

$$x(t) = |A \cos(2\pi F_0 t)|^2$$

$$\begin{aligned} x(t) &= A^2 \cos^2(2\pi F_0 t) \\ &= \frac{A^2 (1 + \cos(4\pi F_0 t))}{2} \\ &= \frac{A^2}{2} + \frac{A^2 \cos(4\pi F_0 t)}{2} \end{aligned}$$

$$\cos^2(x) = \frac{1 + \cos 2x}{2}$$

$$\frac{a_0}{2} + \sum_{n=0}^N a_n \cos(n\omega_0 t) + b_n \sin(n\omega_0 t)$$

$$a_0 = A^2 \quad a_n = \frac{A^2}{2} \quad b_n = 0$$

$$c_n = \frac{a_n - jb_n}{2} = \frac{\frac{A^2}{2} - 0}{2} = \frac{A^2}{4}$$

$$\tilde{x}(t) = \sum_{n=-N}^N c_n e^{jn\omega_0 t} = \sum_{n=-N}^N \frac{A^2}{4} e^{jn\omega_0 t}$$

$$\alpha_n = \sqrt{a_n^2 + b_n^2} = \sqrt{\left(\frac{A^2}{2}\right)^2 + 0^2} = \frac{A^2}{2}$$

$$\Phi_n = \tan^{-1}\left(-\frac{b_n}{a_n}\right) = 0$$

~~$a_0 = \frac{A^2}{T_0}$~~

$$a_0 = \frac{2}{T_0} \int_{-T_0/2}^{T_0/2} \frac{A^2}{2} + \frac{A^2}{2} \cos(4\pi f_0 t) dt$$

$$a_0 = \frac{2}{T_0} \int \frac{A^2}{2} (1 + \cos(4\pi f_0 t)) dt$$

$$= \frac{2A^2}{T_0} \int_{-T_0/2}^{T_0/2} (1 + \cos(4\pi f_0 t)) dt$$

$$= \frac{A^2}{T_0} \left[t + \frac{\sin(4\pi f_0 t)}{4\pi f_0} \right]_{-T_0/2}^{T_0/2}$$

$$= \frac{A^2}{T_0} \left[\frac{T_0}{2} + \frac{\sin(4\pi f_0 T_0/2)}{4\pi f_0} - \left(-\frac{T_0}{2} + \frac{\sin(4\pi f_0 (-T_0/2))}{4\pi f_0} \right) \right]$$

$$= \frac{A^2}{T_0} \left[\frac{T_0}{2} + \frac{\sin(2\pi)}{4\pi f_0} + \frac{T_0}{2} - \frac{\sin(2\pi)}{4\pi f_0} \right]$$

$$= \frac{A^2}{T_0} \left(\frac{2T_0}{2} \right) = \underline{\underline{A^2}}$$

$$a_n = \frac{1}{T} \int_{-T/2}^{T/2} \left(\frac{A^2}{2} + \frac{A^2}{2} \cos(4\pi f_0 t) \right) (\cos(n\omega_0 t)) dt$$

$$\omega_0 = \frac{2\pi}{T_0} = 2\pi f_0$$

$$\frac{1}{T_0} = \frac{2}{T_0}$$

$$a_n = \frac{2}{T_0} \int_{-T_0/2}^{T_0/2} \frac{A^2}{2} (1 + \cos(4\pi f_0 t)) (\cos(n 2\pi f_0 t)) dt$$

$$a_n = \frac{A^2}{T_0} \int_{-T_0/2}^{T_0/2} (1 + \cos(4\pi f_0 t)) (\cos(n 2\pi f_0 t)) dt \quad n=2$$

$$a_n = \frac{A^2}{T_0} \int_{-T_0/2}^{T_0/2} (\cos(4\pi f_0 t) + \cos^2(4\pi f_0 t)) dt$$

$$a_n = \frac{A^2}{T_0} \left[\int_{-T_0/2}^{T_0/2} \cos(4\pi f_0 t) dt + \int_{-T_0/2}^{T_0/2} \left(\frac{1 + \cos(8\pi f_0 t)}{2} \right) dt \right]$$

$$a_n = \frac{A^2}{T_0} \left[\left[-\frac{\cos(4\pi f_0 t)}{4\pi f_0} \right]_{-T_0/2}^{T_0/2} + \frac{1}{2} \int_{-T_0/2}^{T_0/2} (1 + \cos(8\pi f_0 t)) dt \right]$$

$$a_n = \frac{A^2}{T_0} \left[\left(-\frac{\cos(2\pi)}{4\pi f_0} + \frac{\cos(-2\pi)}{4\pi f_0} \right) + \frac{1}{2} \left(t + \frac{\sin(8\pi f_0 t)}{8\pi f_0} \right) \right]_{-T_0/2}^{T_0/2}$$

$$a_n = \frac{A^2}{T_0} \left[-\frac{1}{2} \left(\frac{T_0}{2} + \frac{\sin(4\pi)}{8\pi f_0} + \frac{T_0}{2} - \frac{\sin(-4\pi)}{8\pi f_0} \right) \right]$$

$$a_n = \frac{A^2}{T_0} \left[\frac{1}{2} \left(\frac{T_0}{2} + \frac{T_0}{2} \right) \right] = \frac{A^2}{T_0} \left(\frac{T_0}{2} \right)$$

$$a_n = \frac{A^2}{2}$$

$$\therefore a_2 = \frac{A^2}{2}$$

$$b_n = \frac{2}{T_0} \int_{-T_0/2}^{T_0/2} \left(\frac{A^2}{2} + \frac{A^2}{2} \cos(4\pi f_0 t) \right) \left(\sin(n\omega_0 t) \right) dt \quad \begin{matrix} \omega_0 = 2\pi f_0 \\ n=2 \end{matrix}$$

$$b_n = \frac{2}{T_0} \int_{-T_0/2}^{T_0/2} \frac{A^2}{2} \left(1 + \cos(4\pi f_0 t) \right) \left(\sin(2n\pi f_0 t) \right) dt$$

$$b_n = \frac{A^2}{T_0} \int_{-T_0/2}^{T_0/2} \left(\sin(4\pi f_0 t) + \underbrace{\cos(4\pi f_0 t) \sin(4\pi f_0 t)}_{\frac{\sin(8\pi f_0 t)}{2}} \right) dt$$

$$b_n = \frac{A^2}{T_0} \int_{-T_0/2}^{T_0/2} \sin(4\pi f_0 t) + \frac{1}{2} \sin(8\pi f_0 t) dt$$

$$b_n = \frac{A^2}{T_0} \left[-\frac{\cos(4\pi f_0 t)}{4\pi f_0} - \frac{\cos(8\pi f_0 t)}{8\pi f_0} \right]_{-T_0/2}^{T_0/2}$$

$$b_n = \frac{A^2}{T_0} \left[-\frac{\cos(2\pi)}{4\pi f_0} - \frac{\cos(4\pi)}{8\pi f_0} - \left(-\frac{\cos(-2\pi)}{4\pi f_0} - \frac{\cos(4\pi)}{8\pi f_0} \right) \right]$$

$$b_n = \frac{A^2}{T_0} \left[-\frac{\cancel{\cos(2\pi)}}{\cancel{4\pi f_0}} - \frac{\cancel{\cos(4\pi)}}{\cancel{8\pi f_0}} + \frac{\cancel{\cos(-2\pi)}}{\cancel{4\pi f_0}} + \frac{\cancel{\cos(4\pi)}}{\cancel{8\pi f_0}} \right]$$

$$b_n = 0$$

$$b_2 = 0$$