Recursion

The Art of Self Reference

Goal: use self-reference is a meaningful way

Hofstadter's Law: "It always takes longer than you expect, even when you take into account Hofstadter's Law."

(From Gödel, Escher, Bach)

good advice for CS 220 assignments!

Goal: use self-reference is a meaningful way

Hofstadter's Law: "It always takes longer than you expect, even when you take into account Hofstadter's Law."

(From Gödel, Escher, Bach)

mountain: "a landmass that projects conspicuously above its surroundings and is higher than a **hill**"

hill: "a usually rounded natural elevation of land lower than a mountain"

(Example of unhelpful self reference from Merriam-Webster dictionary)

Overview: Learning Objectives

Recursive information

- What is a recursive definition/structure?
- Arbitrarily vs. infinitely

Recursive code

- What is recursive code?
- Why write recursive code?
- Where do computers keep local variables for recursive calls?
- What happens to programs with infinite recursion?

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What is Recursion?

Recursive definitions contain the term in the body

• Dictionaries, mathematical definitions, etc

A number **x** is a positive even number if:

• x is 2

OR

x equals another positive even number plus two

What is Recursion?

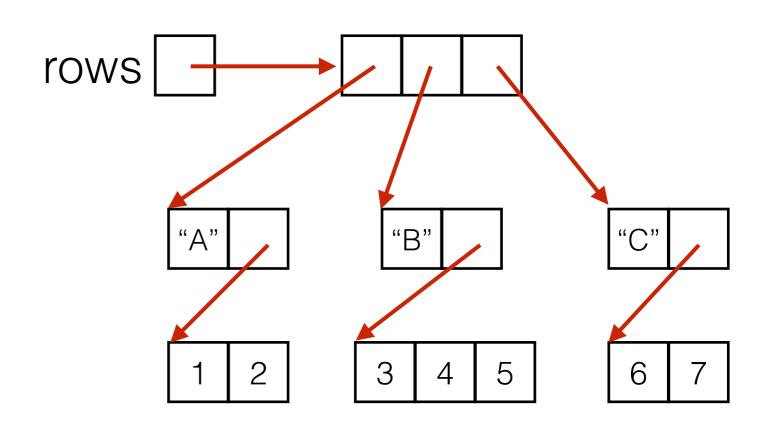
Recursive definitions contain the term in the body

Dictionaries, mathematical definitions, etc

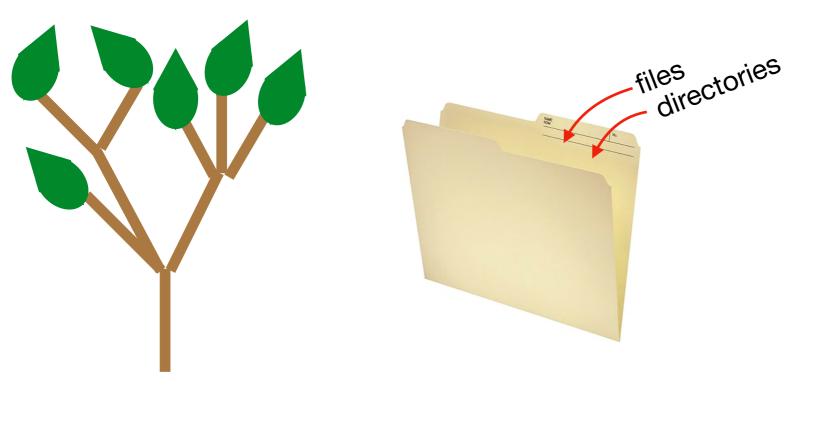
Recursive structures may refer to structures of the same type

data structures or real-world structures

```
rows = [
    ["A",[1,2]],
    ["B",[3,4,5]],
    ["C",[6,7]]
]
```



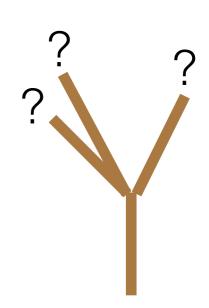
Recursive structures are EVERYWHERE!



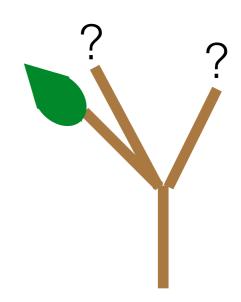
nature files formats

Term: branch

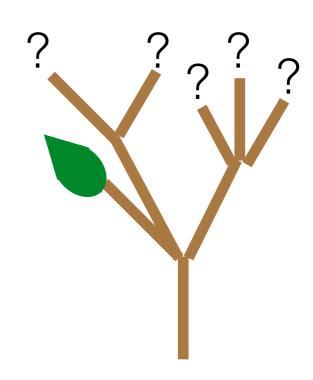
Term: branch



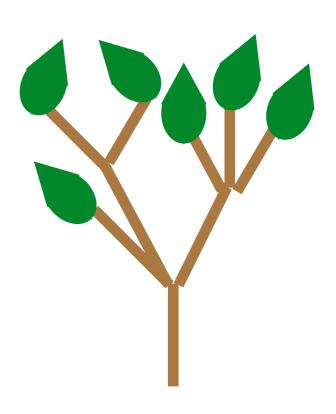
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Term: branch

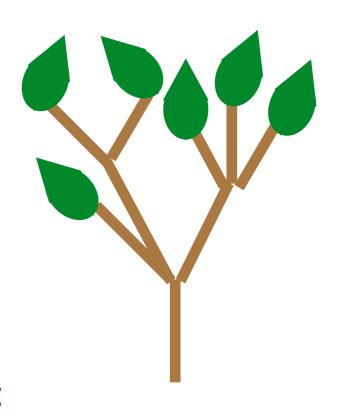


Term: branch



Term: branch

Def: wooden stick, with an end splitting into other branches, OR terminating with a leaf

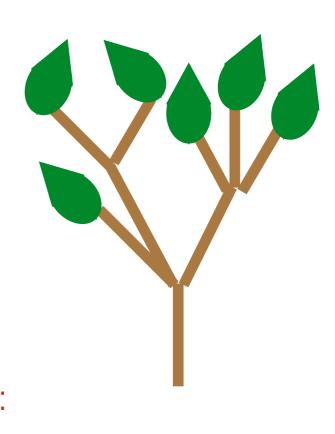


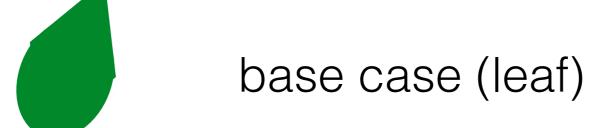
trees are arbitrarily large:
recursive case allows
indefinite growth

Term: branch

Def: wooden stick, with an end splitting into other branches, OR terminating with a leaf

trees are finite: eventual **base case** allows completion trees are arbitrarily large:
recursive case allows
indefinite growth

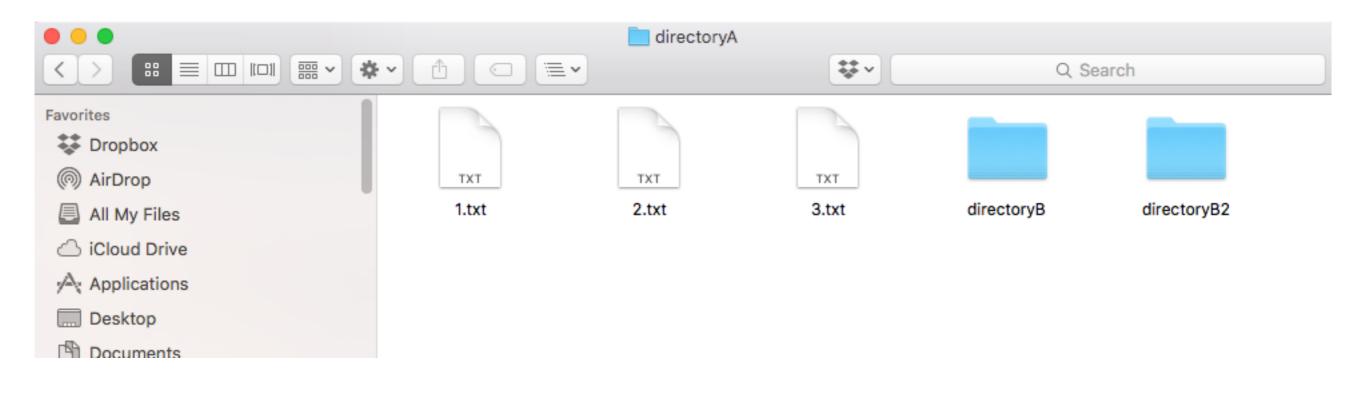






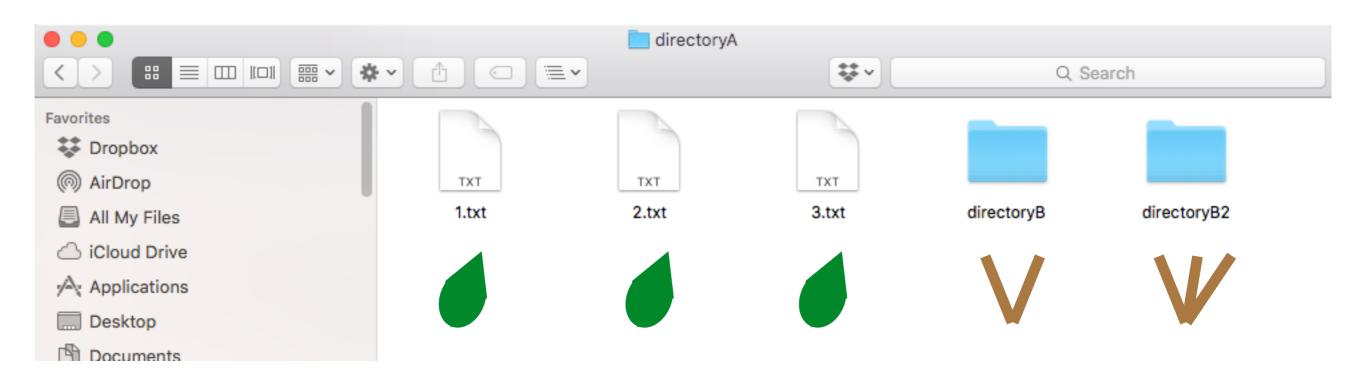
Term: directory

recursive because def contains term



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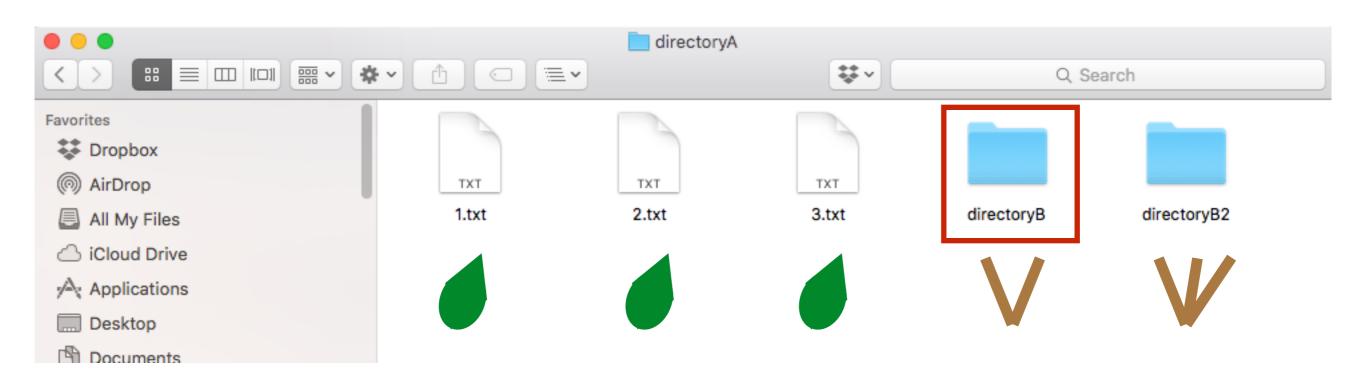
recursive because def contains term



file system tree

Term: directory

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file system tree

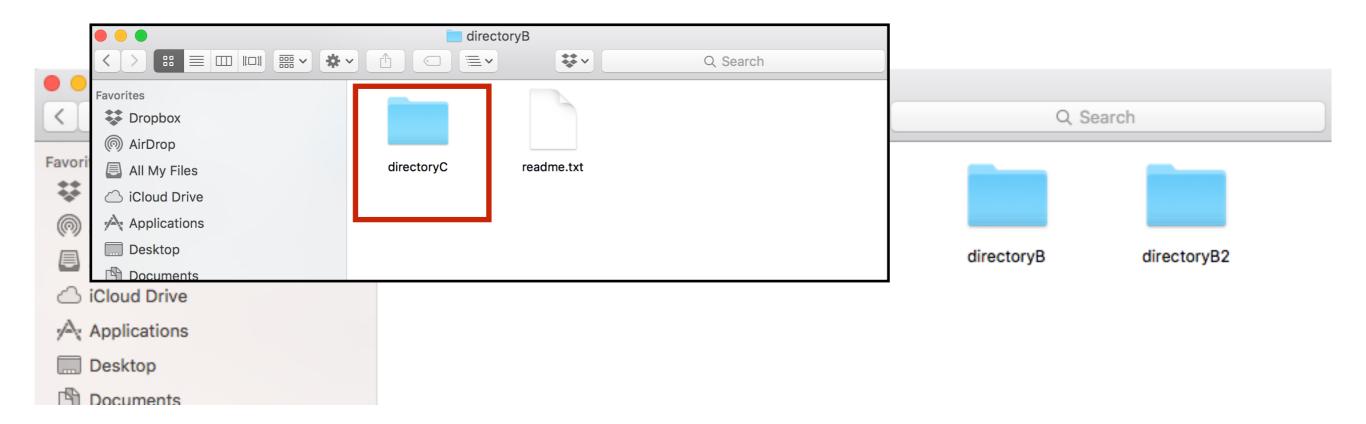
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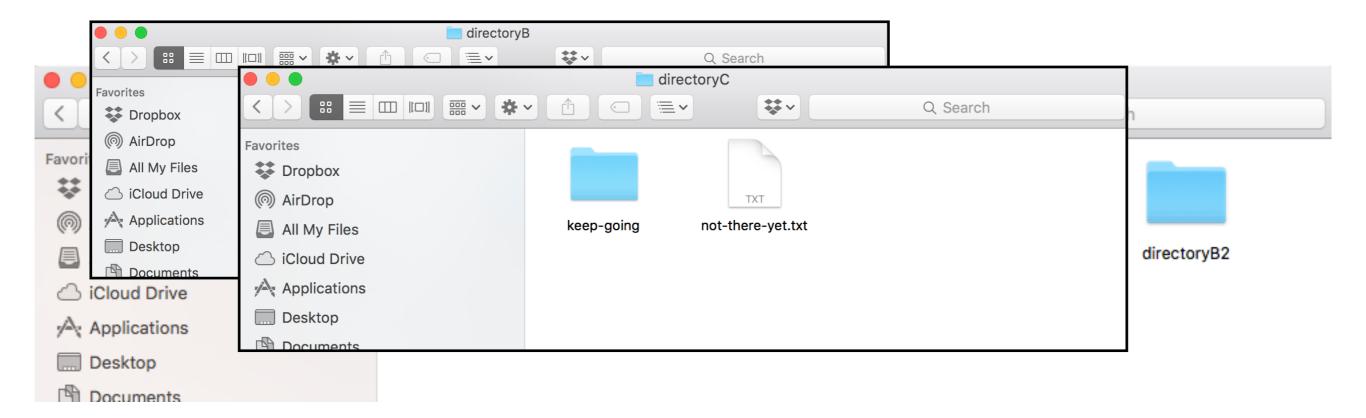
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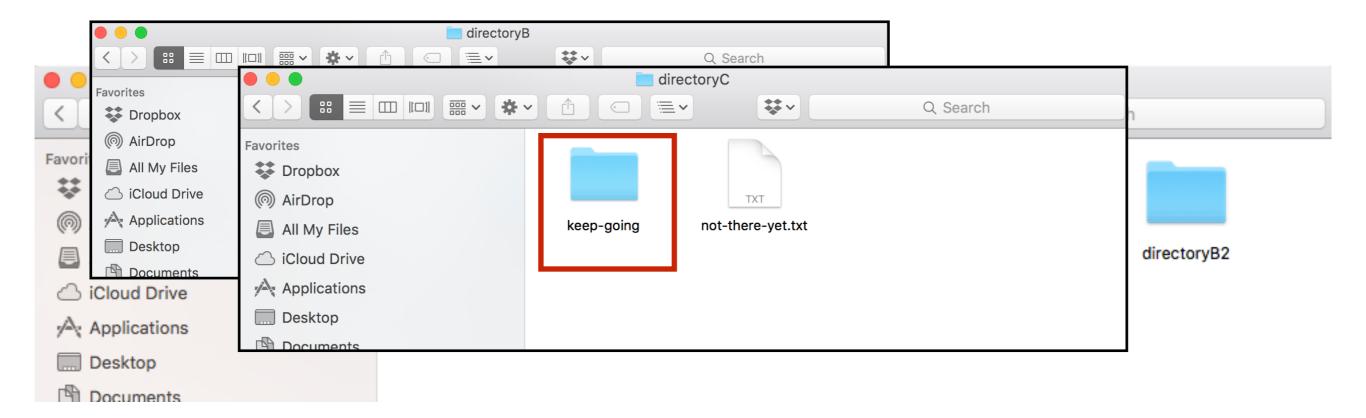
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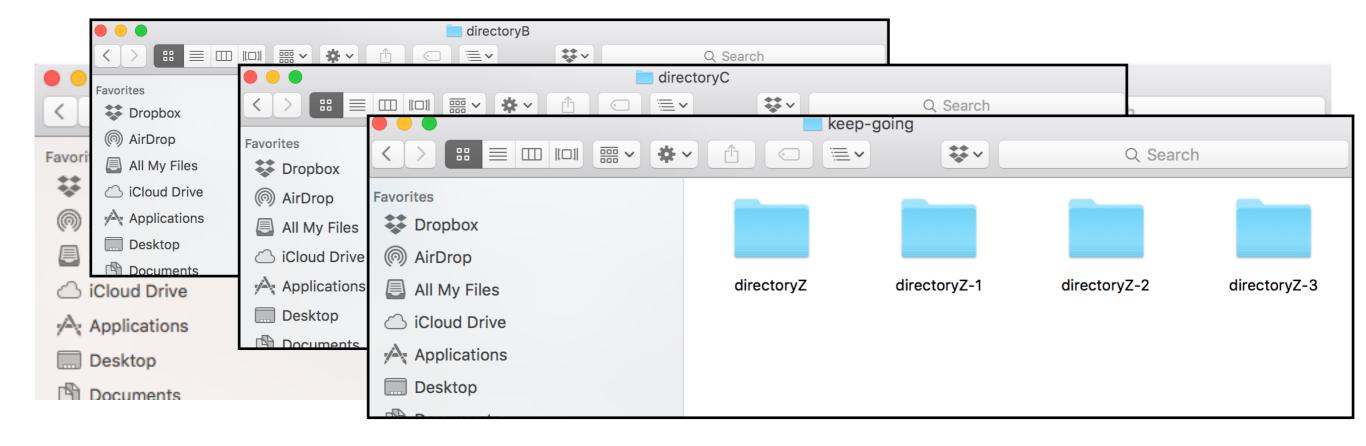
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Term: directory

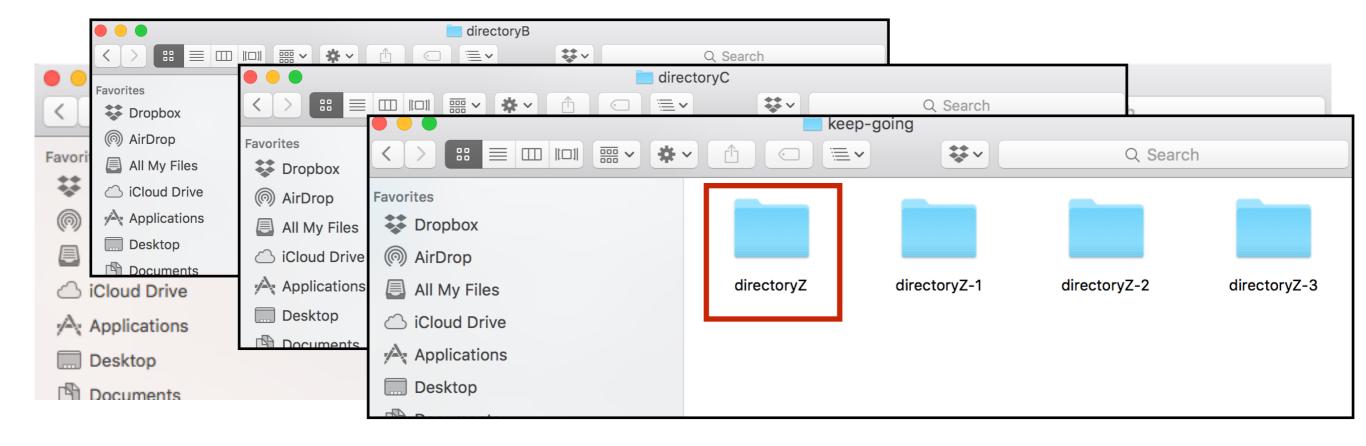
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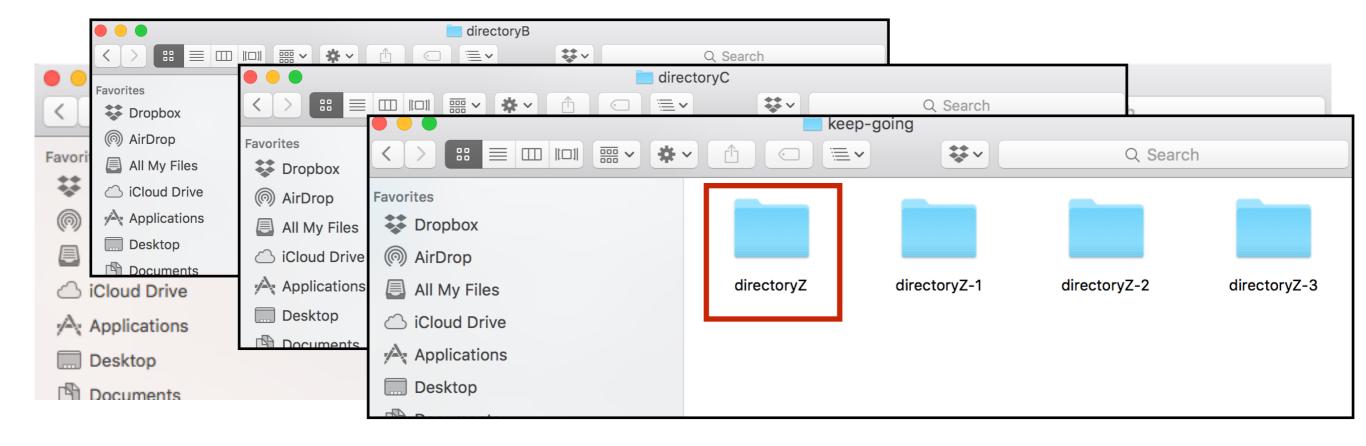
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file system tree

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file system tree

Example JSON Dictionary:

```
{
  "name": "alice",
  "grade": "A",
  "score": 96
}
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Def: a set of *json-mapping*'s

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Term: *json-dict*

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Example JSON Dictionary:

```
"name": "alice",
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keys values
```

Term: *json-dict*

Def: a set of *json-mapping*'s

Term: json-mapping

Def: a *json-string* (KEY) paired with a

json-string OR json-number

Example JSON Dictionary:

```
{
    "name": "alice",
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}
```

Term: json-dict
Def: a set of json-mapping's

Term: json-mapping
Def: a json-string (KEY) paired with a json-string OR json-number
OR json-dict (VALUE)

recursive self reference isn't always direct!

Example JSON Dictionary:

```
"name": "alice",
"grade": "A",
"score": 96,
"exams": {
    "midterm": 94,
    "final": 98
}
```

Term: json-dict

Def: a set of *json-mapping*'s

Term: json-mapping

Def: a *json-string* (KEY) paired with a

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Example JSON Dictionary:

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Recursive information

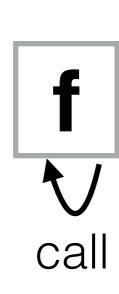
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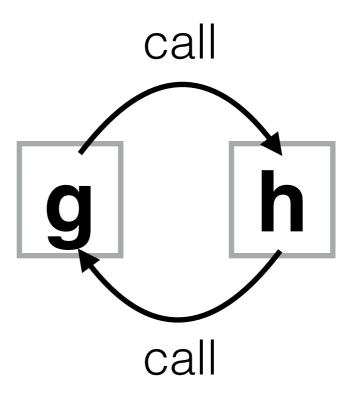
Recursive code

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What is it?

• A function that calls itself (possible indirectly)

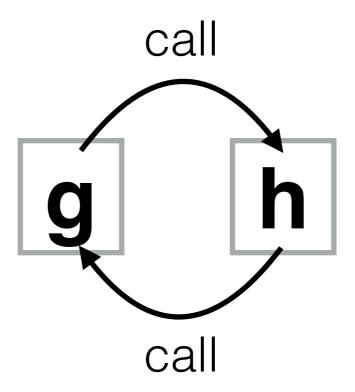




What is it?

A function that calls itself (possible indirectly)

```
def f():
    # other code
    f()
    # other code
```



What is it?

A function that calls itself (possible indirectly)

```
def f():
    # other code
    f()
    # other code
```

```
def g():
    # other code
    h()
    # other code

def h():
    # other code
    g()
    # other code
```

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A function that calls itself (possible indirectly)

Motivation: don't know how big the data is before execution

- Need either iteration or recursion
- In theory, these techniques are equally powerful

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Motivation: don't know how big the data is before execution

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Why recurse? (instead of always iterating)

- in practice, often easier
- recursive code corresponds to recursive data
- reduce a big problem into a smaller problem



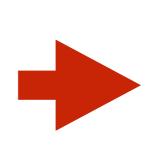
https://texastreesurgeons.com/services/tree-remova

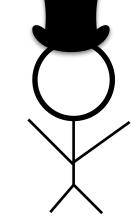


eager CS 220 students in the front row



wise and benevolent teacher wearing a top hat



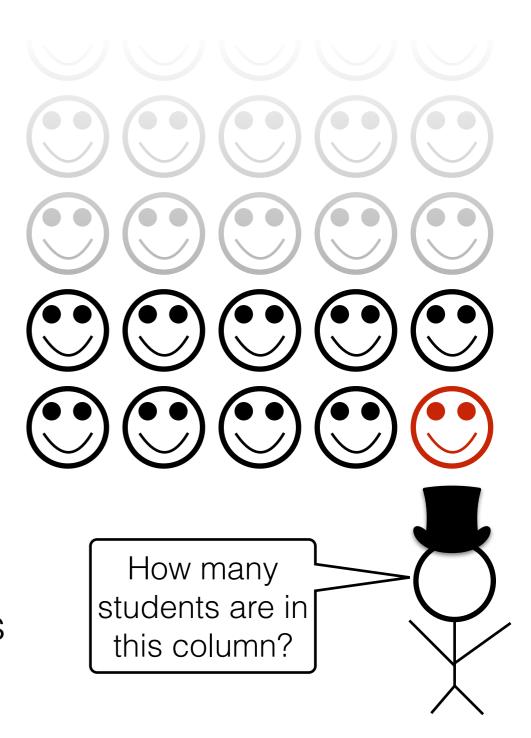


Imagine:

A teacher wants to know how many students are in a column. What should each student ask the person behind them?

Constraints:

- It is dark, you can't see the back
- You can't get up to count
- You may talk to adjacent students
- Mic is broken (students in back can't hear from front)

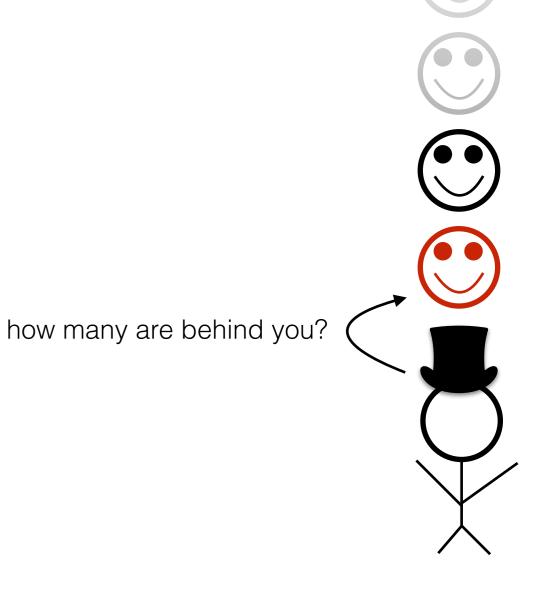


Strategy: reframe question as "how many students are behind you?"



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Reframing is the hardest part



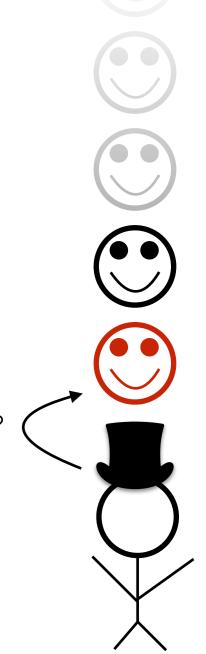
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Process:

if nobody is behind you: say 0

else: ask them, say their answer+1

how many are behind you?



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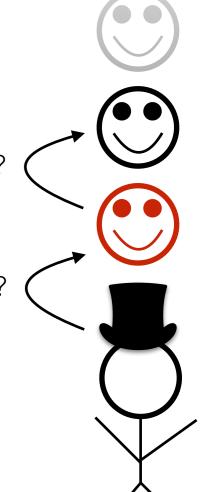
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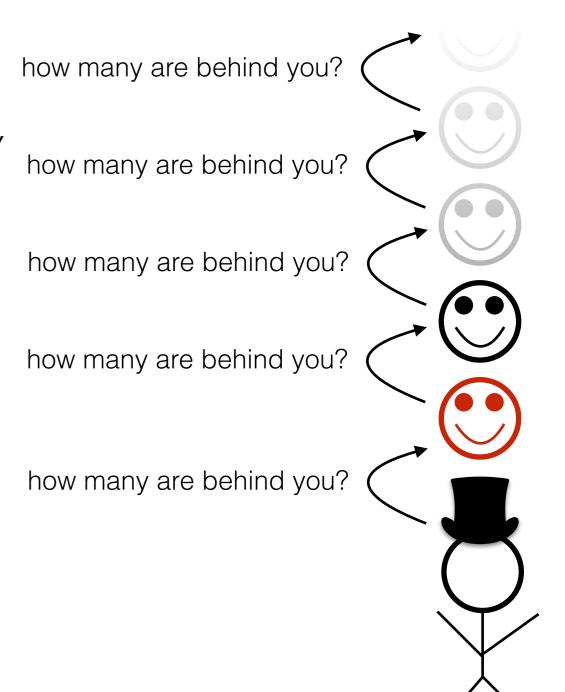
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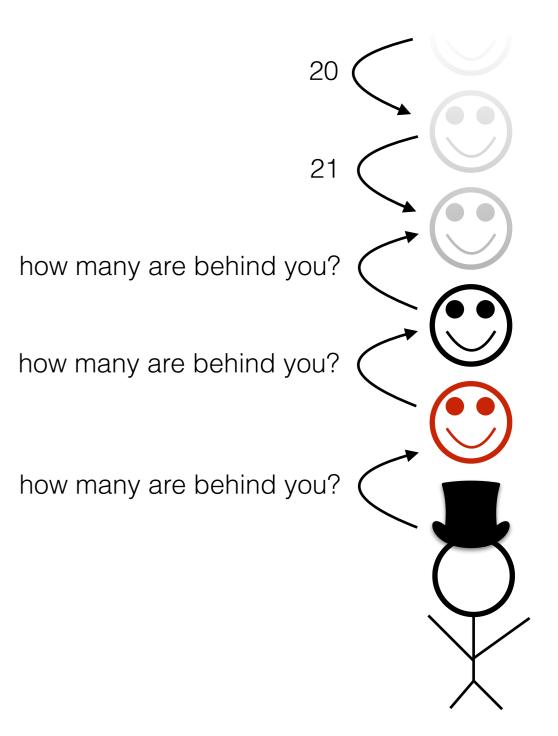
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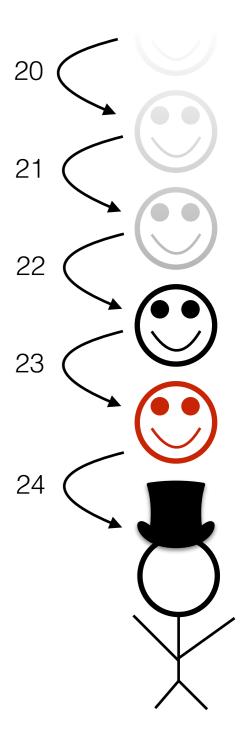
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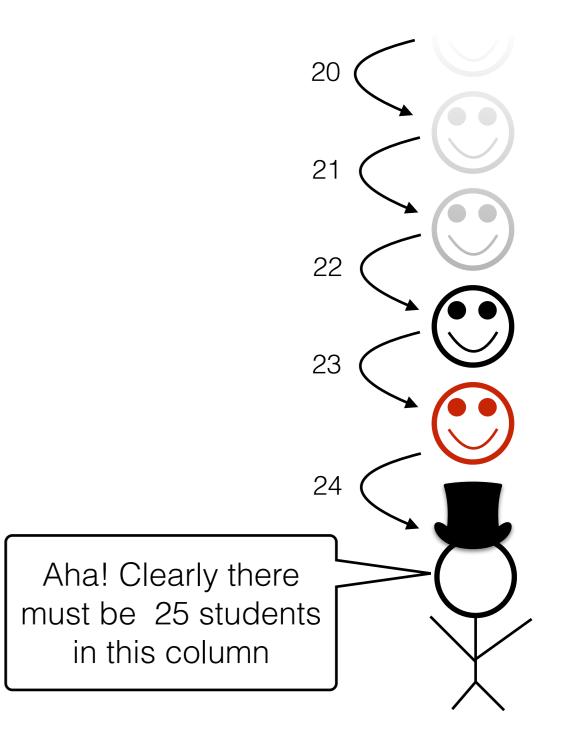
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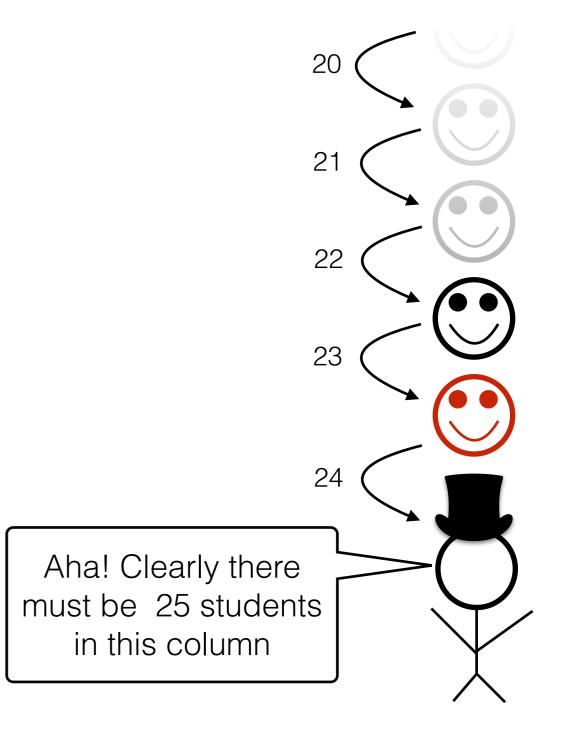
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Observations:

- Each student runs the same "code"
- Each student has their own "state"



Practice: Reframing Factorials

 $N! = 1 \times 2 \times 3 \times ... \times (N-2) \times (N-1) \times N$

1. Examples:

1! = 1 2! = 1*2 = 2 3! = 1*2*3 = 6 4! = 1*2*3*4 = 24 5! = 1*2*3*4*5 = 120

2. Self Reference:

3. Recursive Definition:

4. Python Code:

```
def fact(n):
    pass # TODO
```

Goal: work from examples to get to recursive code

1. Examples:

```
1! = 1
2! = 1*2 = 2
3! = 1*2*3 = 6
4! = 1*2*3*4 = 24
5! = 1*2*3*4*5 = 120
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2. Self Reference:

look for patterns that allow rewrites with self reference

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1! =
2! =
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3. Recursive Definition:

convert self-referring examples to a recursive definition

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2. Self Reference:

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1! = 1

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3. Recursive Definition:

```
1! is 1
N! is ???? for N>1
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4. Python Code:
    def fact(n):
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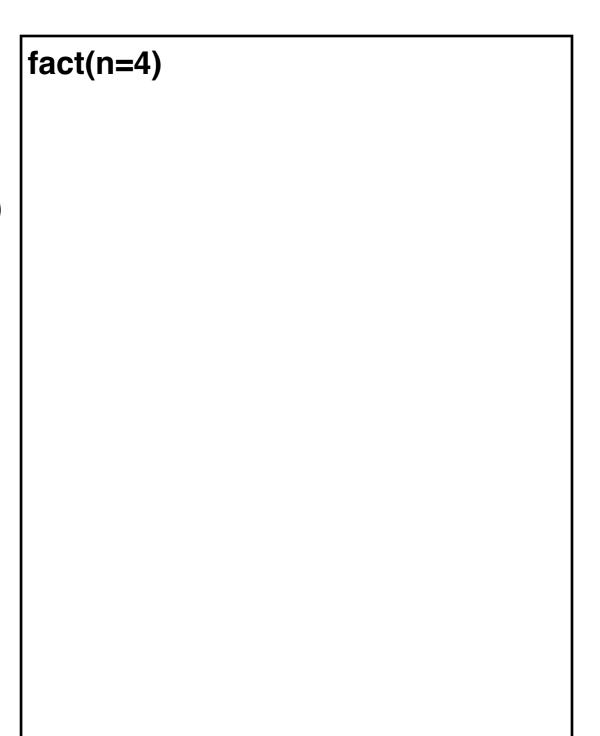
```
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```

Let's "run" it!

Tracing Factorial

```
somebody called fact (4)
```

```
def fact(n):
    if n == 1:
        return 1
    p = fact(n-1)
    return n * p
```



Note, this is **not** a stack frame! We're tracing code line-by-line. Boxes represent which invocation.

Tracing Factorial

```
def fact(n):
    if n == 1:
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    p = fact(n-1)
    return n * p
```

```
fact(n=4)
 if n == 1:
```

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def fact(n):
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```
fact(n=4)
 if n == 1:
 fact(n=3)
   if n == 1:
    fact(n=2)
      if n == 1:
      fact(n=1)
        if n == 1:
         return 1
```

```
def fact(n):
    if n == 1:
        return 1
p = fact(n-1)
return n * p
```

```
fact(n=4)
 if n == 1:
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   if n == 1:
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     if n == 1:
      fact(n=1)
       if n == 1:
         return 1
     p = 1
```

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def fact(n):
    if n == 1:
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```

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   if n == 1:
    fact(n=2)
     if n == 1:
      fact(n=1)
       if n == 1:
         return 1
      p = 1
      return 2
```

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def fact(n):
    if n == 1:
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fact(n=4)
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   if n == 1:
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     if n == 1:
      fact(n=1)
       if n == 1:
         return 1
      p = 1
      return 2
   p = 2
```

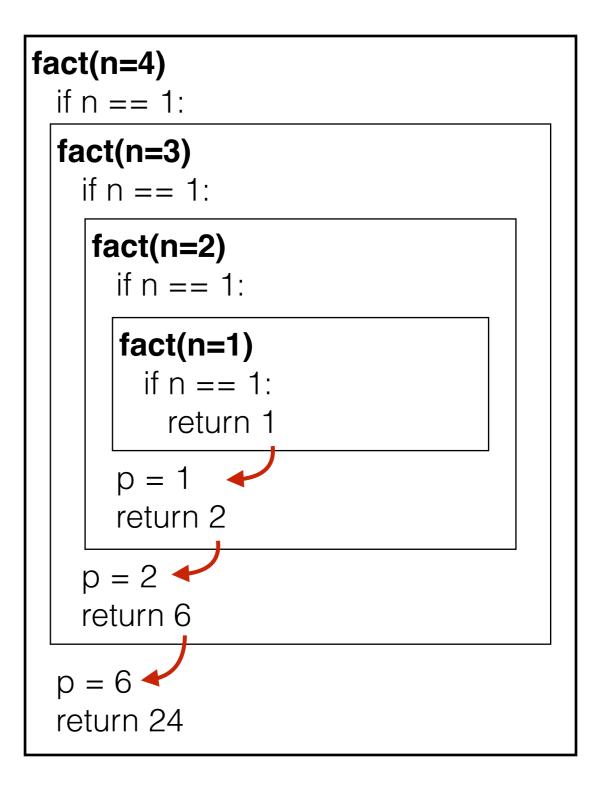
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     if n == 1:
      fact(n=1)
       if n == 1:
         return 1
     p = 1
      return 2
   p = 2 
   return 6
```

```
def fact(n):
    if n == 1:
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```

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fact(n=4)
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   if n == 1:
    fact(n=2)
      if n == 1:
      fact(n=1)
       if n == 1:
         return 1
      p = 1
      return 2
   p = 2 4
   return 6
 p = 6
```

```
def fact(n):
    if n == 1:
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```
def fact(n):
    if n == 1:
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```
fact(n=4)
 if n == 1:
 fact(n=3)
   if n == 1:
    fact(n=2)
      if n == 1:
      fact(n=1)
       if n == 1:
         return 1
      p = 1
      return 2
   p = 2 4
   return 6
 p = 6
 return 24
```

```
def fact(n):
    if n == 1:
        return 1
    p = fact(n-1)
    return n * p
```

How does Python keep all the variables separate?

```
fact(n=4)
 if n == 1:
  fact(n=3)
   if n = 1:
    fact(n=2)
      if n == 1:
      fact(n=1)
       if n = 1:
          return 1
      return 2
   return 6
 p \neq 6
  return 24
```

```
def fact(n):
    if n == 1:
        return 1
    p = fact(n-1)
    return n * p
```

How does Python keep all the variables separate?

frames to the rescue!

```
fac<mark>t(n=</mark>4)
  if n == 1:
  fac(t(n=3))
    if n = 1:
     fact(n=2)
       if n == 1:
       fact(n=1)
        if n == 1:
           return 1
       return 2
    return 6
  p \neq 6
  return 24
```

In recursion, each function invocation has its **own state**, but multiple invocations **share code**.

In recursion, each function invocation has its **own state**, but multiple invocations **share code**.

Variables for an invocation exist in a *frame*

frame: variables

In recursion, each function invocation has its **own state**, but multiple invocations **share code**.

Variables for an invocation exist in a *frame*

the frames are stored in the stack



In recursion, each function invocation has its **own state**, but multiple invocations **share code**.

Variables for an invocation exist in a *frame*

- the frames are stored in the stack
- one invocation is active at a time: its frame is on the top of stack



In recursion, each function invocation has its **own state**, but multiple invocations **share code**.

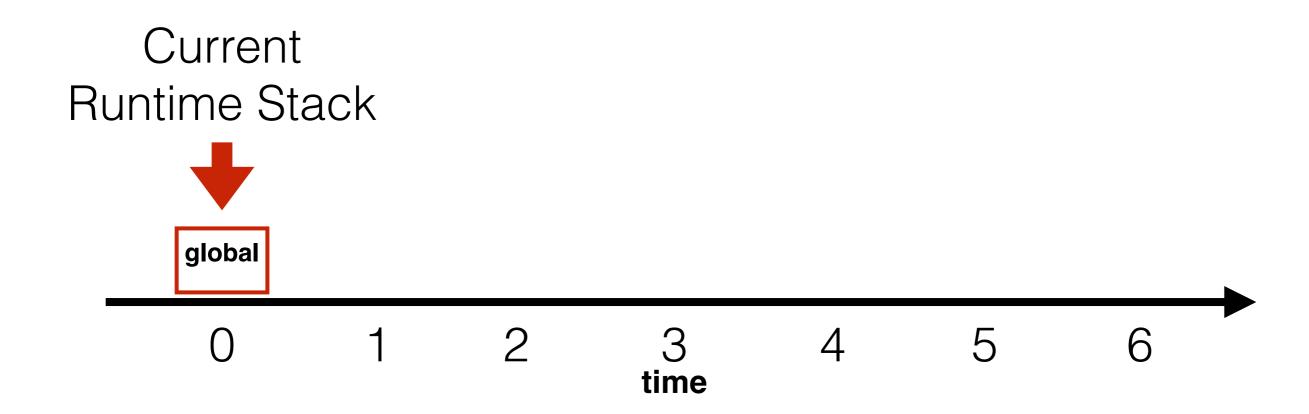
Variables for an invocation exist in a *frame*

- the frames are stored in the stack
- one invocation is active at a time: its frame is on the top of stack
- if a function calls itself, there will be multiple frames at the same time for the multiple invocations of the same function

frame: variables stack: stack: fact fact fact fact global

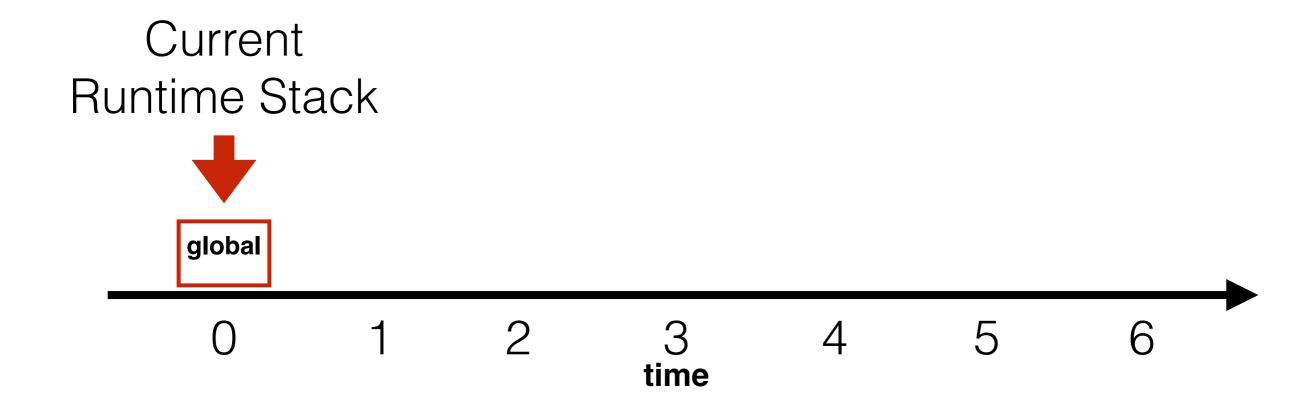
```
def fact(n):
    if n == 1:
        return 1
    p = fact(n-1)
    return n * p
```

TODO: grow down!!!!!!!!!

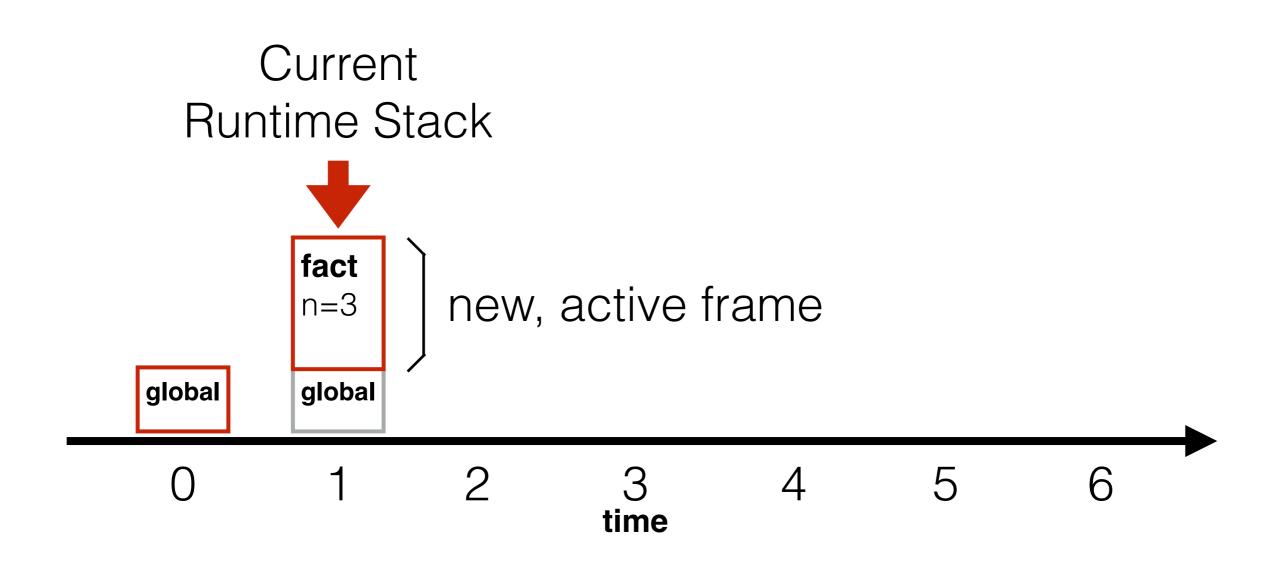


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def fact(n):
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    return n * p
```

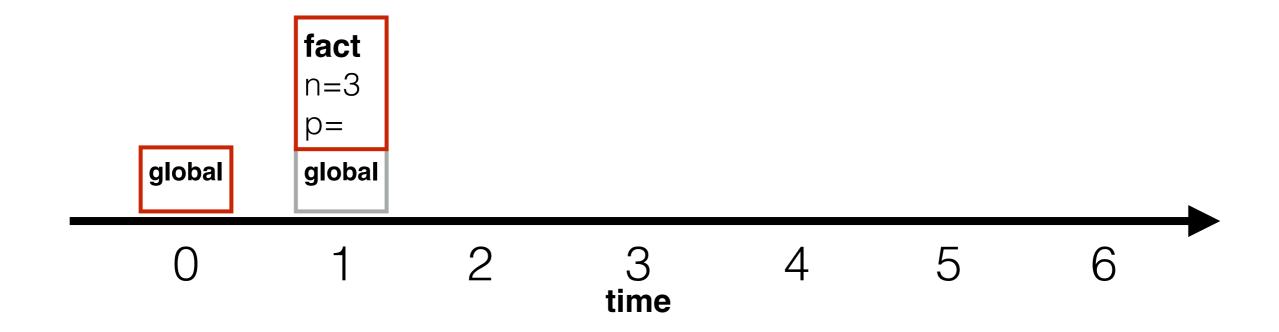
call fact(3)



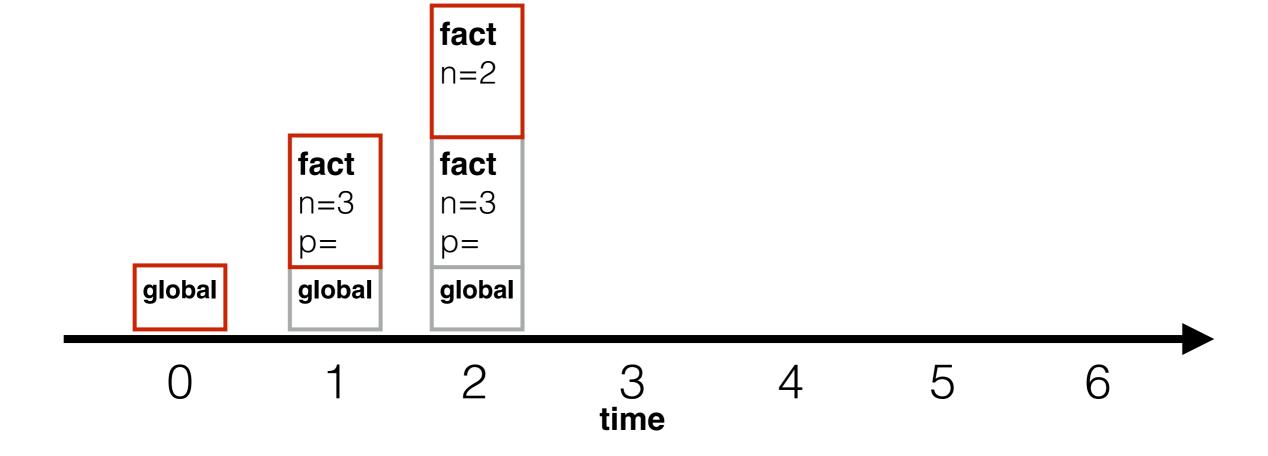
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    return n * p
```



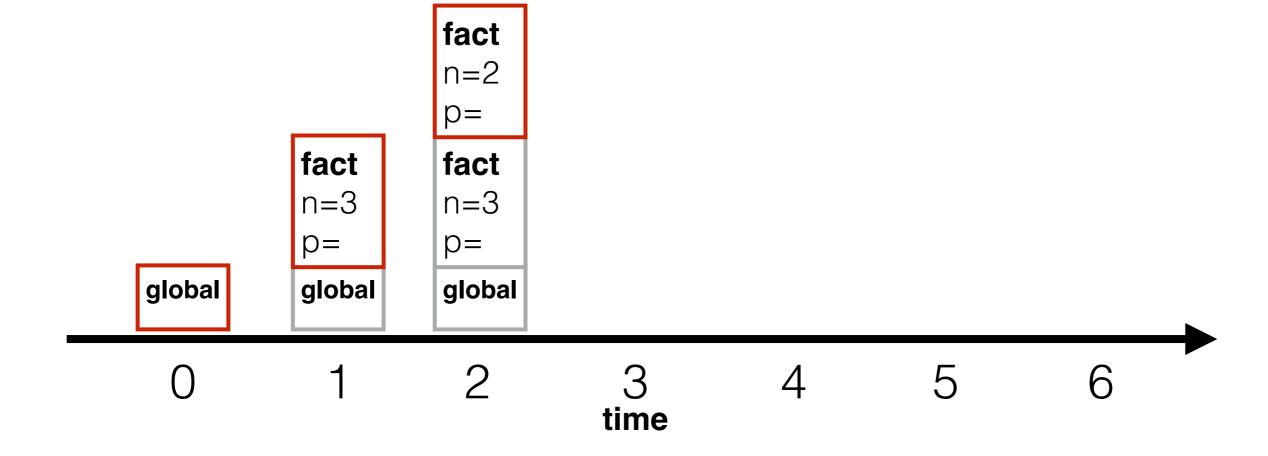
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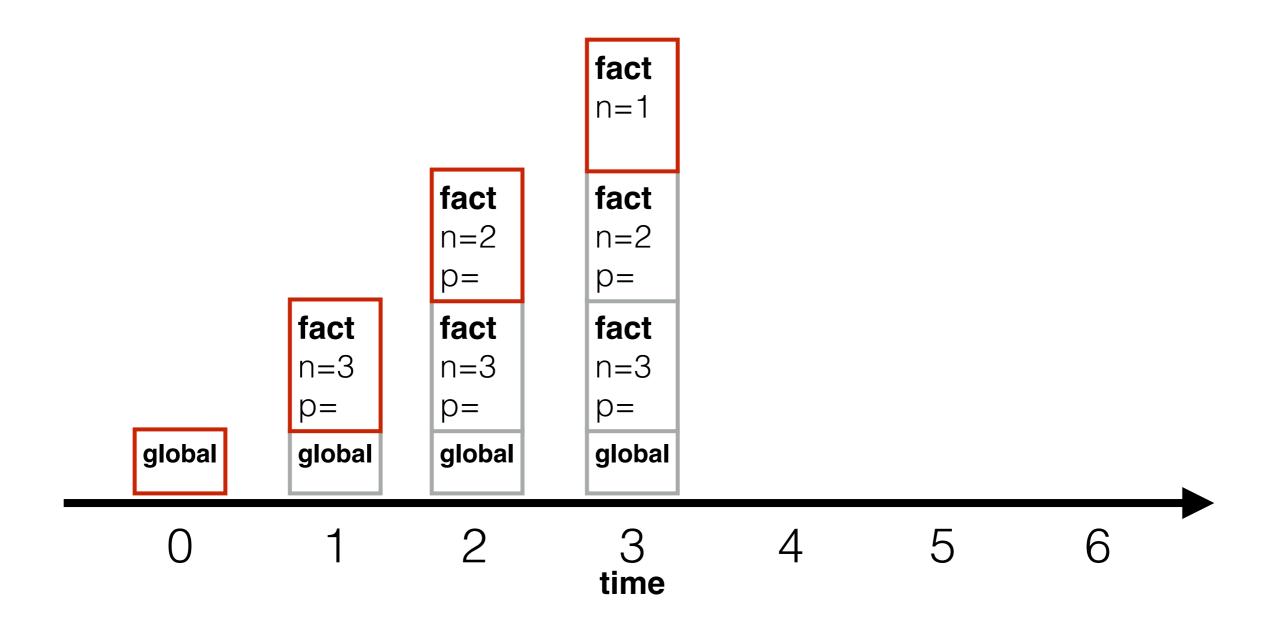
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    return n * p
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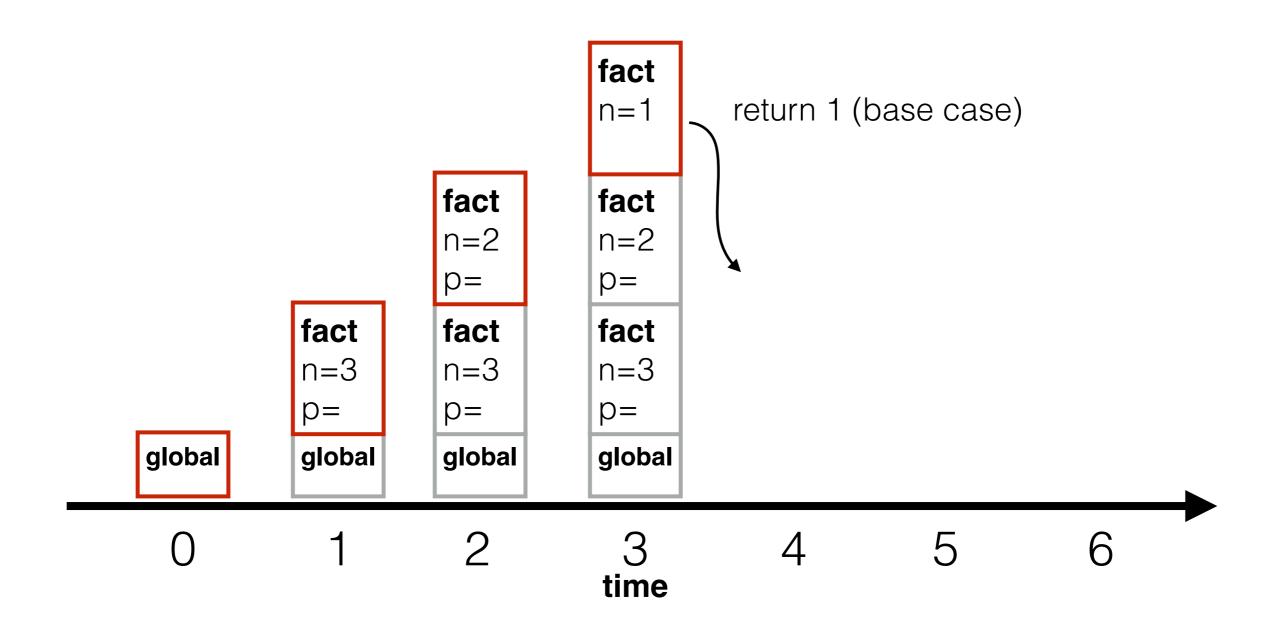
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    return n * p
```



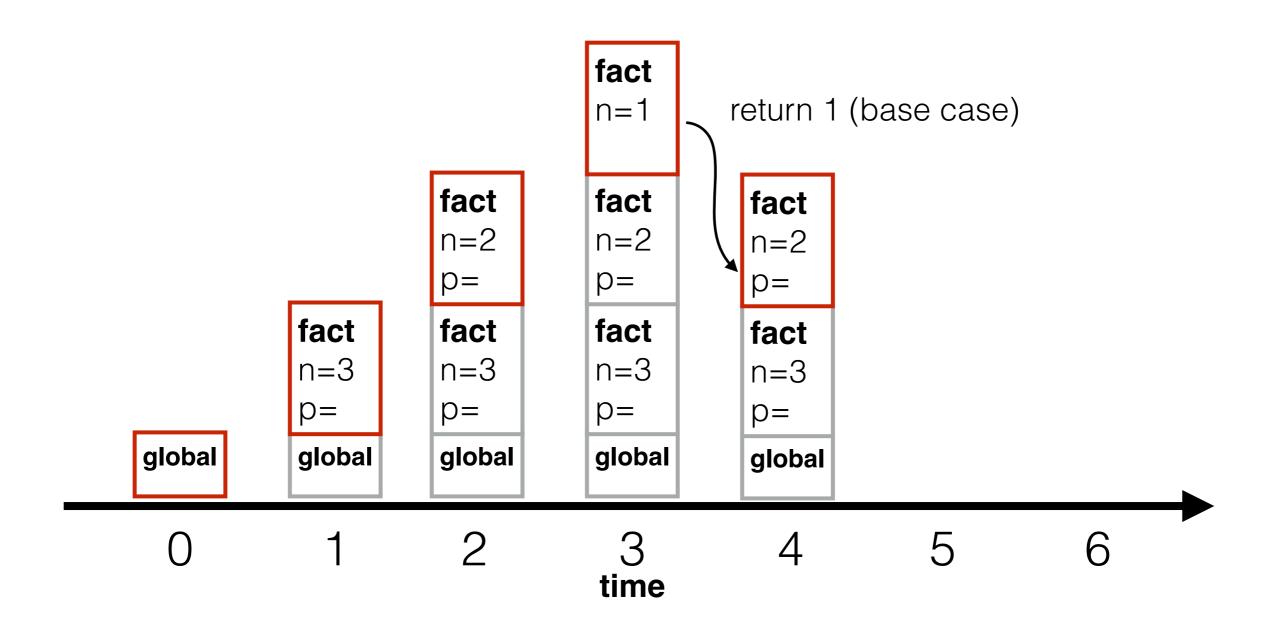
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    return n * p
```



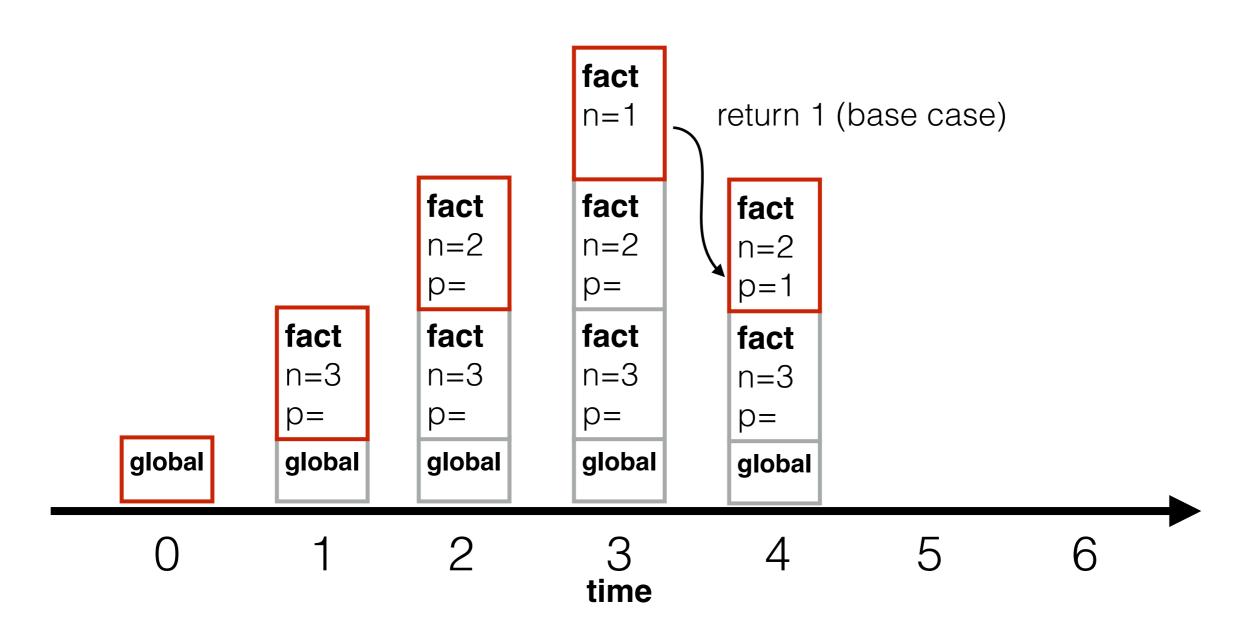
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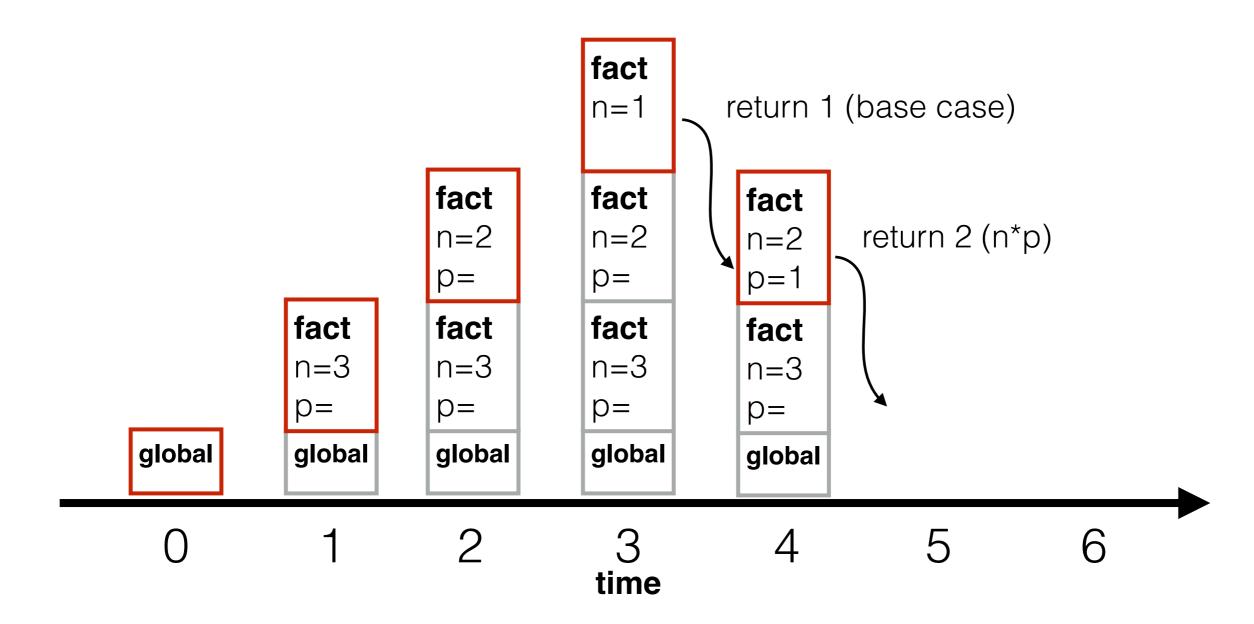
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```



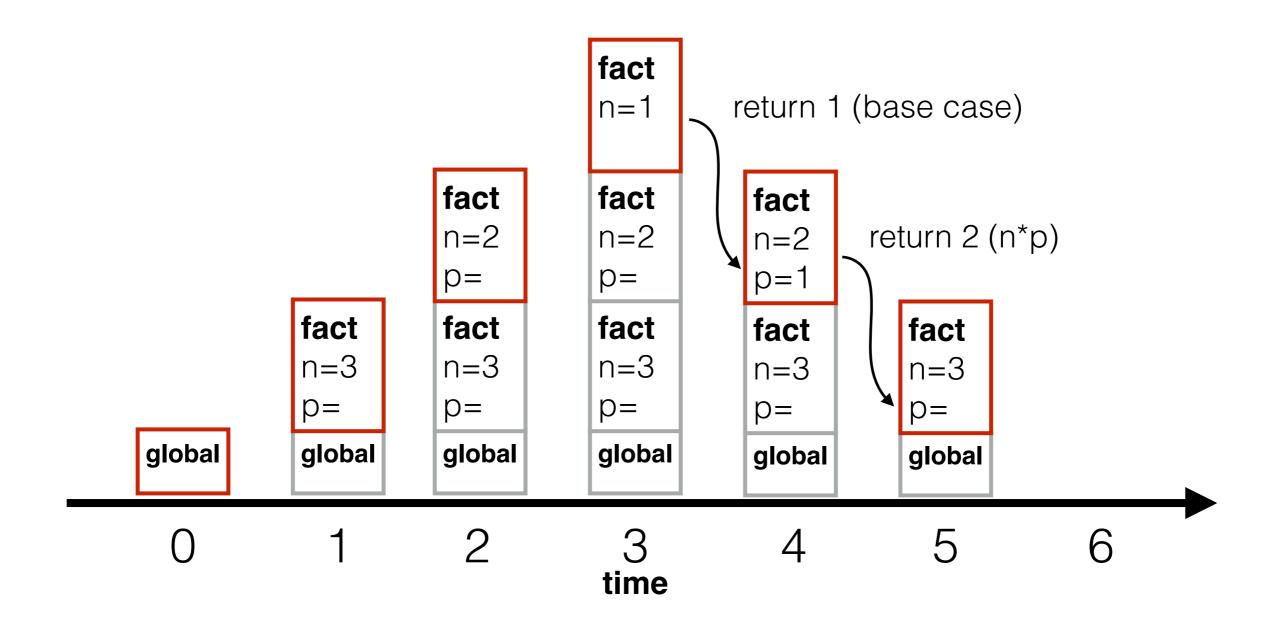
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```



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```

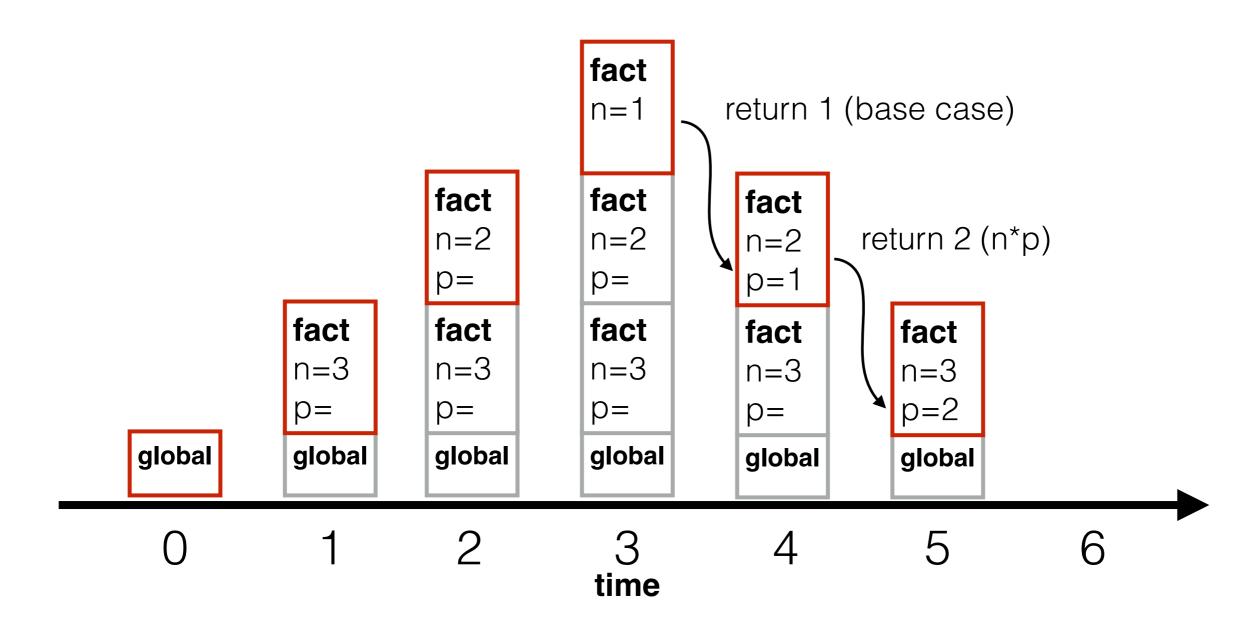


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```



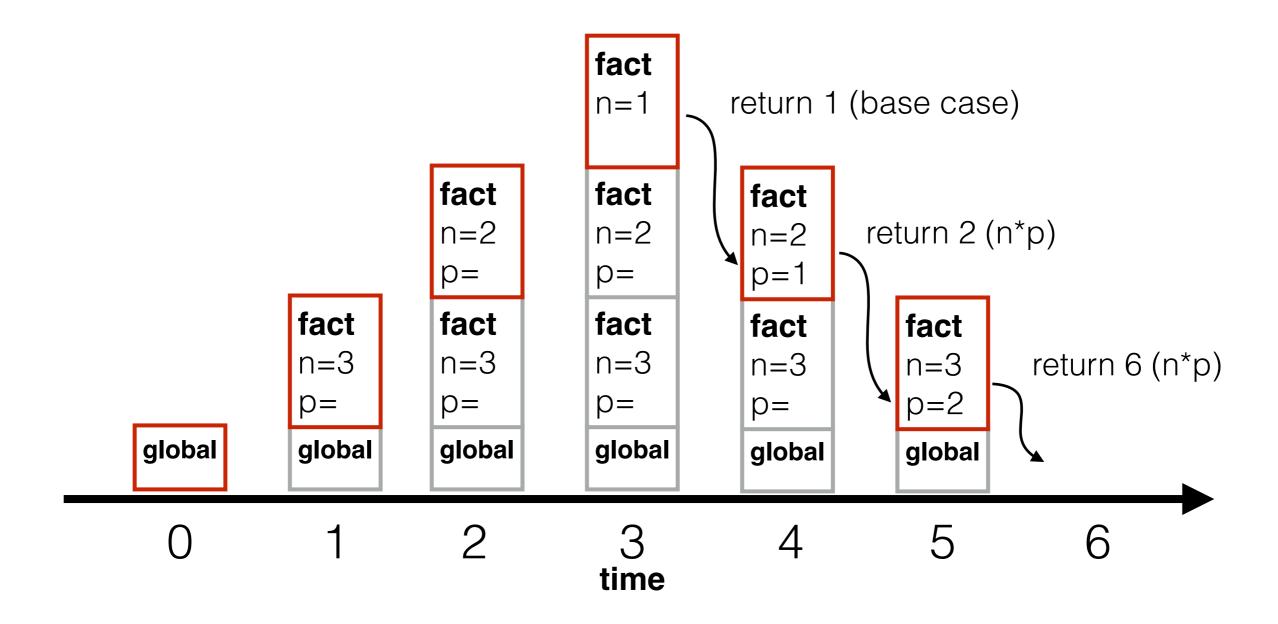
Deep Dive: Runtime Stack

```
def fact(n):
    if n == 1:
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    p = fact(n-1)
    return n * p
```



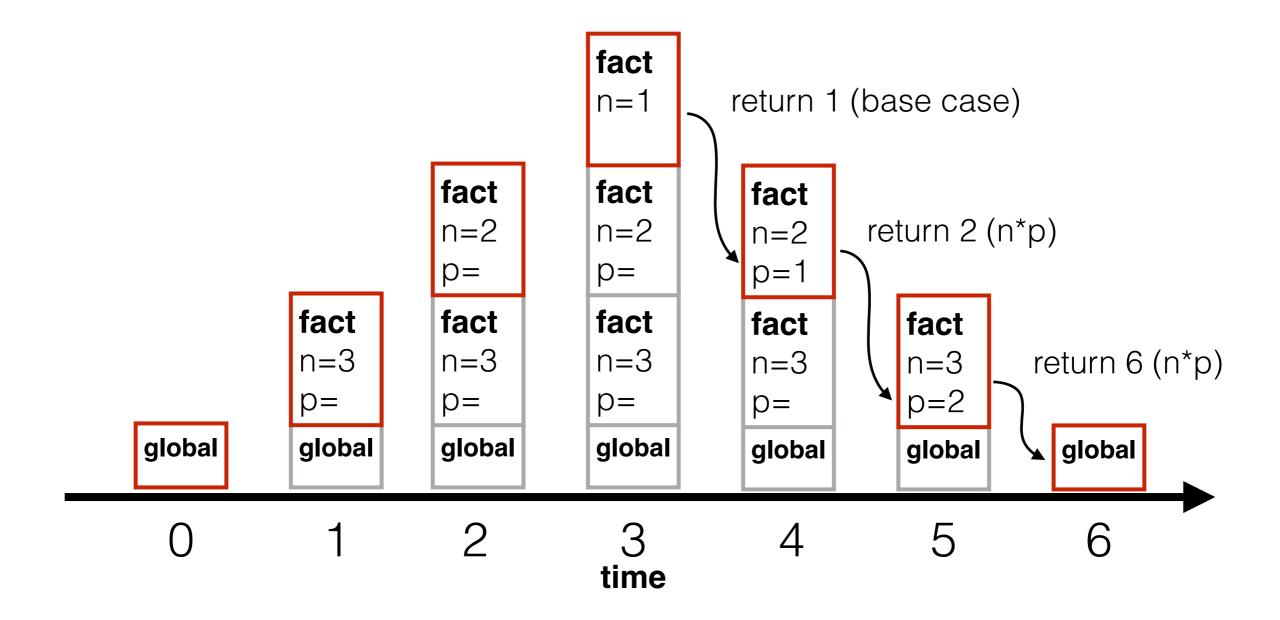
Deep Dive: Runtime Stack

```
def fact(n):
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    return n * p
```



Deep Dive: Runtime Stack

```
def fact(n):
    if n == 1:
        return 1
    p = fact(n-1)
    return n * p
```



What happens if:

•

lacktriangle

```
def fact(n):
    if n == 1:
        return 1
    p = fact(n-1)
    return n * p
```

What happens if:

• we forgot the "n == 1" check?

•

What happens if:

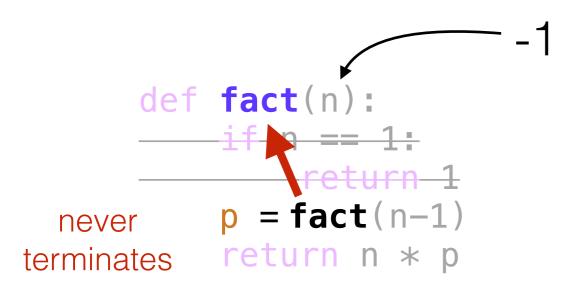
- we forgot the "n == 1" check?
- factorial is called with a negative number?

What happens if:

- we forgot the "n == 1" check?
- factorial is called with a negative number?

What happens if:

- we forgot the "n == 1" check?
- factorial is called with a negative number?



fact

n=2

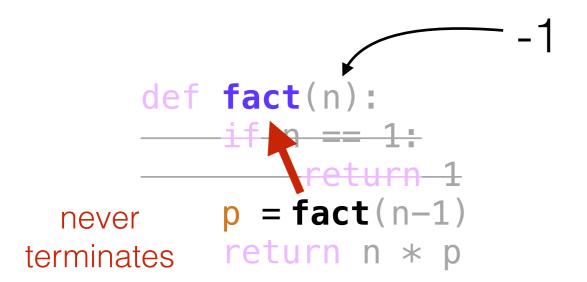
fact

n=3

global

What happens if:

- we forgot the "n == 1" check?
- factorial is called with a negative number?



fact

n = -1

fact

n=0

fact

n=1

fact

n=2

fact

n=3

global

What happens if:

- we forgot the "n == 1" check?
- factorial is called with a negative number?

_ _ _

fact

n = -2

fact

n = -1

fact

n=0

fact

n=1

fact

n=2

fact

n=3

global

Coding Demos

Demo 1: Pretty Print

Goal: format nested lists of bullet points

Input:

The recursive lists

Output:

Appropriately-tabbed items

Example:

Demo 2: Recursive List Search

Goal: does a given number exist in a recursive structure?

Input:

- A number
- A list of numbers and lists (which contain other numbers and lists)

Output:

• True if there's a list containing the number, else False

Example:

```
>>> contains(3, [1,2,[4,[[3],[8,9]],5,6]])
True
>>> contains(12, [1,2,[4,[[3],[8,9]],5,6]])
False
```

Conclusion: Review Learning Objectives

Learning Objectives: Recursive Information

What is a recursive definition/structure?

- Definition contains term
- Structure refers to others of same type
- Example: a dictionary contains dictionaries (which may contain...)



base case

Learning Objectives: Recursive Code

What is recursive code?

Function that sometimes itself (maybe indirectly)

Why write recursive code?

Real-world data/structures are recursive; intuitive for code to reflect data

Where do computers keep local variables for recursive calls?

- In a section of memory called a "frame"
- Only one function is **active** at a time, so keep frames in a stack

What happens to programs with infinite recursion?

- Calls keep pushing more frames
- Exhaust memory, throw StackOverflowError

Questions?

