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Combined ⁷Li NMR, density functional theory and *operando* synchrotron X-ray powder diffraction to investigate a structural evolution of cathode material LiFeV₂O₇†

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In our recent study, we demonstrated using ⁷Li solid-state Nuclear Magnetic Resonance (ssNMR) and single-crystal X-ray diffraction that the cathode LiFeV2O7 possesses a defect associated with the positioning of vanadium atoms. We proposed that this defect could be the source of extra signals detected in the 7 Li spectra. In this context, we now apply density functional theory (DFT) calculations to assign the experimental signals observed in ⁷Li NMR spectra of the pristine sample. The calculation results are in strong agreement with the experimental observations. DFT calculations are a useful tool to interpret the observed paramagnetic shifts and understand how the presence of disorder affects the spectra behavior through the spin-density transfer processes. Furthermore, we conducted a detailed study of the lithiated phase combining operando synchrotron powder X-ray diffraction (SPXRD) and DFT calculations. A noticeable volume expansion is observed through the first discharge cycle which likely contributes to the enhanced lithium dynamics in the bulk material, as supported by previously published ssNMR data. DFT calculations are used to model the lithiated phase and demonstrate that both iron and vanadium participate in the redox process. The unusual electronic structure of the V^{4+} exhibits a single electron on the $3d_{xy}$ orbital perpendicular to the V-O-Li bond being a source of a negative Fermi contact shift observed in the ⁷Li NMR of the lithiated phase.

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1 Introduction

The development and optimization of cathode materials for lithium-ion batteries represent a critical field of research in the search for advanced energy storage solutions. Their performance is intricately related to their chemical structure which may contain crystallographic defects, such as vacancies, antisites, and dislocations, consequently producing disordered systems.^{1,2} In various functional materials, structural and compositional defects are unavoidable, especially when considering large-scale production. With advances in characterization techniques, these irregularities have been identified and their effects on physical and chemical properties have been understood. An example of this is olivine LiFePO₄ (LFP) cathode (theoretical capacity of 170 mA h g⁻¹), which is known for its stability, safety, and long cycle life in lithium-ion batteries. Antisite defects in LiFePO₄ result in a reduced Li⁺ diffusion rate, causing a negative effect on the electrochemical performance.^{1,3} However, in some cases, the defects contribute positively to the electrochemical performance of batteries. Wang et al.4 showed that introducing a considerable number of twin boundary defects into the lattice of spinel lithium manganate oxide (LiMn₂O₄) lowers the barrier of the lithium diffusion process, consequently improving the lithium-ion diffusion rate.

Different types of defects impact the electrochemical performance of electrode materials to greater or lesser extents, depending on their impact on the framework structure including its stability and the exchangeability of lithium ions in the vicinity of the defects. Detecting and understanding these defects in potential cathode structures is crucial for optimizing the performance and advancing the technology in lithium-ion batteries. In a previous study, 17 a new crystal structure for LiFeV₂O₇ was determined by X-ray diffraction that exhibited the presence of disorder, two possible local environments for the vanadium centers. It was found that the V2, V6, and O8 sites shift the position in such a way that the coordination of V2 becomes tetrahedral and V6 trigonal bipyramidal. We hypothesized that the presence of vanadium disorder provides an explanation for the presence of extra signals in the ⁷Li NMR spectra. However, more information is needed to assign the lithium environments to the observed ⁷Li NMR signals. Density functional theory (DFT) calculation has been shown to effectively predict NMR chemical shift assignments and thereby to provide correlations between the local structural details and the resulting Fermi contact shifts. 5-11 Here we combined experimental and theoretical ⁷Li NMR studies of LiFeV₂O₇.

Furthermore, an *operando* and *ex situ* synchrotron powder X-ray diffraction (SPXRD) study of the structural evolution of LiFeV₂O₇ during the first discharge cycle was performed at higher energy wiggler beamline of the Brockhouse X-ray Diffraction and Scattering (BXDS) sector at the Canadian Light Source. Previously, a marked enhancement in lithium-ion dynamics was observed after 0.5 mol of Li⁺ was inserted. Here the lithiated structure Li_{1.71}FeV₂O₇ is determined by combining the data obtained from *ex situ* SPXRD and bond valence energy landscape (BVEL) calculations. ¹²⁻¹⁴ Subsequently, the structure is optimized using DFT calculations to determine all stable atomic positions including new Li sites. This iterative process of modeling is followed by computational validation and

optimization which allow for a robust approximation of the lithium positions within the material's framework, providing a plausible atomic-level understanding of the lithiated phase.

2 Experimental methods

2.1 VASP calculations

First principles calculations were performed within the density functional theory (DFT). Vienna ab initio simulation package (VASP) was chosen to run the calculation utilizing projector augmented wave (PAW) with pseudopotentials. 15,16 We used the standard PAW-Perdew-Burke-Ernzerhof (PBE) potentials for Fe, V, and O and the "sv" PAW-PBE potential for Li that treats the 1s shell as valence states. For Li Fermi contact shift the sv PAW-PBE potential has been shown to yield more accurate results. A plane wave energy cut-off of 750 eV and a K-point grid of 2×4 × 2 were used for all LiFeV₂O₇ structures. The experimental crystal structure was used as the input model, 17,18 and the calculations were spin polarized type with imposed ferromagnetic ordering which is considered appropriate for the Fermi contact interaction.⁵ The energy minimization and electron density for each atom were calculated using two different approaches: the generalized gradient approximation (GGA) and GGA+U method. The GGA+U method incorporates a Hubbard-type interaction to localize d electrons. In this work, U values of 3.5, 4.3 and 5.3 eV for Fe and 3.25 eV for V (lithiated structure only) were examined as part of the testing process.

The isotropic shifts were calculated using eqn (1) and a temperature of 320 K to account for typical heating of the rotor during spinning at 60 kHz.

$$\delta_{\rm iso}(T) = \frac{\chi_{\rm M}(T)}{3SN_{\rm A}} \cdot \frac{A_{\rm iso} \cdot S_{\rm tot}}{\gamma_{\rm N}} \tag{1}$$

where $S_{\rm tot}$ is twice the spin quantum number of the paramagnetic ions in the considered unit cell (*i.e.*, the number of unpaired electrons), S is theoretical spin per LiFeP₂O₇ mole, $\chi_{\rm M}$ is the molar magnetic susceptibility for LiFeP₂O₇ formula unit, $N_{\rm A}$ is Avogadro's number, and $\gamma_{\rm N}$ is the gyromagnetic ratio for the measured nucleus. $A_{\rm iso}$ is the hyperfine coupling constant, which is calculated using the VASP program. As the magnetic measurements for this material are not available, we considered for 7 Li Fermi contact shifts calculations, the molar magnetic susceptibility of LiFeP₂O₇, 19 which also contains Fe³⁺ ions in a rather similar lattice. 3D calculated spin density maps were plotted using VESTA software (visualization for electronic and structural analysis). 20

2.2 Synchrotron X-ray diffraction

2.2.1 Battery preparation. The cathode material was prepared by grinding LiFeV $_2$ O $_7$ and Super P carbon black (CB) followed by an addition of a solution of 2.0% polyvinylidene fluoride (PVDF) in *N*-methyl-2-pyrrolidene (NMP) in 84:10:6 weight% ratio. The mixer was left stirring for 2 hours. The resulting slurry was deposited on an aluminum foil current collector using the doctor blade (15 mils) technique. The electrode was dried under a vacuum overnight at 120 °C. The material was punched into discs 1.27 cm in diameter and assembled in modified CR2025 coin cell casings with LiPF $_6$ (1 M LiPF $_6$ in a 1:1 wt% ethylene carbonate:

diethyl carbonate solution) as the electrolyte, Celgard 2325 as the separator and Li-metal as the negative electrode in an argon-filled glovebox.

For the *operando* Synchrotron Powder X-ray Powder Diffraction (SPXRD) measurement, the coin cells were modified with 5 mm diameter holes at both entry and exit transmission and also in the spacer, as shown in Fig. S1.† The Kapton tape (50.8 \pm 2 μm thick) was used on both anode and cathode casings to avoid any air contamination. The half-coin cell was discharged on the SRS EC301 Potentiostat from 2.75 V to 2.27 V at a constant current of 5.45 \times 10^{-2} mA (approximately C/20) at room temperature.

2.2.2 Synchrotron X-ray measurements. Operando powder diffraction measurements were conducted on a half-cell configuration in a modified coin cell on the BXDS higher energy wiggler (HEW) beamline at the Canadian Light Source (CLS). Each pattern was collected using a PerkinElmer XRD 1621 CN3 EHS 2D detector (pixel size 200 μ m \times 200 μ m) with an exposure time of 0.8 min. The detector distance, position and tilt were precisely calibrated using a reference standard of Ni powder with GSAS-II, prior to integration of 2D images to point detector patterns from 3° to 25°, 2θ $\lambda = 0.3542$ Å, E = 35 keV. A pattern was collected every 8 min during the first discharge process and data collection was undertaken at room temperature. GSAS-II software was used for sequential Rietveld refinement of LiFeV2O7 during electrochemical cycling.21 For the sequential refinement, the unit cell parameters, iron, vanadium, and oxygen coordinates were allowed to vary. Ex situ PXRD was also conducted on the BXDS lower energy wiggler (LEW) beamline. 22 The detector was a Mythen 2 X series 1 K strip detector from Dectris mounted on 1.1 m goniometer arm, with a total exposure time of 5.16 min. The wavelength was precisely calibrated using a reference standard of LaB6 powder to be $\lambda = 0.8193 \text{ Å}$ (15.1328 keV).

3 Results and discussions

Fig. S2† shows an excerpt from our previously reported¹⁷ ⁷Li ssNMR data for LiFeV₂O₇ which revealed a complex ⁷Li spectrum for the pristine phase as well as significant changes in the spectra as a function of lithiation.¹⁷ When synthesized using a bulk powder synthesis at 580 °C, LiFeV₂O₇ was found to crystallize in the monoclinic Cc space group and consists of extended V–O chains that create layers between which Li and Fe–O units alternate. The lattice parameters are a = 13.469(6) Å, b = 8.192(4) Å, c = 14.390(7) Å, and $\beta = 96.600(9)^{\circ}$.¹⁷ It exhibits the presence of two possible local environments for a fraction of 85 and 15% of the vanadium centers. This realization was determined to be the reason for set of signals in the ⁷Li NMR spectrum of the pristine phase. However, more information was needed to give an assignment of the distinct chemical shifts observed in the experimental data, and how they correspond to the local lithium environments. DFT calculations are shown here to be a good approach to providing ⁷Li NMR chemical shift assignments.

3.1 Structure optimization

The first step of the calculations, in order to obtain the value of the hyperfine coupling constant, is to optimize the structure of interest. The initial atomic positions were imported from experimental single-crystal diffraction data, then

the structure was optimized using VASP code to yield the most stable atomic arrangement. There are 33 independent atom positions, including three Li sites, three Fe sites, six V sites, and 21 O atomic sites. Fe is displayed as an octahedral FeO₆ surrounded by five VO₄ tetrahedra. Fe2 shares the last corner with a VO₅ trigonal bipyramid while corner-sharing Fe1 and Fe3 share two adjacent edges with the VO₅ trigonal bipyramid. In the material studied here, two structural models result from the split of V2, V6, and O8 sites into two positions with occupancy of around 85% (named the ORG position18) and 15% (named LFVOD position, V2A, V6A, and O8A). The ORG denotes the original position as delineated in the CIF file published by Benabed18 (Fig. 1a), while LFVOD refers to the vanadium disorder position (Fig. 1b). The difference between the two structures is a small shift of O8A closer toward V6A that changes the coordination environment of V6A into trigonal bipyramidal and V2A into tetrahedra, switching the geometry at both the vanadium sites as shown in Fig. 1c. For this work, we used three different initial positions to create the models: (i) ORG position;¹⁸ (ii) LFVOD position that is related to the disorder position obtained from the new singlecrystal analyses reported, and (iii) ORG-D position that combines both positions. For the last one, the position of one asymmetric unit in the ORG structure was changed to a disordered position (LFVOD). This means that the positions of V2, V6, and O8 were changed to V2A, V6A, and O8A, respectively. The structural models consist of supercells comprising four asymmetric unit cells and a total of 132 atoms each. In the ORG-D structure, only three among the 132 atoms were modified to the disorder position, representing localized disordering.

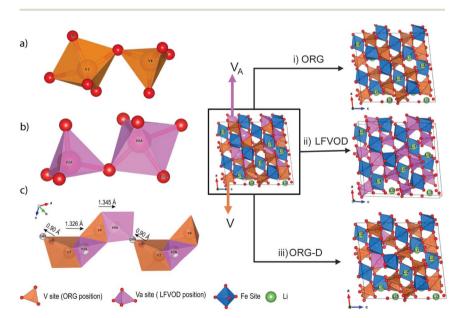


Fig. 1 (a) Vanadium polyhedral original, (b) disordered position, and (c) the vanadium polyhedral disordered model. Representation of the unit cell for the single-crystal refinement from the [010] direction: (i) ORG position, (ii) LFVOD position, and (iii) ORG-D position, one asymmetric unit in the ORG structure is changed to a disordered position (LFVOD).

Atomic coordinates and cell parameters were fully relaxed, followed by a calculation of the final energy of the optimized geometry. It is well known that there is a self-interaction error associated with GGA strategy, which is related to insufficient localization of electrons on the d-orbital of the transition metal compound. To solve this problem, the generalized gradient approximation with the Hubbard parameter correction (GGA+U) of Dudarev et al.23 was employed. The method applied a unique parameter U_{eff} which is the difference between the traditional U (electron-electron repulsion) and I (exchange interaction). Some values of $U_{\rm eff}$ can be found on the materials project website, ²⁴ where they have calibrated $U_{\rm eff}$ values for transition metal oxide systems, for high spin Fe³⁺ it is 5.3 eV. However, no U_{eff} values have been optimized for LiFeV₂O₇. While a value of 5.3 eV was initially selected as suggested by the materials project,24 further investigation into the effects of varying U values on this structure was necessary. Previous studies have shown that Li₃Fe₂(PO₄)₃ (ref. 25) used Hubbard U values of 3.0 and 4.9 eV for Fe³⁺, while Na₂FePO₄F²⁶ used 3.5 and 4.5 eV for Fe²⁺. Motivated by these examples, we decided to test two U values, 3.5 and 4.3 eV, to see how they affect the electronic structure and the Fermi contact shift. Table 1 shows the results of structural optimization by GGA and GGA+U with $U_{\rm eff}$ values of 3.5, 4.3, and 5.3 eV for Fe for all frame models.

All optimized structures showed good agreement with the original reported unit cell. The calculated unit cell parameters exhibited errors of less than 4%. It is worth mentioning that the calculation optimizations were running at 0 K while the experimental results were at room temperature, which can be a source of differences. To a first approximation, the GGA+U approach does not significantly impact the quality of the geometry optimization. However, the difference between the two approaches is evident in the density of states (DOS) plots (Fig. S3†). The plotted total DOS illustrates the orbital occupancies, spin state of the metal and estimates the band gap based on the chosen value of $U_{\rm eff}$. The DOS of Fe 3d orbitals is consistent with the expected high-spin Fe³⁺ octahedral configuration, where up spins $e_{\rm g}$ and $t_{\rm 2g}$ states are occupied while the down spins are available. As expected, Fig. S3† shows an increase in band gap with addition of $U_{\rm eff}$. As

Table 1 Relaxed cell parameters for the GGA and GGA+U optimized LiFeV $_2$ O $_7$ from ORG, LFVOD and ORG-D structure unit cell compared to experimental values

Unit cell parameters	a (Å)	b (Å)	c (Å)	Volume (ų)
Exp ¹⁸	13.463	8.1882	14.386	1575.5
LFVOD exp ¹⁷	13.469	8.1924	14.390	1577.2
ORG-GGA	13.654	8.3003	14.148	1631.4
ORG-GGA+U	13.697	8.2647	14.517	1632.4
$U_{\rm eff} = 5.3 \; {\rm eV}$				
ORG-GGA+U	13.675	8.2529	14.497	1625.0
$U_{\rm eff} = 4.3 {\rm eV}$				
ORG-GGA+U	13.679	8.2531	14.501	1626.2
$U_{\rm eff} = 3.5 \; {\rm eV}$				
LFVOD-GGA	13.663	8.2393	14.454	1615.8
LFVOD-GGA+U	13.656	8.2261	14.530	1620.8
$U_{\rm eff} = 5.3 {\rm eV}$				
ORG-D-GGA+U	13.661	8.2018	14.562	1618.9
$U_{\rm eff} = 5.3 \; {\rm eV}$				

mentioned above, with addition of Hubbard parameter correction ($U_{\rm eff}$) the electron density is more localized at the TM site, Fe, and the difference between the valence and conduction band is increased. These changes directly affect the Fermi contact shift which is sensitive to how much the unpaired electron spin density is transferred from Fe to Li.^{7,9,27}

3.2 Fermi contact shift

For paramagnetic samples, the dominant interaction that affects the isotropic shift is the Fermi contact interactions generated by the unpaired electron spin density transferred from the paramagnetic atoms into the observed nucleus. For simple structures, this interaction can be analyzed *via* local geometries and their capability of electron spin transfer based on two mechanisms, spin delocalization and spin polarization.^{5,10,11} However, for complicated structures where there are no ideal 90- and 180-degree interactions, the chemical shift assignments cannot be qualitatively assessed. DFT calculations are employed here as a primary method to explain the origin of extra ⁷Li signals in the experimental spectra and assign them for LiFeV₂O₇.

According to the experimental data, we infer that there is a positive electron spin density transferred to the lithium environments due to the large positive chemical shift observed in the ⁷Li NMR spectrum (Fig. 2). The results of calculated ⁷Li Fermi contact shifts for ORG and LFVOD structures are compared to the experimental shift values in Table S1.† It is shown that the new position generated by the local disorder generates different values of ⁷Li shifts relative to the original

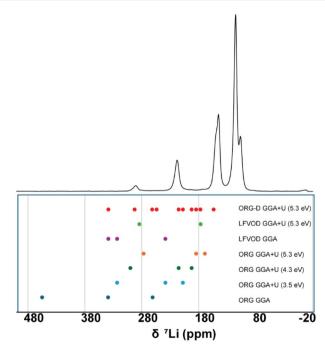


Fig. 2 $\,^{7}$ Li NMR experimental spectrum (top) and DFT calculated $\,^{7}$ Li Fermi contact NMR shifts (bottom). The data points are color-coded according to the computational method used.

structure. This demonstrates that despite being a small variation at the V2, V6, and O8 positions, the Li environments are affected.

In contrast to our observations during structure optimization, there is a notable difference in the calculated Fermi shift when comparing the results from GGA and GGA+U methods. This variation arises due to the influence of electron localization in the GGA+U method, which significantly impacts the predicted magnitude of electron spin density transfer at the Li sites. For ORG structure, the GGA+U approach provides a more accurate Li shift upon addition and increase of the $U_{\rm eff}$ correction term. The increased localization of electron density at Fe minimized the electron spin density transfer to the Li nucleus, which directly affects the Li shift in ssNMR. All values of U_{eff} cause a similar effect to the calculated Li shifts (Table S1 \dagger). As the value of U_{eff} is increased, electrons are more localized in the d orbital which decreases the overlap with the orbital from oxygen. Consequently, the amount of electron spin density transfer from Fe³⁺ to Li sites decreases which results in a smaller paramagnetic shift. Based on the calculations results generated for the ORG structure, the most appropriate Hubbard parameter correction value is 5.3 eV for Fe³⁺. This is also applied to the LFVOD structure. Note however, that will still slightly overestimate the shifts and this may be due to either further need of U_{eff} optimization or to the fact that we did not consider the magnetic susceptibility of LiFeV2O7 but approximated it using the value of LiFeP₂O₇.

Comparing the results obtained for the two modeled structures, there are still fewer resonances calculated than observed in the experimental spectra. The lack of structural disorder in the two distinct ORG and LFVOD structures is consistent with the observed result, namely each structure produces a set of three unique lithium sites in the asymmetric unit which are equivalent throughout the whole unit cell, thus only three different lithium shifts were provided for each set of calculations. However, those separate structures do not represent the real material, but rather what we interpret as two possible structures that co-exist in the experimentally synthesized phase. When the disorder is accounted for, as in the case of ORG-D structure, the lithium sites are no longer equivalent resulting in 12

Table 2 Calculated shifts for Li sites by GGA+U method for the ORG-D structure

ORG-D GGA+U ($U = 5.3 \text{ eV}$)				
CIF site	Site	Fermi shift ⁷ Li (ppm)		
Li1	Li1 _a	192.4		
Li1	Li1 _b	153.9		
Li1	Li1 _c	215.5		
Li1	Li1 _d	177.1		
Li2	$ m Li2_a$	338.7		
Li2	Li2 _b	254.0		
Li2	Li2 _c	292.5		
Li2	Li2 _d	261.7		
Li3	Li3 _a	207.8		
Li3	Li3 _b	184.7		
Li3	Li3 _c	177.0		
Li3	Li3 _d	192.4		

Li shifts being calculated, shown in Table 2. The reason for this change may be related to bond length, the angles, and the volume of the polyhedron at the lithium site, which can lead to the shortening or stretching of the distance to the transition metal. The best correlation with experimental ⁷Li NMR spectra was thus obtained with the defect structure, ORG-D. Given the DFT calculations results obtained for ORG-D, the most shifted experimental 292 ppm, may be correlated with the calculated shift for Li2_a at 338.7 ppm, explaining the presence of a high shift in the experimental ⁷Li NMR. A detailed explanation of the relevant electron spin transfer pathway is described below.

3.3 Spin transfer mechanism

In order to assign the Li signals, spin density maps resulting from the difference between up spin and down spin states, were plotted in three dimensions using the VESTA software (Fig. 3). In these maps, only positive spin density is observed as indicated by the presence of yellow surfaces. Based on the electron spin density transfer mechanism, we propose an explanation for shift magnitudes of positive sign of ^7Li observed for LiFeV_2O_7 structures. Li2 sites are located in a four-coordinated site surrounded by three FeO₆ octahedra where two are sharing a corner and one sharing an edge with LiO_4 (Fig. S4†). The unpaired electrons from the three Fe³⁺ are the source of electron spin density transfer to Li sites and the cause of high paramagnetic shift. In the case of Li1 and Li3, they are located in a six-coordinated site surrounded by two FeO₆ octahedra. They are expected to appear at lower paramagnetic shift than Li2 because they only receive contributions from two Fe³⁺.

Two different spin-transfer mechanisms from Fe to Li are present. (i) For the case that FeO_6 and $\text{LiO}_4/\text{LiO}_5$ share a corner, a delocalization mechanism occurs through hybridization between Fe e_g^* , O p, and Li s. The electrons in the Fe e_g^* orbitals are expected to interact with O p orbitals along the Fe–O–Li pathway through the interaction angle of 180°. In our case, the angles are in the range from 111.69 to 141.72° which differs from 180°, but the transfer is still possible. This mechanism can also be observed for LiFePO₄ and LiNi₂O₄. (ii) In the case of FeO₆ and LiO₄/LiO₅ sharing an edge, the delocalization mechanism occurs through hybridization between Fe t_{2g}^* , O p, and Li s. The Fe–O–Li angles are in the range from 93.45 to 102.71° which only slightly differs from 90°. Based on the

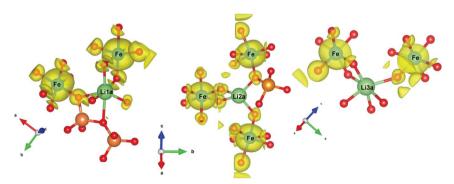


Fig. 3 3D spin density map calculated for ORG-D with GGA+U ($U_{\rm eff}=5.3$ eV) and an isosurface value equal to 0.005 spin per Å²; yellow surfaces indicate positive spin densities.

results of the ORG-D GGA+U approach, we assigned the experimental ⁷Li NMR spectra as listed in Table 2.

For all modeled structures, Li2 was calculated to be the high chemical shift, due to the three Fe³⁺ electron spin density contributions. Conversely, Li1 and Li3, both receive electron spin density transfer from two neighboring Fe³⁺. The distinction in the Fermi contact shifts observed at each lithium site can be attributed to variations in the Fe-Li distance and the Li-O-Fe angle. These geometrical variations directly affect the degree of orbital interaction, consequently adjusting the electron spin transfer magnitude to the lithium sites.

As indicated above, the ORG-D model exhibits the strongest correlation with the experimental ^7Li NMR spectra. Beyond the number of resonances in the presence of disorder, the experimental shift at 292 ppm closely aligns with the calculated shift for Li2a at 338.7 ppm. The introduction of disorder, particularly when V2 occupies a disordered position (V2A), brings it nearer to the lithium site (Li2a), and prompts a structural reorganization among surrounding atoms. This adjustment includes a reduction in the Fe2–Li2a distance from 3.0421 Å in the ORG model to 3.0020 Å in the ORG-D model. Such a decrease enhances the orbital overlap among the Fe t_{2g}^* , O p, and Li s orbitals, resulting in a pronounced Fermi contact shift. Tables S2, S3, and S4† offer information about calculated Li–Fe distances and Li–O–Fe angles for all modeled structures.

This study elucidates how structural disorders modify lithium environments, leading to significant variations in the electron spin density transfer mechanisms consequently in Fermi contact shifts. The ORG-D model exhibits the closest correlation with experimental NMR spectra, highlighting the relationship between local geometry and electronic interactions.

3.4 Structural evolution of LiFeV₂O₇ during half-cell operation

A comprehensive understanding of structural changes of cathode materials during the process of charge and discharge is crucial for the development of new materials and improving existing ones. For LiFeV₂O₇ an increase in local lithium dynamics was observed after 0.5 mol of lithium was inserted into the structure, through the evolution of the ⁷Li NMR spectra *via* both 1D ⁷Li MAS data acquired at 60 kHz MAS and the combination of chemical exchange methods including ⁷Li EXSY and Selective Inversion spectroscopy. Therefore, the chemical composition, Li_{1.x}FeV₂O₇ is an interesting structure that warrants further investigation, to evaluate the unit cell-level changes that facilitate this observed change in lithium dynamics.

3.4.1 *Operando* SPXRD. To understand the evolution of the $\text{Li}_{1,x}\text{FeV}_2\text{O}_7$ structure, *operando* SPXRD is carried out on a half-cell configuration (Fig. S1†). Fig. 4 shows a series of SPXRD patterns that were collected during the electrochemical discharge of LiFeV $_2\text{O}_7$ ν s. Li metal to investigate the structural evolution associated with Li insertion. The cell discharged from 2.75 V to 2.27 V ν s. Li/Li $^+$.

The different colored lines in the plot represent diffraction patterns acquired at successive states of discharge. From the bottom to the top of the data series, there is a clear change in the observed reflections coincident with the progression of the discharge process. The series of diffractograms suggests a continuous change in the structure. It is evident that there are shifts in the positions of individual reflections as well as variations in intensity, and the coalescence of

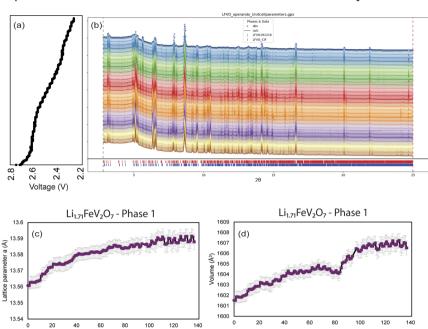


Fig. 4 (a) Voltage profile of first discharge cycle for the *operando* coin cell from 2.75 V to 2.27 V vs. Li/Li⁺; (b) the evolution of the X-ray diffraction patterns of Li_{1.x}FeV₂O₇; (c) and (d) the plots indicate how the a unit cell parameters, and volume, change over time, with error bars indicating the measurement's reliability and precision at each point.

certain peaks as the electrochemical discharge progresses. These changes are indicative of alterations in the crystal structure, suggesting phase transformations or changes in the lattice parameters due to lithium-ion insertion in the material.

The sequential Rietveld refinement of unit cell parameters over the course of the 139 scans for LiFeV $_2$ O $_7$ is performed using a two phases model. Even though the second phase is only detected after 0.5 mol of lithium is inserted, we choose to approach the data in this way to monitor the main phase transformation during the lithiated process. Li $_x$ FeV $_2$ O $_7$ electrode material undergoes a complex Li $^+$ insertion mechanism with sequential biphasic and solid–solution reactions during the first discharge process. The complexity of the data, characterized by a large number of peaks and their overlapping plus complex Li $^+$ insertion mechanism, poses a significant challenge to conducting a detailed analysis. The proximity of many peaks makes it difficult to isolate and analyze individual peak variations with high confidence. Due to these limitations, we focus our analysis on the unit cell parameters evolution during the first discharge cycle for phase 1. This approach provided valuable insights into the structural transformations occurring within the material. Extra information about phase 2 is found in Fig. S5.†

Fig. 4 shows the evolution of the a-lattice parameter as well as the unit cell volume for phase 1 during the electrochemical lithiation of $\text{Li}_{1.x}\text{FeV}_2\text{O}_7$. Overall, the unit cell volume expands as the experiment progresses, which increases by 0.37% during the lithiation. This phenomenon can be attributed to the increment

a lithiated sample by ⁷Li NMR.

in ionic radii of vanadium and iron produced upon Li insertion due to the reduction process and also the amount of lithium inserted. An increase in the unit cell volume often results in larger interstitial spaces within the crystal structure. These spaces can serve as pathways for lithium ions to move more freely through the electrode material resulting in an increase in the lithium dynamics.

This result explains why an increase in lithium dynamics was observed in

The *operando* SPXRD data provided a comprehensive overview of the transformations occurring within the unit cell. Nonetheless, the evident modification in the diffraction data exhibited a more gradual progression in comparison to the abrupt change in the ⁷Li NMR spectra. To elucidate the impact of lithium insertion on the local structure with greater clarity, further investigation was conducted through *ex situ* synchrotron X-ray powder diffraction and *ab initio* computational studies.

3.5 Structure determination of Li_{1.71}FeV₂O₇

3.5.1 Ex situ SPXRD. In order to obtain a more comprehensive understanding of the phases present during the enhancement of lithium-ion dynamics, the ex situ SPXRD pattern of $\mathrm{Li}_{1.71}\mathrm{FeV}_2\mathrm{O}_7$ was obtained by discharging the half coin cell to 2.39 V vs. $\mathrm{Li/Li}^+$. The Rietveld refinement process involves adjusting the scale, background, and lattice parameters of the reference patterns to align with the experimental peaks, resulting in a low R_{wp} value of 4.75%. $\mathrm{Li}_{1.71}\mathrm{FeV}_2\mathrm{O}_7$ consists of two phases: 65.54% phase 1 and 34.46% phase 2 (Fig. S6†). Although these phases share a similar structural framework, they exhibit slight variations in lattice parameters and are presumed to differ in their lithium content. The coexistence of structurally similar crystal phases with subtle differences in elemental composition can be observed not only in cycled battery materials, 29,30 but also in mineralogical system. 31

Following lithiation, notable modifications in the lattice dimensions and volume were observed compare to the parent structure, while the crystallographic space group, monoclinic *Cc*, remained unchanged. This indicates that the structural symmetry is preserved even as the framework accommodates extra lithium ions. Table 3 provides the detailed lattice parameters obtained with the Rietveld refinement.

Given the complexity of the material, we narrowed our investigation to the predominant phase, Phase 1, for further investigation. This choice allows for a more in-depth exploration of the phase that plays the most significant role in the interpretation of the ⁷Li NMR spectra. The *ex situ* SPXRD diffractogram pattern

Table 3 Rietveld refinement unit cell parameters for both phases in the $Li_{1.71}FeV_2O_7$ compared with the pristine phase

Unit cell parameters	Pristine LiFeV ₂ O ₇ (ref. 17)	Li _{1.71} FeV ₂ O ₇ Phase 1	Li _{1.71} FeV ₂ O ₇ Phase 2
a (Å)	13.469(6)	13.594(5)	13.599(9)
$b(\mathring{A})$	8.192(4)	8.250(3)	8.272(6)
b (Å) c (Å)	14.390(7)	14.216(6)	14.308(6)
β (°)	96.600(9)	94.866(5)	95.309(8)
Volume (Å ³)	1577.2(1)	1588.7(7)	1602.9(2)

does not allow for precise determination of lithium positions. The new lithium sites in Li_{1.71}FeV₂O₇ were deduced from the bond valence energy landscape (BVEL) and then the structures were re-examined by DFT calculations.

3.5.2 Bond valence energy landscape. BVEL calculations have been used to predict possible positions for ions and also to prove ion diffusion pathways in diverse materials. ^{13,32–37} With this approach, BVEL were generated, where valence units are transformed into energy units as implemented in the program BondSTR of the Fullprof Suite. ³⁸ Calculations were made using the soft bond valence parameters developed by S. Adams. ³⁹ This approach considers the polarizability of the mobile species, in this case Li⁺, and the influence of the counterions of the structure up to a distance of 10 Å. This approach allows for visualizing conduction pathways in the structure while giving hints to possible conduction mechanisms. In our case, these calculations served as a guide for identifying plausible sites for lithium insertion.

Fig. 5 shows the calculated BVEL for Li $^+$ conduction pathways in the Li $_{1.71}$ -FeV $_2$ O $_7$ structure phase 1 obtained from the Rietveld refinement with an isosurfaces value of 0.2 valence units. The yellow isosurfaces represent the most likely migration route for Li ions. Utilizing VESTA software, we incorporated eight new lithium sites into a structure refined Li $_{1.71}$ FeV $_2$ O $_7$ guided by the results obtained by BVEL calculations. After inserting the new lithium ions, the modified structure was submitted to geometry optimization by DFT calculation in VASP to get the stable atomic position of the modified structure. The same approach has been used to predict the lithium position in the LiH $_2$ V $_3$ O $_8$ structure which exhibited agreement with the data obtained with neutron diffraction.

3.6 Ab initio DFT studies of lithiated sample

Density functional theory (DFT) calculations were conducted in VASP to investigate the stability of the modeled structure and to elucidate the correlation

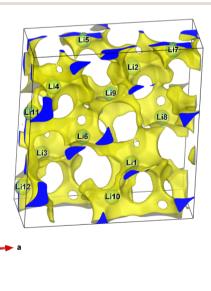


Fig. 5 Bond Valence Energy Landscape (BVEL) calculation for Li-ions in $\text{Li}_{1.71}\text{FeV}_2\text{O}_7$ phase 1 with the isosurfaces of 0.2 plotted in VESTA.

between experimental 7 Li NMR shifts and specific sites within the phases formed during the electrochemical lithiation of LiFeV $_2$ O $_7$. For the lithiated phase Li $_{1.71}$ -FeV $_2$ O $_7$, geometry optimization focused on Phase 1, which was identified from the Rietveld refinement of Li $_{1.71}$ -FeV $_2$ O $_7$ and further analyzed for new lithium sites using BVEL calculations. The original structure LiFeV $_2$ O $_7$ contained 12 Li per unit cell, whereas the modeled Phase 1 of Li $_{1.71}$ FeV $_2$ O $_7$ featured 20 Li. This model served as the basis for structural relaxation, leading to an optimized structure that was subsequently compared with the experimental results in Table S5.† The optimized lattice parameters (a, b, and c) obtained via the GGA+U method showed a deviation within a 3% error margin when compared with those determined experimentally through the diffraction technique.

As mentioned in the *operando* and *ex situ* SPXRD data, an increase in lattice parameters and unit cell volume suggests more open pathways or larger interstitial sites, providing a reason for increased lithium mobility observed in our previously published NMR data.¹⁷ With the structure optimized, we can have a more detailed understanding of the effects of unit cell changes on lithium dynamics. The Li–Li distances and the size of the channels, or bottlenecks, can significantly affect lithium dynamics in cathode materials for lithium-ion batteries.

Summarized in Table 4, it is possible to compare the lithium dynamics in the pristine and lithiated structure of LiFeV₂O₇ using the Li–Li distances and the Li–O bottleneck. Lithium–oxygen (Li–O) bottleneck diffusion area was calculated by the area of the face that the mobile lithium ions share when exchanging with their respective partners. In the pristine structure, the lack of energy barrier data implies that the lithium dynamics were not quantified under the conditions studied. There is a noticeable change in the bottleneck size for the Li_{1B}–Li_{2A}, and Li_{1B}–Li_{3C} pairs, which increases from 4.32 to 4.48 Å² and 3.84 to 4.06 Å² respectively. This enlargement of the bottleneck potentially allows for easier lithium-ion movement, contributing to improved lithium dynamics in the lithiated structure.

The Li-Li distances do not change significantly upon lithiation, with only slight variations. This suggests that the average spacing between lithium ions

Table 4 Summary of activation energy values for the three Li-Li exchange pairs as well as the calculated Li-O bottlenecks of diffusion for pristine and lithiated structures

Pristine	Lithium pair	Energy barrier	Li–Li distance (Å)	Li-O bottleneck (Ų)
	Li1 _B -Li2 _A	_	4.46	4.32
	Li1 _B -Li3 _C	_	3.2	3.84
	Li2 _A –Li3 _C	_	4.68	4.86
Lithiated				
model			Li–Li	Li-O
Li _{1.71} FeV ₂ O ₇	Lithium pair	Energy barrier ¹⁷	distance (Å)	bottleneck (Ų)
	Li1 _B -Li2 _A	0.59 ± 0.06	4.38	4.48
	Li1 _B -Li3 _C	0.48 ± 0.07	3.2	4.06
	Li2 _A -Li3 _C	0.4 ± 0.3	4.64	4.95

does not drastically impact lithium dynamics after lithiation, at least not to the extent that would be indicated by the Li–Li distances alone. However, it is also notable that a short Li–Li distance facilitates easier lithium hopping between these sites, resulting in a lower energy barrier, as observed for the Li_{1B}–Li_{3C} pair. Both interatomic Li distances and bottleneck sizes are important factors to consider for understanding ionic conductivity in cathode material.

All these changes were evidenced by ssNMR spectroscopy, reflecting altered local environments and enhanced dynamics of lithium ions during the discharge process. The NMR data showed these changes through shifts in signal positions, changes in line widths (indicating changes in lithium mobility), and the appearance of a new signal in negative chemical shift, indicating that a new lithium environment was created.

3.7 Fermi contact shift and spin transfer mechanism

The calculated spin density of state (DOS) for the optimized phase 1 of Li_{1,71}- FeV_2O_7 is given in Fig. 6. Different from what was observed in the pristine material, the plotted DOS for Li_{1.71}FeV₂O₇ shows a change in the relative contributions of the Fe and V in d orbitals suggesting that both are going towards the redox process. The high-spin 3d electron configuration of Fe²⁺ ions is confirmed by the appearance of occupied $e_{\rm g}$ orbitals and a lift in degeneracy of the $t_{\rm 2g}$ down orbitals, one being occupied. For vanadium ions, which previously did not have any d orbital occupied, now a single unpaired electron is located in the t_{2g} orbital. In LiFeV₂O₇, there are six vanadium sites situated in two different environments: five of these sites form VO₄ tetrahedra, while one adopts a [5]-coordinated VO₅ polyhedral geometry. In the presence of new occupied lithium sites, it is noted that vanadium atoms in 5 coordination are reduced in priority relative to the other vanadium atoms during the lithiation process. This is explained based on the charge compensation and the size of polyhedron to better accommodate the large V⁴⁺ cation. This result confirmed the hypothesis raised by Benabed. ¹⁸ Initially, the theoretical capacity of LiFeV₂O₇ was calculated assuming one Li⁺ per formula unit, 97 mA h g^{-1} . However, the measured discharge capacity at the first cycle

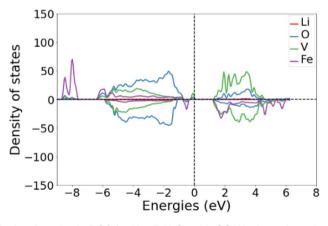


Fig. 6 Calculated total spin DOS for $\rm Li_{1.71}FeV_2O_7$ with GGAU where the color coding of lines represents elements.

reached 100 mA h g^{-1} , which was slightly higher than the theoretical capacity, suggesting that vanadium was also partly reduced.

DFT calculations confirm that the two transition metals are reduced throughout the discharge process. For paramagnetic samples, the dominant interaction that affects the isotropic shift is the Fermi contact interactions and now in addition to the unpaired electrons from Fe^{3+}/Fe^{2+} , we also have unpaired electrons from V^{4+} . The 7Li ssNMR Fermi contact shift was computed using the GGA+U method and the results can be found in Table S6.† All computed 7Li Fermi shifts for $Li_{1.71}FeV_2O_7$ are compared to the experimental spectrum in Fig. 7. The experimental data is characterized by multiple signals, including four intense peaks at 211, 178, 144 and -55 ppm. The signal observed around 0 ppm is attributed to electrolyte. The signals are very broad and thus it is possible for multiple signals to overlap.

In order to understand the electronic spin transfer mechanism from the V⁴⁺ ions to Li⁺ in the optimized Li_{1,71}FeV₂O₇ structure, we plotted the calculated 3D spin density map in selected regions of the cell as shown in Fig. 8. The 3D spin density maps of the entire structure can also be found in the ESI (Fig. S7†). The positive and negative electron spins are presented in yellow and blue isosurfaces, respectively. The V^{4+} ion exhibits one unpaired electron localized in the d_{xy} orbital perpendicular to the V-O-Li axis. The z-direction used to define the orientation of the orbitals was chosen to run along the V2-O10 interatomic axis as shown in Fig. 8. All of them are independent of the a, b, and c crystallographic directions of the unit cell. As seen in Fig. 8, no orbital overlap involves this V^{4+} $3d_{xy}$ orbital and the spin density does not point toward Li, the V-O-Li angle is equal to 159.76°. However, as can be seen also in Fig. 8, the O 2p orbital is negatively polarized. This is the case where the electron spin density is transferred to the s orbital via a polarization mechanism. The unpaired electron of the partially filled Vt_{2g} bands polarizes deeper fully occupied levels resulting from the Veg-Op-Lis orbitals hybridization leading to a negative electronic spin on Li and consequently to a negative shift for 7Li NMR.10,40 This behavior has been seen for V4+ in other

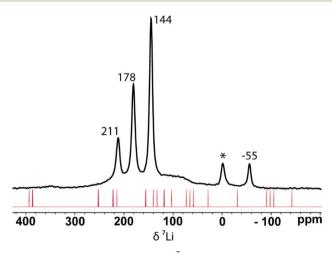


Fig. 7 Comparison between the experimental ^7Li MAS NMR signals of $\text{Li}_{1.71}\text{FeV}_2\text{O}_7$ and the calculated ones for the modeled supercell. The asterisk indicates the signal from electrolyte residual salt.

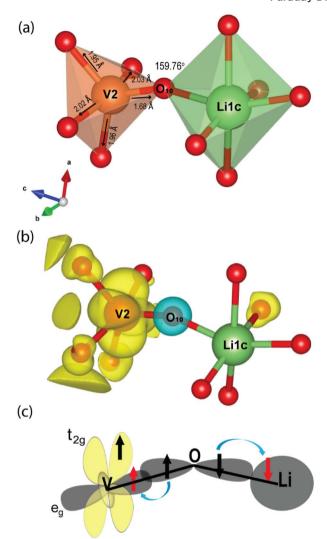


Fig. 8 (a) Local environment of V^{4+} and Li^+ in $Li_{1.71}$ FeV₂O₇ modeled structure. (b) 3D calculated spin density map showing the electron spin density surrounding a V^{4+} ion (0.005 spin per Å² isosurface value). (c) Schematic representation of orbital overlap that results in a negative electronic spin density being transferred to the 2s orbital *via* a polarization mechanism.

structures, such as LiVOPO₄ (ref. 41) and $Na_3V_2(PO_4)_2FO_2$. These results explain the single resonances observed at -55 ppm in the experimental ⁷Li NMR spectrum and thus confirm the reduction of V^{5+} ions upon discharge.

The reduction of vanadium increases the number of paramagnetic species in the structure. The orientation of the vanadium d orbitals leads to some large shifts compared to the pristine material. However, for the Li1_b site, the computed Fermi shift is larger than the experimentally observed shifts. With the addition of new lithium sites, the optimized lithiated structure is reorganized decreasing the Fe2-V4 distance from 3.3342 to 2.9906 Å. This structural change alters the

coordination at some vanadium sites from $\mathrm{VO_4}$ to $\mathrm{VO_5}$. Unlike the scenario with $\mathrm{Li1_c}$, for this case the orientation of the vanadium d orbital is such that it aligns towards the Li orbital, facilitating a delocalization mechanism that shifts the chemical shift to higher ppm values. Consequently, the lithium site receives electron spin density from both vanadium and iron. This theoretical outcome, however, does not align with experimental observations, suggesting that additional models should be explored for a more accurate representation.

4 Conclusion

In conclusion, the research presented provides a comprehensive investigation into the electronic structure and associated ⁷Li NMR chemical shifts of LiFeV₂O₇ as a lithium cathode material, utilizing a combination of Density Functional Theory (DFT) calculations and operando SPXRD. The study elucidates the influence of defect-associated vanadium atom positioning on the ⁷Li NMR shifts. The computed Fermi shift values for the modeled disordered structure (ORG-D) are in good agreement with the experimental data, showing the sensitivity of NMR spectroscopy to a minimal local alteration. We also examined the structural evolution of LiFeV₂O₇ during the lithiation process, correlating it with the dynamics of lithium insertion. The observed volume expansion during the first discharge cycle by operando SPXRD contributed to the enhanced lithium dynamics in the bulk material. The lithiated phase Li_{1.71}FeV₂O₇ was analyzed using ex situ SPXRD and modeled through BVEL calculations and verified by DFT calculations. Upon comparison between the optimized lithiated structure and its parent framework, an expansion of the bottleneck regions was observed. This structural modification facilitates the movement of lithium ions, significantly enhancing the lithium dynamics within the lithiated structure. Our findings established the involvement of vanadium in the redox processes giving rise to a negative Fermi contact shift through the polarization mechanism. This study shows how ssNMR and DFT calculations are essential tools for gaining detailed insights into the structural intricacies of solid materials. These methodologies are particularly essential for revealing the complexities of local environments and domain structures in oxide materials, such as lithium-ion battery cathodes.

Conflicts of interest

There are no conflicts to declare.

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