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1) For script $\chi^2 = 15264.645$. This is generally not considered to be acceptable

With the new parameters $\chi^2 = 3272.57$.

$$\text{mean} = 2561, \sigma = \sqrt{2(2561)} \quad \text{mean} + 4\sigma = \chi^2 \rightarrow \frac{\chi^2 - \text{mean}}{\sigma}$$

15264.645 is ~ 180 sigma from the mean.

3272.57 is ~ 11 sigma from the mean. A clear improvement

2) Find best fit params using LM or Newton numerical derivatives

Newton's $A_m^T N^{-1} A_m d_m = A_m^T N^{-1} r$

LM:

$$[A_m^T N^{-1} A_m + \lambda \text{diag}(1)] d_m = A_m^T N^{-1} r$$

("step works" $\rightarrow \chi^2 \nless inc$)

$$d_m = (A_m^T N^{-1} A_m)^{-1}$$

\hookrightarrow derivative matrix

do derivative for each parameter separately, pick

$dx = 0.01 x_i$ where x_i is the value of the param you're changing

$$3) \Omega_A = 1 - \Omega_B - \Omega_C$$

$$C_{\text{chain}}(1) = R_0 h^2 \quad C_{\text{chain}}(2) = R_0 h^2$$

$$h = \frac{h_0}{100} \quad \swarrow C_{\text{chain}}(\omega)$$

$$\Omega_A = 1 - \frac{C_{\text{chain}}(1)}{h^2} - \frac{C_{\text{chain}}(2)}{h^2}$$

$$\text{err.} \quad \frac{\text{err}(1)}{h^2} \pm \frac{\text{err}(2)}{h^2}$$

Dark energy is 0.697 ± 0.008 .

The chains are not yet converged. This is likely due to the inferiority of Newton's method as opposed to Levenberg Marquadt. However, as can be seen from the zoomed in chisq image, chisq is approaching a nice like behaviour, meaning that it is on its way to converging.

4)

I used Levenberg Marquadt with importance sampling to re-estimate the covariance matrix.

When comparing the answer to importance sampled problem 3 the chsq from importance sampling prob 3 is actually marginally improved and the errors are smaller.