[220 / 319] Randomness

Meena Syamkumar Andy Kuemmel

Announcements

- Follow-up courses
 - Direct follow up course: CS 320
 - Computer Sciences: CS 200, 300, 400, 537, 564, 640
- Office Hours
 - Last day of office hours: Friday April 30th.
 - Instructors will be available via Piazza over this weekend to answer questions about final exam.

Final exam

- Recommended prep
 - make sure you understand all the worksheet problems
 - review the readings, slides, lecture demo code
 - review everything you got wrong on the midterms
 - review the code you wrote for the projects
 - prepare a note sheet (despite open material!)
- Live review session on Friday April 30th
 - LEC 001 / LEC 002 / LEC 003 BBC sessions
 - LEC 004 office hours
 - attend any session

Course evaluations

- We value student feedback greatly
- Please bring a smile to your instructors' face by spending a few minutes to fill out evals ©
 - CS220 SEC 001
 - CS220 SEC 002
 - CS220 SEC 003
 - CS220 SEC 004
 - CS319 SEC 001
 - CS319 SEC 002
 - CS319 SEC 003

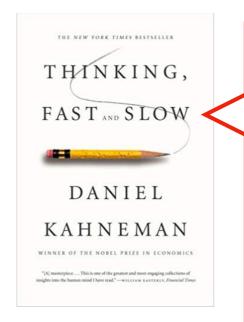
Which series was randomly generated? Which did I pick by hand?



2

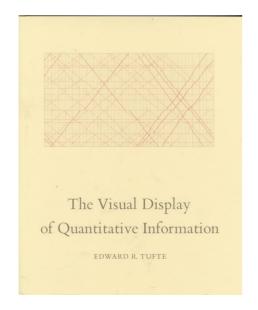


Recommended summer reading

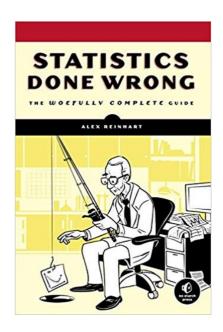


Thinking, Fast and Slo by Daniel Kahnemar

Misconceptions of chance. People expect that a sequence of events generated by a random process will represent the essential characteristics of that process even when the sequence is short. In considering tosses of a coin for heads or tails, for example, people regard the sequence H-T-H-T-T-H to be more likely than the sequence H-H-H-T-T-T, which does not appear random, and also more likely than the sequence H-H-H-H-T-H, which does not represent the fairness of the coin. 7 Thus,

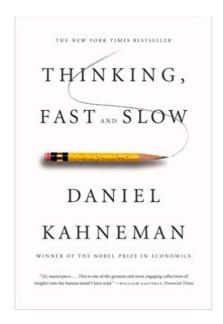




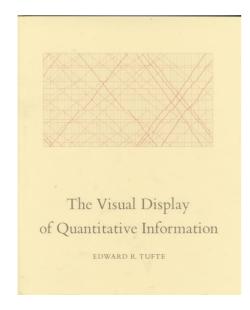


Statistics Done Wrong by Alex Reinhart

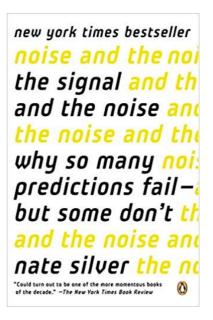
Recommended summer reading



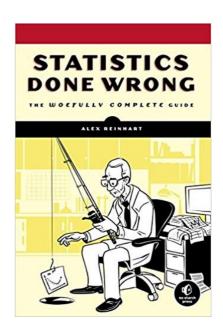
Thinking, Fast and Slow by Daniel Kahneman



The Visual Display of Quantitative Information by Edward R. Tufte

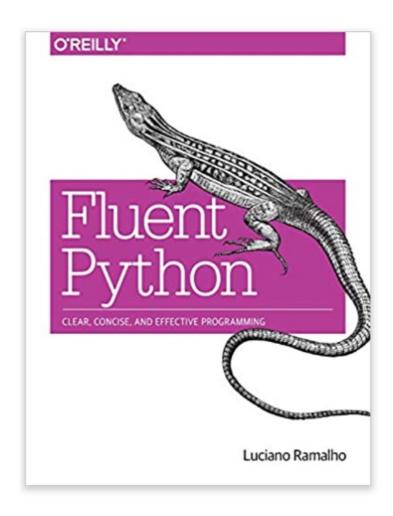


The Signal and the Noise by Nate Silver

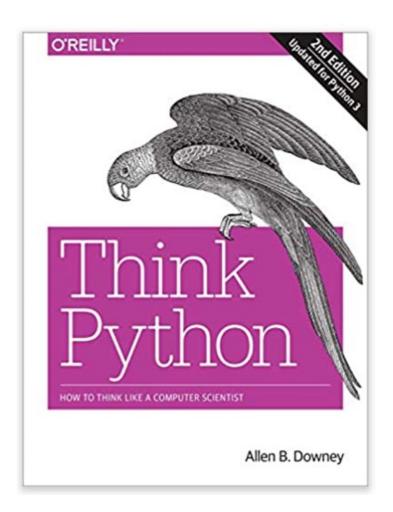


Statistics Done Wrong by Alex Reinhart

Recommended summer reading



Fluent Python: Clear, Concise, and Effective Programming by Luciano Ramalho



Think Python: How to Think Like a Computer Scientist by Allen B. Downey

Why Randomize?

Games

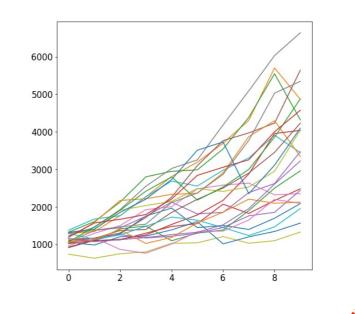




Security



Simulation



our focus

Outline

choice()

bugs and seeding

significance

histograms

normal()

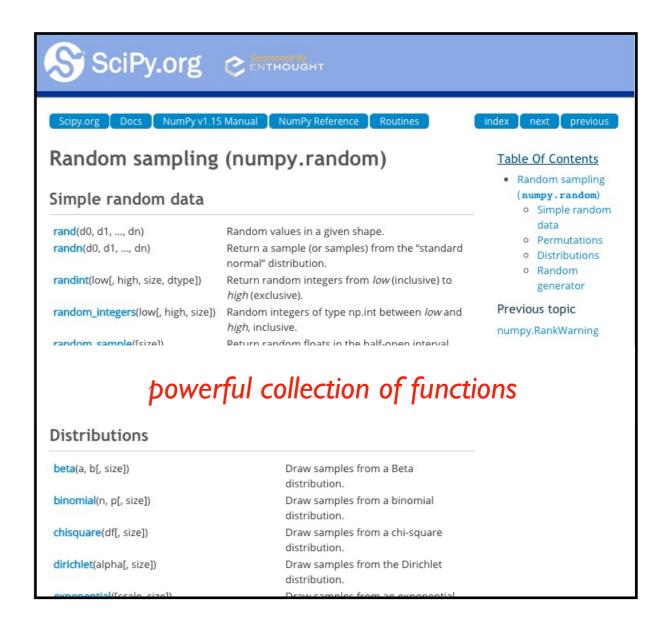
New Functions Today

numpy.random:

- powerful collection of functions
- choice

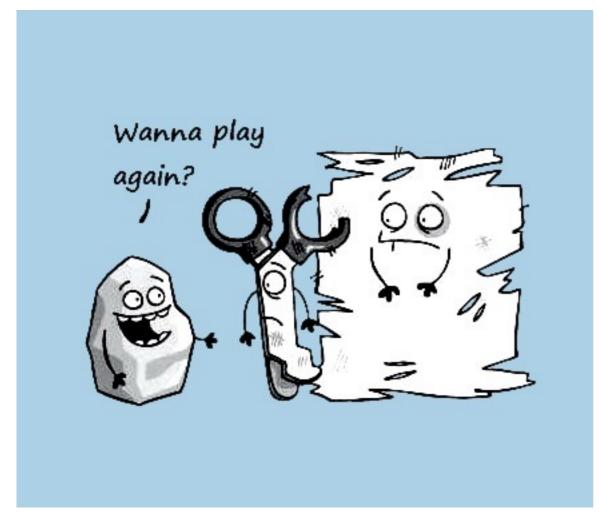
Series.plot.hist:

- similar to bar plot
- visualize spread of random results



```
from numpy.random import choice
result = choice([<choice1, choice2, ...])

list of things to
    randomly choose from</pre>
```



 $\underline{https://www.securifera.com/blog/2015/09/09/mmactf-2015-rock-paper-scissors-rps/paper-$

```
from numpy.random import choice
result = choice(["rock", "paper", "scissors"])
print(result)
result = choice(["rock", "paper", "scissors"])
print(result)
                                      Output:
                                      scissors
                                      rock
                 each time choice is
               called, a value is randomly
             selected (will vary run to run)
```

```
from numpy.random import choice
choice(["rock", "paper", "scissors"], size=5)
```

for simulation, we'll often want to compute many random results

```
from numpy.random import choice
choice(["rock", "paper", "scissors"], size=5)
array(['rock', 'scissors', 'paper', 'rock', 'paper'], dtype='<U8')
it's list-like</pre>
```

Random values and Pandas

```
from numpy.random import choice

# random Series
Series(choice(["rock", "paper", "scissors"], size=5))
```

```
0 rock
1 rock
2 scissors
3 paper
4 scissors
dtype: object
```

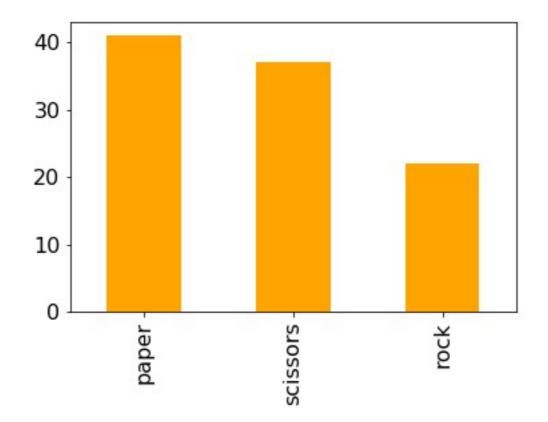
Random values and Pandas

	0	1
0	paper	rock
1	scissors	rock
2	rock	rock
3	scissors	paper
4	rock	scissors

Demo: exploring bias

```
choice(["rock", "paper", "scissors"])
```

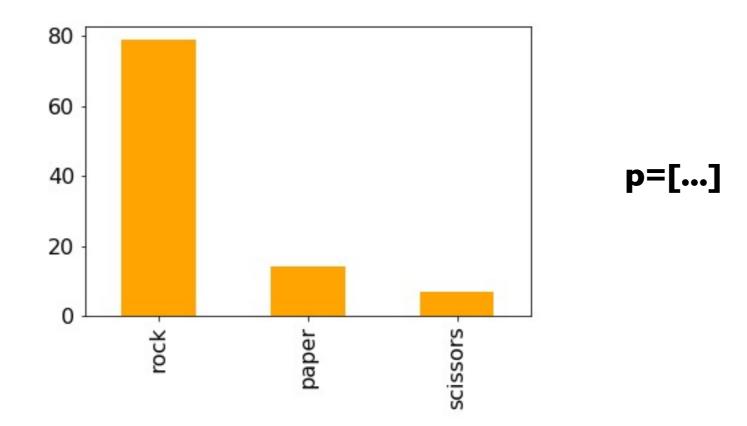
Question I: how can we make sure the randomization isn't biased?



Demo: exploring bias

Question I: how can we make sure the randomization isn't biased?

Question 2: how can we make it biased (if we want it to be)?



Random Strings vs. Random Ints

```
from numpy.random import choice, normal
# random string: rock, paper, or scissors
choice(["rock", "paper", "scissors"])
# random int: 0, 1, or 2
choice([0, 1, 2])
         same
# random int (approach 2): 0, 1, or 2
choice(3)
                random non-negative int
                 that is less than 3
```

Outline

choice()

bugs and seeding

significance

histograms

normal()

Example: change over time

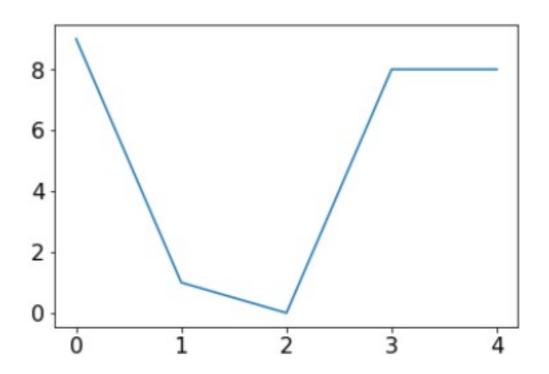
```
s = Series(choice(10, size=5))
                                         6
      6
 0
                                         5
                                         4
                                         3
                                         2
dtype: int64
s.plot.line()
                                               20
percents = []
for i in range(1, len(s)):
                                                0
    diff = 100 * (s[i] / s[i-1] - 1)
                                              -20
    percents.append(diff)
Series(percents).plot.line()
                                              -40
                                              -60
    what are we computing for diff?
                                                      0.5
                                                                      2.5
                                                 0.0
                                                          1.0
                                                             1.5
                                                                  2.0
                                                                          3.0
```

Example: change over time

```
s = Series(choice(10, size=5))

0     9
1     1
2     0
3     8
4     8
dtype: int64

s.plot.line()
```

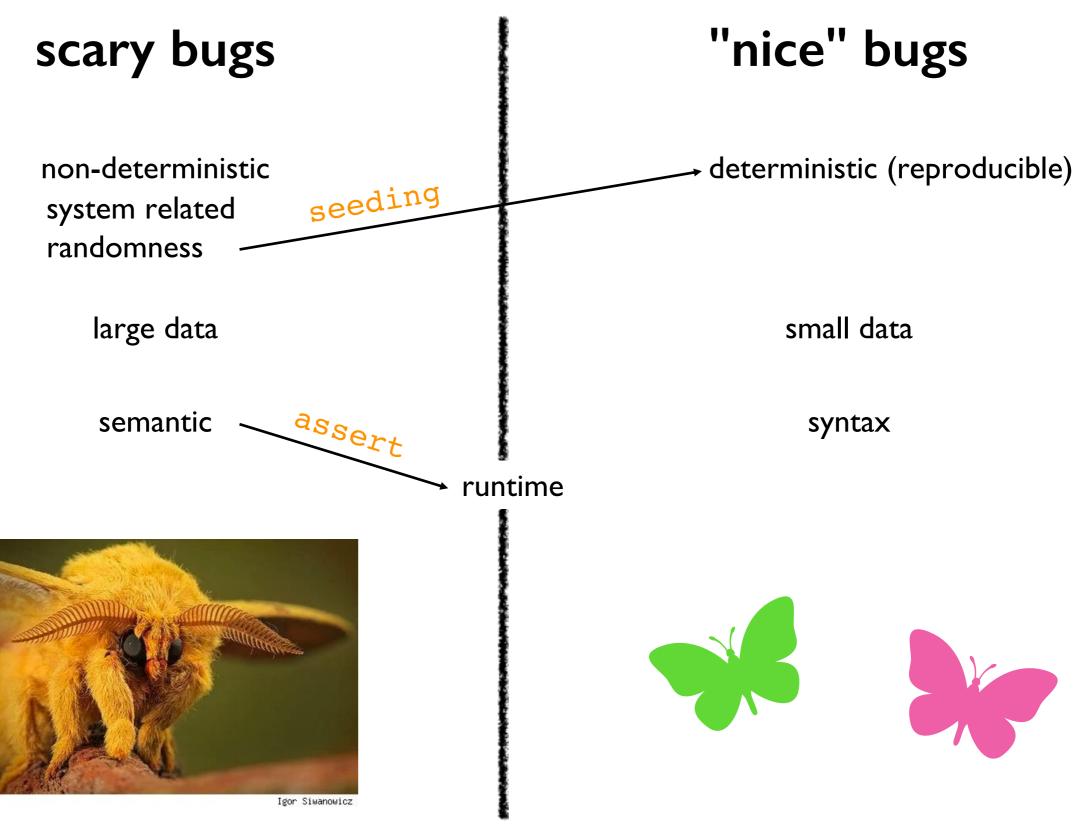


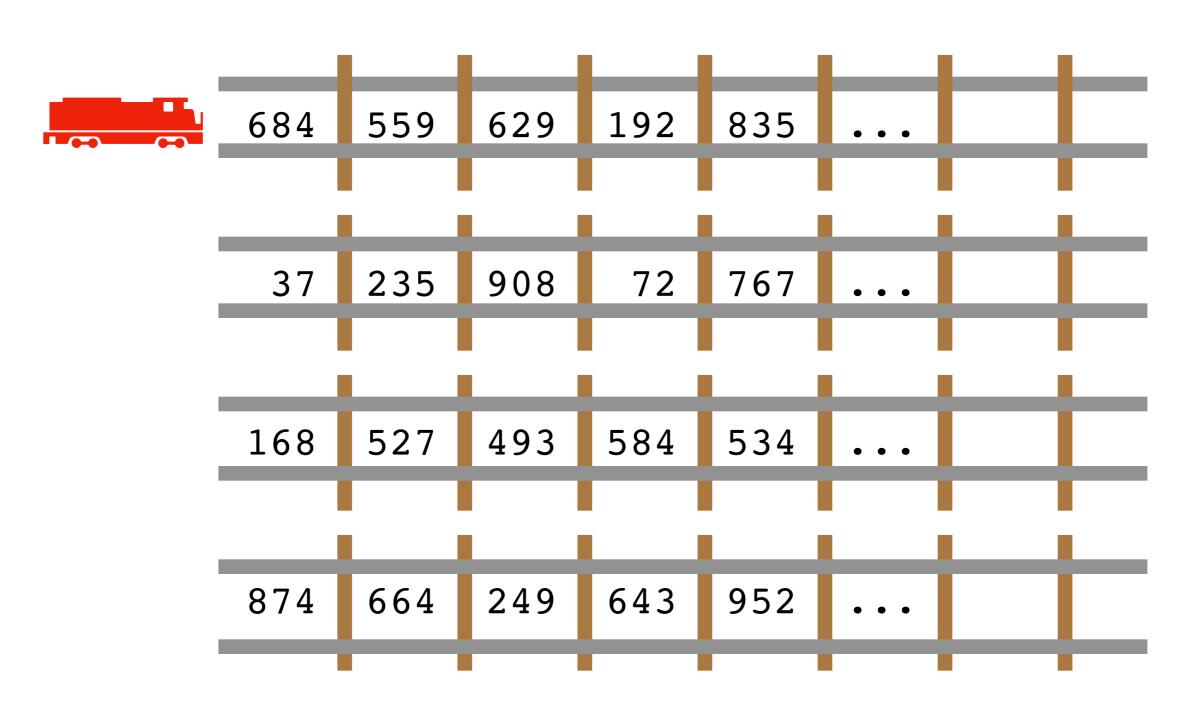
```
percents = []
for i in range(1, len(s)):
    diff = 100 * (s[i] / s[i-1] - 1)
    percents.append(diff)
Series(percents).plot.line()
/Library
```

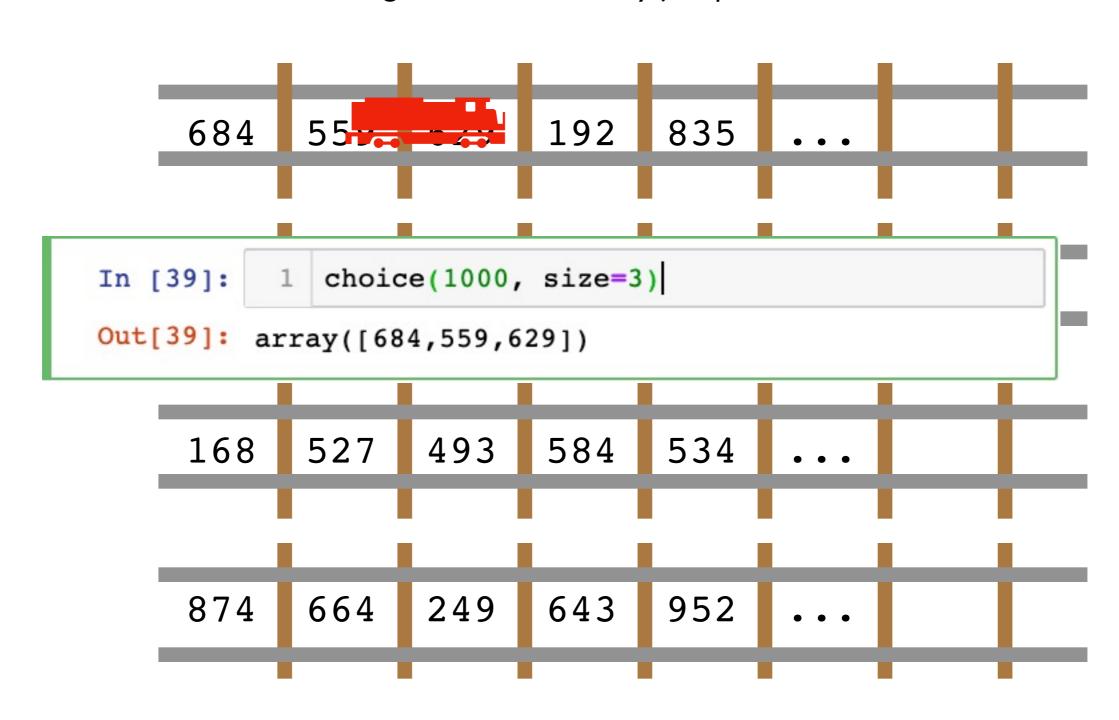
/Library/Frameworks/Python.framework/Versions/3.7/lib/ python3.7/site-packages/ipykernel_launcher.py:3: Runti meWarning: divide by zero encountered in long_scalars This is separate from the ipykernel package so we can avoid doing imports until

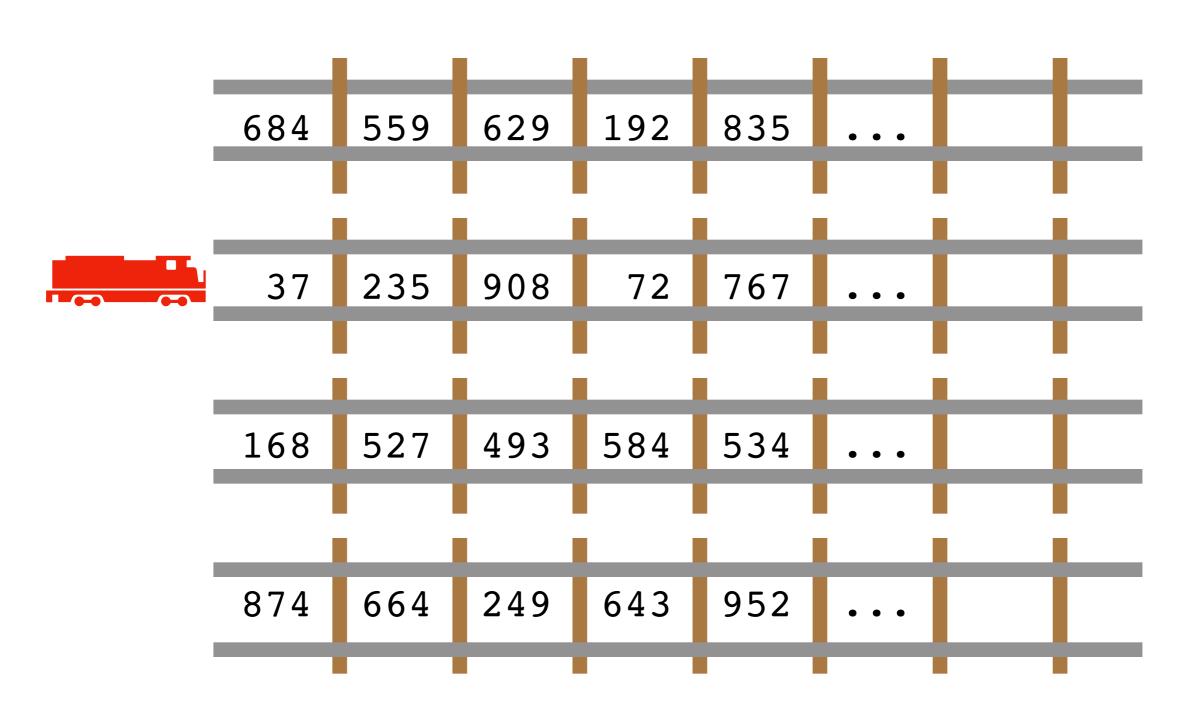
can you identify the bug in the code?

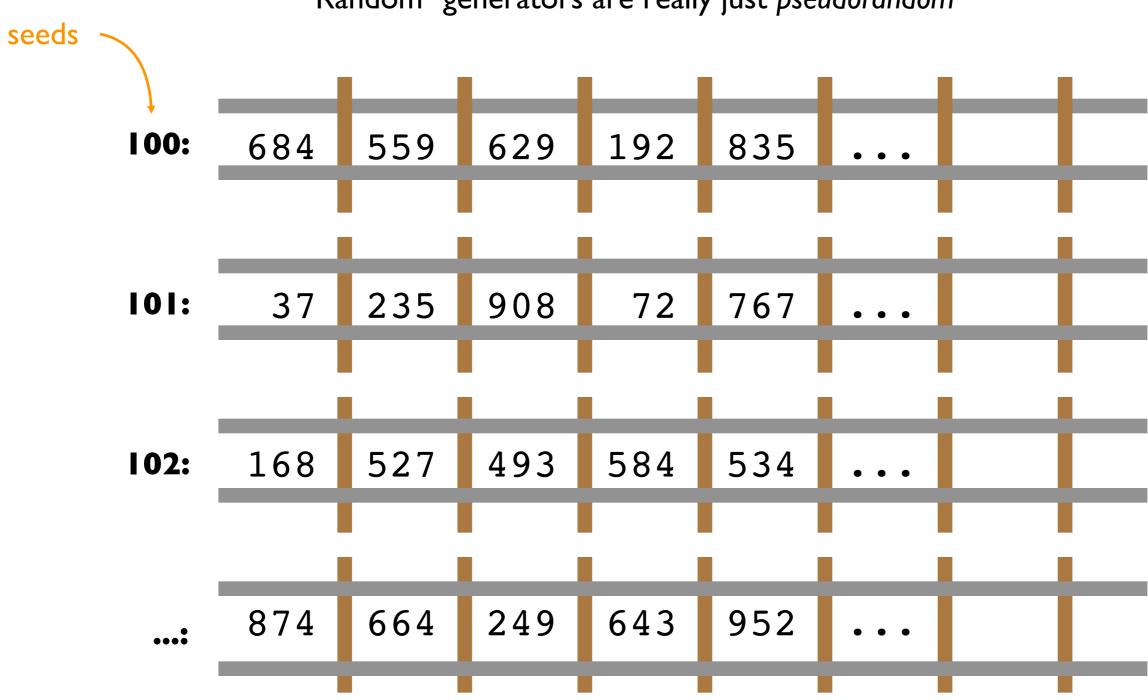
Not all bugs are equal!



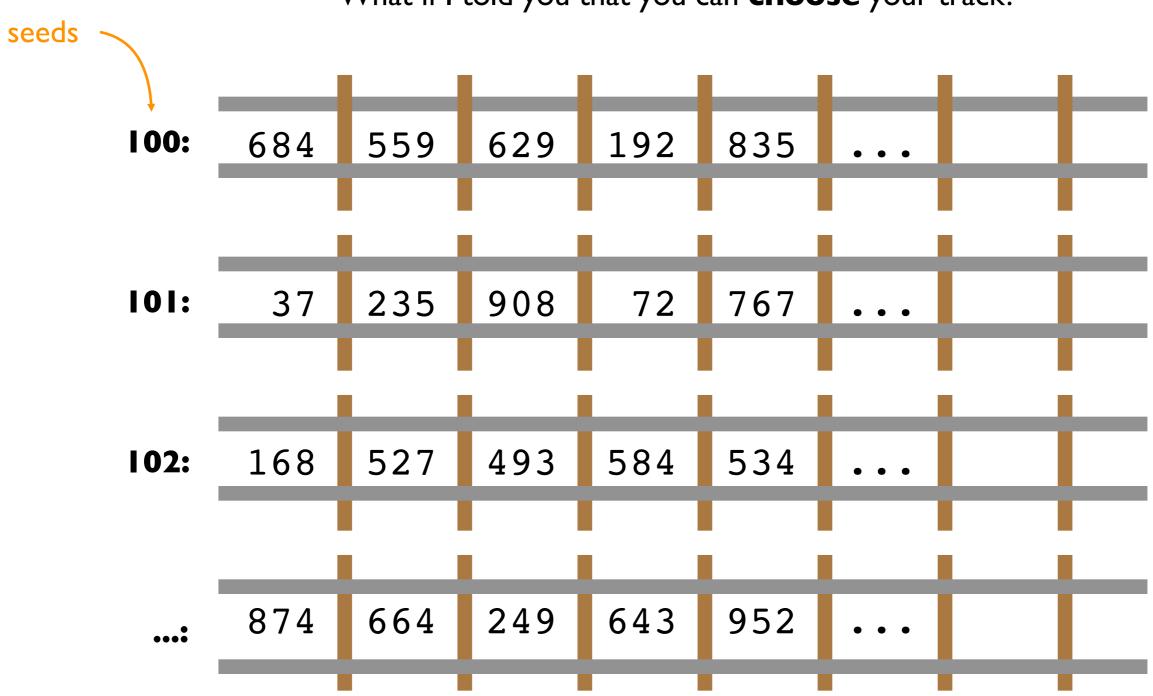








What if I told you that you can **choose** your track?



Seeding

What if I told you that you can **choose** your track?

```
In [2]:
        1 np.random.seed(220)
         2 choice(1000, size = 3)
Out[2]: array([883, 732, 15])
In [3]: 1 np.random.seed(220)
         2 choice(1000, size = 3)
Out[3]: array([883, 732, 15])
In [4]: 1 np.random.seed(220)
         2 choice(1000, size = 3)
Out[4]: array([883, 732, 15])
```

Seeding

Common approach for simulations:

- I. seed using current time
- 2. print seed
- 3. use the seed for reproducing bugs, as necessary

Outline

choice()

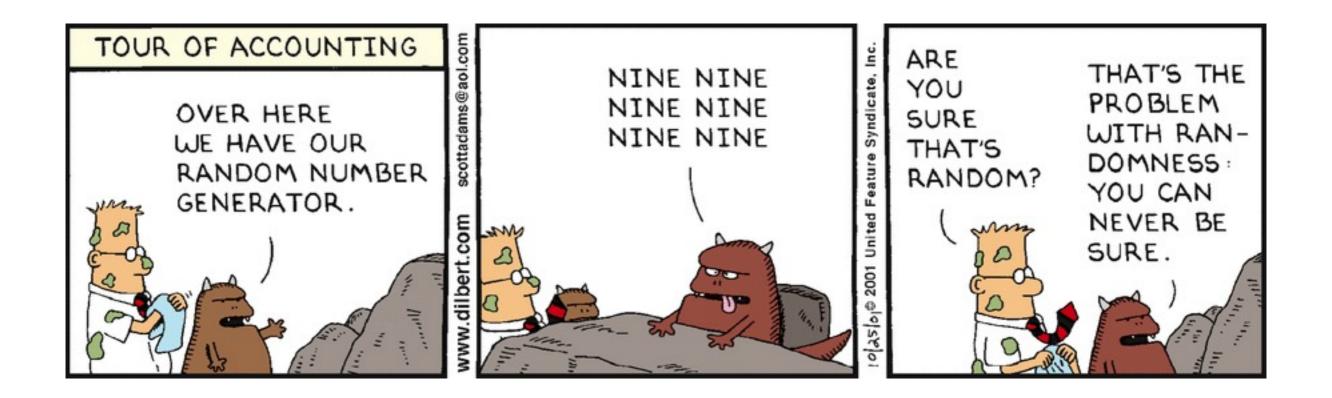
bugs and seeding

significance

histograms

normal()

In a noisy world, what is noteworthy?



Is this coin biased?



Call shenanigans?

a statistician might say we're trying to decide if the evidence that the coin isn't fair is statistically significant

whoever has the coin cheated (it's not 50/50 heads/tails)

Is this coin biased?



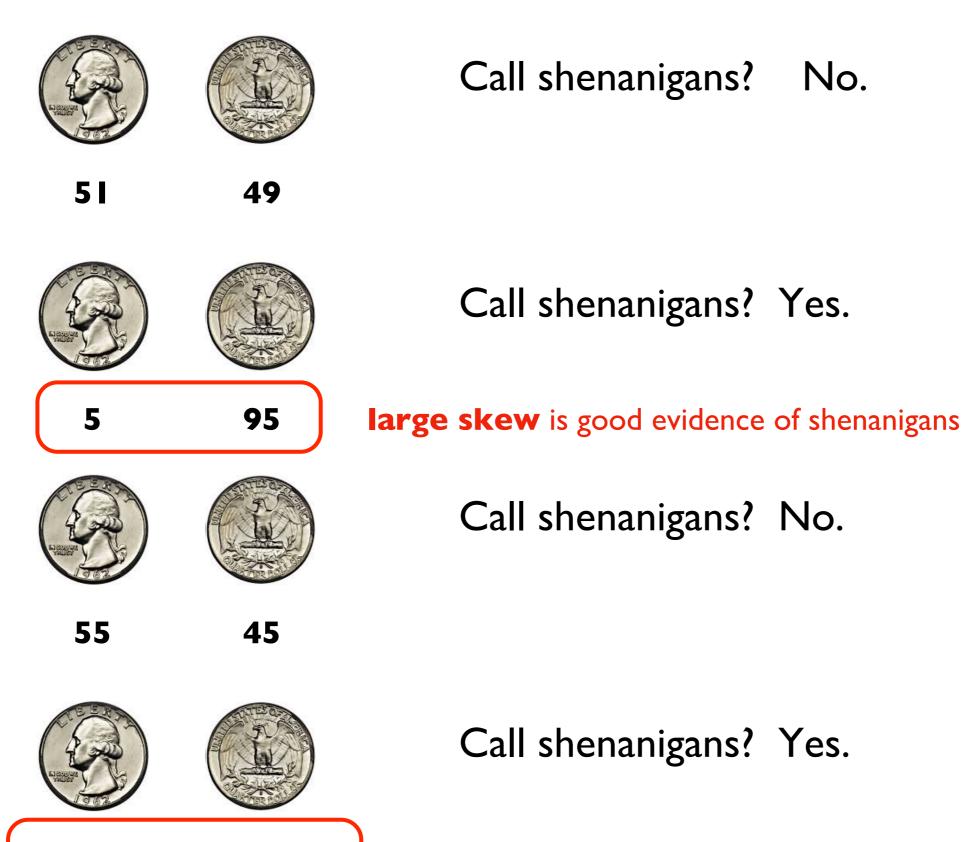
Call shenanigans? No.

Call shenanigans? Yes.

Note: there is a non-zero probability that a fair coin will do this, but the odds are slim

Is this coin biased?

55 million 45 million



small skew over large samples is good evidence

Demo: CoinSim



60

Call shenanigans?

we got 10 more heads than we expect on average how common is this?

Strategy: simulate a fair coin

- I. "flip" it 100 times using numpy.random.choice
- 2. count heads
- 3. repeat above 10K times

40

```
[50, 61, 51, 44, 39, 43, 51, 49, 49, 38, ...]

Il more

I2 less
```

Outline

choice()

bugs and seeding

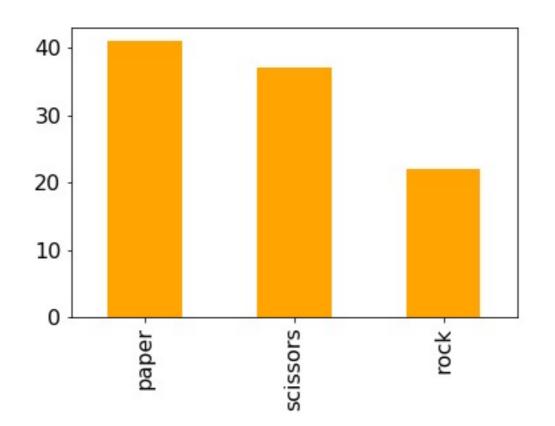
significance

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Frequencies across categories

bars are a good way to view frequencies across categories



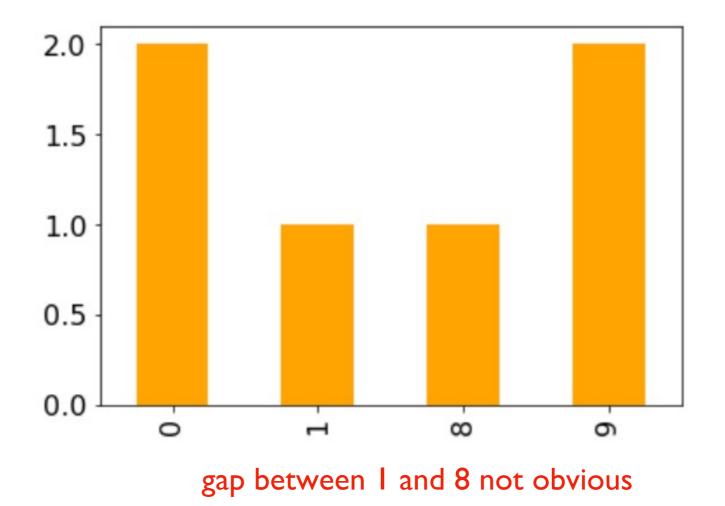
bars are a bad way to view frequencies across numbers

```
s = Series([0, 0, 1, 8, 9, 9])
s.value_counts().plot.bar(color="orange")
```



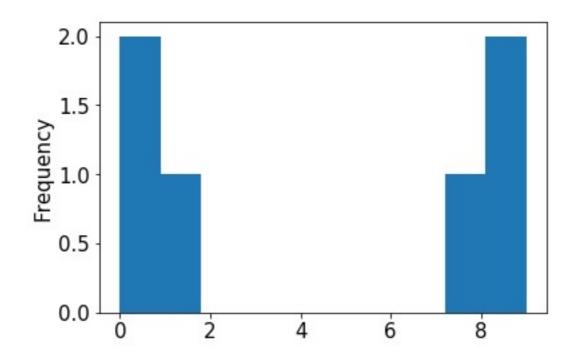
bars are a bad way to view frequencies across numbers

```
s = Series([0, 0, 1, 8, 9, 9])
s.value counts().sort index().plot.bar(color="orange")
```

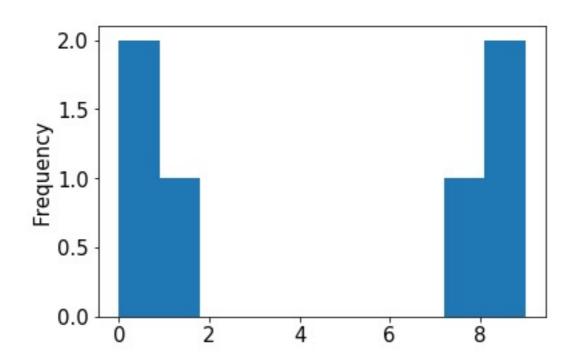


bars are a bad way to view frequencies across numbers

```
s = Series([0, 0, 1, 8, 9, 9])
s.value_counts().sort_index().plot.bar()
s.plot.hist()
```



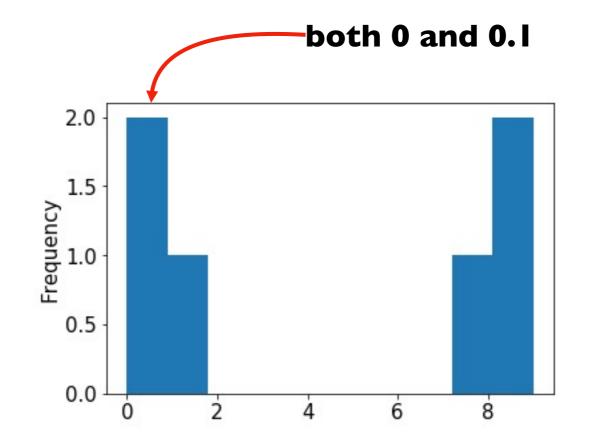
```
s = Series([0, 0, 1, 8, 9, 9])
s.value_counts().sort_index().plot.bar()
s.plot.hist()
```



this kind of plot is called a histogram

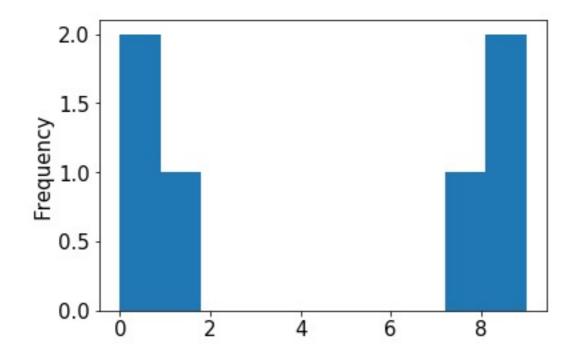
histograms are a good way to view frequencies across numbers

```
s = Series([0.1, 0, 1, 8, 9, 9.2])
s.value_counts().sort_index().plot.bar()
s.plot.hist()
```



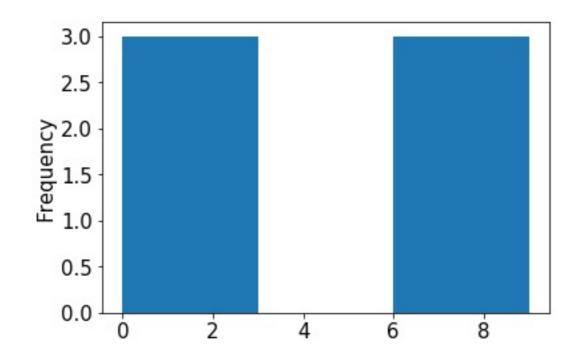
a histogram "bins" nearby numbers to create discrete bars

```
s = Series([0.1, 0, 1, 8, 9, 9.2])
s.value_counts().sort_index().plot.bar()
s.plot.hist(bins=10)
```



we can control the number of bins

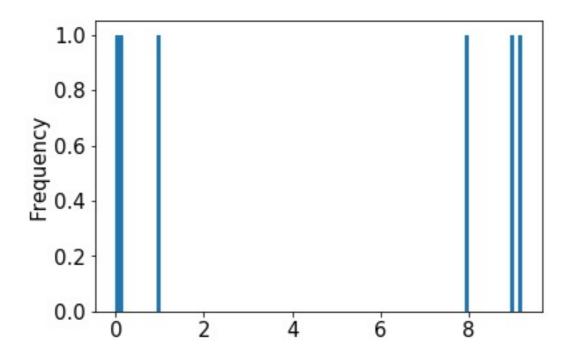
```
s = Series([0.1, 0, 1, 8, 9, 9.2])
s.value_counts().sort_index().plot.bar()
s.plot.hist(bins=3)
```



too few bins provides too little detail

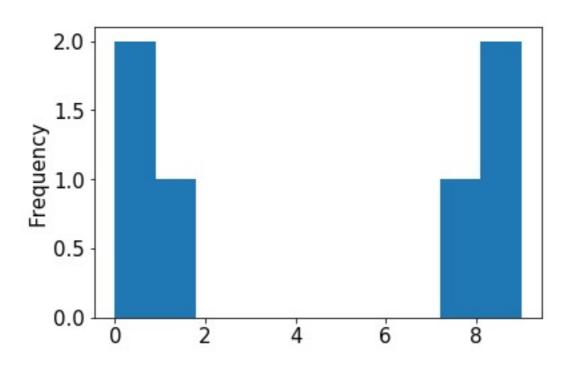
histograms are a good way to view frequencies across numbers

```
s = Series([0.1, 0, 1, 8, 9, 9.2])
s.value_counts().sort_index().plot.bar()
s.plot.hist(bins=100)
```



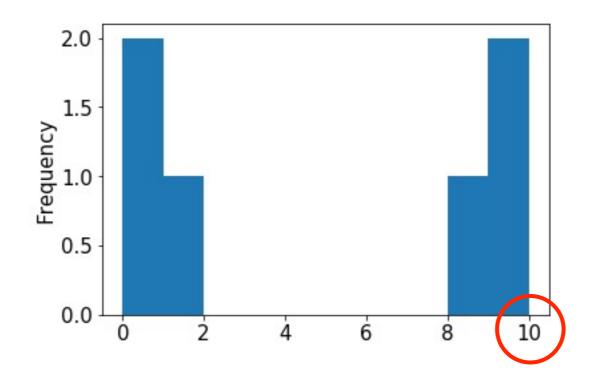
too many bins provides too much detail (equally bad)

```
s = Series([0.1, 0, 1, 8, 9, 9.2])
s.value_counts().sort_index().plot.bar()
s.plot.hist(bins=10)
```



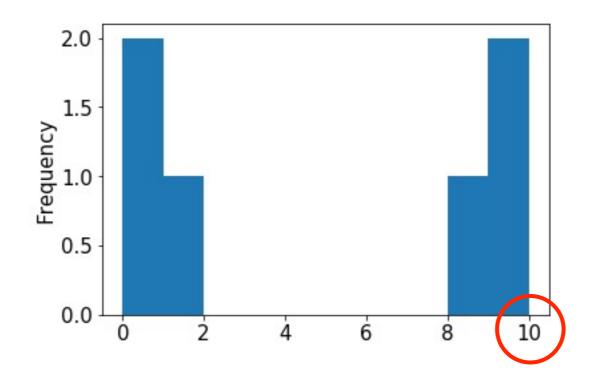
pandas chooses the default bin boundaries

```
s = Series([0.1, 0, 1, 8, 9, 9.2])
s.value_counts().sort_index().plot.bar()
s.plot.hist(bins=[0,1,2,3,4,5,6,7,8,9,10])
```



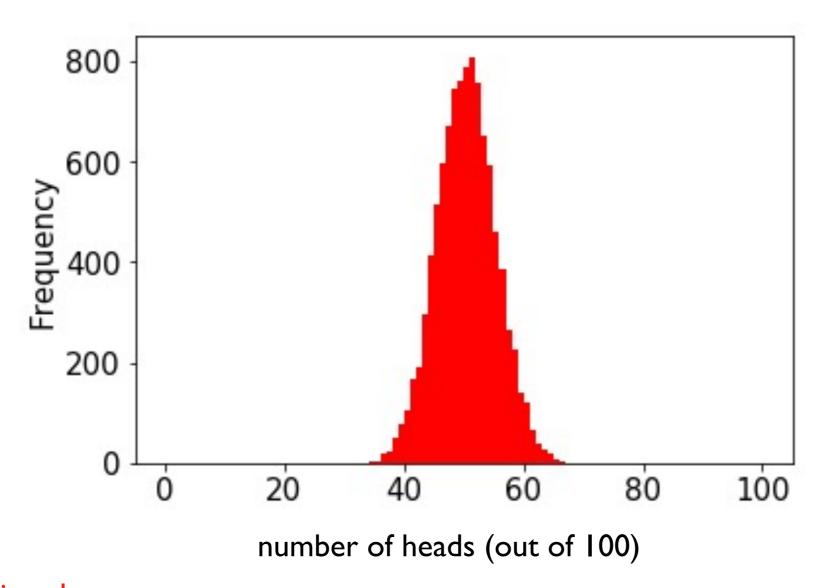
we can override the defaults

```
s = Series([0.1, 0, 1, 8, 9, 9.2])
s.value_counts().sort_index().plot.bar()
s.plot.hist(bins=range(11))
```



this is easily done with range

Demo: Visualize CoinSim Results



numpy can directly generate random numbers fitting a normal distribution

this shape resembles what we often call a normal distribution or a "bell curve"

in general, if we take large samples enough times, the sample averages will look like this (we won't discuss exceptions here)

Outline

choice()

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normal()

normal

```
from numpy.random import choice, normal
import numpy as np
for i in range(10):
    print(normal())
                                    Output:
                                     -0.18638553993371157
                                     0.02888452916769247
             average is 0 (over many calls)
                                     1.2474561113726423
                                     -0.5388224399358179
             numbers closer to 0 more likely
                                     -0.45143322136388525
                      -x just as likely as x
                                     -1.4001861112018241
                                     0.28119371511868047
                                     0.2608861898556597
```

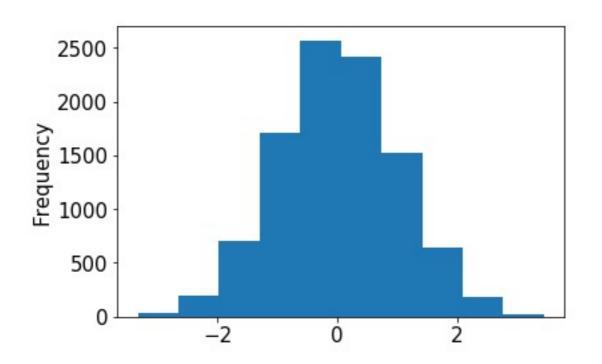
-0.19246288728955144

0.2979572961710292

normal

```
from numpy.random import choice, normal
import numpy as np

s = Series(normal(size=10000))
s.plot.hist()
```



normal

```
from numpy.random import choice, normal
import numpy as np

s = Series(normal(size=10000))

s.plot.hist(bins=100)
```

