

$$1) ((\forall x \exists y P(x,z) \vee Q(y)) [x:=f(z)]) [y:=g(z,x)]$$

$$(\forall x \exists y P(x,z) \vee Q(y)) [y:=g(z,x)] \quad \text{regla 1}$$

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$$2) ((\forall y P(x,y,z) \wedge \forall x Q(x,y,z)) [x:=f(y,z)]) [y:=g(x,z)]$$

$$(((\forall y P(x,y,z)) [x:=f(y,z)] \wedge (\forall x Q(x,y,z)) [x:=f(y,z)]) [y:=g(x,z)])$$

$$(((\forall w P(x,y,z) [y:=w]) [x:=f(y,z)] \wedge \forall x Q(x,y,z)) [y:=g(x,z)]) \quad \begin{matrix} \text{regla 3} \\ \downarrow y \\ \text{regla 1} \end{matrix}$$

$$(((\forall w P(x,w,z)) [x:=f(y,z)] \wedge \forall x Q(x,y,z)) [y:=g(x,z)])$$

$$((\forall w P(f(y,z), w, z) \wedge \forall x Q(x,y,z)) [y:=g(x,z)]) \quad \text{regla 2}$$

$$((\forall w P(f(y,z), w, z)) [y:=g(x,z)] \wedge (\forall x Q(x,y,z)) [y:=g(x,z)])$$

$$(\forall w P(f(g(x,z), z), w, z) \wedge (\forall v Q(x,y,z) [x:=v]) [y:=g(x,z)]) \quad \begin{matrix} \text{regla 2} \\ y \text{ regla 3} \end{matrix}$$

$$(\forall w P(f(g(x,z), z), w, z) \wedge (\forall v Q(v,y,z)) [y:=g(x,z)])$$

$$(\forall w P(f(g(x,z), z), w, z) \wedge \forall v Q(v, g(x,z), z)) \quad \text{regla 2}$$