ICS Lab Report - lab2

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### Lab Name

Lending Your Name

# Lab Purpose

Store the n-th number of a sequence into register R7.

#### Lab Content

In mathematics, the Fibonacci numbers, commonly denoted  $F_n$ , form a sequence, called the Fibonacci sequence, such that each number is the sum of the two preceding ones, starting from 0 and 1. That is F(0) = 0, F(1) = 1, F(n) = F(n-1) + F(n-2).

As the Fibonacci sequence grows quite rapidly, we made a little difference with the origin Fibonacci sequence:

```
F(0) = 1

F(1) = 1

F(2) = 2

F(n) = (F(n-1) + 2 * F(n-3)) \mod 1024 (1 <= n <= 16384)
```

In the beginning, n is stored in R0. All other registers' initial values are 0. Your tasks are:

- Store F(n) in register R7.
- Divide your student number into four equal segments, labelling them with a, b, c and d. For example, TA's student ID is PB17000144, so a = 17, b = 0, c = 14, d = 44. Store value of F(a), F(b), F(c) and F(d) at the end of your code with ".FILL" pseudo command.

#### Lab Environment

Windows 11 Home Edition version 21H2, Visual Studio Code, LC3Tools v2.0.2.

# Lab Procedure

This time, it is only acquired to provide l-version of the program. To help understand the content of this lab, also help to verify the correctness of the program, a C program is firstly written as below.

```
#include <stdio.h>
   #include <stdlib.h>
3
   int main(int argc, char const *argv[]) {
       int n = 0;
4
       if (argc == 1) scanf("%d", &n);
5
       else sscanf(argv[1], "%d", &n);
6
7
       int a0, a1 = 2, a2 = 1, a3 = 1;
8
       if (n >= 3) for (int i = 3; i <= n; ++i) {
9
            a0 = (a1 + 2 * a3) \% 1024;
10
            a3 = a2; a2 = a1; a1 = a0;
11
12
       else if (n == 0) a0 = 1;
13
       else if (n == 1) a0 = 1;
14
       else if (n == 2) a0 = 2;
       printf("%d\n", a0);
15
16
       return 0;
17
```

However, the C program is only easy to read but not easy to translate to LC-3 Assembly Language. So after variable renaming and rearrange of statements, we get the code below which is easy to translate.

```
#include <stdio.h>
1
2
   #include <stdlib.h>
   int main(int argc, char const *argv[]) {
        int16_t R0 = 0;
       if (argc == 1) scanf("%hd", &R0);
5
       else sscanf(argv[1], "%hd", &R0);
6
7
       int16_t R7, R2 = 2, R3 = 1, R4 = 1;
       if (R0 == 0) R7 = 1;
8
9
       else if (R0 == 1) R7 = 1;
10
       else if (R0 == 2) R7 = 2;
       else for (int16 t i = 3; i <= R0; ++i) {
11
            R7 = (R2 + 2 * R4) \% 1024;
12
13
            R4 = R3; R3 = R2; R2 = R7;
14
       }
       printf("%hd\n", R7);
15
16
       return 0;
17
   }
```

Standing here, it seems that all we need to do is translating. But notice that decimal number 1023 cannot be stored using a 5-bit 2's complement number, we need to store it at another position of memory.

Another thing is to "lend my name". My student number is "PB20000061", which will be divided into a = 20, b = 0, c = 0, d = 61. After computing we know that F(a) = 930, F(b) = 1, F(c) = 930, F(d) = 930.

Finally we get the answer code below, whose length is 28, satisfying the standard of full marks.

```
.ORIG x3000
   ADD R0, R0, #-1
   BRz EXIT1
3
4
   ADD R0, R0, #-1
  BRz EXIT2
5
6
   ADD R2, R2, #2
7
   ADD R3, R3, #1
   ADD R4, R4, #1
   LD R5, MOD
9
   LOOP ADD R0, R0, #-1
10
   BRn OUTLOOP
11
12 ADD R6, R4, R4
13
   ADD R7, R2, R6
14
   AND R7, R7, R5
   ADD R4, R3, #0
15
   ADD R3, R2, #0
16
17
   ADD R2, R7, #0
18
   BRnzp LOOP
19
   OUTLOOP BRnzp EXIT
20
  EXIT1 ADD R7, R7, #1
21
   BRnzp EXIT
22
   EXIT2 ADD R7, R7, #2
   BRnzp EXIT
24
   MOD .FILL #1023
25
   Fa .FILL #930
26
   Fb .FILL #1
   Fc .FILL #1
28
   Fd .FILL #262
29
   EXIT
30
   .END
```

Initially, it was mistakenly considered that command HALT would change the value stored in R7. But

that is only correct in the second edition of LC-3. Also, through rearranging the BR command to judge specificly, we get a shorter version of the answer whose length 26.

```
1
   .ORIG x3000
2
   ADD R0, R0, #-1
3
   BRz EXIT2
   ADD R0, R0, #-1
   BRz EXIT1
   ADD R2, R2, #2
7
   ADD R3, R3, #1
   ADD R4, R4, #1
9
   LD R5, MOD
10
   LOOP ADD R0, R0, #-1
11
   BRn OUTLOOP
12
   ADD R6, R4, R4
   ADD R7, R2, R6
13
14
   AND R7, R7, R5
15
   ADD R4, R3, #0
16
  ADD R3, R2, #0
17
   ADD R2, R7, #0
18
   BRnzp LOOP
   OUTLOOP HALT
  EXIT1 ADD R7, R7, #1
21
   EXIT2 ADD R7, R7, #1
22
  HALT
23
   MOD .FILL #1023
24~{\sf Fa} .FILL #930
25
   Fb .FILL #1
   Fc .FILL #1
26
27
   Fd .FILL #262
28
   . END
```

### Correctness Verification

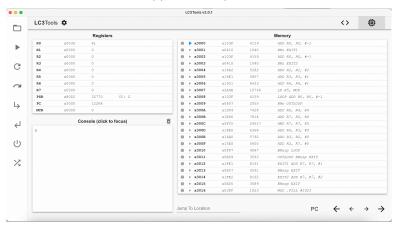
We use program written in LC-3 Assembly to calculate the answer of F(n) and than compare the result with the one get from the C program above.

We have tested the integer n more than the following: 1, 2, 3, 20, 61, 16384. One of the cases in listed below as Figure 1.

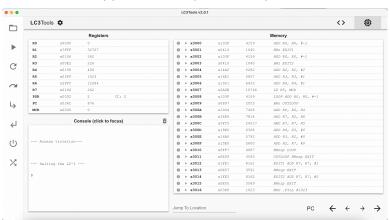
Note: Due to some reasons, tests were run on macOS Monterey with LC3Tools v2.0.1.



(a) The C Program



(b) Before Running the LC3 Program



(c) After Running the LC3 Program

Figure 1: One Example of Correctness Verification