MA684

Homework 7

1. Let's explore some model diagnostic simulations. Consider the following models:

$$\begin{aligned} \textit{Model 1: } y_i &= \beta_0 + \beta_1 x_i + \varepsilon_i \\ \textit{Model 2: } y_i &= \beta_0 + \beta_1 x_i + \beta_2 x_i^2 + \varepsilon_i \\ \textit{Model 3: } y_i &= \beta_0 + \beta_1 x_i + \sqrt{x_i} \varepsilon_i \\ \textit{Model 4: } y_i &= \beta_0 + \beta_1 x_i + \beta_2 x_i^2 + \sqrt{x_i} \varepsilon_i \\ \textit{Model 5: } y_i &= \beta_0 + \beta_1 x_i + \eta_i \end{aligned}$$

where $\beta_0=0.1, \beta_1=0.5, \beta_2=2.0, x_i \sim Uniform(0,2), \varepsilon_i \sim N(0,0.2), \eta_i \sim t_4$ distributions. Note that t_4 is the t-distribution with 4 degrees of freedom.

- a. Generate n=100 samples from each model. Obtain the scatter plot of the data.
- b. For each data, fit the linear regression model: $y_i = \beta_0 + \beta_1 x_i + \varepsilon_i$.
- c. Generate the residual plot and normal QQ plot. In each case, white a short description of the two plots. What features of the plots suggest that your fitted model may not be adequate?

```
#generate samples for ε
eps=rnorm(100,0,0.2)
#generate x values
x=runif(100,0,2)
#generate y values from the model
y=0.1+0.5*x+eps
#create a data frame for the data so that we are not confused with so many datasets
data mod1=data.frame(x,y)
#Let's have a look at the scatter plot of the data
plot(x,y, main = "Scatterplot for model 1")
#Fit linear model
fit1=lm(y~x,data=data mod1)
#create a place holder for the two plots
par(mfrow=c(1,2))
#plot residual
plot(fit1, which=1, col="blue")
#QQ plot
plot(fit1,which=2, col="red3")
```

- 2. We will be using the "surgical" data in the "olsrr" package for this homework. The data is related to patients' survival times who had undergone a type of liver operation. The response variable is "survival," and for now, we consider only the continuous predictors in the dataframe.
 - a. Create a scatter plot matrix of the data. Describe how the predictors are related to the response variable.

- b. Fit a multiple regression model. Is the model statistically significant? Explain your answer
- c. Which of the predictors are statistically significant given the other variables are already in the model? Explain your answer.
- d. Carry out the residual analysis. Is the model adequate? Explain your answer.
- e. Carry out a hypothesis test for normality and equal variance. What are your conclusions?
- f. Now, we want to fit a new model with the response variable "survival" replaced by "log(survival)" and all the predictors the same as before. Repeat parts (a)-(e), and explain how the new model is different from the old.