Energy System Modelling

Karlsruhe Institute of Technology Institute for Automation and Applied Informatics Summer Term 2020

TUTORIAL II: NETWORK THEORY AND POWER FLOW

Will be worked on in the exercise session on Friday, 5 June 2020.

PROBLEM II.1 (PROGRAMMING) - NETWORK THEORY BASICS

Consider the simple network shown ins Figure 1. Calculate in Python or by hand:

(a) Compile the *nodes list* and the *edge list*.

Remark: While graph-theoretically both lists are unordered sets, let's agree on an ordering now which can serve as basis for the matrices in the following exercises: we sort everything in ascending numerical order, i.e. node 1 before node 2 and edge (1,2) before (1,4) before (2,3).

- (b) Determine the *order* and the *size* of the network.
- (c) Compute the *adjacency matrix A* and check that it is symmetric.
- (d) Find the *degree* k_n of each node n and compute the *average degree* of the network.
- (e) Determine the *incidence matrix K* by assuming the links are always directed from smaller-numbered node to larger-numbered node, i.e. from node 2 to node 3, instead of from 3 to 2.
- (f) Compute the *Laplacian* L of the network using k_n and A. Remember that the Laplacian can also be computed as $L = KK^T$ and check that the two definitions agree.
- (g) Find the *diameter* of the network by looking at Figure 1.

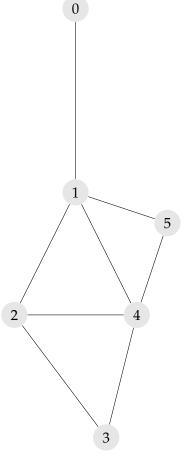


Figure 1: Simple Network

PROBLEM II.2 (PROGRAMMING) - LINEAR POWER FLOW

If you map the nodes to countries like <code>0=DK</code>, <code>1=DE</code>, <code>2=CH</code>, <code>3=IT</code>, <code>4=AT</code>, <code>5=CZ</code> the network in Figure 2 represents a small part of the European electricity network (albeit very simplified). You can find the *power imbalance* time series for the six countries for January 2017 in hourly MW in the file <code>imbalance.csv</code>. They have been derived from physical flows as published by ENTSO-E.

The linear power flow is given by

$$p_i = \sum_j \tilde{L}_{i,j} \theta_j$$
 and $f_l = \frac{1}{x_l} \sum_i K_{i,l} \theta_i$, where $\tilde{L}_{i,j} = \sum_l K_{i,l} \frac{1}{x_l} K_{j,l}$ (1)

is the weighted Laplacian. For simplicity, we assume identity reactance on all links $x_l = 1$.

(a) Compute the *voltage angles* θ_j and *flows* f_l for the first hour in the dataset with the convention of $\theta_0 = 0$; i.e. the slack bus is at node 0.

Remark: Linear equation systems are solved efficiently using numpy.linalg.solve.

(b) Determine the average flow on each link for 01-2017 and draw it as a directed network.

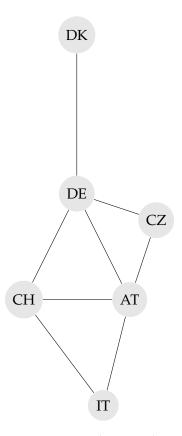


Figure 2: Simple Network

¹https://transparency.entsoe.eu/transmission-domain/physicalFlow/show