HTML tags, capitalization, punctuation, stop words etc.
- 3 cut document up into useful elementary pieces: tokenization.
- add descriptive annotations that preserve context: tagging.
- map tokens back to common form: lemmatization, stemming.
- operate/model.

• collect raw text in machine readable/electronic form. Decide what constitutes a document.

"PREPROCESSING"

operate/model.

a type is a unique sequence of characters that are grouped together in some meaningful way.

a type is a unique sequence of characters that are grouped together in some meaningful way. Mostly a word (for us),

a type is a unique sequence of characters that are grouped together in some meaningful way. Mostly a word (for us), but might also be a word plus punctuation,

a type is a unique sequence of characters that are grouped together in some meaningful way. Mostly a word (for us), but might also be a word plus punctuation, or a number etc.

a type is a unique sequence of characters that are grouped together in some meaningful way. Mostly a word (for us), but might also be a word plus punctuation, or a number etc.

e.g. 'France', 'American Revolution', '1981'

a type is a unique sequence of characters that are grouped together in some meaningful way. Mostly a word (for us), but might also be a word plus punctuation, or a number etc.

```
e.g. 'France', 'American Revolution', '1981'
```

a token is a particular instance of type.

e.g. "Dog eat dog world",

a type is a unique sequence of characters that are grouped together in some meaningful way. Mostly a word (for us), but might also be a word plus punctuation, or a number etc.

e.g. 'France', 'American Revolution', '1981'

a token is a particular instance of type.

e.g. "Dog eat dog world", contains three types,

a type is a unique sequence of characters that are grouped together in some meaningful way. Mostly a word (for us), but might also be a word plus punctuation, or a number etc.

e.g. 'France', 'American Revolution', '1981'

a token is a particular instance of type.

e.g. "Dog eat dog world", contains three types, but four tokens (for most purposes).

a type is a unique sequence of characters that are grouped together in some meaningful way. Mostly a word (for us), but might also be a word plus punctuation, or a number etc.

e.g. 'France', 'American Revolution', '1981'

a token is a particular instance of type.

e.g. "Dog eat dog world", contains three types, but four tokens (for most purposes).

a term is a type that is part of the system's 'dictionary' (i.e. what the quantitative analysis technique recognizes as a type to be recorded etc). Could be different from the tokens, but often closely related.

()

a type is a unique sequence of characters that are grouped together in some meaningful way. Mostly a word (for us), but might also be a word plus punctuation, or a number etc.

- e.g. 'France', 'American Revolution', '1981'
  - a token is a particular instance of type.
- e.g. "Dog eat dog world", contains three types, but four tokens (for most purposes).
  - a term is a type that is part of the system's 'dictionary' (i.e. what the quantitative analysis technique recognizes as a type to be recorded etc). Could be different from the tokens, but often closely related.
- e.g. stemmed word like 'treasuri', which doesn't appear in the document itself.

• when we use the vector space model we remove some information and throw it away

• when we use the vector space model we remove some information and throw it away (e.g. word order, numbers, capitals, stop words).

- when we use the vector space model we remove some information and throw it away (e.g. word order, numbers, capitals, stop words).
- → this means we cannot restore the original representation of the data:

- when we use the vector space model we remove some information and throw it away (e.g. word order, numbers, capitals, stop words).
- → this means we cannot restore the original representation of the data: we have a lossy compression.

- when we use the vector space model we remove some information and throw it away (e.g. word order, numbers, capitals, stop words).
- $\rightarrow$  this means we cannot restore the original representation of the data: we have a lossy compression.

but presumably, life becomes a lot simpler and the tradeoff is worth it.

- when we use the vector space model we remove some information and throw it away (e.g. word order, numbers, capitals, stop words).
- → this means we cannot restore the original representation of the data: we have a lossy compression.

but presumably, life becomes a lot simpler and the tradeoff is worth it. How much simpler?

- when we use the vector space model we remove some information and throw it away (e.g. word order, numbers, capitals, stop words).
- → this means we cannot restore the original representation of the data: we have a lossy compression.

but presumably, life becomes a lot simpler and the tradeoff is worth it. How much simpler?

- when we use the vector space model we remove some information and throw it away (e.g. word order, numbers, capitals, stop words).
- $\rightarrow$  this means we cannot restore the original representation of the data: we have a lossy compression.

but presumably, life becomes a lot simpler and the tradeoff is worth it. How much simpler?

e.g. Reuters Corpus Volume 1 (RCV1) (2004) is a benchmark text collection of  $\sim 800000$  manually coded news stories.

- when we use the vector space model we remove some information and throw it away (e.g. word order, numbers, capitals, stop words).
- $\rightarrow$  this means we cannot restore the original representation of the data: we have a lossy compression.

but presumably, life becomes a lot simpler and the tradeoff is worth it. How much simpler?

e.g. Reuters Corpus Volume 1 (RCV1) (2004) is a benchmark text collection of  $\sim 800000$  manually coded news stories.

- when we use the vector space model we remove some information and throw it away (e.g. word order, numbers, capitals, stop words).
- → this means we cannot restore the original representation of the data: we have a lossy compression.

but presumably, life becomes a lot simpler and the tradeoff is worth it. How much simpler?

e.g. Reuters Corpus Volume 1 (RCV1) (2004) is a benchmark text collection of  $\sim 800000$  manually coded news stories.

RCV1 has 484, 494 types and 197, 879, 290 tokens (MR&S book, Table 5.1).

rm numbers 473,723 | 179,158,204

- when we use the vector space model we remove some information and throw it away (e.g. word order, numbers, capitals, stop words).
- $\rightarrow$  this means we cannot restore the original representation of the data: we have a lossy compression.

but presumably, life becomes a lot simpler and the tradeoff is worth it. How much simpler?

e.g. Reuters Corpus Volume 1 (RCV1) (2004) is a benchmark text collection of  $\sim 800000$  manually coded news stories.

rm numb	ers	473,723	179,158,204
lowercase		391,523	179,158,204

- when we use the vector space model we remove some information and throw it away (e.g. word order, numbers, capitals, stop words).
- → this means we cannot restore the original representation of the data: we have a lossy compression.

but presumably, life becomes a lot simpler and the tradeoff is worth it. How much simpler?

e.g. Reuters Corpus Volume 1 (RCV1) (2004) is a benchmark text collection of  $\sim 800000$  manually coded news stories.

rm numbers	473,723	179,158,204
lowercase	391,523	179,158,204
rm 150 stopwords	391,373	94,516,599

- when we use the vector space model we remove some information and throw it away (e.g. word order, numbers, capitals, stop words).
- → this means we cannot restore the original representation of the data: we have a lossy compression.

but presumably, life becomes a lot simpler and the tradeoff is worth it. How much simpler?

e.g. Reuters Corpus Volume 1 (RCV1) (2004) is a benchmark text collection of  $\sim 800000$  manually coded news stories.

rm numbers	473,723	179,158,204
lowercase	391,523	179,158,204
rm 150 stopwords	391,373	94,516,599
stemming	322,383	94,516,599

So pre-processing 'works' in the sense that it serves to simplify the problem.

So pre-processing 'works' in the sense that it serves to simplify the problem.

but how does the total number of types M, change as total number of tokens T increases ?

So pre-processing 'works' in the sense that it serves to simplify the problem.

but how does the total number of types M, change as total number of tokens T increases ?

Heap's Law:

So pre-processing 'works' in the sense that it serves to simplify the problem.

but how does the total number of types M, change as total number of tokens T increases ?

Heap's Law:  $M = kT^b$ 

So pre-processing 'works' in the sense that it serves to simplify the problem.

but how does the total number of types M, change as total number of tokens T increases ?

Heap's Law: 
$$M = kT^b$$

- So pre-processing 'works' in the sense that it serves to simplify the problem.
- but how does the total number of types M, change as total number of tokens T increases ?

Heap's Law: 
$$M = kT^b$$

where  $k \in (30, 100)$  and  $b \in (0.4, 0.6)$  for English.

if we preprocess in different ways,

()

- So pre-processing 'works' in the sense that it serves to simplify the problem.
- but how does the total number of types M, change as total number of tokens T increases ?

Heap's Law: 
$$M = kT^b$$

where  $k \in (30, 100)$  and  $b \in (0.4, 0.6)$  for English.

if we preprocess in different ways, we cause k to be different.

()

- So pre-processing 'works' in the sense that it serves to simplify the problem.
- but how does the total number of types M, change as total number of tokens T increases ?

Heap's Law: 
$$M = kT^b$$

- if we preprocess in different ways, we cause k to be different.
- NB number of types increases rapidly at first,

- So pre-processing 'works' in the sense that it serves to simplify the problem.
- but how does the total number of types M, change as total number of tokens T increases ?

Heap's Law: 
$$M = kT^b$$

- if we preprocess in different ways, we cause k to be different.
- NB number of types increases rapidly at first, then less rapidly.

- So pre-processing 'works' in the sense that it serves to simplify the problem.
- but how does the total number of types M, change as total number of tokens T increases ?

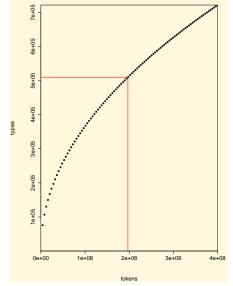
Heap's Law: 
$$M = kT^b$$

- if we preprocess in different ways, we cause k to be different.
- NB number of types increases rapidly at first, then less rapidly. Need to preprocess, especially for long collections!

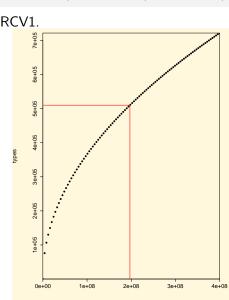
k = 44, b = 0.49, T = 400,000

# k = 44, b = 0.49, T = 400,000



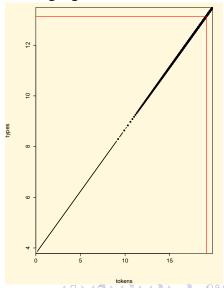


k = 44, b = 0.49, T = 400,000



tokens

RCV1, log-log.



Heap's Law tells us about the relationship between tokens and types.

Heap's Law tells us about the relationship between tokens and types.

but what about the relationship between the relative frequency of terms in the corpus?

Heap's Law tells us about the relationship between tokens and types.

- but what about the relationship between the relative frequency of terms in the corpus?
  - → how much more common is the most common term relative to the second common term?

Heap's Law tells us about the relationship between tokens and types.

- but what about the relationship between the relative frequency of terms in the corpus?
  - → how much more common is the most common term relative to the second common term? What about relative to the third most common term? And the fourth...

Heap's Law tells us about the relationship between tokens and types.

- but what about the relationship between the relative frequency of terms in the corpus?
  - → how much more common is the most common term relative to the second common term? What about relative to the third most common term? And the fourth...

Zipf's Law: corpus frequency of *i*th most common term is  $\propto \frac{1}{i}$ 



Heap's Law tells us about the relationship between tokens and types.

- but what about the relationship between the relative frequency of terms in the corpus?
  - → how much more common is the most common term relative to the second common term? What about relative to the third most common term? And the fourth...

Zipf's Law: corpus frequency of *i*th most common term is  $\propto \frac{1}{i}$ 



so second most common term is half as common as most common,

Heap's Law tells us about the relationship between tokens and types. but what about the relationship between the relative frequency of terms in the corpus?

→ how much more common is the most common term relative to the second common term? What about relative to the third most common term? And the fourth...

Zipf's Law: corpus frequency of *i*th most common term is  $\propto \frac{1}{i}$ 



so second most common term is half as common as most common, and third most common term is one third as common as most common,

Heap's Law tells us about the relationship between tokens and types. but what about the relationship between the relative frequency of terms in the corpus?

→ how much more common is the most common term relative to the second common term? What about relative to the third most common term? And the fourth...

Zipf's Law: corpus frequency of *i*th most common term is  $\propto \frac{1}{i}$ 



so second most common term is half as common as most common, and third most common term is one third as common as most common, and fourth most common term is one quarter as common as most common.

Heap's Law tells us about the relationship between tokens and types. but what about the relationship between the relative frequency of terms in the corpus?

→ how much more common is the most common term relative to the second common term? What about relative to the third most common term? And the fourth...

Zipf's Law: corpus frequency of *i*th most common term is  $\propto \frac{1}{i}$ 



so second most common term is half as common as most common, and third most common term is one third as common as most common, and fourth most common term is one quarter as common as most common.

etc Can rewrite as:

Heap's Law tells us about the relationship between tokens and types. but what about the relationship between the relative frequency of terms in the corpus?

→ how much more common is the most common term relative to the second common term? What about relative to the third most common term? And the fourth...

Zipf's Law: corpus frequency of *i*th most common term is  $\propto \frac{1}{i}$ 



so second most common term is half as common as most common, and third most common term is one third as common as most common, and fourth most common term is one quarter as common as most

etc Can rewrite as: corpus frequency of  $i = ci^k$  or

common.

in the corpus?

Heap's Law tells us about the relationship between tokens and types. but what about the relationship between the relative frequency of terms

→ how much more common is the most common term relative to the second common term? What about relative to the third most common term? And the fourth...

Zipf's Law: corpus frequency of *i*th most common term is  $\propto \frac{1}{i}$ 



- so second most common term is half as common as most common,
- and third most common term is one third as common as most common,
- and fourth most common term is one quarter as common as most common,
- etc Can rewrite as: corpus frequency of  $i = ci^k$  or log(corpus frequency) = log <math>c + k log i,

Heap's Law tells us about the relationship between tokens and types.

- but what about the relationship between the relative frequency of terms in the corpus?
  - → how much more common is the most common term relative to the second common term? What about relative to the third most common term? And the fourth...

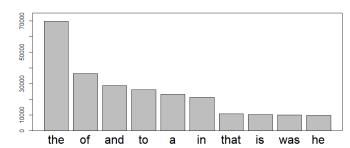
Zipf's Law: corpus frequency of *i*th most common term is  $\propto \frac{1}{i}$ 



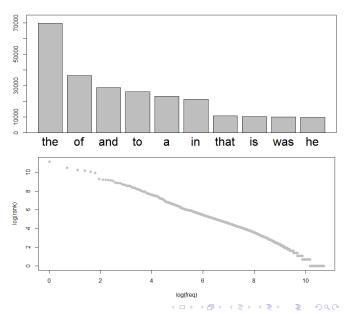
- so second most common term is half as common as most common,
- and third most common term is one third as common as most common,
- and fourth most common term is one quarter as common as most common,
- etc Can rewrite as: corpus frequency of  $i = ci^k$  or  $\log(\text{corpus frequency}) = \log c + k \log i$ , where i is the rank, k = -1.

term	freq
the	69836
of	36365
and	28826
to	26126
a	23157
in	21314
that	10777
is	10182
was	9968
he	9801

term	freq
the	69836
of	36365
and	28826
to	26126
a	23157
in	21314
that	10777
is	10182
was	9968
he	9801

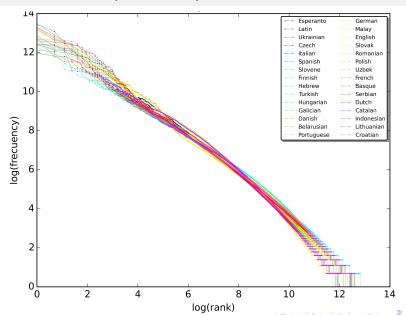


term	freq
the	69836
of	36365
and	28826
to	26126
a	23157
in	21314
that	10777
is	10182
was	9968
he	9801



# Other Languages (Wikipedia)

# Other Languages (Wikipedia)



City Populations in US (Gabaix, 1999)

# City Populations in US (Gabaix, 1999)

740 QUARTERLY JOURNAL OF ECONOMICS

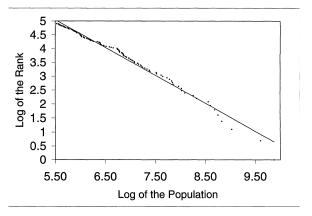


FIGURE I

Log Size versus Log Rank of the 135 largest U. S. Metropolitan Areas in 1991 Source: Statistical Abstract of the United States [1993].

Recall that the vector space model represents a document as a point in the feature space.

i.e.  $\mathbf{y}_d \in \mathbb{R}^W$  is a representation of document d.

- i.e.  $\mathbf{y}_d \in \mathbb{R}^W$  is a representation of document d.
  - q how 'far' is that document from some other document (in the same space)?

- i.e.  $\mathbf{y}_d \in \mathbb{R}^W$  is a representation of document d.
  - q how 'far' is that document from some other document (in the same space)?
- → tells us about similarity of documents

- i.e.  $\mathbf{y}_d \in \mathbb{R}^W$  is a representation of document d.
  - q how 'far' is that document from some other document (in the same space)?
- → tells us about similarity of documents
- and is typically required for application of multivariate techniques, anyway

- i.e.  $\mathbf{y}_d \in \mathbb{R}^W$  is a representation of document d.
  - q how 'far' is that document from some other document (in the same space)?
- → tells us about similarity of documents
- and is typically required for application of multivariate techniques, anyway
- e.g. principal components analysis operates on distance matrix.

NB not all measures of distance or similarity are metrics.

NB not all measures of distance or similarity are metrics. To be a metric, the measure of *distance* between documents i and j,  $s_{ij}$  must have certain properties:

NB not all measures of distance or similarity are metrics. To be a metric, the measure of *distance* between documents i and j,  $s_{ij}$  must have certain properties:

1 no negative distances:  $s_{ij} \ge 0$ 

- NB not all measures of distance or similarity are metrics. To be a metric, the measure of *distance* between documents i and j,  $s_{ij}$  must have certain properties:
  - 1 no negative distances:  $s_{ij} \ge 0$
  - 2 distance between documents is zero ← documents are identical

- NB not all measures of distance or similarity are metrics. To be a metric, the measure of *distance* between documents i and j,  $s_{ij}$  must have certain properties:
  - 1 no negative distances:  $s_{ii} \ge 0$
  - 2 distance between documents is zero  $\iff$  documents are identical
  - 3 distance between documents is symmetric:

- NB not all measures of distance or similarity are metrics. To be a metric, the measure of *distance* between documents i and j,  $s_{ij}$  must have certain properties:
  - 1 no negative distances:  $s_{ii} \ge 0$
  - 2 distance between documents is zero  $\iff$  documents are identical
  - 3 distance between documents is symmetric:  $s_{ij} = s_{ji}$

- NB not all measures of distance or similarity are metrics. To be a metric, the measure of *distance* between documents i and j,  $s_{ij}$  must have certain properties:
  - 1 no negative distances:  $s_{ii} \ge 0$
  - 2 distance between documents is zero  $\iff$  documents are identical
  - 3 distance between documents is symmetric:  $s_{ij} = s_{ji}$
  - 4 measures satisfy triangle inequality.  $s_{ik} \leq s_{ij} + s_{jk}$

- NB not all measures of distance or similarity are metrics. To be a metric, the measure of *distance* between documents i and j,  $s_{ij}$  must have certain properties:
  - 1 no negative distances:  $s_{ii} \ge 0$
  - 2 distance between documents is zero ← documents are identical
  - 3 distance between documents is symmetric:  $s_{ij} = s_{ji}$
  - 4 measures satisfy triangle inequality.  $s_{ik} \leq s_{ij} + s_{jk}$
- i.e. if doc i is similar to doc j and doc j is similar to doc k,

- NB not all measures of distance or similarity are metrics. To be a metric, the measure of *distance* between documents i and j,  $s_{ij}$  must have certain properties:
  - 1 no negative distances:  $s_{ii} \ge 0$
  - 2 distance between documents is zero ← documents are identical
  - 3 distance between documents is symmetric:  $s_{ij} = s_{ji}$
  - 4 measures satisfy triangle inequality.  $s_{ik} \leq s_{ij} + s_{jk}$
- i.e. if doc i is similar to doc j and doc j is similar to doc k, then doc i is similar to doc k

-0

- NB not all measures of distance or similarity are metrics. To be a metric, the measure of *distance* between documents i and j,  $s_{ij}$  must have certain properties:
  - 1 no negative distances:  $s_{ii} \ge 0$
  - 2 distance between documents is zero ← documents are identical
  - 3 distance between documents is symmetric:  $s_{ij} = s_{ji}$
  - 4 measures satisfy triangle inequality.  $s_{ik} \leq s_{ij} + s_{jk}$
- i.e. if doc i is similar to doc j and doc j is similar to doc k, then doc i is similar to doc k (we have an upper bound on how far apart they can be)

()

The 'ordinary', 'straight line' distance between two points in space. Recall that  $\mathbf{y}_i$  and  $\mathbf{y}_i$  are documents,

The 'ordinary', 'straight line' distance between two points in space. Recall that  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are documents,

$$\|\mathbf{y}_i - \mathbf{y}_j\| = \sqrt{(\mathbf{y}_i - \mathbf{y}_j) \cdot (\mathbf{y}_i - \mathbf{y}_j)} = \sqrt{\sum (\mathbf{y}_i - \mathbf{y}_j)^2}$$

The 'ordinary', 'straight line' distance between two points in space. Recall that  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are documents,

$$\|\mathbf{y}_i - \mathbf{y}_j\| = \sqrt{(\mathbf{y}_i - \mathbf{y}_j) \cdot (\mathbf{y}_i - \mathbf{y}_j)} = \sqrt{\sum (\mathbf{y}_i - \mathbf{y}_j)^2}$$

e.g.  $\mathbf{y}_i = [0.00, 0.00, 1.38, 1.52, 0.00]$  and  $\mathbf{y}_j = [0.00, 2.13, 3.24, 0.01, 0.06]$ 

The 'ordinary', 'straight line' distance between two points in space. Recall that  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are documents,

$$\|\mathbf{y}_i - \mathbf{y}_j\| = \sqrt{(\mathbf{y}_i - \mathbf{y}_j) \cdot (\mathbf{y}_i - \mathbf{y}_j)} = \sqrt{\sum (\mathbf{y}_i - \mathbf{y}_j)^2}$$

e.g. 
$$\mathbf{y}_i = [0.00, 0.00, 1.38, 1.52, 0.00]$$
 and  $\mathbf{y}_j = [0.00, 2.13, 3.24, 0.01, 0.06]$  well  $(\mathbf{y}_i - \mathbf{y}_i) = [0.00, -2.13, -1.86, 1.51, -0.06]$ 

The 'ordinary', 'straight line' distance between two points in space. Recall that  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are documents,

$$\|\mathbf{y}_i - \mathbf{y}_j\| = \sqrt{(\mathbf{y}_i - \mathbf{y}_j) \cdot (\mathbf{y}_i - \mathbf{y}_j)} = \sqrt{\sum (\mathbf{y}_i - \mathbf{y}_j)^2}$$

e.g. 
$$\mathbf{y}_i = [0.00, 0.00, 1.38, 1.52, 0.00]$$
 and  $\mathbf{y}_j = [0.00, 2.13, 3.24, 0.01, 0.06]$  well  $(\mathbf{y}_i - \mathbf{y}_j) = [0.00, -2.13, -1.86, 1.51, -0.06]$  and  $(\mathbf{y}_i - \mathbf{y}_i) \cdot (\mathbf{y}_i - \mathbf{y}_i) = [0.00, -2.13, -1.86, 1.51, -0.06]$ 

The 'ordinary', 'straight line' distance between two points in space. Recall that  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are documents,

$$\|\mathbf{y}_i - \mathbf{y}_j\| = \sqrt{(\mathbf{y}_i - \mathbf{y}_j) \cdot (\mathbf{y}_i - \mathbf{y}_j)} = \sqrt{\sum (\mathbf{y}_i - \mathbf{y}_j)^2}$$

e.g. 
$$\mathbf{y}_i = [0.00, 0.00, 1.38, 1.52, 0.00]$$
 and  $\mathbf{y}_j = [0.00, 2.13, 3.24, 0.01, 0.06]$  well  $(\mathbf{y}_i - \mathbf{y}_j) = [0.00, -2.13, -1.86, 1.51, -0.06]$  and  $(\mathbf{y}_i - \mathbf{y}_j) \cdot (\mathbf{y}_i - \mathbf{y}_j) = (0 \times 0) + (-2.13 \times -2.13) + (-1.86 \times -1.86) + (1.51 \times 1.51) + (-0.06 \times -0.06) = 10.2802$ 

()

The 'ordinary', 'straight line' distance between two points in space. Recall that  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are documents,

$$\|\mathbf{y}_i - \mathbf{y}_j\| = \sqrt{(\mathbf{y}_i - \mathbf{y}_j) \cdot (\mathbf{y}_i - \mathbf{y}_j)} = \sqrt{\sum (\mathbf{y}_i - \mathbf{y}_j)^2}$$

e.g. 
$$\mathbf{y}_i = [0.00, 0.00, 1.38, 1.52, 0.00]$$
 and  $\mathbf{y}_j = [0.00, 2.13, 3.24, 0.01, 0.06]$  well  $(\mathbf{y}_i - \mathbf{y}_j) = [0.00, -2.13, -1.86, 1.51, -0.06]$  and  $(\mathbf{y}_i - \mathbf{y}_j) \cdot (\mathbf{y}_i - \mathbf{y}_j) = (0 \times 0) + (-2.13 \times -2.13) + (-1.86 \times -1.86) + (1.51 \times 1.51) + (-0.06 \times -0.06) = 10.2802$ 

and 
$$\sqrt{(\mathbf{y}_i - \mathbf{y}_j) \cdot (\mathbf{y}_i - \mathbf{y}_j)} = 3.206275$$
 larger distances imply lower similarity.

()

Euclidean distance rewards magnitude, rather than direction.

Euclidean distance rewards magnitude, rather than direction.

i.e. doesn't reward being close in relative use of terms.

Euclidean distance rewards magnitude, rather than direction.

i.e. doesn't reward being close in relative use of terms. Instead, rewards documents that are similarly 'far' from the origin.

Euclidean distance rewards magnitude, rather than direction.

i.e. doesn't reward being close in relative use of terms. Instead, rewards documents that are similarly 'far' from the origin.

We can do better by normalizing document length,

Euclidean distance rewards magnitude, rather than direction.

i.e. doesn't reward being close in relative use of terms. Instead, rewards documents that are similarly 'far' from the origin.

We can do better by normalizing document length, and rewarding relatively similar uses of terms.

Euclidean distance rewards magnitude, rather than direction.

i.e. doesn't reward being close in relative use of terms. Instead, rewards documents that are similarly 'far' from the origin.

We can do better by normalizing document length, and rewarding relatively similar uses of terms.

→ divide out each of the components (the documents) by their length:

Euclidean distance rewards magnitude, rather than direction.

i.e. doesn't reward being close in relative use of terms. Instead, rewards documents that are similarly 'far' from the origin.

We can do better by normalizing document length, and rewarding relatively similar uses of terms.

 $\rightarrow$  divide out each of the components (the documents) by their length: the  $L^2$  norm,  $||\mathbf{y}_i|| = \sqrt{\sum w^2}$ ,

Euclidean distance rewards magnitude, rather than direction.

i.e. doesn't reward being close in relative use of terms. Instead, rewards documents that are similarly 'far' from the origin.

We can do better by normalizing document length, and rewarding relatively similar uses of terms.

 $\rightarrow$  divide out each of the components (the documents) by their length: the  $L^2$  norm,  $||\mathbf{y}_i|| = \sqrt{\sum w^2}$ , where w refers to the (weighted) frequency of a feature in the document vector.

Euclidean distance rewards magnitude, rather than direction.

- i.e. doesn't reward being close in relative use of terms. Instead, rewards documents that are similarly 'far' from the origin.
  - We can do better by normalizing document length, and rewarding relatively similar uses of terms.
- $\rightarrow$  divide out each of the components (the documents) by their length: the  $L^2$  norm,  $||\mathbf{y}_i|| = \sqrt{\sum w^2}$ , where w refers to the (weighted) frequency of a feature in the document vector.
- so when the document has generally high term frequencies (because it is longer),

Euclidean distance rewards magnitude, rather than direction.

- i.e. doesn't reward being close in relative use of terms. Instead, rewards documents that are similarly 'far' from the origin.
  - We can do better by normalizing document length, and rewarding relatively similar uses of terms.
- $\rightarrow$  divide out each of the components (the documents) by their length: the  $L^2$  norm,  $||\mathbf{y}_i|| = \sqrt{\sum w^2}$ , where w refers to the (weighted) frequency of a feature in the document vector.
- so when the document has generally high term frequencies (because it is longer),  $w^2$  will be larger,

Euclidean distance rewards magnitude, rather than direction.

- i.e. doesn't reward being close in relative use of terms. Instead, rewards documents that are similarly 'far' from the origin.
  - We can do better by normalizing document length, and rewarding relatively similar uses of terms.
- $\rightarrow$  divide out each of the components (the documents) by their length: the  $L^2$  norm,  $||\mathbf{y}_i|| = \sqrt{\sum w^2}$ , where w refers to the (weighted) frequency of a feature in the document vector.
- so when the document has generally high term frequencies (because it is longer),  $w^2$  will be larger, which makes  $||\mathbf{y}_i||$  larger.

()

$$c_{ij} = \frac{\mathbf{y}_i \cdot \mathbf{y}_j}{\|\mathbf{y}_i\| \|\mathbf{y}_j\|}$$

$$c_{ij} = \frac{\mathbf{y}_i \cdot \mathbf{y}_j}{\|\mathbf{y}_i\| \|\mathbf{y}_j\|}$$

 $\rightarrow$  we have a measure of similarity, which (since  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are non-negative) must be between 0 and 1.

$$c_{ij} = \frac{\mathbf{y}_i \cdot \mathbf{y}_j}{\|\mathbf{y}_i\| \|\mathbf{y}_j\|}$$

 $\rightarrow$  we have a measure of similarity, which (since  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are non-negative) must be between 0 and 1.

If  $y_i$  and  $y_j$  are vectors,  $c_{ij}$  is the cosine of the angle between them.

$$c_{ij} = \frac{\mathbf{y}_i \cdot \mathbf{y}_j}{\|\mathbf{y}_i\| \|\mathbf{y}_j\|}$$

 $\rightarrow$  we have a measure of similarity, which (since  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are non-negative) must be between 0 and 1.

If  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are vectors,  $c_{ij}$  is the cosine of the angle between them. and document length is controlled for.

$$c_{ij} = \frac{\mathbf{y}_i \cdot \mathbf{y}_j}{\|\mathbf{y}_i\| \|\mathbf{y}_j\|}$$

 $\rightarrow$  we have a measure of similarity, which (since  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are non-negative) must be between 0 and 1.

If  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are vectors,  $c_{ij}$  is the cosine of the angle between them. and document length is controlled for.

so intuitively,

$$c_{ij} = \left| \begin{array}{c} \mathbf{y}_i \cdot \mathbf{y}_j \\ \|\mathbf{y}_i\| \ \|\mathbf{y}_j\| \end{array} \right|$$

 $\rightarrow$  we have a measure of similarity, which (since  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are non-negative) must be between 0 and 1.

If  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are vectors,  $c_{ij}$  is the cosine of the angle between them. and document length is controlled for.

so intuitively, cosine similarity captures some notion of relative 'direction' (e.g. style or topics in the document)

()

$$c_{ij} = \left| \begin{array}{c} \mathbf{y}_i \cdot \mathbf{y}_j \\ \|\mathbf{y}_i\| \ \|\mathbf{y}_j\| \end{array} \right|$$

 $\rightarrow$  we have a measure of similarity, which (since  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are non-negative) must be between 0 and 1.

If  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are vectors,  $c_{ij}$  is the cosine of the angle between them. and document length is controlled for.

so intuitively, cosine similarity captures some notion of relative 'direction' (e.g. style or topics in the document) rather than 'magnitude' (distance from origin).

$$c_{ij} = \frac{\mathbf{y}_i \cdot \mathbf{y}_j}{\|\mathbf{y}_i\| \ \|\mathbf{y}_j\|}$$

 $\rightarrow$  we have a measure of similarity, which (since  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are non-negative) must be between 0 and 1.

If  $\mathbf{y}_i$  and  $\mathbf{y}_j$  are vectors,  $c_{ij}$  is the cosine of the angle between them. and document length is controlled for.

so intuitively, cosine similarity captures some notion of relative 'direction' (e.g. style or topics in the document) rather than 'magnitude' (distance from origin). Is the Pearson correlation between two vectors that have been demeaned.

-0

$$\mathbf{y}_i = [2.3, 4.3]; \ \mathbf{y}_j = [3.9, 2.1]$$

$$\mathbf{y}_i = [2.3, 4.3]; \ \mathbf{y}_j = [3.9, 2.1]$$

then 
$$\mathbf{y}_i \cdot \mathbf{y}_j = [2.3 \times 3.9] + [4.3 \times 2.1] = 18$$
.

$$\mathbf{y}_i = [2.3, 4.3]; \ \mathbf{y}_j = [3.9, 2.1]$$

then 
$$\mathbf{y}_i \cdot \mathbf{y}_j = [2.3 \times 3.9] + [4.3 \times 2.1] = 18.$$

and 
$$||\mathbf{y}_i|| = \sqrt{2.3^2 + 4.3^2} = 4.88$$
;  $||\mathbf{y}_i|| = \sqrt{3.9^2 + 2.1^2} = 4.43$ 

$$\mathbf{y}_i = [2.3, 4.3]; \ \mathbf{y}_i = [3.9, 2.1]$$

then 
$$\mathbf{y}_i \cdot \mathbf{y}_j = [2.3 \times 3.9] + [4.3 \times 2.1] = 18.$$

and 
$$||\mathbf{y}_i|| = \sqrt{2.3^2 + 4.3^2} = 4.88$$
;  $||\mathbf{y}_j|| = \sqrt{3.9^2 + 2.1^2} = 4.43$ 

so 
$$c_{ij} = \frac{18}{4.88 \times 4.43} =$$

$$\mathbf{y}_i = [2.3, 4.3]; \ \mathbf{y}_i = [3.9, 2.1]$$

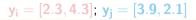
then 
$$\mathbf{y}_i \cdot \mathbf{y}_j = [2.3 \times 3.9] + [4.3 \times 2.1] = 18.$$

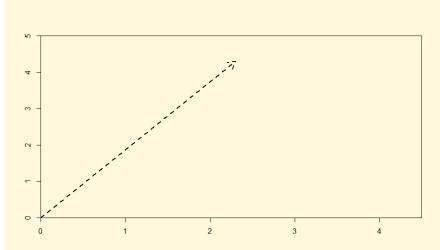
and 
$$||\mathbf{y}_i|| = \sqrt{2.3^2 + 4.3^2} = 4.88$$
;  $||\mathbf{y}_j|| = \sqrt{3.9^2 + 2.1^2} = 4.43$ 

so 
$$c_{ij} = \frac{18}{4.88 \times 4.43} = 0.83$$
.

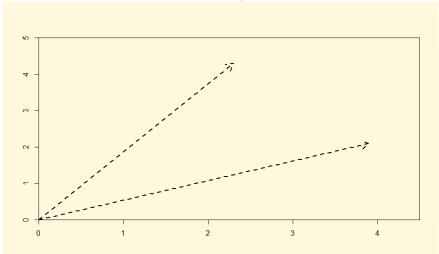
()

$$y_i = [2.3, 4.3]; y_j = [3.9, 2.1]$$

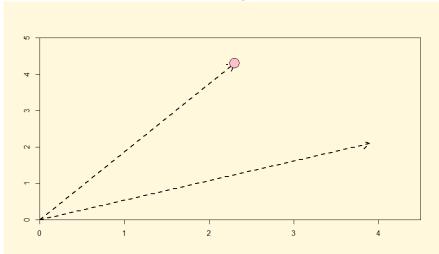




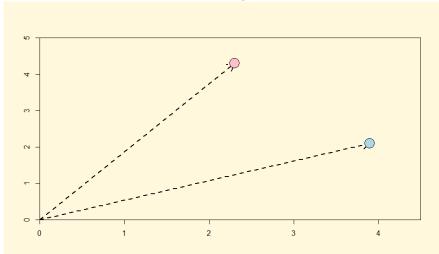
$$y_i = [2.3, 4.3]; y_j = [3.9, 2.1]$$



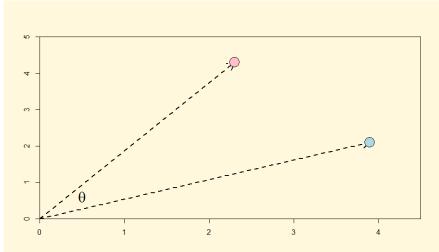
$$y_i = [2.3, 4.3]; y_j = [3.9, 2.1]$$

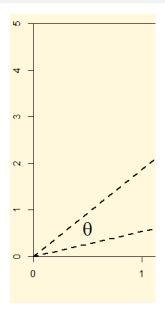


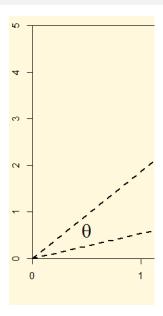
$$y_i = [2.3, 4.3]; y_j = [3.9, 2.1]$$

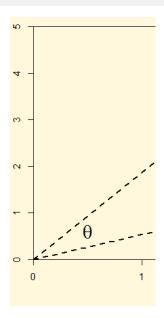


$$y_i = [2.3, 4.3]; y_j = [3.9, 2.1]$$

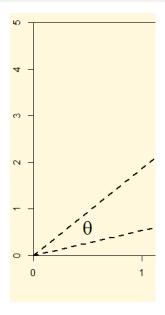






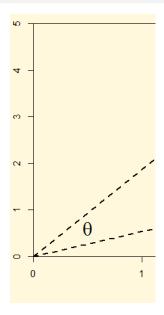


$$\mathbf{y}_i \cdot \mathbf{y}_j = ||\mathbf{y}_i||||\mathbf{y}_j||\cos\theta$$



$$\mathbf{y}_i \cdot \mathbf{y}_j = ||\mathbf{y}_i||||\mathbf{y}_j|| \cos \theta$$

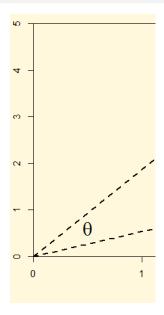
then 
$$\cos \theta = \frac{\mathbf{y}_i \cdot \mathbf{y}_j}{||\mathbf{y}_i|| ||\mathbf{y}_j||}$$



$$\mathbf{y}_i \cdot \mathbf{y}_j = ||\mathbf{y}_i||||\mathbf{y}_j||\cos\theta$$

then 
$$\cos \theta = \frac{\mathbf{y}_i \cdot \mathbf{y}_j}{||\mathbf{y}_i||||\mathbf{y}_j||}$$

and 
$$\theta = \arccos\left(\frac{\mathbf{y}_i \cdot \mathbf{y}_j}{||\mathbf{y}_i||||\mathbf{y}_j||}\right)$$
.

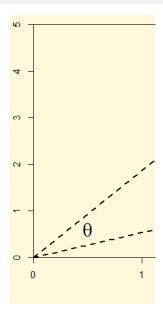


$$\mathbf{y}_i \cdot \mathbf{y}_j = ||\mathbf{y}_i|| ||\mathbf{y}_j|| \cos \theta$$

then 
$$\cos \theta = \frac{\mathbf{y}_i \cdot \mathbf{y}_j}{||\mathbf{y}_i|| ||\mathbf{y}_j||}$$

and 
$$\theta = \arccos\left(\frac{\mathbf{y}_i \cdot \mathbf{y}_j}{||\mathbf{y}_i||||\mathbf{y}_j||}\right)$$
.

so 
$$\theta = \arccos\left(\frac{18}{21.62}\right)$$



know dot product of vectors:

$$\mathbf{y}_i \cdot \mathbf{y}_j = ||\mathbf{y}_i||||\mathbf{y}_j|| \cos \theta$$

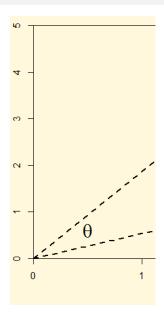
then 
$$\cos \theta = \frac{\mathbf{y}_i \cdot \mathbf{y}_j}{||\mathbf{y}_i|| ||\mathbf{y}_j||}$$

and 
$$\theta = \arccos\left(\frac{\mathbf{y}_i \cdot \mathbf{y}_j}{||\mathbf{y}_i||||\mathbf{y}_j||}\right)$$
.

so 
$$\theta = \arccos\left(\frac{18}{21.62}\right) = 0.58$$

()

# Algebra



know dot product of vectors:

$$\mathbf{y}_i \cdot \dot{\mathbf{y}}_j = ||\mathbf{y}_i||||\mathbf{y}_j||\cos\theta$$

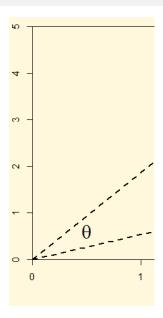
then 
$$\cos \theta = \frac{\mathbf{y}_i \cdot \mathbf{y}_j}{||\mathbf{y}_i||||\mathbf{y}_j||}$$

and 
$$\theta = \arccos\left(\frac{\mathbf{y}_i \cdot \mathbf{y}_j}{||\mathbf{y}_i||||\mathbf{y}_j||}\right)$$
.

so 
$$\theta = \arccos\left(\frac{18}{21.62}\right) = 0.58$$

$$ightarrow 0.58 imes rac{180}{\pi} = 33.63^{\circ}.$$

# Algebra



know dot product of vectors:

$$\mathbf{y}_i \cdot \dot{\mathbf{y}}_j = ||\mathbf{y}_i||||\mathbf{y}_j||\cos\theta$$

then 
$$\cos \theta = \frac{\mathbf{y}_i \cdot \mathbf{y}_j}{||\mathbf{y}_i|| ||\mathbf{y}_j||}$$

and 
$$\theta = \arccos\left(\frac{\mathbf{y}_i \cdot \mathbf{y}_j}{||\mathbf{y}_i||||\mathbf{y}_j||}\right)$$
.

so 
$$\theta = \arccos\left(\frac{18}{21.62}\right) = 0.58$$

$$\rightarrow 0.58 \times \frac{180}{\pi} = 33.63^{\circ}.$$

Looks about right.

40.40.45.45. 5 000



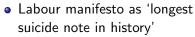


• Labour manifesto as 'longest suicide note in history'



- Labour manifesto as 'longest suicide note in history'
- unilateral nuclear disarmament, withdrawal from the EEC, abolition of the Lords, re-nationalisation





 unilateral nuclear disarmament, withdrawal from the EEC, abolition of the Lords, re-nationalisation





- Labour manifesto as 'longest suicide note in history'
- unilateral nuclear disarmament, withdrawal from the EEC, abolition of the Lords, re-nationalisation



• Conservative manifesto promised trade union curbs, deflation etc.



- Labour manifesto as 'longest suicide note in history'
- unilateral nuclear disarmament, withdrawal from the EEC, abolition of the Lords, re-nationalisation



• Conservative manifesto promised trade union curbs, deflation etc.

 $c_{ij} \approx 0.70$ 





 Conservative manifesto promised continuation of moderate Major years.



 Conservative manifesto promised continuation of moderate Major years.



 Conservative manifesto promised continuation of moderate Major years.



'New Labour' and 'Third Way'



 Conservative manifesto promised continuation of moderate Major years.



- 'New Labour' and 'Third Way'
- committed to Conservative spending plans (for next two years),



 Conservative manifesto promised continuation of moderate Major years.



- 'New Labour' and 'Third Way'
- committed to Conservative spending plans (for next two years), no income tax rises.



 Conservative manifesto promised continuation of moderate Major years.



- 'New Labour' and 'Third Way'
- committed to Conservative spending plans (for next two years), no income tax rises.

 $c_{ij} \approx 0.90$ 

ullet we can produce a cosine dissimilarity measure via  $1-c_{ij}$  (though not a metric)

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

Jaccard: size of the intersection of the two documents (number of common words between the documents) divided by the size of the union of the two documents (total number of unique words in docs).

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

Jaccard: size of the intersection of the two documents (number of common words between the documents) divided by the size of the union of the two documents (total number of unique words in docs).

Manhattan:

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

Jaccard: size of the intersection of the two documents (number of common words between the documents) divided by the size of the union of the two documents (total number of unique words in docs).

Manhattan: known as 'taxicab' distance or 'city block' distance.

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

Jaccard: size of the intersection of the two documents (number of common words between the documents) divided by the size of the union of the two documents (total number of unique words in docs).

Manhattan: known as 'taxicab' distance or 'city block' distance. Absolute difference between coordinates:  $||\mathbf{y}_i - \mathbf{y}_j|| = \sum |\mathbf{y}_i - \mathbf{y}_j|$ .

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

Jaccard: size of the intersection of the two documents (number of common words between the documents) divided by the size of the union of the two documents (total number of unique words in docs).

Manhattan: known as 'taxicab' distance or 'city block' distance. Absolute difference between coordinates:  $||\mathbf{y}_i - \mathbf{y}_j|| = \sum |\mathbf{y}_i - \mathbf{y}_j|$ . As we go from  $\mathbf{y}_i$  to  $\mathbf{y}_j$ ,

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

Jaccard: size of the intersection of the two documents (number of common words between the documents) divided by the size of the union of the two documents (total number of unique words in docs).

Manhattan: known as 'taxicab' distance or 'city block' distance. Absolute difference between coordinates:  $||\mathbf{y}_i - \mathbf{y}_j|| = \sum |\mathbf{y}_i - \mathbf{y}_j|$ . As we go from  $\mathbf{y}_i$  to  $\mathbf{y}_j$ , have to do so at right angles: travel along, turn  $90^\circ$  and then up (or down), then turn  $90^\circ$  and go along, turn  $90^\circ$  etc.

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

Jaccard: size of the intersection of the two documents (number of common words between the documents) divided by the size of the union of the two documents (total number of unique words in docs).

Manhattan: known as 'taxicab' distance or 'city block' distance. Absolute difference between coordinates:  $||\mathbf{y}_i - \mathbf{y}_j|| = \sum |\mathbf{y}_i - \mathbf{y}_j|$ . As we go from  $\mathbf{y}_i$  to  $\mathbf{y}_j$ , have to do so at right angles: travel along, turn  $90^\circ$  and then up (or down), then turn  $90^\circ$  and go along, turn  $90^\circ$  etc.

#### Canberra:

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

Jaccard: size of the intersection of the two documents (number of common words between the documents) divided by the size of the union of the two documents (total number of unique words in docs).

Manhattan: known as 'taxicab' distance or 'city block' distance. Absolute difference between coordinates:  $||\mathbf{y}_i - \mathbf{y}_j|| = \sum |\mathbf{y}_i - \mathbf{y}_j|$ . As we go from  $\mathbf{y}_i$  to  $\mathbf{y}_j$ , have to do so at right angles: travel along, turn  $90^\circ$  and then up (or down), then turn  $90^\circ$  and go along, turn  $90^\circ$  etc.

Canberra: weighted version of Manhattan distance.

()

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

Jaccard: size of the intersection of the two documents (number of common words between the documents) divided by the size of the union of the two documents (total number of unique words in docs).

Manhattan: known as 'taxicab' distance or 'city block' distance. Absolute difference between coordinates:  $||\mathbf{y}_i - \mathbf{y}_j|| = \sum |\mathbf{y}_i - \mathbf{y}_j|$ . As we go from  $\mathbf{y}_i$  to  $\mathbf{y}_j$ , have to do so at right angles: travel along, turn  $90^\circ$  and then up (or down), then turn  $90^\circ$  and go along, turn  $90^\circ$  etc.

Canberra: weighted version of Manhattan distance.  $\sum \frac{|\mathbf{y}_i - \mathbf{y}_j|}{|\mathbf{y}_i| + |\mathbf{y}_j|}$ 

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

Jaccard: size of the intersection of the two documents (number of common words between the documents) divided by the size of the union of the two documents (total number of unique words in docs).

Manhattan: known as 'taxicab' distance or 'city block' distance. Absolute difference between coordinates:  $||\mathbf{y}_i - \mathbf{y}_j|| = \sum |\mathbf{y}_i - \mathbf{y}_j|$ . As we go from  $\mathbf{y}_i$  to  $\mathbf{y}_j$ , have to do so at right angles: travel along, turn  $90^\circ$  and then up (or down), then turn  $90^\circ$  and go along, turn  $90^\circ$  etc.

Canberra: weighted version of Manhattan distance.  $\sum \frac{|\mathbf{y}_i - \mathbf{y}_j|}{|\mathbf{y}_i| + |\mathbf{y}_j|}$ 

Minowski: generalized version of Euclidean and Manhattan.

()

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

Jaccard: size of the intersection of the two documents (number of common words between the documents) divided by the size of the union of the two documents (total number of unique words in docs).

Manhattan: known as 'taxicab' distance or 'city block' distance. Absolute difference between coordinates:  $||\mathbf{y}_i - \mathbf{y}_j|| = \sum |\mathbf{y}_i - \mathbf{y}_j|$ . As we go from  $\mathbf{y}_i$  to  $\mathbf{y}_j$ , have to do so at right angles: travel along, turn  $90^\circ$  and then up (or down), then turn  $90^\circ$  and go along, turn  $90^\circ$  etc.

Canberra: weighted version of Manhattan distance.  $\sum \frac{|\mathbf{y}_i - \mathbf{y}_j|}{|\mathbf{y}_i| + |\mathbf{y}_j|}$ 

Minowski: generalized version of Euclidean and Manhattan.  $(\sum |\mathbf{y}_i - \mathbf{y}_i|^c)^{\frac{1}{c}}$ .

()

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

Jaccard: size of the intersection of the two documents (number of common words between the documents) divided by the size of the union of the two documents (total number of unique words in docs).

Manhattan: known as 'taxicab' distance or 'city block' distance. Absolute difference between coordinates:  $||\mathbf{y}_i - \mathbf{y}_j|| = \sum |\mathbf{y}_i - \mathbf{y}_j|$ . As we go from  $\mathbf{y}_i$  to  $\mathbf{y}_j$ , have to do so at right angles: travel along, turn  $90^\circ$  and then up (or down), then turn  $90^\circ$  and go along, turn  $90^\circ$  etc.

Canberra: weighted version of Manhattan distance.  $\sum \frac{|\mathbf{y}_i - \mathbf{y}_j|}{|\mathbf{y}_i| + |\mathbf{y}_j|}$ 

Minowski: generalized version of Euclidean and Manhattan.  $(\sum |\mathbf{y}_i - \mathbf{y}_j|^c)^{\frac{1}{c}}$ . If c is 1, this is Manhattan. If c is 2, this is Euclidean.

• we can produce a cosine dissimilarity measure via  $1 - c_{ij}$  (though not a metric)

but there are a large number of other distance measures on offer:

Jaccard: size of the intersection of the two documents (number of common words between the documents) divided by the size of the union of the two documents (total number of unique words in docs).

Manhattan: known as 'taxicab' distance or 'city block' distance. Absolute difference between coordinates:  $||\mathbf{y}_i - \mathbf{y}_j|| = \sum |\mathbf{y}_i - \mathbf{y}_j|$ . As we go from  $\mathbf{y}_i$  to  $\mathbf{y}_j$ , have to do so at right angles: travel along, turn 90° and then up (or down), then turn 90° and go along, turn 90° etc.

Canberra: weighted version of Manhattan distance.  $\sum \frac{|\mathbf{y}_i - \mathbf{y}_j|}{|\mathbf{y}_i| + |\mathbf{y}_j|}$ 

Minowski: generalized version of Euclidean and Manhattan.  $(\sum |\mathbf{y}_i - \mathbf{y}_j|^c)^{\frac{1}{c}}$ . If c is 1, this is Manhattan. If c is 2, this is Euclidean.

### Exercise



Suppose a block is one unit long and one unit wide.

- what is Euclidean distance between Dojo and White Oak Tavern?
- what is Manhattan distance between Dojo and White Oak Tavern?

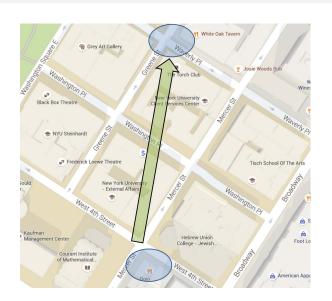
-0

## Solution

### Solution

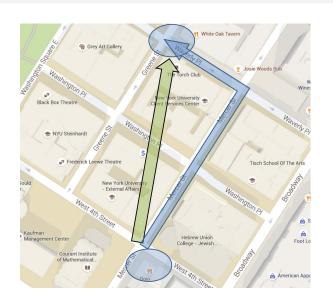


#### Solution



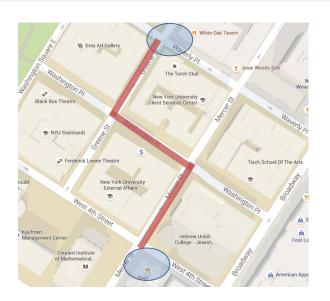
• Euclidean  $(\sqrt{5})$ 

#### Solution



- Euclidean  $(\sqrt{5})$
- Manhattan (3)

#### Solution



- Euclidean  $(\sqrt{5})$
- Manhattan (3)
- Manhattan (3)

So far,

So far, we've treated the features in a 'bag of words' style.

So far, we've treated the features in a 'bag of words' style. In some cases, may also want to think seriously about collocations:

So far, we've treated the features in a 'bag of words' style. In some cases, may also want to think seriously about collocations: words that co-occur in a document.

So far, we've treated the features in a 'bag of words' style. In some cases, may also want to think seriously about collocations: words that co-occur in a document, adjacent (or close to adjacent) to one another.

So far, we've treated the features in a 'bag of words' style. In some cases, may also want to think seriously about collocations: words that co-occur in a document, adjacent (or close to adjacent) to one another.

defn group of two or more adjacent words that are seen together more often than we would 'expect' were words placed in document independent of the others.

So far, we've treated the features in a 'bag of words' style. In some cases, may also want to think seriously about collocations: words that co-occur in a document, adjacent (or close to adjacent) to one another.

defn group of two or more adjacent words that are seen together more often than we would 'expect' were words placed in document independent of the others. Mean something specific. Describe as strong collocation if the link between the words is fixed and restrictive.

So far, we've treated the features in a 'bag of words' style. In some cases, may also want to think seriously about collocations: words that co-occur in a document, adjacent (or close to adjacent) to one another.

defn group of two or more adjacent words that are seen together more often than we would 'expect' were words placed in document independent of the others. Mean something specific. Describe as strong collocation if the link between the words is fixed and restrictive.

e.g. 'do business' (not 'make business'),

So far, we've treated the features in a 'bag of words' style. In some cases, may also want to think seriously about collocations: words that co-occur in a document, adjacent (or close to adjacent) to one another.

defn group of two or more adjacent words that are seen together more often than we would 'expect' were words placed in document independent of the others. Mean something specific. Describe as strong collocation if the link between the words is fixed and restrictive.

So far, we've treated the features in a 'bag of words' style. In some cases, may also want to think seriously about collocations: words that co-occur in a document, adjacent (or close to adjacent) to one another.

defn group of two or more adjacent words that are seen together more often than we would 'expect' were words placed in document independent of the others. Mean something specific. Describe as strong collocation if the link between the words is fixed and restrictive.

So far, we've treated the features in a 'bag of words' style. In some cases, may also want to think seriously about collocations: words that co-occur in a document, adjacent (or close to adjacent) to one another.

- defn group of two or more adjacent words that are seen together more often than we would 'expect' were words placed in document independent of the others. Mean something specific. Describe as strong collocation if the link between the words is fixed and restrictive.
- e.g. 'do business' (not 'make business'), 'save money' (not 'preserve money'). Note that one of the terms is chosen freely (e.g. money), but the other is constrained by language.

()

So far, we've treated the features in a 'bag of words' style. In some cases, may also want to think seriously about collocations: words that co-occur in a document, adjacent (or close to adjacent) to one another.

- defn group of two or more adjacent words that are seen together more often than we would 'expect' were words placed in document independent of the others. Mean something specific. Describe as strong collocation if the link between the words is fixed and restrictive.
- e.g. 'do business' (not 'make business'), 'save money' (not 'preserve money'). Note that one of the terms is chosen freely (e.g. money), but the other is constrained by language.

()

Collocations are a type of phraseme: an idiomatic, 'set phrase' in a language.

Collocations are a type of phraseme: an idiomatic, 'set phrase' in a language. Has at least one word or part that is constrained.

Collocations are a type of phraseme: an idiomatic, 'set phrase' in a language. Has at least one word or part that is constrained. In the extreme, the meaning may not be implied by any of the lexical components.

Collocations are a type of phraseme: an idiomatic, 'set phrase' in a language. Has at least one word or part that is constrained. In the extreme, the meaning may not be implied by any of the lexical components.

e.g. 'He was pulling my leg'

Collocations are a type of phraseme: an idiomatic, 'set phrase' in a language. Has at least one word or part that is constrained. In the extreme, the meaning may not be implied by any of the lexical components.

e.g. 'He was pulling my leg', 'At the drop of a hat.'

Collocations are a type of phraseme: an idiomatic, 'set phrase' in a language. Has at least one word or part that is constrained. In the extreme, the meaning may not be implied by any of the lexical components.

e.g. 'He was pulling my leg', 'At the drop of a hat.'

Phrasemes are interesting in that they tell us something about history or culture of language.

Collocations are a type of phraseme: an idiomatic, 'set phrase' in a language. Has at least one word or part that is constrained. In the extreme, the meaning may not be implied by any of the lexical components.

e.g. 'He was pulling my leg', 'At the drop of a hat.'

Phrasemes are interesting in that they tell us something about history or culture of language.

Why do we talk of 'strong tea' but 'powerful drugs'?

Collocations are a type of phraseme: an idiomatic, 'set phrase' in a language. Has at least one word or part that is constrained. In the extreme, the meaning may not be implied by any of the lexical components.

e.g. 'He was pulling my leg', 'At the drop of a hat.'

Phrasemes are interesting in that they tell us something about history or culture of language.

Why do we talk of 'strong tea' but 'powerful drugs'?

+ Very important when studying named entities, like people or cities

Collocations are a type of phraseme: an idiomatic, 'set phrase' in a language. Has at least one word or part that is constrained. In the extreme, the meaning may not be implied by any of the lexical components.

e.g. 'He was pulling my leg', 'At the drop of a hat.'

Phrasemes are interesting in that they tell us something about history or culture of language.

Why do we talk of 'strong tea' but 'powerful drugs'?

+ Very important when studying named entities, like people or cities

e.g. 'Prime Minister'

Frequency? Typically not enough to look for (say) common bigrams (NYT corpus):

Frequency? Typically not enough to look for (say) common bigrams (NYT corpus):

frequency	$w_1$	W <sub>2</sub>
80871	of	the
58841	in	the
26430	to	the
21842	on	the
21839	for	the
18568	and	the
16121	that	the
15630	at	the
15494	to	be
13899	in	a
13689	of	a
13361	by	the
13183	with	the
12622	from	the
11428	New	York
10007	he	said
9775	as	a
9231	is	a
8753	has	been
8573	for	а

Frequency? Typically not enough to look for (say) common bigrams (NYT corpus):

,		
frequency	$w_1$	$W_2$
80871	of	the
58841	in	the
26430	to	the
21842	on	the
21839	for	the
18568	and	the
16121	that	the
15630	at	the
15494	to	be
13899	in	a
13689	of	a
13361	by	the
13183	with	the
12622	from	the
11428	New	York
10007	he	said
9775	as	a
9231	is	a
8753	has	been
8573	for	a

→ most of these are uninteresting pairs of function words

Frequency? Typically not enough to look for (say) common bigrams (NYT corpus):

,		
frequency	$w_1$	$W_2$
80871	of	the
58841	in	the
26430	to	the
21842	on	the
21839	for	the
18568	and	the
16121	that	the
15630	at	the
15494	to	be
13899	in	a
13689	of	a
13361	by	the
13183	with	the
12622	from	the
11428	New	York
10007	he	said
9775	as	a
9231	is	a
8753	has	been
8573	for	a

→ most of these are uninteresting pairs of function words (except 'New York')

Frequency? Typically not enough to look for (say) common bigrams (NYT corpus):

,		
frequency	$w_1$	$w_2$
80871	of	the
58841	in	the
26430	to	the
21842	on	the
21839	for	the
18568	and	the
16121	that	the
15630	at	the
15494	to	be
13899	in	a
13689	of	a
13361	by	the
13183	with	the
12622	from	the
11428	New	York
10007	he	said
9775	as	a
9231	is	а
8753	has	been
8573	for	а

→ most of these are uninteresting pairs of function words (except 'New York')

Justeson and Katz (1995) improve performance considerably by applying parts-of-speech tagger,

Frequency? Typically not enough to look for (say) common bigrams (NYT corpus):

,		
frequency	$w_1$	$W_2$
80871	of	the
58841	in	the
26430	to	the
21842	on	the
21839	for	the
18568	and	the
16121	that	the
15630	at	the
15494	to	be
13899	in	a
13689	of	a
13361	by	the
13183	with	the
12622	from	the
11428	New	York
10007	he	said
9775	as	а
9231	is	a
8753	has	been
8573	for	a

→ most of these are uninteresting pairs of function words (except 'New York')

Justeson and Katz (1995) improve performance considerably by applying parts-of-speech tagger, and only keeping those bigrams and trigrams that fulfill certain criteria.

Justeson and Katz (1995)

# Justeson and Katz (1995)

N noun.

# Justeson and Katz (1995)

N noun.

A adjective.

# Justeson and Katz (1995)

- N noun.
- A adjective.
- P preposition.

# Justeson and Katz (1995)

- N noun.
- A adjective.
- P preposition.

then following offers marked improvement:

# Justeson and Katz (1995)

- N noun.
- A adjective.
- P preposition.

then following offers marked improvement:

pattern	example
AN	Prime Minister
NN	surface area
AAN	little green men
ANN	real estate agent
NAN	home sweet home
N N N	term document matrix
NPN	Secretary of State

# Reanalyzing NYT corpus: top ranked bi-grams

# Reanalyzing NYT corpus: top ranked bi-grams

frequency	w <sub>1</sub> w <sub>2</sub>	
11487	New York	ΑN
7261	United States	ΑN
5412	Los Angeles	ΝN
3301	last year	ΑN
3191	Saudi Arabia	ΝN
2699	last week	ΑN
2514	vice president	ΑN
2378	Persian Gulf	ΑN
2161	San Francisco	ΝN
2106	President Bush	ΝN
2001	Middle East	ΑN
1942	Saddam Hussein	ΝN
1867	Soviet Union	ΑN
1850	White House	ΑN
1633	United Nations	ΑN
1337	York City	ΝN
1328	oil prices	ΝN
1210	next year	ΑN
1074	chief executive	ΑN
1073	real estate	ΑN

In Information Retrieval it is often extremely helpful to know how and where a particular token of interest appears,

In Information Retrieval it is often extremely helpful to know how and where a particular token of interest appears, in terms of the words around it.

In Information Retrieval it is often extremely helpful to know how and where a particular token of interest appears, in terms of the words around it.

→ quick overview of general use,

In Information Retrieval it is often extremely helpful to know how and where a particular token of interest appears, in terms of the words around it.

ightarrow quick overview of general use, and allows for easy, follow up inspection of the document in question.

In Information Retrieval it is often extremely helpful to know how and where a particular token of interest appears, in terms of the words around it.

ightarrow quick overview of general use, and allows for easy, follow up inspection of the document in question.

also true in social science applications where we might want to understand how a given concept appears,

In Information Retrieval it is often extremely helpful to know how and where a particular token of interest appears, in terms of the words around it.

ightarrow quick overview of general use, and allows for easy, follow up inspection of the document in question.

also true in social science applications where we might want to understand how a given concept appears, or when we are looking for prototypical examples.

In Information Retrieval it is often extremely helpful to know how and where a particular token of interest appears, in terms of the words around it.

ightarrow quick overview of general use, and allows for easy, follow up inspection of the document in question.

also true in social science applications where we might want to understand how a given concept appears, or when we are looking for prototypical examples.

1 keyword of interest.

In Information Retrieval it is often extremely helpful to know how and where a particular token of interest appears, in terms of the words around it.

- ightarrow quick overview of general use, and allows for easy, follow up inspection of the document in question.
- also true in social science applications where we might want to understand how a given concept appears, or when we are looking for prototypical examples.
  - 1 keyword of interest.
  - 2 context —typically the sentence in which it appears.

In Information Retrieval it is often extremely helpful to know how and where a particular token of interest appears, in terms of the words around it.

- ightarrow quick overview of general use, and allows for easy, follow up inspection of the document in question.
- also true in social science applications where we might want to understand how a given concept appears, or when we are looking for prototypical examples.
  - 1 keyword of interest.
  - 2 context —typically the sentence in which it appears.
  - 3 location code —document details.



DERBY, 1867. DIZZY WINS WITH "REFORM BILL."





SOON have been broke word "Depoin DAY



1867 House of Commons considers extending suffrage to urban working class men,







1867 House of Commons considers extending suffrage to urban working class men, via 'Representation of the People Act'



SOUR 1985 BLASS MING MAIN "BERNISM BILLY



- 1867 House of Commons considers extending suffrage to urban working class men, via 'Representation of the People Act'
  - → represents approximate doubling of electorate.



DERBY, 1867. DIZZY WINS WITH "REFORM BILL."



- 1867 House of Commons considers extending suffrage to urban working class men, via 'Representation of the People Act'
  - → represents approximate doubling of electorate.

Debates of the time are lively and long.



DERBY, 1867. DIZZY WINS WITH "REFORM BILL



- 1867 House of Commons considers extending suffrage to urban working class men, via 'Representation of the People Act'
  - → represents approximate doubling of electorate.

Debates of the time are lively and long. Normative notions of extending 'rights' on one hand (and pragmatic politics) vs fear of mob rule.



DERBY, 1867. DIZZY WINS WITH "REFORM BILL



- 1867 House of Commons considers extending suffrage to urban working class men, via 'Representation of the People Act'
  - → represents approximate doubling of electorate.

Debates of the time are lively and long. Normative notions of extending 'rights' on one hand (and pragmatic politics) vs fear of mob rule.

q What role did 'democratic' play in the debate?

# Some KWIC from the debates: kwic() in quanteda

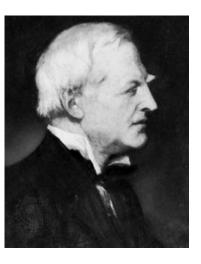
	preword	word	postword
:	:	:	•
[s267549.txt, 994]	evil that attends a purely	democratic	form of Government. There could be
[s267549.txt, 1015]	here, not possibly towards a	democratic	form of government, but in
[s267738.txt, 1492]	swept away in some further	democratic	change. And it is for
[s267738.txt, 1560]	throne. When you get a	democratic	basis for your institutions, you
[s267738.txt, 1952]	differences between ourselves and other	democratic	legislatures? Where is the democratic
[s267738.txt, 1957]	democratic legislatures? Where is the	democratic	legislature which enjoys the powers
[s267738.txt, 2243]	almost utterly useless against a	democratic	Chamber, and the question to
[s267738.txt, 2286]	to the violence of the	democratic	Chamber you are creating, and,
[s267738.txt, 2294]	are creating, and, as the	democratic	principle brooks no rival, this
[s267738.txt, 2374]	spirit of democracy that the	democratic	Chamber itself would become an
[s267738.txt, 2678]	power is given to the	democratic	majority, that majority does not
[s267738.txt, 2767]	job? In accordance with the	democratic	principle the army would demand
[s267744.txt, 204]	Conservative patronage, of the most	democratic	Reform Bill ever brought in.

Detail: s267738.txt

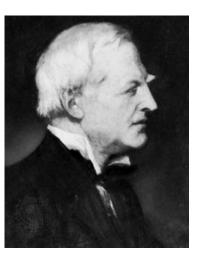
#### Detail: s267738.txt

preword	word	postword
swept away in some further	democratic	change. And it is for
throne. When you get a	democratic	basis for your institutions, you
differences between ourselves and other	democratic	legislatures? Where is the democratic
democratic legislatures? Where is the	democratic	legislature which enjoys the powers
almost utterly useless against a	democratic	Chamber, and the question to
to the violence of the	democratic	Chamber you are creating, and,
are creating, and, as the	democratic	principle brooks no rival, this
spirit of democracy that the	democratic	Chamber itself would become an
power is given to the	democratic	majority, that majority does not
iob? In accordance with the	democratic	principle the army would demand





You cannot trust to a majority elected by men just above the status of paupers. The experiment has been tried; it has answered nowhere; it has failed in America, and it will not answer here.



You cannot trust to a majority elected by men just above the status of paupers. The experiment has been tried; it has answered nowhere; it has failed in America, and it will not answer here.

In accordance with the democratic principle the army would demand to elect their own officers, and there would be endless change in the Constitution arising out of the present Bill, which, so far from being an end to our evils, is only the first step to them.

()

#### Partner Exercise

#### Exercise

The context of key words is especially important when comparing usage across time and space.

#### Exercise

The context of key words is especially important when comparing usage across time and space.

Suppose you were studying the history of entertainment technology. Consider the key word 'wireless'. How has the frequency of this term changed over time? How has the context changed?

#### Exercise

The context of key words is especially important when comparing usage across time and space.

Suppose you were studying the history of entertainment technology. Consider the key word 'wireless'. How has the frequency of this term changed over time? How has the context changed?

Give an example of a political key word that might appear in a different *context* if we study the US vs some other country.

#### Use of 'Wireless'

