

ELEG 2202A Homework 4Due: 11:59 pm, Dec. 7, 2020 (**Monday**) (HKT)Submission: Please submit your answer (**PDF ONLY**) through the **Blackboard** system.

You are required to show the steps of your calculations, otherwise, marks will be deducted.

If you have questions about this homework, please send an email to minglei@link.cuhk.edu.hk.

Q1. Obtain the power factor of the circuit in Fig. 1 (seen from points a and b), please also specify the factor as leading or lagging. **(20)**

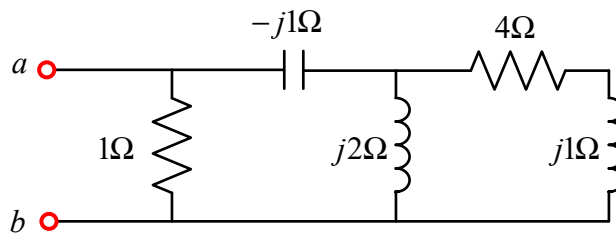


Fig. 1

Q2. For the circuit shown in Fig. 2, $V_s = 200\sqrt{2} \cos(\omega t)$, $\omega = 100 \text{ rad/s}$, $L = 10 \text{ mH}$, $R = 10 \Omega$, $C = 5 \text{ mF}$, Solving: **(30)**

- 1) Active and reactive power drawn from source;
- 2) Apparent power from the source;
- 3) Power factor seen from the source;
- 4) If the value of C (capacitor) is unknown, and other parameters keep unchanged, please find the proper value of C to make the power factor equals to 1.

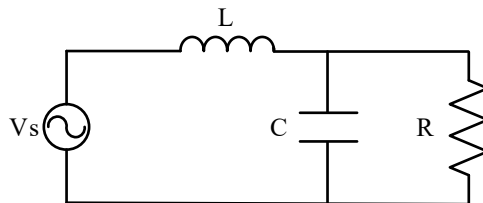


Fig. 2

Q3. In Fig.3, $V_p = 100\sqrt{2}$ V, $R = 1 \Omega$, $L = 10$ mH, $\omega = 100$ rad/s. Solving: (25)

1) I_{aA} , I_{bB} , I_{cC} , and V_{Nn} ;

2) Make Y- Δ transformation on both the source side and load side, draw the circuit and compute the value of each load and source (please mark on the circuit as well).

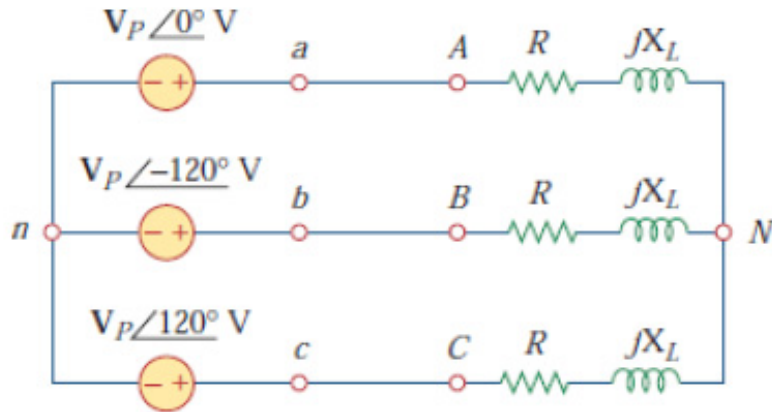


Fig. 3

Q4. In Fig. 4, $v_{s1} = 5$ V; $v_{s2} = 3$ V, please determine the value of v_o . (25)

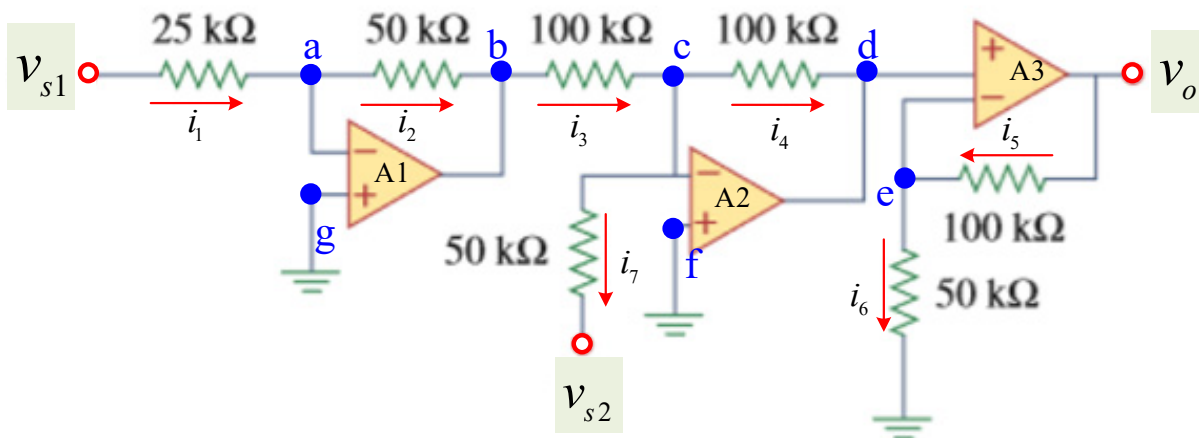
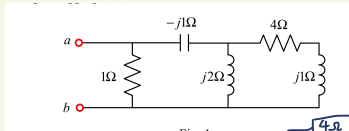


Fig. 4

1.)



∴ for above side,

let Z_{j1} be in above side,

$$\begin{aligned}
 Z_{j1} &= \frac{(4\Omega + j1\Omega)j2}{4\Omega + j1 + j2} + -j1 = \frac{(4+j)(j2)}{4+j3} + -j1 \\
 &= \frac{(4+j)(j2) + (-j)(4+j3)}{4+j3} \\
 &= \frac{j2 \cdot 4 + j2 \cdot j - j4 - j \cdot j3}{4+j3} \\
 &= \frac{j8 - 2 - j4 + 3}{4+j3} \\
 &= \frac{1+j4}{4+j3}
 \end{aligned}$$

Z_{j1} is parallel with 1Ω

$$\begin{aligned}
 \therefore Z_F &= \frac{1 \cdot \left(\frac{1+j4}{4+j3}\right)}{1 + \frac{1+j4}{4+j3}} = \frac{1+j4}{4+j3+1+j4} = \frac{1+j4}{5+j7} \cdot \left(\frac{5-j7}{5-j7}\right) = \frac{33+j13}{74}
 \end{aligned}$$

For impedance,

$$\begin{aligned}
 Z &= R + jX \\
 &= \frac{33}{74} + \frac{j13}{74}
 \end{aligned}$$

$$\begin{aligned}
 \therefore |Z| &= \sqrt{\left(\frac{33}{74}\right)^2 + \left(\frac{13}{74}\right)^2} \\
 &= 0.4793
 \end{aligned}$$

$$\begin{aligned}
 \therefore \cos\theta &= \frac{33}{74} / 0.4793 \\
 &= 0.9304
 \end{aligned}$$

$$\begin{aligned}
 \therefore \text{Power factor} &= 0.9304 \\
 &> 0
 \end{aligned}$$

∴ It is lagging Power factor

Q2. For the circuit shown in Fig. 2, $V_s = 200\sqrt{2} \cos(\omega t)$, $\omega = 100 \text{ rad/s}$, $L = 10 \text{ mH}$, $R = 10 \Omega$, $C = 5 \text{ mF}$, Solving: **(30)**

- 1) Active and reactive power drawn from source;
- 2) Apparent power from the source;
- 3) Power factor seen from the source;
- 4) If the value of C (capacitor) is unknown, and other parameters keep unchanged, please find the proper value of C to make the power factor equals to 1.

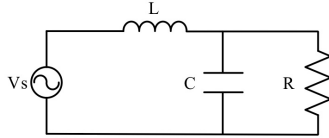


Fig. 2

$$V_s = 200\sqrt{2} \cos(\omega t), \omega = 100 \text{ rad/s}, L = 10 \text{ mH}, R = 10 \Omega, C = 5 \text{ mF}$$

$$V_{\text{rms}} = 200$$

$$jX_C = \frac{1}{j\omega C} = \frac{1}{j100 \cdot 5 \cdot 10^{-3}} = -j2 \Omega$$

$$jX_L = j\omega L = j \cdot 100 \cdot 10 \cdot 10^{-3} = j\Omega$$

$$Z_{\text{Total}} = \frac{-j2(10)}{-j2+10} + j = \frac{-j20}{10-j2} \cdot \frac{(10+j2)}{(10+j2)} + j$$

$$= \frac{-j200+40}{104} + j$$

$$= \frac{5-j25}{13} + j$$

$$= \frac{5}{13} - \frac{j25}{13} + j$$

$$\therefore I = \frac{200}{\frac{5}{13} - \frac{j25}{13} + j} = 200 \angle 67.38^\circ \text{ A}$$

$$\text{Active Power, } P = V_s I_s \cos \theta$$

$$= 200 \cdot 200 \cos(67.38^\circ)$$

$$= 15.385 \text{ kW}$$

$$\text{Reactive Power, } Q = V_s I_s \sin \theta$$

$$= 200 \cdot 200 \sin(67.38^\circ)$$

$$= 36.92 \text{ kVAr}$$

$$\text{Apparent Power, } |S| = |V| |I|$$

$$= 200 \cdot 200$$

$$= 40 \text{ kVA}$$

$$\text{Power factor} = \cos(67.38^\circ) = 0.375$$

For C unknown, and power factor equal zero, the θ should be zero so the imaginary part is zero.

$$\text{We set } C \text{ as } \frac{-j}{100} C$$

$$Z_{\text{Total}} = j + \frac{10 \left(\frac{-j}{100} C \right)}{10 - \frac{j}{100} C}$$

$$= j - \frac{j10}{(1000C)} \cdot \frac{1000C+j}{1000C+j}$$

$$= j - \frac{j10(1000C+j)}{(1000C)^2 + 1}$$

$$= j - \frac{j10000C}{(1000C)^2 + 1} + \frac{10}{(1000C)^2 + 1}$$

$$\text{For Imag Part} = 0$$

$$j - \frac{j10000C}{(1000C)^2 + 1} = 0$$

$$\therefore 10^6 C^2 - 10^4 C + 1 = 0$$

$$\therefore C = 9.819 \cdot 10^{-3} \text{ or } 1.01 \cdot 10^{-4} \text{ F}$$

Q3. In Fig.3, $V_p = 100\sqrt{2}$ V, $R = 1 \Omega$, $L = 10$ mH, $\omega = 100$ rad/s. Solving: (25)

1) I_{aA} , I_{bB} , I_{cC} , and V_{NN} ;

2) Make Y- Δ transformation on both the source side and load side, draw the circuit and compute the value of each load and source (please mark on the circuit as well).

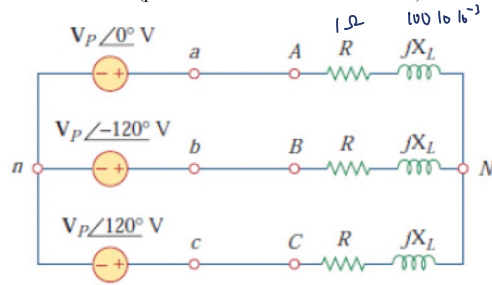
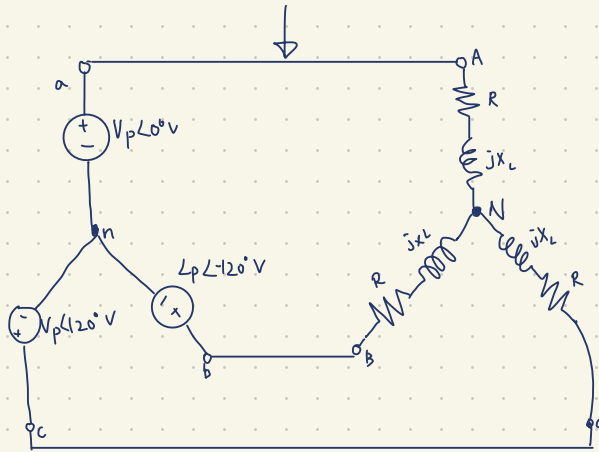


Fig. 3



$$jX_L = j\omega L$$

$$= j(100)(10 \cdot 10^{-3}) = j$$

$$R = 1 \Omega$$

\therefore Each Impedance is $(1 + j)\Omega$

$$I_{aA} = \frac{100\sqrt{2}\angle 0^\circ}{(1 + j)} = 100\angle -45^\circ \text{ A}$$

$$I_{bB} = 100\angle -165^\circ \text{ A}$$

$$I_{cC} = 100\angle 75^\circ \text{ A}$$

$$\therefore I_{NN} = I_{aA} + I_{bB} + I_{cC}$$

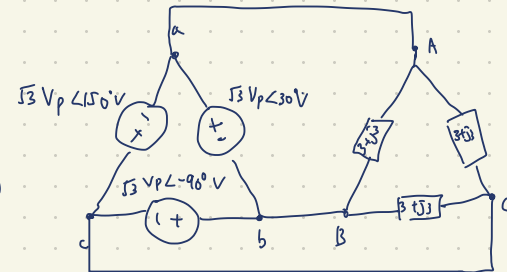
$$= 0 \text{ A}$$

$$\therefore V_{NN} = 0 \text{ V}$$

For Z_Δ in N,

$$Z_\Delta = 3(1 + j)$$

$$= 3 + j3$$



Q4. In Fig. 4, $v_{s1} = 5 \text{ V}$; $v_{s2} = 3 \text{ V}$, please determine the value of v_o . (25)

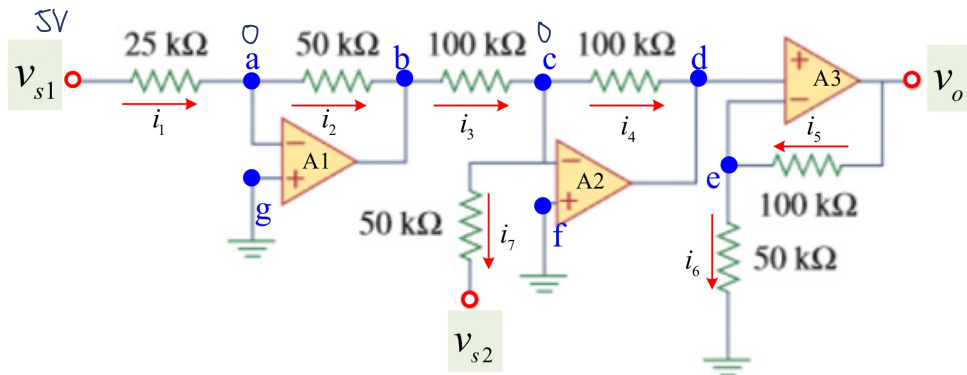


Fig. 4

For ideal Op.Amp,

voltage of two input is the same.

Since node g & node f connect to grd,

$\therefore V$ at node a (V_a) = 0V

V at node c (V_c) = 0V

Let V_b & V_d be the voltage at node b & d

$$\frac{0 - V_{s1}}{25k} + \frac{0 - V_b}{50k} = 0$$

$$\frac{-V_{s1}}{25k} = \frac{V_b}{50k}$$

$$V_b = -2V_{s1} \\ = -10$$

$$\frac{0 - V_b}{100k} + \frac{0 - V_{s2}}{50k} + \frac{0 - V_d}{100k} = 0$$

$$\therefore V_d = -V_b - 2V_{s2}$$

$$= -(-10) - 2(3) \\ = 4V$$

$$V_d = \frac{V_o \cdot 50k}{100k + 50k}$$

$$V_o = 3V_d$$

$$\therefore V_o = 3 \cdot 4V \\ = 12V$$