

Output tables for the test of Multiple comparisons.

October 15, 2023

1 Average rankings of Friedman test

Average ranks obtained by applying the Friedman procedure

| Algorithm             | Ranking |
|-----------------------|---------|
| Average Fitness HC    | 4       |
| Average Fitness HCRR  | 2.4     |
| Average Fitness SA    | 1.6     |
| Average Fitness GRASP | 2       |

Table 1: Average Rankings of the algorithms

Friedman statistic considering reduction performance (distributed according to chi-square with 3 degrees of freedom: 9.96.  
P-value computed by Friedman Test: 0.01890922825443197.

## 2 Post hoc comparisons

Results achieved on post hoc comparisons for  $\alpha = 0.05$ ,  $\alpha = 0.10$  and adjusted p-values.

### 2.1 P-values for $\alpha = 0.05$

| $i$ | algorithms                                     | $z = (R_0 - R_i)/SE$ | $p$      |
|-----|--|----------------------|----------|
| 6   | Average Fitness HC vs. Average Fitness SA      | 2.939388             | 0.003289 |
| 5   | Average Fitness HC vs. Average Fitness GRASP   | 2.44949              | 0.014306 |
| 4   | Average Fitness HC vs. Average Fitness HCRR    | 1.959592             | 0.050044 |
| 3   | Average Fitness HCRR vs. Average Fitness SA    | 0.979796             | 0.327187 |
| 2   | Average Fitness HCRR vs. Average Fitness GRASP | 0.489898             | 0.624206 |
| 1   | Average Fitness SA vs. Average Fitness GRASP   | 0.489898             | 0.624206 |

Table 2: P-values Table for  $\alpha = 0.05$

Nemenyi's procedure rejects those hypotheses that have an unadjusted p-value  $\leq 0.008333$ .

## 2.2 P-values for $\alpha = 0.10$

| $i$ | algorithms                                     | $z = (R_0 - R_i)/SE$ | $p$      |
|-----|--|----------------------|----------|
| 6   | Average Fitness HC vs. Average Fitness SA      | 2.939388             | 0.003289 |
| 5   | Average Fitness HC vs. Average Fitness GRASP   | 2.44949              | 0.014306 |
| 4   | Average Fitness HC vs. Average Fitness HCRR    | 1.959592             | 0.050044 |
| 3   | Average Fitness HCRR vs. Average Fitness SA    | 0.979796             | 0.327187 |
| 2   | Average Fitness HCRR vs. Average Fitness GRASP | 0.489898             | 0.624206 |
| 1   | Average Fitness SA vs. Average Fitness GRASP   | 0.489898             | 0.624206 |

Table 3: P-values Table for  $\alpha = 0.10$

Nemenyi's procedure rejects those hypotheses that have an unadjusted p-value  $\leq 0.016667$ .

## 2.3 Adjusted p-values

| i | hypothesis                                     | unadjusted $p$ | $p_{N_{eme}}$ |
|---|--|----------------|---------------|
| 1 | Average Fitness HC vs .Average Fitness SA      | 0.003289       | 0.019732      |
| 2 | Average Fitness HC vs .Average Fitness GRASP   | 0.014306       | 0.085835      |
| 3 | Average Fitness HC vs .Average Fitness HCRR    | 0.050044       | 0.300261      |
| 4 | Average Fitness HCRR vs .Average Fitness SA    | 0.327187       | 1.963121      |
| 5 | Average Fitness HCRR vs .Average Fitness GRASP | 0.624206       | 3.745237      |
| 6 | Average Fitness SA vs .Average Fitness GRASP   | 0.624206       | 3.745237      |

Table 4: Adjusted  $p$ -values