Energy System Modelling

Karlsruhe Institute of Technology Institute for Automation and Applied Informatics Summer Term 2020

TUTORIAL I: TIME SERIES ANALYSIS

Will be worked on in the exercise session on Thursday, 4 June 2020.

Problems which are discussed in the tutorial are marked with \(\begin{aligned} \\ \\ \ext{\text{2}} \end{aligned}. \)

Exercises to study at home are marked with

Questions on both kind of tasks are answered in the tutorial and **all exercises are** relevant for the exam.

PROBLEM I.1 (PROGRAMMING) – DATA ANALYSIS

The following data are made available to you on the course home page¹ and the github repository ²:

They describe (quasi-real) time series for wind power generation W(t), solar power generation S(t) and load L(t) in Great Britain (GB), Germany (DE) and Europe (EU). The time step is 1 h and the time series are several years long.

- (a) Check that the wind and solar time series are normalized to 'per-unit of installed capacity', and that the load time series is normalized to MW.
- (b) For all three regions, calculate the maximum, mean, and variance of the time series.
- (c) For all three regions, plot the time series W(t), S(t), L(t) for a winter month (January) and a summer month (July).
- (d) Resample the time series to daily, weekly and monthly data points and visualise them in plots. Can you identify some recurring patterns?
- (e) For all three regions, plot the duration curve for W(t), S(t), L(t).
- (f) For all three regions, plot the probability density function of W(t), S(t), L(t).
- (g) Recurring patterns of time series can also be visualised more rigorously by applying a Fourier Transform. Apply a (Fast) Fourier Transform to the three time series $X \in W(t)$, S(t), L(t):

$$\tilde{X}(\omega) = \int_0^T X(t)e^{\mathrm{i}\omega t} \,\mathrm{d}t$$
.

For all three regions, plot the energy spectrum $|\tilde{X}(\omega)|^2$ as a function of ω . Discuss the relationship of these results with the findings obtained in (b)-(f).

¹https://nworbmot.org/courses/esm-2020/

²https://github.com/lisazeyen/ESM_tutorial/tree/master/tutorial/01-tutorial-04. 06.2020/notebooks/data

(h) Normalize the time series to one, so that $\langle W \rangle = \langle S \rangle = \langle L \rangle = 1$. Now, for all three regions, plot the mismatch time series

$$\Delta(t) = \gamma \alpha W(t) + \gamma (1 - \alpha) S(t) - L(t)$$

for the same winter and summer months as in (c). Choose $\alpha \in \{0.0, 0.5, 0.75, 1.0\}$ with $\gamma = 1$, and $\gamma \in \{0.5, 0.75, 1.0, 1.25, 1.5\}$ with $\alpha = 0.75$.

Which configuration entails the lowest mismatch on average and in extremes?

(i) For all three regions, repeat (b)-(g) for the mismatch time series.

PROBLEM I.2 (ANALYTICAL) – EFFECT OF SEASONALITY A

Figure 1 shows approximations to the seasonal variations of wind and solar power generation W(t) and S(t) and load L(t):

$$W(t) = 1 + A_W \cos \omega t$$

$$S(t) = 1 - A_S \cos \omega t$$

$$L(t) = 1 + A_L \cos \omega t$$

The time series are normalized to $\langle W \rangle = \langle S \rangle = \langle L \rangle := \frac{1}{T} \int_0^T L(t) dt = 1$, and the constants have the values

$$\omega = \frac{2\pi}{T}$$
 $T = 1 \text{ year}$ $A_W = 0.4$ $A_S = 0.75$ $A_L = 0.1$

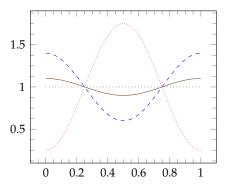


Figure 1: Seasonal variations of wind and solar power generation W(t) - - and S(t) —, and load L(t) — around the mean 1 —.

(a) What is the seasonal optimal mix α , which minimizes

$$\langle [\alpha W(t) + (1 - \alpha)S(t) - L(t)]^2 \rangle = \frac{1}{T} \int_0^T [\alpha W(t) + (1 - \alpha)S(t) - L(t)]^2 dt,$$

- (b) How does the optimal mix change if we replace $A_L \rightarrow -A_L$?
- (c) Now assume that there is a seasonal shift in the wind signal

$$W(t) = 1 + A_W \cos(\omega t - \phi).$$

Express the optimal mix α as a function of ϕ .

(d) A constant conventional power source $C(t) = 1 - \gamma$ is now introduced. The mismatch then becomes

$$\Delta(t) = \gamma \left[\alpha W(t) + (1 - \alpha)S(t) \right] + C(t) - L(t).$$

Analogously to (a), find the optimal mix α as a function of $0 \le \gamma \le 1$, which minimizes $\langle \Delta^2 \rangle$.