

# Lenses from the ground up

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# What is a Lens?

Good question!

- A pure functional approach to manipulating both the content and structure of (often) deeply-nested data structures.

# Why use a Lens?

Another good question!

- Provides a powerful mechanism for manipulating data structures, and composing these manipulations to perform higher-order operations.

# Let's take a step back!

- The focus of this talk will be on exploring some *very basic* lens(-like) operations.
- Our goal is to gain an intuitive understanding of what lenses *are*, and how they work.
- The lenses we define here are not quite the same as *real* lenses. They are much simpler, and much less powerful.

# Tuples

Let's start with something simple: *tuples*.

A *tuple* is just two associated values wrapped up, so that you can treat it as one *thing*.

```
> (1, 2)  
(1, 2)
```

```
> (, ) 42 42  
(42, 42)
```

```
> :t (, )  
(, ) :: a -> b -> (a, b)
```

# Tuples

Let's define `get` and `set` functions for the *first* element of the tuple, i.e. here: `(1,2)`.

```
-- retrieve the value x
get1 :: (x, y) -> x
get1 (x, _) = x

-- replace the value x with x'
set1 :: x' -> (x, y) -> (x', y)
set1 x' (_, y) = (x', y)
```

# Tuples

```
> get1 (1, 2)  
1
```

```
> set1 10 (1, 2)  
(10, 2)
```

# Tuples

Similarly we can define `get` and `set` functions for the *second* element of the tuple, i.e. (1,2)

```
get2 :: (x, y) -> y  
get2 = snd
```

```
set2 :: y -> (x, y) -> (x, y)  
set2 y' (x, _) = (x, y')
```



# Tuples

```
> get2 (1, 2)  
2
```

```
> set2 0 (1, 2)  
(1, 0)
```

None of this has anything to do with *Lens* ... it's just vanilla *pattern matching*.

# Defining a Lens

Using standard record syntax, define a type constructor called `Lens`

```
data Lens a b =  
  Lens { get :: a -> b  
        , set :: b -> a -> a  
        }
```

To create a *Lens*, you need to pass two functions, one of type `a -> b`, and the other of type `b -> a -> a`.

# Defining a Lens

Hey, we already have some!

```
get1 :: (x, y) -> x  
set1 :: x -> (x, y) -> (x, y)
```

Here the tuple type  $(x, y)$  corresponds to  $a$ , and  $x$  corresponds to  $b$  (in `Lens a b`).

In Lens terminology, we call  $a$  the *object*, and we call  $b$  the *focus*.

# Defining a Lens

So, let's make a *lens* ...

```
_1 = Lens get1 set1
```

# Defining a Lens

Recall from Haskell record syntax, we automatically get *helper methods* for each named record field.

```
> :t get
Lens a b -> a -> b
--
--           ^^^^
--           |-- this is the signature of get1

> :t set
Lens a b -> b -> a -> a
--
--           ^^^^^^^
--           |-- this is the signature of set1
```

# Using a lens

Before, we had

```
> get1 (1, 2)  
1
```

Now with our lens, we have

```
> get _1 (1, 2)  
1
```

# Using a lens

Similarly, before we had

```
> set1 5 (1,2)  
(5,2)
```

Now with our lens, we have

```
> set _1 5 (1,2)  
(5,2)
```

# Using a lens

We have decoupled the `set` and `get` operations from the specific location on which they operate.

Intuitively, this sounds like a good thing, right?

I think so.



# Using a lens

Let's make another lens ...

```
_2 = Lens get2 set2
```

Alternatively (and perhaps more typically), we can use *anonymous* functions rather than named ones.

```
_2 = Lens (\(_, y) -> y) (\y (x, _) -> (x, y))
```

# Using a lens

```
> get _2 (1, 2)  
2
```

```
> set _2 5 (1, 2)  
(1, 5)
```

# Is that all?

# NO!

# Lens composition

Lenses *compose*!

```
-- Define a composition operator (>-) ...  
  
(>-) :: Lens a b -> Lens b c -> Lens a c  
  
(>-) l1 l2 = Lens (get l2 . get l1) $  
                  (\part whole -> set l1 (  
                      set l2 part (get l1 whole)) whole)
```

Admittedly, composing set is a little funky!

# Lens composition

Let's do it!

```
_1_1 = _1 >- _1
```

```
_1_2 = _1 >- _2
```

```
-- Looking at the types can be helpful!
```

```
> :t _1_1
_1_1 :: Lens ((c, b1), b) c
--      ^^^      ^^^
```

```
> :t _1_2
_1_2 :: Lens ((a, c), b) c
--      ^^^      ^^^
```

# Lens composition

```
> get _1_1 ((1,2),(3,4))  
1
```

```
> get _1_2 ((1,2),(3,4))  
2
```

```
> set _1_1 5 ((1,2),(3,4))  
((5,2),(3,4))
```

```
> set _1_2 5 ((1,2),(3,4))  
((1,5),(3,4))
```

# Is that all?

# NO!

# Shortcut operators

$(.\sim) :: \text{Lens } a \ b \rightarrow b \rightarrow a \rightarrow a$

$(.\sim) = \text{set}$

`infixr 4 .~`

$(^.) :: a \rightarrow \text{Lens } a \ b \rightarrow b$

$(^.) = \text{flip get}$

`infixl 8 ^.`



# Shortcut operators

-- Get

```
> (1,2) ^. _1  
1
```

```
> (1,2) ^. _2  
2
```

-- Set

```
> _1 .~ 4 $ (1,2)  
(4,2)
```

```
> _2 .~ 5 $ (1,3)  
> (1,5)
```

# Over

over is like fmap for a lens

```
over :: Lens a b -> (b -> b) -> a -> a
over l f a = set l (f (get l a)) a
(%~) = over
infixr 4 %~
```

```
> _1 %~ (*2) $ (3,2)
(6,2)
```

```
> _2 %~ (*2) $ (3,2)
(3,4)
```

# Lens Laws

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execrabilis ista turba, quae non  
novit legem

— Francis Bacon

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# Lens Laws

Three of them.

1. Get-Set Law
2. Set-Get Law
3. Set-Set Law

## Get-Set Law

```
get_set_law :: Eq a => Lens a b -> a -> Bool
get_set_law l =
  \a ->
    set l (get l a) a == a
```

Doing a `set` using a value obtained from a `get` is equivalent to doing *nothing at all*.

# Get-Set Law

```
> get_set_law _1 (3,2)
True
> get_set_law _1 (99,23)
True
> get_set_law _1 (1,2)
True
```

## Basically equivalent to

```
> let v = (1,2) ^. _1 -- get
> _1 .~ v $ (1,2) -- set
(1,2)
```

## Set-Get Law

```
set_get_law :: Eq b => Lens a b -> b -> a -> Bool
set_get_law l =
  \s a ->
    get l (set l s a) == s
```

**Doing a set operation followed by a get operation returns the value that was set.**



## Set-Get Law

```
> set_get_law _1 5 (1,2)
True
> set_get_law _1 5 (3,2)
True
> set_get_law _1 5 (2,1)
True
```

## Set-Set Law

```
set_set_law :: Eq a => Lens a b -> b -> b -> a -> Bool
set_set_law l =
  \s1 s2 a ->
    set l s2 (set l s1 a) == set l s2 a
--      ^^^^^^^^^ ^^^^^^^^^^^^^^^^^
--      |           |- first (inner) set operation (s1)
--      |- second (outer) set operation (s2)
```

**If perform one set operation (s1) followed by a second set operation (s2), only the result of the second operation is preserved.**

# Set-Set Law

```
> set_set_law _1 12 24 (1,2)
True
```

## Basically equivalent to

```
-- First set operation (s1)
> _1 .~ 12 $ (1,2)
(12,2)

-- Second set operation (s2)
> _1 .~ 24 $ (12,2)
(24,2)

-- (12,2) is gone!
```

**Is that all?**

*Cue laughter!*

We're just getting started.

# References / Next Steps

1. David Peterson, [Lets.TupleLens](#) (code for this talk!)
2. Tony Morris, [Let's Lens](#) (a whole lens course!)
3. Gabriel Gonzales, [Control.Lens.Tutorial](#) (on hackage)
4. Joseph Abrahamson, [A Little Lens Starter Tutorial](#)