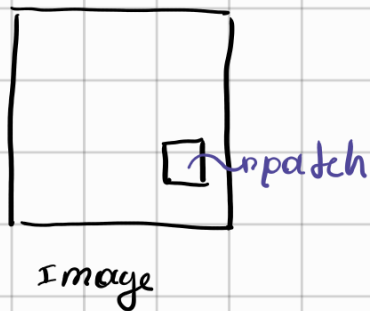


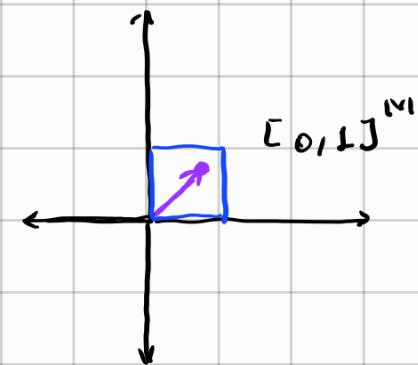
Signals and sparsity

we will consider signals and images as vectors



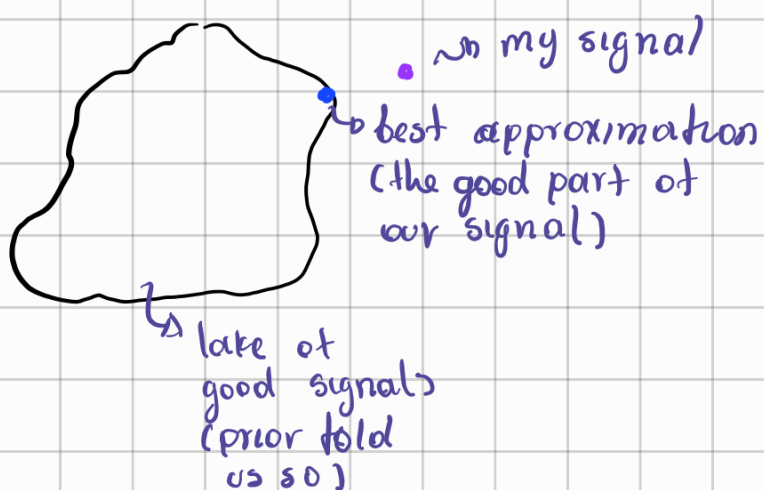
to see images as vectors we need to unfold them so we get a signal which can represent a vector.

so to normalize a signal means,



Priors

what we need is a prior to restrict our search in the space and find the good signal.



we assume that if s is our measured signal:

$$s = y + \eta$$

\hookrightarrow noise

we also assume that $\|n\| < \delta$ \hookrightarrow maximum noise
 \hookrightarrow "the effect of the noise"

Conclusions

Priors guide us to evaluate what a good signal is, it's a function $f: \mathbb{R}^M \rightarrow [0, 1]$, where the closest to f the most likely to be a "true signal".

Sparsity

we assume that every signal can be approximated as or sparse linear combination of some basis elements.

\rightarrow go to linear algebra recap

so, assume:

$$\underline{s} = D\underline{x} \quad \hookrightarrow \text{sparsity tell us that } x \text{ should have few non-zero entries}$$

so, with this in mind we make the following algorithms.

Enforce sparsity

Steps:

1. change basis (get x)
2. threshold x (set to 0 small coefficients)
3. come back to \hat{s}

For this algorithm to "work", we assume

$$s = y + n$$

↓ ↗ noise
true signal

- $D^T y$ is sparse
- $D^T n$ is not sparse
- (with low coefficients in the suitable basis)?

$$x = \overbrace{D^T y}^{\text{recover } y} + \underbrace{D^T n}_{\substack{\text{remove this} \\ \text{part} \\ \text{(thresholding)}}$$

Footnote: Sparsity is not relevant in canonical basis that's why we need to change basis, one where we think sparsity is more relevant,