```
In [1]: import pandas as pd
    import numpy as np
    import seaborn as sns
    import matplotlib.pyplot as plt
    import scipy.stats as stats
    %matplotlib inline
    #import statsmodels.api as sm
    #import statsmodels.stats.api as sms
    #from statsmodels.stats.proportion import proportion_confint
    #import pylab
    #import warnings
    #warnings.simplefilter(action='ignore', category=FutureWarning)

In [96]: data_1 = pd.read_csv('hcmv-263hxkx-lqhtfgz.txt')

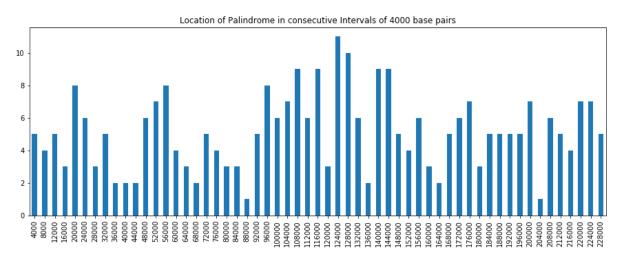
In [3]: # from original data set, n = 296 (Palindromes), N = 229354 (Base pairs)
    n, N = 296, 229354
```

In [4]: # Generate three uniformed distributed
 samples = [pd.Series(np.random.uniform(0,N,n)).sort_values() for i in ra
 nge(3)]

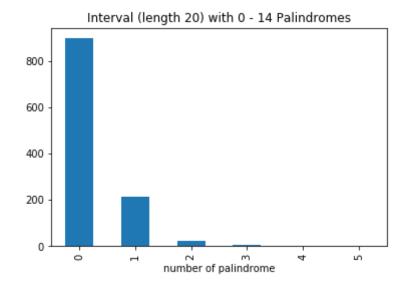
```
In [ ]:
```

```
In [ ]:
```

In [5]: pd.cut(samples[0], range(0, N+1, 4000)).apply(lambda x: x.right).value_c
 ounts().sort_index()\
 .plot(kind = 'bar',figsize=(15,5))
 plt.title('Location of Palindrome in consecutive Intervals of 4000 base
 pairs')



Out[15]: Text(0.5,1,'Interval (length 20) with 0 - 14 Palindromes')

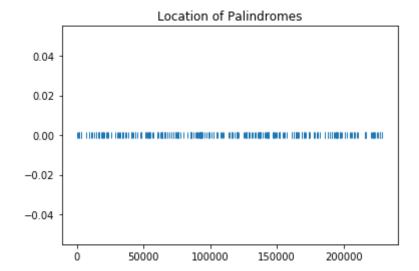


In []:

Random Scatter

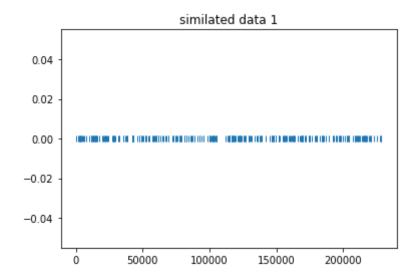
```
In [5]: #'Location of Palindromes'
   plt.plot(data_1.location, np.zeros_like(data_1.location) + 0, '|')
   plt.title('Location of Palindromes')
```

Out[5]: Text(0.5,1,'Location of Palindromes')



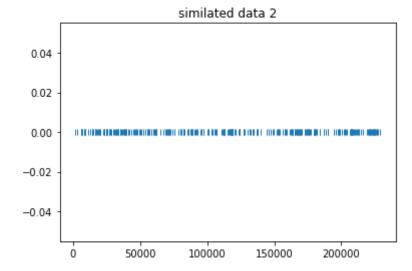
```
In [6]: # Location of three simulated samples
#for i in samples:
    plt.plot(samples[0], np.zeros_like(samples[0]) + 0, '|')
    plt.title('similated data 1')
```

Out[6]: Text(0.5,1,'similated data 1')



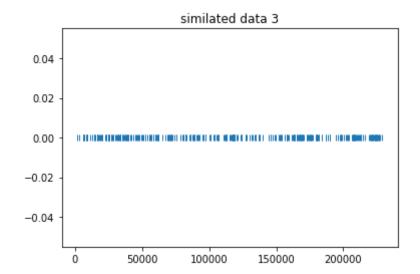
```
In [7]: plt.plot(samples[1], np.zeros_like(samples[1]) + 0, '|')
    plt.title('similated data 2')
```

Out[7]: Text(0.5,1,'similated data 2')

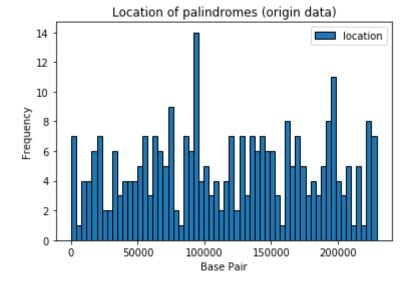


```
In [8]: plt.plot(samples[1], np.zeros_like(samples[2]) + 0, '|')
    plt.title('similated data 3')
```

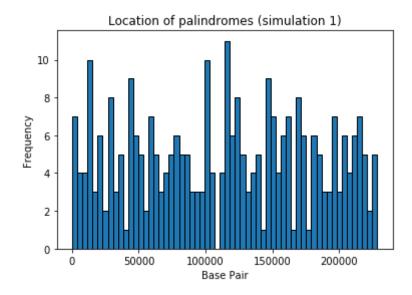
Out[8]: Text(0.5,1,'similated data 3')



Out[9]: Text(0.5,0,'Base Pair')

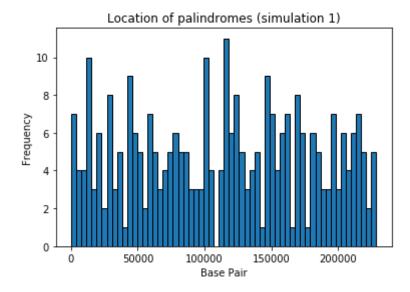


Out[10]: Text(0.5,0,'Base Pair')



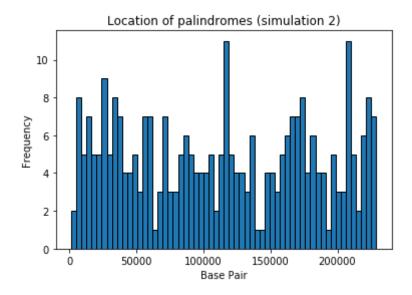
```
In [11]: pd.Series(samples[0]).plot(kind= 'hist', bins = 60, edgecolor = 'k',titl
    e = ('Location of palindromes (simulation 1)'))
    plt.xlabel("Base Pair")
```

Out[11]: Text(0.5,0,'Base Pair')



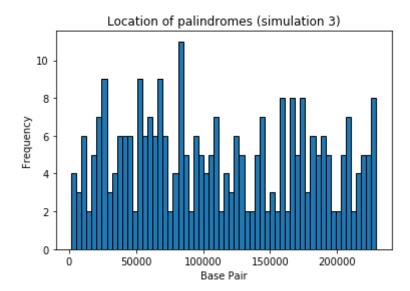
```
In [12]: pd.Series(samples[1]).plot(kind= 'hist', bins = 60, edgecolor = 'k',titl
    e = ('Location of palindromes (simulation 2)'))
    plt.xlabel("Base Pair")
```

Out[12]: Text(0.5,0,'Base Pair')



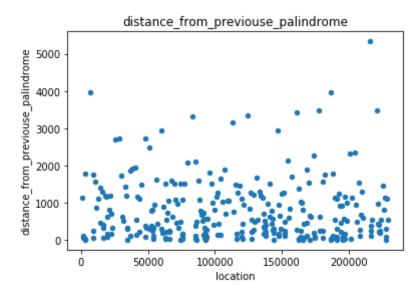
```
In [13]: pd.Series(samples[2]).plot(kind= 'hist', bins = 60, edgecolor = 'k',titl
    e = ('Location of palindromes (simulation 3)'))
    plt.xlabel("Base Pair")
```

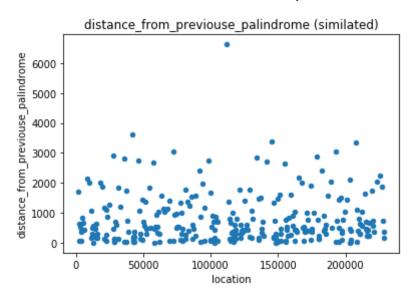
Out[13]: Text(0.5,0,'Base Pair')

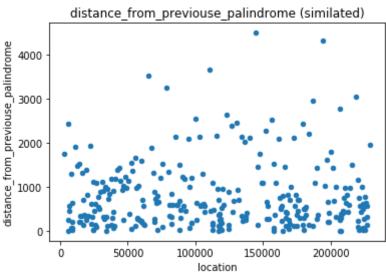


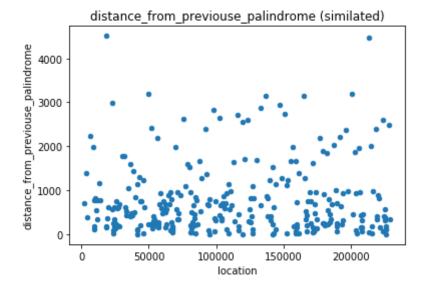
/Users/syeehyn/anaconda3/envs/UCSD/lib/python3.6/site-packages/ipykerne l_launcher.py:2: FutureWarning: set_value is deprecated and will be rem oved in a future release. Please use .at[] or .iat[] accessors instead

Out[15]: Text(0.5,1,'distance_from_previouse_palindrome')

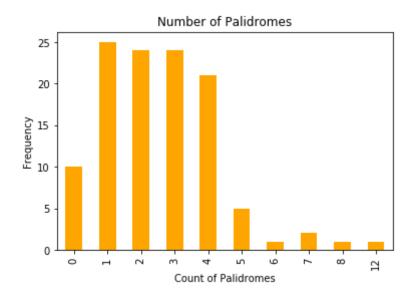




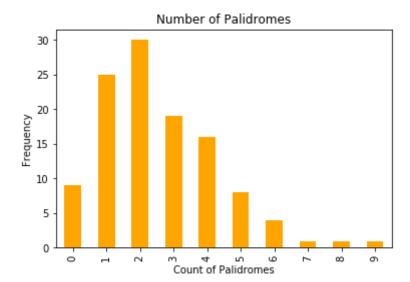




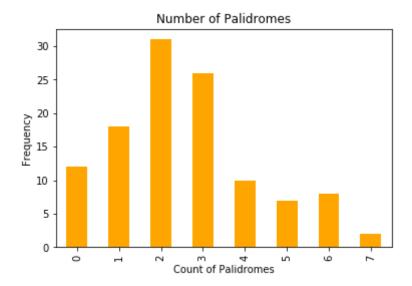
Out[17]: Text(0,0.5,'Frequency')



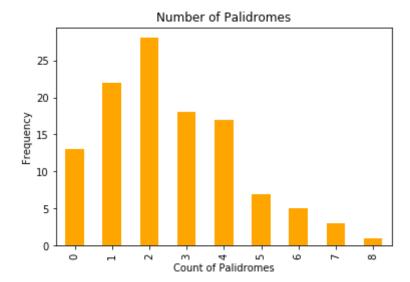
Out[18]: Text(0,0.5,'Frequency')



Out[19]: Text(0,0.5,'Frequency')



Out[20]: Text(0,0.5,'Frequency')



```
In [ ]:
```

Location and Spacing

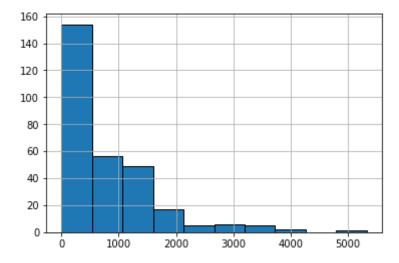
In [31]: spacingdf.head()

Out[31]:

	original_spacing	simulated_sample_1	simulated_sample_2	simulated_sample_3
0	1.0	2.069215	0.150657	0.574688
1	5.0	2.515219	0.727582	1.988005
2	5.0	3.468276	0.828988	3.917049
3	6.0	7.693870	0.996015	7.395344
4	6.0	15.863547	3.789403	8.157143

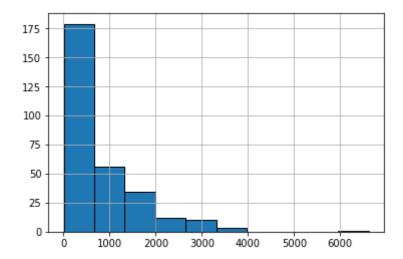
```
In [32]: spacing.hist(edgecolor = 'k', bins = 10)
#plt.title('spacing histogram of original data set')
```

Out[32]: <matplotlib.axes._subplots.AxesSubplot at 0x1a2261fac8>



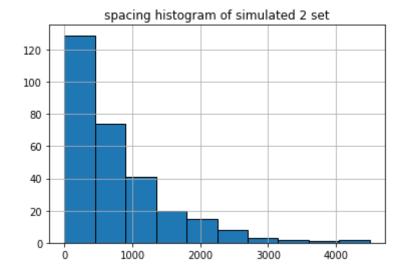
```
In [33]: spacing_1.hist(edgecolor = 'k', bins = 10)
#plt.title('spacing histogram of simulated 1 set')
```

Out[33]: <matplotlib.axes._subplots.AxesSubplot at 0x1a227044a8>



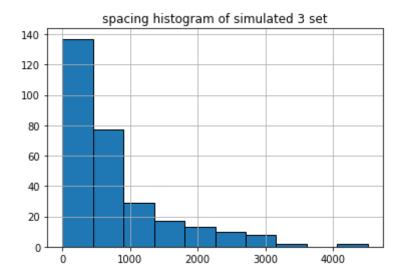
```
In [34]: spacing_2.hist(edgecolor = 'k')
plt.title('spacing histogram of simulated 2 set')
```

Out[34]: Text(0.5,1,'spacing histogram of simulated 2 set')



```
In [35]: spacing_3.hist(edgecolor = 'k')
   plt.title('spacing histogram of simulated 3 set')
```

Out[35]: Text(0.5,1,'spacing histogram of simulated 3 set')



```
In [36]: #chi-square test
```

```
In [95]: chisquare_pool = []
    for i in range(4):
        chisquare_pool += [spacingdf.iloc[:,i]/10]
        #chisquare_pool += [pd.cut(spacingdf.iloc[:,i], range(0, 5501, 50)).
        apply(lambda x: x.right)]
```

Power_divergenceResult(statistic=384.24061324216177, pvalue=0.000308635 1443201081)

Power_divergenceResult(statistic=428.1581850767412, pvalue=5.0764502145 65519e-07)

Power_divergenceResult(statistic=481.11042854318333, pvalue=3.268524524 159802e-11)

In [41]: # Sum of two consecutive pairs, and spacing.

```
In [43]: diff_pair_table.head()
```

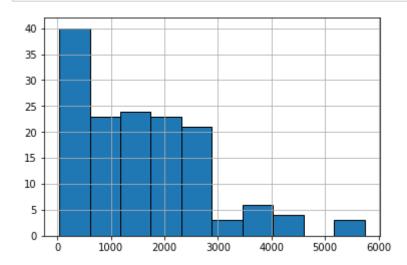
Out[43]:

	spacing of original data distance two pairs	spacing of sample_1 data distance two pairs	spacing of sample_2 data distance two pairs	spacing of sample_3 data distance two pairs
0	38.0	92.432669	26.953491	86.209950
1	39.0	93.286902	71.831406	103.314287
2	46.0	138.480830	87.550081	120.300769
3	48.0	141.311440	209.049002	151.041726
4	77.0	150.954169	252.936388	194.251758

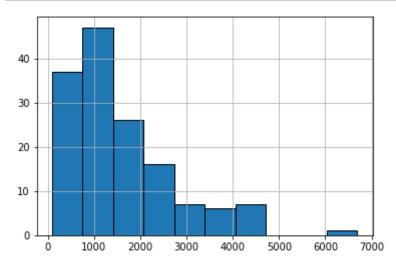
```
In [44]: diff_pair_table.columns[0]
```

Out[44]: 'spacing of original data distance two pairs'

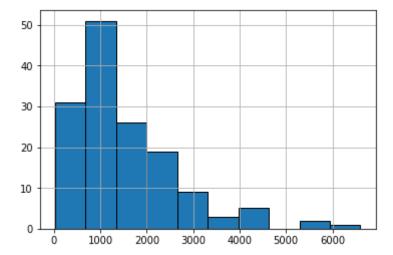
```
In [45]: diff_pair_table.dropna().iloc[:,0].hist(edgecolor = 'k')
   plt.title = (diff_pair_table.columns[0])
```



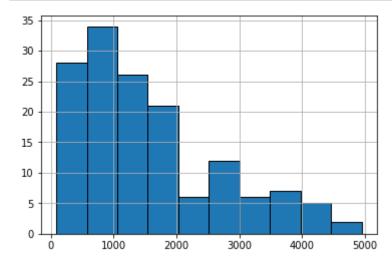
```
In [46]: diff_pair_table.dropna().iloc[:,1].hist(edgecolor = 'k')
plt.title = (diff_pair_table.columns[1])
```



```
In [47]: diff_pair_table.dropna().iloc[:,2].hist(edgecolor = 'k')
plt.title = (diff_pair_table.columns[2])
```



```
In [48]: diff_pair_table.dropna().iloc[:,3].hist(edgecolor = 'k')
    plt.title = (diff_pair_table.columns[3])
```



```
In [50]: #chi-square test pairs
    for i in range(1,4):
        print(stats.chisquare(chisquare_pool[0].dropna(), chisquare_pool[i].
        dropna()))
```

Power_divergenceResult(statistic=490.46073724428703, pvalue=8.129807811 07305e-39)

Power_divergenceResult(statistic=560.6054022716725, pvalue=6.8623605836 98973e-50)

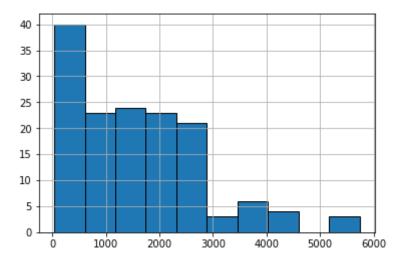
Power_divergenceResult(statistic=401.43936649405805, pvalue=1.045047574 5456958e-25)

In [52]: diff_pair_table_1.head()

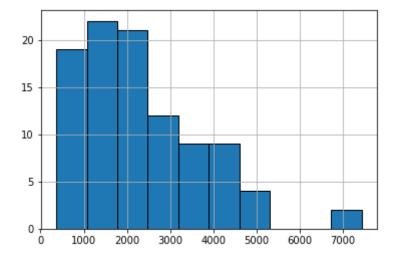
Out[52]:

	spacing of original data distance three pairs	spacing of sample_1 data distance three pairs	spacing of sample_2 data distance three pairs	spacing of sample_3 data distance three pairs
0	109.0	363.577638	289.190892	280.488765
1	139.0	379.409156	499.556538	331.352884
2	150.0	563.576203	638.575908	377.052167
3	256.0	584.022688	678.890549	408.246189
4	380.0	716.939085	679.389147	436.102848

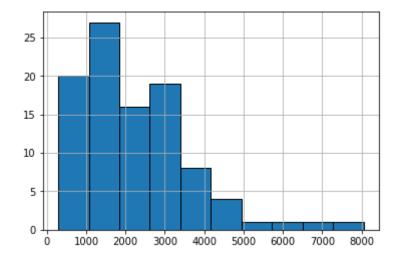
```
In [53]: diff_pair_table.dropna().iloc[:,0].hist(edgecolor = 'k')
plt.title = (diff_pair_table_1.columns[0])
```



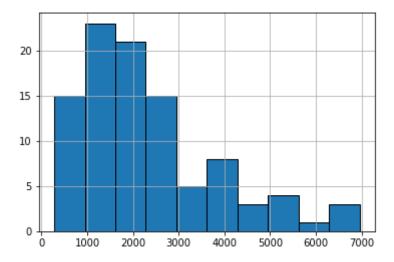
```
In [54]: diff_pair_table_1.dropna().iloc[:,1].hist(edgecolor = 'k')
    plt.title = (diff_pair_table_1.columns[1])
```



```
In [55]: diff_pair_table_1.dropna().iloc[:,2].hist(edgecolor = 'k')
    plt.title = (diff_pair_table_1.columns[2])
```



In [56]: diff_pair_table_1.dropna().iloc[:,3].hist(edgecolor = 'k')
 plt.title = (diff_pair_table_1.columns[3])



Counts

```
In [1]: import pandas as pd
import numpy as np
import seaborn as sns
import matplotlib.pyplot as plt
import scipy.stats as stats
%matplotlib inline

In [2]: data_1 = pd.read_csv('hcmv-263hxkx-lqhtfgz.txt')

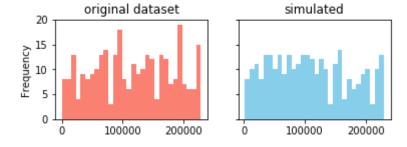
In [3]: # from original data set, n = 296 (Palindromes), N = 229354 (Base pairs)
n, N = 296, 229354

In [4]: # Generate three uniformed distributed
samples = [pd.Series(np.random.uniform(0,N,n)).sort_values() for i in ra
nge(3)]
```

Location & Spacing

```
In [31]: plt.subplot(221)
    data_1['location'].plot(kind='hist',bins=30, ylim=(0,20), title = 'origi
    nal dataset', sharex = True, sharey= True, color = 'salmon')
    plt.subplot(222)
    pd.Series(samples[0]).plot(kind='hist',bins=30, ylim=(0,20), title = 'si
    mulated', sharex = True, sharey= True, color = 'skyblue')
    #plt.subplot(223)
    #pd.Series(samples[1]).plot(kind='hist',bins=30, ylim=(0,20), title = 's
    imulated 2', sharex = True, sharey= True, color = 'skyblue')
    #pd.Series(samples[2]).plot(kind='hist',bins=30, ylim=(0,20), title = 's
    imulated 3', sharex = True, sharey= True, color = 'skyblue')
```

Out[31]: <matplotlib.axes._subplots.AxesSubplot at 0x1a229b4c18>

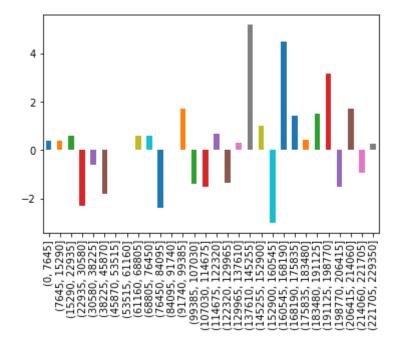


```
In [68]: orig_i30=pd.cut(data_1.location, bins = range(0, N, N//30)).value_counts
()
    sim_i30 = pd.cut(samples[0], bins = range(0, N, N//30)).value_counts()
```

```
In [69]: res30 = pd.DataFrame({
    'orig': orig_i30,
    'sim': sim_i30
})
```

```
In [70]: res30.apply(lambda x: (x.orig - x.sim)/x.sim**(0.5), axis = 1).plot(kind = 'bar')
```

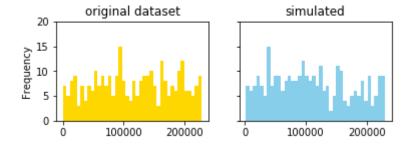
Out[70]: <matplotlib.axes._subplots.AxesSubplot at 0x1107fda90>



```
In [ ]:
```

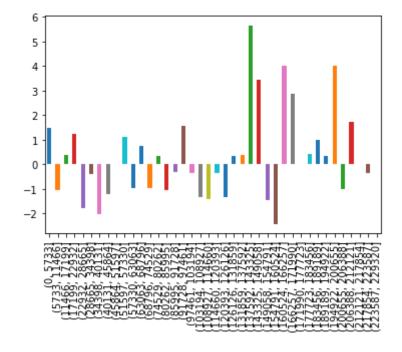
```
In [32]: plt.subplot(221)
    data_1['location'].plot(kind='hist',bins=40, ylim=(0,20), title = 'origi
    nal dataset', sharex = True, sharey= True, color = 'gold')
    plt.subplot(222)
    pd.Series(samples[0]).plot(kind='hist',bins=40, ylim=(0,20), title = 'si
    mulated', sharex = True, sharey= True, color = 'skyblue')
    #plt.subplot(223)
    #pd.Series(samples[1]).plot(kind='hist',bins=40, ylim=(0,20), title = 's
    imulated 2', sharex = True, sharey= True, color = 'skyblue')
    #pd.Series(samples[2]).plot(kind='hist',bins=40, ylim=(0,20), title = 's
    imulated 3', sharex = True, sharey= True, color = 'skyblue')
```

Out[32]: <matplotlib.axes._subplots.AxesSubplot at 0x1a22a91c18>



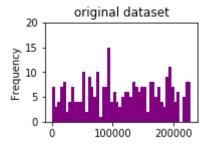
```
In [67]: orig_i40=pd.cut(data_1.location, bins = range(0, N, N//40)).value_counts
()
    sim_i40 = pd.cut(samples[0], bins = range(0, N, N//40)).value_counts()
    res40 = pd.DataFrame({
        'orig': orig_i40,
        'sim': sim_i40
    })
    res40.apply(lambda x: (x.orig - x.sim)/x.sim**(0.5), axis = 1).plot(kind = 'bar')
```

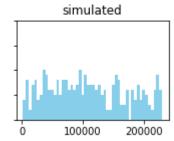
Out[67]: <matplotlib.axes._subplots.AxesSubplot at 0x1a241be940>



```
In [33]: plt.subplot(221)
    data_1['location'].plot(kind='hist',bins=50, ylim=(0,20), title = 'origi
    nal dataset', sharex = True, sharey= True, color = 'purple')
    plt.subplot(222)
    pd.Series(samples[0]).plot(kind='hist',bins=50, ylim=(0,20), title = 'si
    mulated', sharex = True, sharey= True, color = 'skyblue')
    #plt.subplot(223)
    #pd.Series(samples[1]).plot(kind='hist',bins=50, ylim=(0,20), title = 's
    imulated 2', sharex = True, sharey= True, color = 'skyblue')
    #pd.Series(samples[2]).plot(kind='hist',bins=50, ylim=(0,20), title = 's
    imulated 3', sharex = True, sharey= True, color = 'skyblue')
```

Out[33]: <matplotlib.axes._subplots.AxesSubplot at 0x1a22c25940>

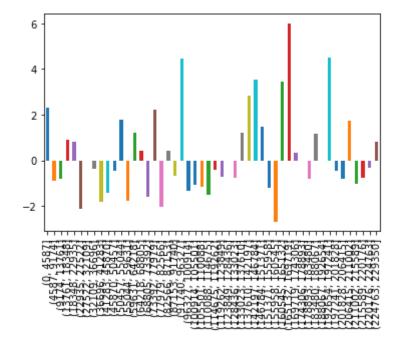




```
In [71]: orig_i50=pd.cut(data_1.location, bins = range(0, N, N//50)).value_counts
()
    sim_i50 = pd.cut(samples[0], bins = range(0, N, N//50)).value_counts()
    res50 = pd.DataFrame({
        'orig': orig_i50,
        'sim': sim_i50
})
    res50.apply(lambda x: (x.orig - x.sim)/x.sim**(0.5), axis = 1).plot(kind = 'bar')
```

/anaconda3/lib/python3.6/site-packages/ipykernel_launcher.py:7: Runtime Warning: divide by zero encountered in true_divide import sys

Out[71]: <matplotlib.axes. subplots.AxesSubplot at 0x1a2444dcf8>



```
In [74]: from scipy.stats import chisquare
    print('with #interval = 30, performing chi-square test, p-val is: ')
    print(chisquare(res30.orig, res30.sim))
```

with #interval = 30, performing chi-square test, p-val is:
Power_divergenceResult(statistic=103.73113275613277, pvalue=2.452971852
5712304e-10)

```
In [76]: print('with #interval = 40, performing chi-square test, p-val is: ')
    print(chisquare(res40.orig, res40.sim))
```

with #interval = 40, performing chi-square test, p-val is:
Power_divergenceResult(statistic=125.00010822510822, pvalue=6.109891996
538827e-11)

```
In [78]: print('with #interval = 50, performing chi-square test, p-val is: ')
    res50 = res50[res50['sim']!=0]
    print(chisquare(res50.orig, res50.sim))

with #interval = 50, performing chi-square test, p-val is:
    Power_divergenceResult(statistic=175.77052669552668, pvalue=1.815456407
    8507857e-16)
In []:

In []:
```

```
In [52]: for i in range(2000, 5001, 1000):
    original = pd.cut(data_1.location, range(0, N+1, i)).value_counts().
    rename('count')\
        .to_frame().groupby('count')['count'].count()
        simulated = pd.cut(sample, range(0, N+1, i)).value_counts().rename(
'count')\
        .to_frame().groupby('count')['count'].count()
        for j in original.index:
              output.loc['orginial_data interval = {}'.format(i),j] = original
        .loc[j]
        for j in simulated.index:
              output.loc['simulated_data interval = {}'.format(i),j] = simulat
        ed.loc[j]
```

In [53]: output = output.drop(0, axis = 1).fillna(0)

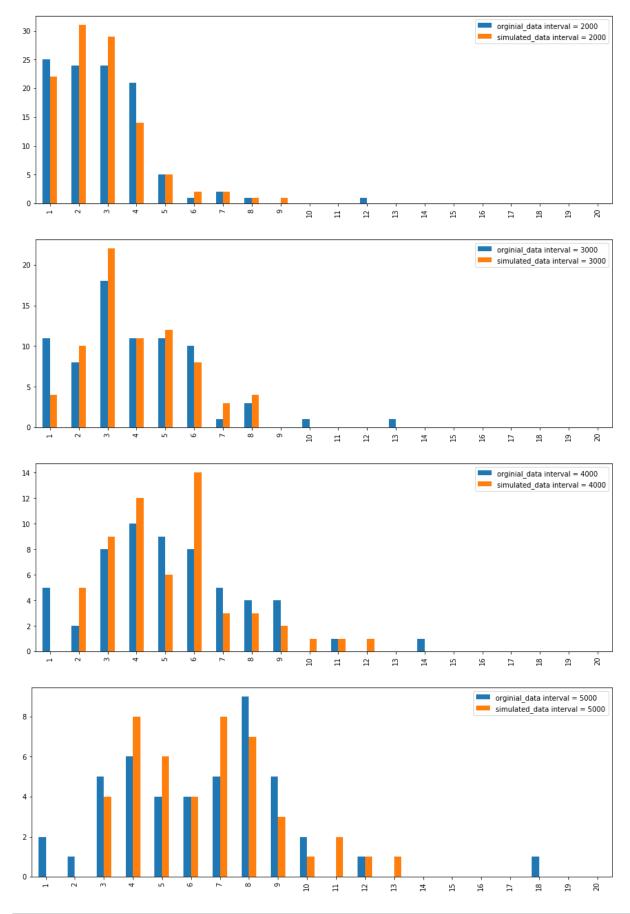
In [54]: output

Out[54]:

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
orginial_data interval = 2000	25	24	24	21	5	1	2	1	0	0	0	1	0	0	0	0	0	0	0	0
simulated_data interval = 2000	22	31	29	14	5	2	2	1	1	0	0	0	0	0	0	0	0	0	0	0
orginial_data interval = 3000	11	8	18	11	11	10	1	3	0	1	0	0	1	0	0	0	0	0	0	0
simulated_data interval = 3000	4	10	22	11	12	8	3	4	0	0	0	0	0	0	0	0	0	0	0	0
orginial_data interval = 4000	5	2	8	10	9	8	5	4	4	0	1	0	0	1	0	0	0	0	0	0
simulated_data interval = 4000	0	5	9	12	6	14	3	3	2	1	1	1	0	0	0	0	0	0	0	0
orginial_data interval = 5000	2	1	5	6	4	4	5	9	5	2	0	1	0	0	0	0	0	1	0	0
simulated_data interval = 5000	0	0	4	8	6	4	8	7	3	1	2	1	1	0	0	0	0	0	0	0

```
In [55]: for i in range(0,len(output),2):
    # fig = plt.figure() # Create matplotlib figure
    # ax = fig.add_subplot(111) # Create matplotlib axes
    # ax2 = ax.twinx() # Create another axes that shares the same x-axis
    as ax.
    # width = 0.4

t1 = output.iloc[i:i+2]
    #t2 = output.iloc[i+1]
    t1.T.plot(kind='bar', figsize=(15,5))
    #t2.plot(kind='bar', figsize=(15,5))
    plt.show()
```



In [56]: #Performing chi-square test for count
from scipy.stats import chisquare

```
obs = output.iloc[0:11:2]
          exp = output.iloc[1:11:2]
In [58]: # We choosing the first 0 - 8 counts to roughly enlimulate outliers, mak
          ing the chi-sugure test not too greedy
In [62]:
         counter = [(1,8), (1,8), (1,8), (2, 11)]
          for i in range(len(obs)):
              print('with interval = {}, performing chi-square test, p-val is: '.f
          ormat((i+1)*1000 + 1000))
              print(chisquare(obs.iloc[i,counter[i][0]:counter[i][1]], exp.iloc[i,
          counter[i][0]:counter[i][1]])[1])
         with interval = 2000, performing chi-square test, p-val is:
          0.3754643358182173
         with interval = 3000, performing chi-square test, p-val is:
         0.7711521463799177
         with interval = 4000, performing chi-square test, p-val is:
         0.2393852869355991
         with interval = 5000, performing chi-square test, p-val is:
          0.4893186745810869
In [64]:
          # P-Val is large
In [65]:
          # ploting standardlize residuals
In [66]:
          import seaborn as sns
          for i in range(len(obs)):
              sns.residplot(obs.iloc[i], exp.iloc[i])
              6
          simulated data interval = 5000
             2
             -2
             -4
            -6
                           orginial data interval = 5000
 In [ ]:
```

The Biggest Cluster

```
In [27]: #bins
         bins = [40, 60, 80, 100, 120]
In [28]: out = pd.DataFrame(index = bins, columns = ['lambda', 'interval_width',
         'probability', 'maximum', 'prediction interval'])
         for i in bins:
             interval = N//i
             k = pd.cut(data_1.location, range(0, N+1, interval)).value_counts().
         rename('count').max()
             x bar = pd.cut(data 1.location, range(0, N+1, interval)).value count
         s().rename('count').mean()
             pred = pd.cut(data_1.location, range(0, N+1, interval)).value_counts
         ().rename('count').idxmax()
             P = (x_bar^*(k) / np.math.factorial((k))) * np.exp(-x_bar)
             out.loc[i] = x_bar, interval, P, k, pred
In [29]: out
Out[29]:
```

	lambda	interval_width	probability	maximum	prediction_interval
40	7.4	5733	0.00510737	15	(91728, 97461]
60	4.93333	3822	0.000417868	14	(91728, 95550]
80	3.7	2866	2.5558e-05	14	(91712, 94578]
100	2.96	2293	1.1143e-05	13	(91720, 94013]
120	2.46667	1911	1.70567e-06	13	(91728, 93639]

In []:

Additional hypothesis

```
In [99]: additional_data.head()
```

```
Out[99]:
```

```
location
177
1321
1433
1477
3248
```

```
In [101]: additional_data.shape
```

Out[101]: (283, 1)

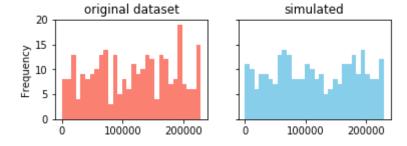
```
In [102]: # Test for location and spacing
```

```
In [103]: n, N = 283, 229354
```

```
In [105]: data_1 = additional_data
```

```
In [106]: plt.subplot(221)
    data_1['location'].plot(kind='hist',bins=30, ylim=(0,20), title = 'origi
    nal dataset', sharex = True, sharey= True, color = 'salmon')
    plt.subplot(222)
    pd.Series(samples[0]).plot(kind='hist',bins=30, ylim=(0,20), title = 'si
    mulated', sharex = True, sharey= True, color = 'skyblue')
```

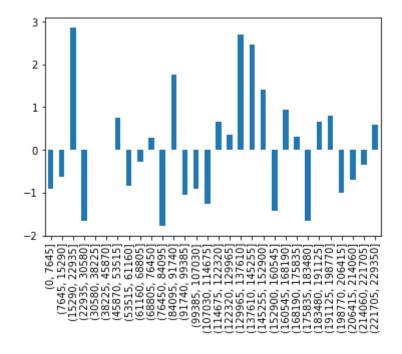
Out[106]: <matplotlib.axes._subplots.AxesSubplot at 0x1a19c00e80>



```
In [107]: orig_i30=pd.cut(data_1.location, bins = range(0, N, N//30)).value_counts
()
    sim_i30 = pd.cut(samples[0], bins = range(0, N, N//30)).value_counts()
```

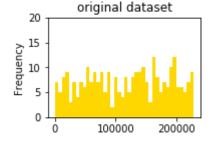
```
In [109]: res30.apply(lambda x: (x.orig - x.sim)/x.sim**(0.5), axis = 1).plot(kind = 'bar')
```

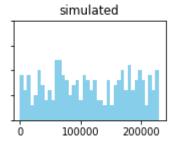
Out[109]: <matplotlib.axes. subplots.AxesSubplot at 0x1a19d5d4a8>



```
In [110]: plt.subplot(221)
    data_1['location'].plot(kind='hist',bins=40, ylim=(0,20), title = 'origi
    nal dataset', sharex = True, sharey= True, color = 'gold')
    plt.subplot(222)
    pd.Series(samples[0]).plot(kind='hist',bins=40, ylim=(0,20), title = 'si
    mulated', sharex = True, sharey= True, color = 'skyblue')
```

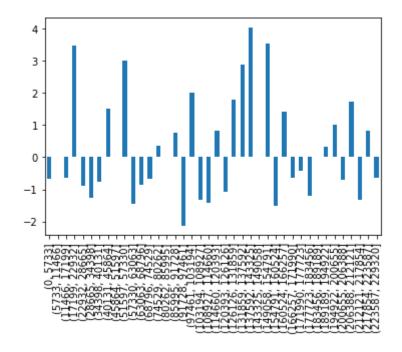
Out[110]: <matplotlib.axes. subplots.AxesSubplot at 0x1a19ebb780>





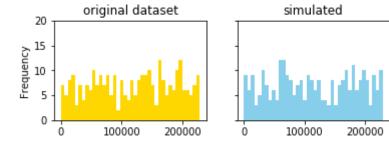
```
In [111]: orig_i40=pd.cut(data_1.location, bins = range(0, N, N//40)).value_counts
()
    sim_i40 = pd.cut(samples[0], bins = range(0, N, N//40)).value_counts()
    res40 = pd.DataFrame({
        'orig': orig_i40,
        'sim': sim_i40
    })
    res40.apply(lambda x: (x.orig - x.sim)/x.sim**(0.5), axis = 1).plot(kind = 'bar')
```

Out[111]: <matplotlib.axes. subplots.AxesSubplot at 0x1a1a0555c0>



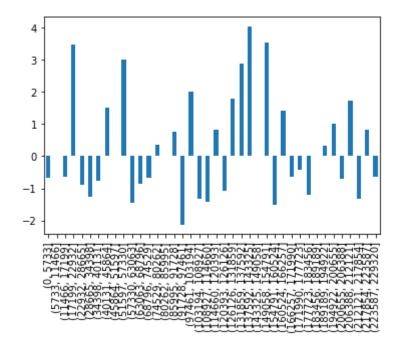
```
In [112]: plt.subplot(221)
    data_1['location'].plot(kind='hist',bins=40, ylim=(0,20), title = 'origi
    nal dataset', sharex = True, sharey= True, color = 'gold')
    plt.subplot(222)
    pd.Series(samples[0]).plot(kind='hist',bins=40, ylim=(0,20), title = 'si
    mulated', sharex = True, sharey= True, color = 'skyblue')
    #plt.subplot(223)
```

Out[112]: <matplotlib.axes._subplots.AxesSubplot at 0x1a1a2416a0>



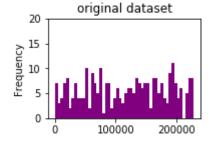
```
In [113]: orig_i40=pd.cut(data_1.location, bins = range(0, N, N//40)).value_counts
()
    sim_i40 = pd.cut(samples[0], bins = range(0, N, N//40)).value_counts()
    res40 = pd.DataFrame({
        'orig': orig_i40,
        'sim': sim_i40
})
    res40.apply(lambda x: (x.orig - x.sim)/x.sim**(0.5), axis = 1).plot(kind = 'bar')
```

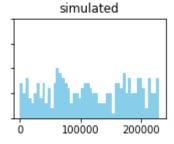
Out[113]: <matplotlib.axes. subplots.AxesSubplot at 0x1a1a33fdd8>



```
In [114]: plt.subplot(221)
    data_1['location'].plot(kind='hist',bins=50, ylim=(0,20), title = 'origi
    nal dataset', sharex = True, sharey= True, color = 'purple')
    plt.subplot(222)
    pd.Series(samples[0]).plot(kind='hist',bins=50, ylim=(0,20), title = 'si
    mulated', sharex = True, sharey= True, color = 'skyblue')
```

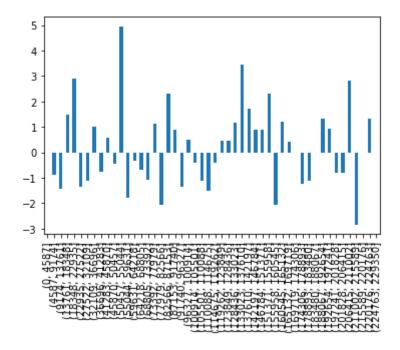
Out[114]: <matplotlib.axes._subplots.AxesSubplot at 0x1a1a4e6d30>





```
In [115]: orig_i50=pd.cut(data_1.location, bins = range(0, N, N//50)).value_counts
()
    sim_i50 = pd.cut(samples[0], bins = range(0, N, N//50)).value_counts()
    res50 = pd.DataFrame({
        'orig': orig_i50,
        'sim': sim_i50
})
    res50.apply(lambda x: (x.orig - x.sim)/x.sim**(0.5), axis = 1).plot(kind = 'bar')
```

Out[115]: <matplotlib.axes. subplots.AxesSubplot at 0x1a1a6b4b38>



```
In [116]: from scipy.stats import chisquare
    print('with #interval = 30, performing chi-square test, p-val is: ')
    print(chisquare(res30.orig, res30.sim))
```

with #interval = 30, performing chi-square test, p-val is:
Power_divergenceResult(statistic=47.943115218115224, pvalue=0.014898755
726929839)

```
In [117]: print('with #interval = 40, performing chi-square test, p-val is: ')
    print(chisquare(res40.orig, res40.sim))
```

with #interval = 40, performing chi-square test, p-val is:
Power_divergenceResult(statistic=99.23867243867244, pvalue=3.7358384318
85617e-07)

```
In [118]: print('with #interval = 50, performing chi-square test, p-val is: ')
    res50 = res50[res50['sim']!=0]
    print(chisquare(res50.orig, res50.sim))
```

with #interval = 50, performing chi-square test, p-val is:
Power_divergenceResult(statistic=119.5277777777779, pvalue=7.956403480
48162e-08)

In [119]: bins = [40, 60, 80, 100, 120]

In [121]: out

Out[121]:

	lambda	interval_width	probability	maximum	prediction_interval
 40	7.075	5733	0.0277809	12	(194922, 200655]
60	4.71667	3822	0.00226393	12	(194922, 198744]
80	3.5375	2866	0.00245971	10	(194888, 197754]
100	2.83	2293	0.000535856	10	(194905, 197198]
120	2.35833	1911	0.00761368	7	(74529, 76440]

In []: