

## RESEARCH ARTICLE

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# Distributed manufacturing for electrified chemical processes in a microgrid

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**Abstract**

To alleviate the greenhouse gas emissions by the chemical industry, electrification has been proposed as a solution where electricity from renewable sources is used to power processes. The adoption of renewable energy is complicated by its spatial and temporal variations. To address this challenge, we investigate the potential of distributed manufacturing for electrified chemical processes installed in a microgrid. We propose a multiscale mixed-integer linear programming model for locating modular electrified plants, renewable-based generating units, and power lines in a microgrid that includes monthly transportation and hourly scheduling decisions. We propose a K-means clustering-based aggregation disaggregation metaheuristic to solve the model efficiently. The model and algorithm are tested using a case study with 20 candidate locations in Western Texas. Additionally, we define a new concept, “the Value of the Multi-scale Model,” to demonstrate the additional economic benefits of our model compared with a single-scale model.

**KEYWORDS**

distributed manufacturing, electrification, mathematical optimization, multiscale integration

## 1 | INTRODUCTION

Chemical industries are a major source of greenhouse gas emissions and are responsible for 7% of the global greenhouse gas emissions<sup>1</sup> as they are mostly powered by the combustion of fossil fuels. To alleviate greenhouse gas emissions, electrification of the chemical industry is a promising solution that is currently being explored by chemical engineers.<sup>2,3</sup> Electrification helps decarbonize the chemical industry and transition from fossil fuels to more renewable energy sources such as solar and wind. Electrification can be done in different parts of a process, including reactions, such as in electrochemical reactions,<sup>4</sup> and heating, such as in resistive heating.<sup>3</sup>

The major technical challenge to transitioning to renewable-based processes is that renewable resources, including solar and wind, have high spatial and temporal variations. A good way to take advantage of these

variations is to adopt the concept of Distributed Chemical Manufacturing (DCheM). DChEM aims to improve chemical process industries by developing modular process plants, which take advantage of distributed resources and address distributed environmental problems. DChEM paves the way for introducing numerous new process technologies and simultaneously supports and enables energy and environmental sustainability while reducing chemical transportation costs. Modular processes increase the flexibility in dealing with the variability of conditions.<sup>5-8</sup>

While work has been done on the design and optimization of electrified plants and on the supply chain optimization of a particular set of chemicals produced by electricity, the combination of spatial and temporal variations (across different time scales) of renewable power-generating units has rarely been exploited with distributed manufacturing. Thus, there is a need to model both spatial and temporal features across time scales for electrified chemical processes and

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integrate the planning of the power resources with it. In this article, we address this gap where we model a network of electrified chemical plants and power-generating units with three-time scales, that is, single-time, monthly, and hourly. The problem is considered under the context of a microgrid, which typically consists of a network of low-voltage power-generating units, storage devices, and loads capable of supplying a local area such as a suburban area, an industrial park, or any commercial area with electric power and heat.<sup>9</sup> Microgrids support flexible operations, strengthen grid resilience and reduce energy losses making the electric power system efficient.<sup>10</sup> The location or point at which the microgrid is connected to the power utility is called the point of common coupling. Power can be purchased or sold to the power utility at the point of common coupling.

This article aims to design a network to facilitate DChEM for electrified chemical processes with the power demand satisfied by renewable sources and power from an external source coordinated by a microgrid operator by using a mixed-integer linear programming (MILP) model. The model incorporates both the electricity network (generating units and power lines) and chemical plant expansion in a single model. The transportation of chemicals and the transmission of power are two competing energy transportation approaches that are both captured in the lower-level decisions. Therefore, the tradeoffs between the transportation of chemicals and the transmission of power are studied. The model has more than millions of variables and constraints and is very difficult to solve directly using an MILP solver. To solve the model efficiently, we propose a tailored algorithm that combines mathematical programming and heuristics. Mathematical programming involves the study of techniques that can be used to generate provable optimal solutions to optimization problems. From a practical standpoint, the field of heuristics has a similar goal: to generate near-optimal and feasible solutions to optimization problems despite the lack of optimality guarantees. *Matheuristics*<sup>11</sup> are algorithms that combine mathematical programming and heuristics. Examples of matheuristics include local branching,<sup>12</sup> and feasibility pump<sup>13</sup> that have been implemented in mixed-integer programming solvers such as CPLEX,<sup>14</sup> and DICOPT.<sup>15</sup> Matheuristics are different from metaheuristic methods like the genetic algorithm and simulated annealing as matheuristic methods integrate mathematical programming techniques to construct solutions. The algorithm we propose in this article is a decomposition-based matheuristic, where we break down the problem into a sequence of subproblems where each subproblem is modeled as a mathematical program and solved to optimality. The major contributions of this article are listed below:

1. The proposed model encompasses three-time scales taking into account investment decisions, as well as monthly decisions and hourly decisions, and thus captures the temporal and spatial variations.
2. The size of the model can easily exceed millions of variables. We develop a tailored aggregation-disaggregation algorithm to solve the model efficiently, which is applicable to any multiscale facility location problem.
3. We propose a new concept, “the Value of the multiscale Model” (VMM), as a quantitative metric to characterize the additional economic savings of the multiscale model (MM) compared with a single-scale model that ignores the temporal variations.

4. The proposed model and algorithms are made available as open-source software through our GitHub repository EDChEM.jl with URL: <https://github.com/li-group/EDChEM.jl>

The rest of this article is organized as follows. In Section 2, a literature review of related works is provided. In Section 3, we describe the problem and the main assumptions. In Section 4, we describe the proposed algorithm. In Section 5, the definition of the VMM is described. In Section 6, we illustrate the benefits of the proposed model and the effectiveness of the proposed solution techniques. The conclusions are drawn in Section 7.

## 2 | LITERATURE REVIEW

A number of works have been done in the optimization of the electrified production of various chemicals. Some work has been done with a focus on optimizing the design of processes.<sup>16–25</sup> For example, Lazouski et al.<sup>16</sup> carried out a techno-economic analysis of the cost-optimal design and operation of a fully electrified ammonia generation process that utilizes intermittent renewable energy sources by modeling it as a MILP model. Sánchez and Martín<sup>17</sup> modeled the scale-up and scale-down of a renewable ammonia-based facility considering different technologies as a mixed-integer nonlinear programming (MINLP) model. Cooper et al.<sup>18</sup> developed a framework to optimize the design and operation of a large-scale electrolyzer hub under a variable power supply. Demirhan et al.<sup>19</sup> presented a process synthesis and global optimization framework for efficiently using renewable resources in ammonia production, where competing technologies were incorporated in a process superstructure.

Several works have been done with a focus on optimizing the scheduling of electrified processes.<sup>26–34</sup> For example, Brée et al.<sup>26</sup> formulated and solved a model for the optimal scheduling of a chloralkali plant operating under different modes utilizing Demand Side Management. Allman and Daoutidis<sup>27</sup> developed a formulation for the optimal scheduling for a renewable ammonia plant. Bødal and M. Korpås<sup>28</sup> developed a two-stage stochastic model in a rolling horizon framework to consider uncertainties and used the model to study hydrogen production from electrolysis in a future scenario of a remote region in Norway with a focus on scheduling. Zheng et al.<sup>29</sup> modeled and optimized the operation of a grid-connected power-to-methanol system considering its flexibility.

For supply chain optimization of electrified plants, He et al.<sup>35</sup> developed a supply chain planning model that determines the least cost of hydrogen generation, storage, transmission, and compression facilities to meet hydrogen demand and is combined with power systems through electricity prices with the location of the renewable power-generating units fixed beforehand. Welder et al.<sup>36</sup> worked on potential future energy systems for power-to-hydrogen applications in Germany by developing a supply chain optimization model which takes the spatial and temporal resolution of the energy system into account with power through power lines not considered. These models consider the hourly demand as opposed to the monthly demand. Li et al.<sup>37</sup> proposed a co-planning approach for the regional wind resources-based ammonia industry and the electric network to

optimize the wind-to-ammonia configuration and the expansion of the electrical network with ammonia demand being satisfied locally rather than transporting ammonia and for a one-time demand. Other papers have also considered supply chain optimization of electrified plants.<sup>38–42</sup> All these papers do not consider mode-based production of chemicals as well as local microgrid-based production, and most of them also do not consider multiple time scales and multiple products (chemicals) requirements in a network.

The co-expansion of the chemical and electricity network, like Reference 37, is a less explored area. Another area that has not been studied in the electrification of the chemical industry is utilizing three-time scales in the optimization model—single time, monthly, and hourly. This is important because the output of renewable resources such as wind and solar varies hourly and by location, while the chemical delivery contract typically varies monthly. Multiple time scales have been explored in other areas, such as in the production of bioproducts<sup>43</sup> or in more general energy planning problems, such as Reference 44, where the focus was more on central planning of the power utility as opposed to regional planning of microgrids.

As for algorithm development for solving integrated planning and scheduling models, Reinert et al.<sup>45</sup> proposed an algorithm to solve multitime scale large-scale energy planning problems. Maravelias and Sung<sup>46</sup> reviewed techniques that can be used in integrating planning and scheduling. Li et al.<sup>47</sup> propose a tailored Benders decomposition algorithm for a multiscale power systems planning problem. Allen et al.<sup>48</sup> propose improvements to decomposition algorithms by adding valid inequalities for multiscale energy systems planning problems.

### 3 | PROBLEM STATEMENT

We first provide a general problem statement. An illustrative example shown in Figure 1 will be explained in detail after the generic description. We take the role of a company/conglomerate planning to invest in a regional microgrid or an industrial park. Our network has a set of consumers and suppliers of electrically produced chemical products, a point of common coupling (the location at which the microgrid is connected to the power utility), and a set of candidate locations. We can set up modular chemical plants or/and power-generating units at each candidate location. Modular chemical plants can be selected from several given technologies that involve electrochemical processes. For each plant, we are given the chemicals involved, the associated electrochemical reactions under different operating modes, and the equations to determine the power requirements. The modular power-generating units are all renewable, like solar panels and wind turbines. The capacity factors of the power-generating units for several historical years on an hourly basis are given. Power lines can be installed between any two different locations or between any of the locations and the point of common coupling, whose location is predetermined. The time span of our problem is a given year.

Raw materials are obtained from suppliers with predetermined locations and transported to the installed chemical plants on a monthly basis. The required chemicals are produced in the plants

and transported to consumers in certain given locations on a monthly basis. The electrochemical reactions in the plants consume the power obtained through the connected power lines. The consumed power can come from the installed generating units. In addition, when the microgrid produces excess electricity, the excess electricity can be sold to the electric utility through the point of common coupling. On the other hand, the microgrid operator has the option of purchasing electricity from the electric utility as well. The monthly demand forecasts for each chemical for each of the consumers are given. In addition, we are given the resistance and inductance of the candidate power lines, the electricity price at each hour, the variable transportation costs, the capital cost of all the generating units, plants, and power lines, and the cost of different chemicals. We are also given the limits on production rates in different plants, as well as the capacity for power transmission in power lines, and the capacity for power generation of the generating units.

The proposed MILP model makes decisions across three-time scales: investment decisions at the beginning of the time horizon, monthly delivery of the chemical products to the customers as well as the monthly purchase of raw materials, and hourly operating decisions of chemical plants, power-generating units and power through power lines. To simplify the problem, we consider one year of operating decisions. The investment decisions include

- which chemical plants and power-generating units to install and the locations to install them,
- which power lines should be installed.

The monthly decisions include

- the amount of each chemical sold from each plant to each consumer,
- the amount of each chemical purchased from each supplier,
- the amount of consumer demand that is satisfied by other vendors,
- the amount of chemicals stored in the inventory of each plant at the end of each month.

The hourly operating decisions include

- the power flow of all the installed power lines,
- the amount of power required by each of the plants,
- the amount of each chemical produced in each plant,
- the mode at which each chemical plant operates,
- the amount of net electricity purchased/sold from/to the utility.

As an illustrative example, in the region considered, as shown in Figure 1, we are given three candidate locations denoted by rectangles. Three modular technologies, including chemical plants, wind turbines, and solar panels, are given, with the maximum number of each technology that can be installed in the network being one. Also, in the region shown, there are two consumers and two suppliers of raw materials and a point of common coupling whose locations are known.

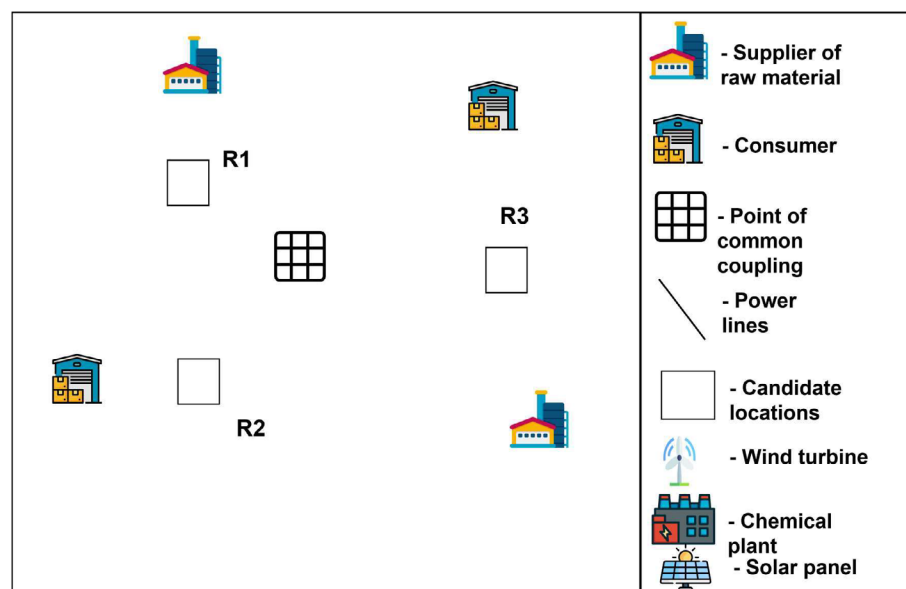


FIGURE 1 Region representation.

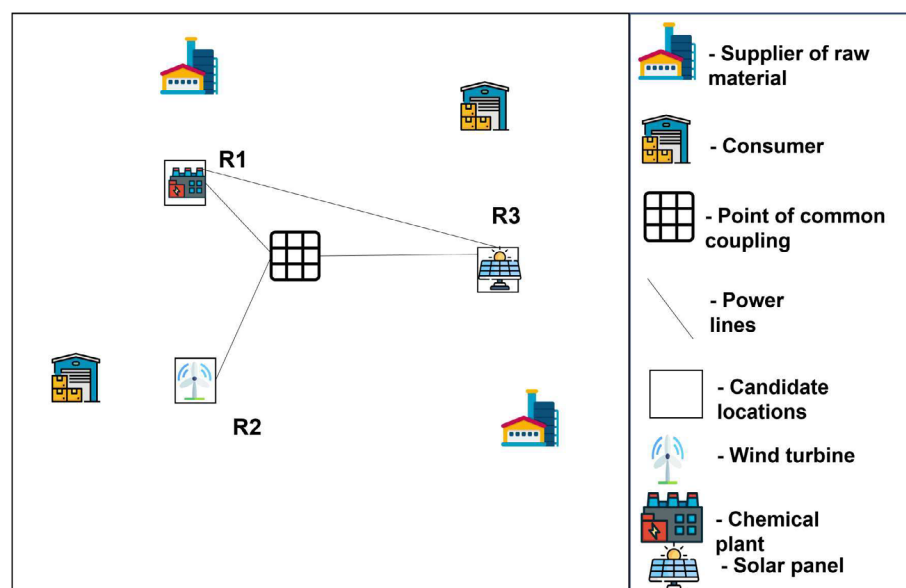
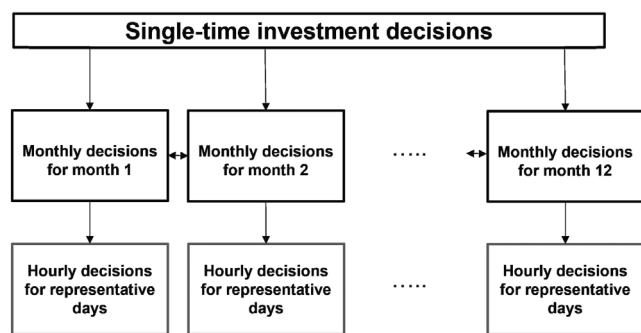


FIGURE 2 Solution representation.

Power lines can be installed between any two different locations and between any of the locations and the point of common coupling. A solution to the problem is shown in Figure 2. In the solution, one chemical plant is placed at R1, one solar panel at R3, and one wind turbine at R2 to meet the demand of the consumers most economically with appropriate power lines connected.

The assumptions we make are the following:

- The capacities of each type of modular plant and generating unit are assumed to be fixed to their standard values.
- At most, one reaction takes place in each electrochemical process at a particular time.
- The power lines in the network are of the same type, that is, have the same base voltage and base power.
- The chemical plant undergoes a mode-based operation.
- The time subperiods are hours.
- The transportation cost for transporting a specific amount of chemical is a linear function of the distance between the two locations and the amount of chemical transported.
- Chemicals are not transported between two plants.
- Each consumer has a monthly demand. We do not have to satisfy the entire demand of the consumers with the chemicals produced by our installed chemical plants. However, a penalty cost higher than the chemical price is paid for the part of the demand satisfied by other vendors.
- The interface between the point of common coupling and the electric utility is set up, and the location of the point of common coupling is fixed.
- A chemical plant runs in different modes, and a chemical cannot be a reactant in one mode and a product in another mode for a



**FIGURE 3** Decisions taken in the multiscale model.

chemical plant. In other words, a chemical is either a reactant for a plant or a product for the plant.

- Each plant has a shutdown mode where there is no production.
- The differences between adjacent bus voltage angles are small.
- The chemical storage cost is assumed to be fixed and included in the capital cost of the plant.
- The ramping constraints, as well as constraints on the restrictions imposed on mode switching, which connect days, are relaxed.
- The transmission interconnection charges are neglected, that is, the electricity from the microgrid can be sold at the point of common coupling at the market price without extra charges.
- The microgrid is assumed to be a price-taker in the electricity market, that is, it does not impact the electricity price.

### 3.1 | Temporal simplification

Modeling each hour for each of the 365 days will make the problem extremely large. To reduce the number of variables while preserving the information in the data associated with the 365 days,  $k$  representative days can be selected in each month of the planning problem to represent the whole planning horizon where  $k \ll$  number of the days in the month, as shown in Figure 3. A clustering algorithm, such as  $k$ -means clustering or  $k$ -medoids clustering, can be used to divide the whole historical dataset into  $k$  clusters based on some of the characteristics of the historical days. The centroid or the medoid of each cluster is selected as the representative day. In this problem,  $k$  representative days are chosen for each month by applying a  $k$ -means clustering algorithm on the normalized power output of the renewable resources and electricity prices for the same month over several historical years.<sup>49</sup>

With this temporal simplification, we propose a multiscale MILP model. The mathematical formulation of the MILP is given in Appendix B.

## 4 | ALGORITHM

### 4.1 | Overview

The model can easily have millions of variables. Even for a small number of locations (5~10), it is very difficult to solve the model directly using

an MILP solver. In addition, decomposition algorithms such as Benders decomposition and Lagrangian decomposition cannot be applied to solve this problem efficiently. We provide the details of the applicability of existing decomposition methods in Appendix D. To solve it efficiently, we propose a matheuristic to obtain a good feasible solution in a reasonable amount of time. Before presenting the details of our algorithm, we provide an overview of the algorithm to help the reader build some intuition. The algorithm has two major steps. The first step is to aggregate variables such that a smaller MILP is solved. The second step is a disaggregation heuristic to find a feasible solution to the original problem.

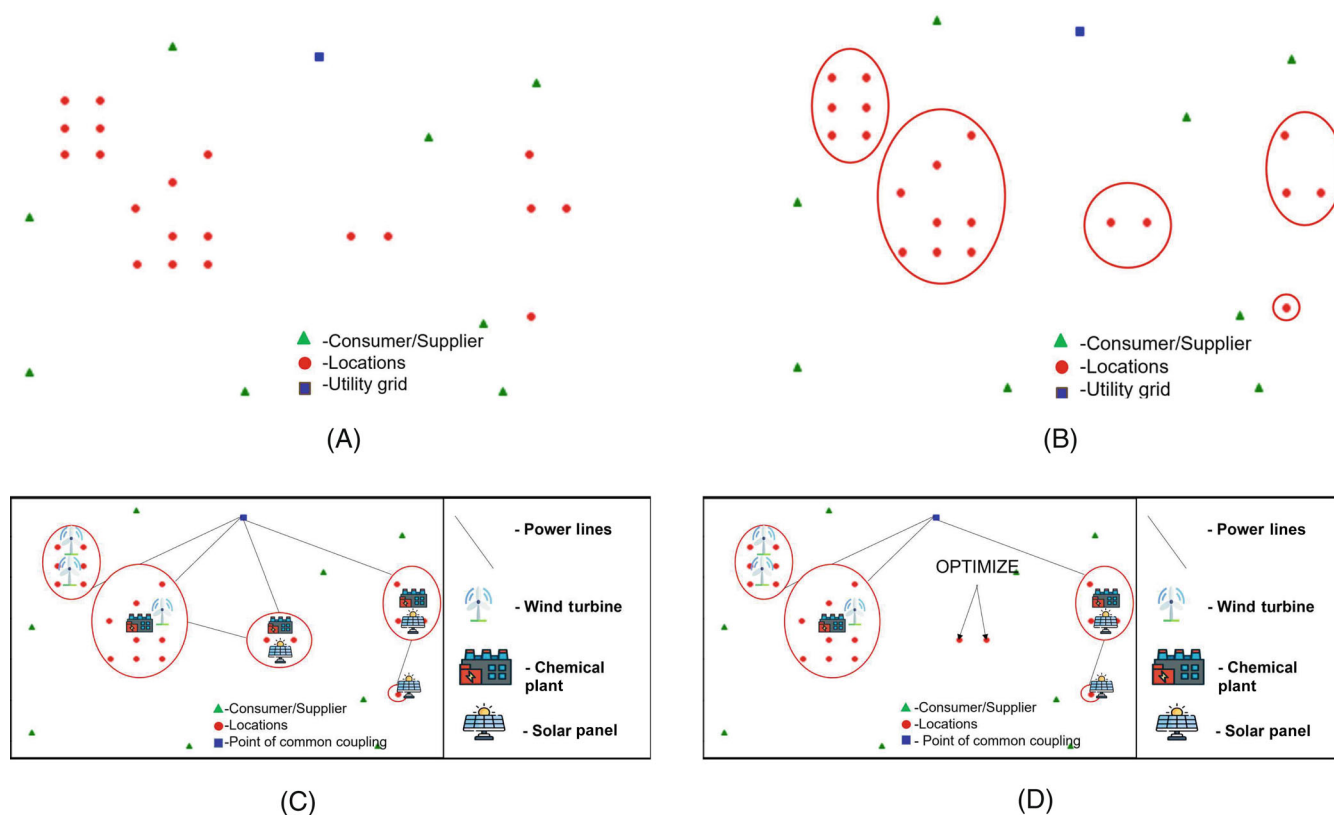
For the aggregation step, the integral operating variables are initially relaxed and the locations are grouped into a smaller number of clusters by applying the  $k$ -means algorithm on their coordinates. The variables of the locations belonging to the same cluster are then aggregated and the cluster centers are used as candidate locations. Thus the problem has been reduced from a large number of candidate locations to a problem with a reasonable number of candidate locations that can be solved using an MILP solver in a reasonable amount of time. From this, the number of plants and power-generating units in each cluster, as well as a fair idea of the number of power lines between any two cluster centers, can be obtained. Figure 4C represents an example of the investment decisions obtained from the aggregated problem.

In the disaggregation step, an MILP to disaggregate each individual cluster is solved while fixing most of the investment decision variables of the rest of the clusters including the number of plants, power-generating units, and the power lines among them. Note that the clusters are disaggregated independently and not sequentially here. Therefore, these disaggregating MILPs can be parallelized.

After completely disaggregating each cluster, the number of plants and the number of power-generating units in each location can be fixed. However, the number of power lines between any two locations is not fully determined since we are disaggregating each cluster independently. Essentially, the solution to the disaggregation MILP has two types of power lines: (a) power lines between a candidate location and the point of common coupling or between two candidate locations that are within the same cluster in the disaggregating MILPs and (b) power lines between a candidate location and a cluster center. Note that the second type of power line does not correspond to a line in the original problem. We propose a heuristic to obtain the number of power lines between any two locations based on the number of the second type of lines from the disaggregating MILPs. To this end, an integer program is solved to match the power lines to the solution of the disaggregating MILPs. While more detailed steps are given in the next subsection, detailed mathematical formulations of the first few steps and details on speeding up the algorithm are given in section C of the Data S1.

### 4.2 | Details

In this subsection, more details are given on the implementation of Algorithm 1.



**FIGURE 4** Steps of the algorithm. (A) 20 Locations; (B) 20 Locations clustered – Step 1; (C) example solution from aggregated problem; (D) disaggregating one of the clusters.

#### ALGORITHM 1 Aggregate disaggregate algorithm

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1 Function Aggregate_Disaggregate Algorithm:
2   Step 1: Cluster the locations based on coordinates
3   Step 2: Solve the aggregated problem (C.2) after relaxing the integral operational variables
4   Step 3:
5   foreach cluster do
6     Solve Problem (C.3) to disaggregate the cluster keeping all the other clusters and their investment decisions fixed to the
       optimal solution of the aggregated problem.
7   end
8   Step 4: Solve Problem (1) to match power lines between clusters obtained from the previous step.
9   Step 5: Fix all the investment decisions and solve for the lower-level decisions to obtain a feasible solution to the original
       full-scale MILP based on all the original candidate locations.
10 return

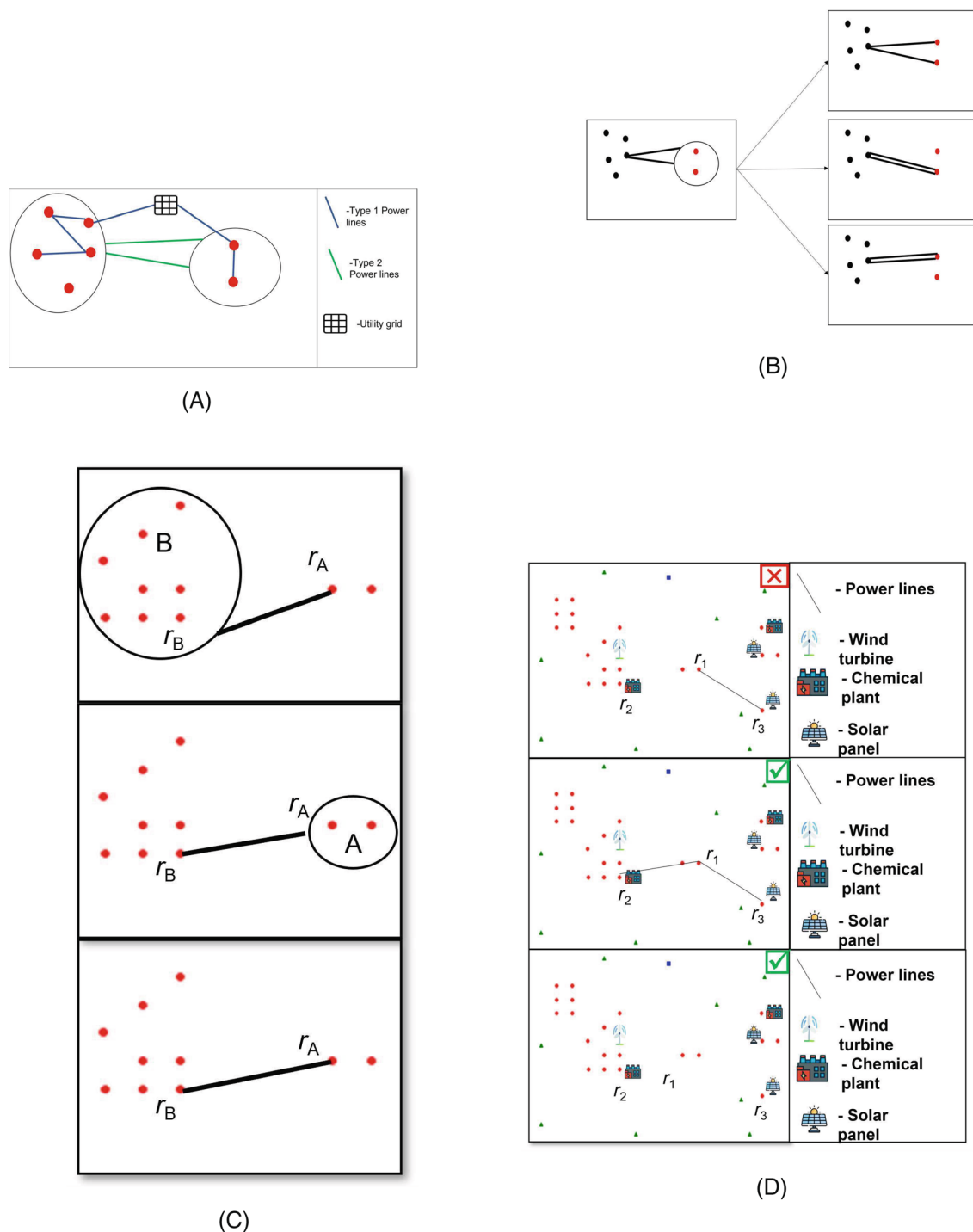
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In Step 1 of the algorithm, the k-means clustering algorithm is run on the coordinates of the locations to cluster the locations. The number of clusters is chosen such that the aggregated MILP in Step 2 of the algorithm, can be solved in a reasonable amount of time. For example, for the

locations shown in Figure 4A, we cluster the locations into five clusters and Figure 4B shows an image of the clusters derived from this step.

Using the centers of the clusters obtained from Step 1 of the algorithm as candidate locations, an aggregated problem is solved in Step





**FIGURE 5** Step 4 of algorithm. (A) Two types of power lines; (B) Constraining the sum of power lines in Step 4 (1b); (C) Symmetry heuristic in Step 4 (1c); (D) Configurations for power lines with no plant or generator in Step 4 (1f) and (1g).

2. Here, the constraints on the investment decisions are aggregated based on the number of locations in each cluster. The operating variables are also relaxed. After solving the aggregated problem in Step 2 of the algorithm, the number of plants and power-generating units in each cluster, as well as a rough estimate of power lines between locations in different clusters, are obtained. Each cluster is then disaggregated in Step 3 of the algorithm, keeping the other clusters' investment decisions fixed. For example, Figure 4C represents the investment decisions obtained from the aggregated problem, Figure 4D represents the process of

disaggregating one of the clusters, where the investment decisions concerning the two locations marked are solved, keeping the investment decisions of all the other clusters fixed.

From Step 3, the number of plants and power-generating units in each location are obtained as well as the power lines. As shown in Figure 5A, there are two types of power lines:

- Power lines between two candidate locations, which happens between two candidate locations in the same cluster on which we

**TABLE 1** Notations in Section 4.

Notation	Definition
$R_c$	Set of locations in the cluster with center $c$
$R^{\text{empty}}$	Set of locations with no plant or power-generating unit, that is, $r \in R^{\text{empty}}$ if $r \in \mathcal{R}$ , $\sum_{i \in \{I_{\text{plant}} \cup I_{\text{power}}\}} x_{i,r} = 0$ .
$nt_{r,c}^{\text{disagg}}$	Number of power lines between $r$ and $c$ obtained from the disaggregation step
$\mathcal{L}^{td}$	Set of potential candidates to optimize for which includes all power lines of type two, that is, $\forall nt_{r,c}^{\text{disagg}} \geq 1, (r, r') \in \mathcal{L}^{td}, r' \in R_c$ .
$c$	Cluster center
$r$	Candidate location
$nt_{r,r'}$	Integer variable denoting the number of power lines between locations $r$ and $r'$
$p_{r,r'}$	Binary variable indicating if there is at least one power line connecting locations $r$ and $r'$
$q_r$	Binary variable indicating if there are more than two different sets of power lines connected to $r$

solve the disaggregation MILP, or a candidate location and the point of common coupling (there is atleast one candidate power line from each location in the cluster to the point of common coupling when we solve the disaggregation MILP) shown by the blue lines in Figure 5A.

- Power lines between a candidate location and a cluster center, which happens as there are candidate lines from the locations of a cluster to the other cluster centers when we solve the disaggregation MILP shown by the green lines in Figure 5A.

Note that cluster centers are not real candidate locations and the investment decisions must involve lines between two real candidate locations. In order to convert the second type of power lines into the form of the first type, we solve the integer programming problem (1).

With a slight abuse of notation, we use the notations in Table 1 in this section.

Problem (1) aims to minimize the sum of the product of the number of power lines between two locations and the distance between the two corresponding locations, over all the potential power lines (defined in  $\mathcal{L}^{td}$ ), as the distance between two locations reflects the price of a power line between the two locations. Note that when we define the set  $\mathcal{L}^{td}$ , we only define one set of power lines and not the lines going both ways, that is, if we have both (p,v) and (v,p) as potential power line, we include only one of them in set  $\mathcal{L}^{td}$ . The sum of the power lines connected to locations in a cluster is constrained based on the number of power lines connected to these locations which is obtained from the previous step. This is shown in Figure 5B and is described by Equation (1b). To make the problem more accurate, the power lines of type 1 which are not connected to the point of common coupling can be included as well in the set  $\mathcal{L}^{td}$ , and the clusters can be defined as individual locations.

The symmetry of power lines is used as part of the heuristic, which is depicted in Figure 5C. If there is at least one power line between one location  $r_A$  in cluster A and the center of cluster B, and

at least one line between a location  $r_B$  in cluster B and the center of cluster A obtained from the solution of the disaggregation step, then at least one power line can be constructed between the locations  $r_A$  and  $r_B$ . This heuristic rule is described by Equation (1c).

If there is a location with no plant or power-generating unit, there cannot be exactly 1 set of power lines connected to it, as shown in Figure 5D. For example, if there is only one power line connected to location  $r_1$  (from  $r_3$ ) in Figure 5D, power transmitted from  $r_3$  is neither consumed nor transmitted from  $r_1$ . To ensure the power balance, there would be no power flowing through it, making it redundant. Therefore, there should be either no power line or at least two distinct sets of power lines connected to a location with no plant or power-generating unit (where power can flow in and out of the node). To ensure this, constraints (1f) and (1g) are added.

$$\min \sum_{r,r' \in \mathcal{L}^{td}} d_{r,r'} nt_{r,r'}, \quad (1a)$$

$$\text{s.t.} \quad \sum_{r' \in R_{\text{dis},c}} nt_{r,r'} \geq nt_{r,c}^{\text{disagg}}, \quad \forall nt_{r,c}^{\text{disagg}} \geq 1, \quad (1b)$$

$$nt_{r,r'} \geq 1, \quad \forall nt_{r,c}^{\text{disagg}} \geq 1 \text{ and } nt_{c,r'}^{\text{disagg}} \geq 1, r \in R_c, r' \in R_{c'}, \quad (1c)$$

$$nt_{r,r'} \leq M p_{r,r'}, \quad \forall (r, r') \in \mathcal{L}^{td}, \quad (1d)$$

$$nt_{r,r'} \geq p_{r,r'}, \quad \forall (r, r') \in \mathcal{L}^{td}, \quad (1e)$$

$$\sum_{(r,r') \in \mathcal{L}^{td}} p_{r,r'} + \sum_{(r',r) \in \mathcal{L}^{td}} p_{r',r} \leq M q_r, \quad \forall r \in R^{\text{empty}}, \quad (1f)$$

$$\sum_{(r,r') \in \mathcal{L}^{td}} p_{r,r'} + \sum_{(r',r) \in \mathcal{L}^{td}} p_{r',r} \geq 2 q_r, \quad \forall r \in R^{\text{empty}}. \quad (1g)$$

After Step 4 of the algorithm, we have all the investment decisions for the model. In Step 5, we fix the investment decisions in the original model to the values obtained in the previous steps and solve the restricted problem to find feasible operating decisions.

## 5 | THE VALUE OF THE MULTISCALE MODEL (VMM)

Although the value of solving multiscale models to consider lower-level operational decisions is well-recognized by the PSE community, there has not been a metric to quantify the additional value a multiscale model (MM) can create compared with a single time-scale model. In this section, we introduce such a metric that we call the *Value of the Multiscale Model* (VMM). The metric is inspired by the Value of the Stochastic Solution (VSS) introduced by the stochastic programming community to quantify the additional value stochastic solutions can bring compared with the optimal solutions to the deterministic model.<sup>50</sup>

To define VMM, we introduce several new notations. Note that these new notations are only valid for this section and should be distinguished from the notations already introduced in previous sections.



Here, we use  $\mathbf{x}$  to represent all the upper-level decisions, for example, the investment decisions and the monthly decisions in our problem. Lower-level decisions are represented as  $\mathbf{y}_s$  defined for each subperiod  $s$ . In our model,  $\mathbf{y}_s$  corresponds to the hourly operating decisions on each representative day where  $s$  is the index for each day. The MM can be defined as,

$$\text{MM} = \min_{\mathbf{x}, \mathbf{y}_s} f(\mathbf{x}) + \sum_{s \in \mathcal{S}} w_s q(\mathbf{x}, \mathbf{y}_s, \boldsymbol{\theta}_s), \quad \text{s.t. } g(\mathbf{x}) \leq 0, \quad h(\mathbf{x}, \mathbf{y}_s, \boldsymbol{\theta}_s) \leq 0, \quad \forall s \in \mathcal{S}. \quad (2)$$

where  $\boldsymbol{\theta}_s$  denotes the parameters associated with subperiod  $s$ , for example, the hourly capacity factors and electricity prices for a given representative day indexed by  $s$ . The objective is a weighted sum of the costs of the subperiods.  $h(\mathbf{x}, \mathbf{y}_s, \boldsymbol{\theta}_s)$  corresponds to the detailed operating constraints for the lower-level problem.

A single-scale model will ignore the detailed operating decisions during the subperiods. Instead, only the upper-level decisions  $\mathbf{x}$  are kept in the model. The nominal single-scale model (SM) is denoted as

$$\text{SM} = \min_{\mathbf{x}, \mathbf{z}} f(\mathbf{x}) + Q(\mathbf{x}, \mathbf{z}, \hat{\boldsymbol{\theta}}), \quad \text{s.t. } g(\mathbf{x}) \leq 0, \quad H(\mathbf{x}, \mathbf{z}, \hat{\boldsymbol{\theta}}) \leq 0. \quad (3)$$

where variables  $\mathbf{z}$  are introduced as a surrogate to the operating decisions.  $\hat{\boldsymbol{\theta}}$  is a nominal parameter that serves as a surrogate to the parameters  $\boldsymbol{\theta}_s$ . Typically, the dimensions of  $\mathbf{z}$  and  $\hat{\boldsymbol{\theta}}$  are lower than the dimensions of  $\mathbf{y}_s$  and  $\boldsymbol{\theta}_s$  because the detailed operations are ignored in the SM. For example, in our model,  $\hat{\boldsymbol{\theta}}$  can be the average of the hourly electricity prices and capacity factors over the whole historical dataset. Similarly, the functions  $Q$ , and  $H$  are surrogates of the functions  $q$  and  $h$ . The reduction of the MM to the SM is not a trivial task and usually depends on the engineering insight of the problem. By solving (3), we can obtain an upper-level solution denoted as  $\mathbf{x}^{\text{SM}}$ .

We further define a concept called the *Multiscale Performance of the Single-scale Solution* (MPSS). The idea is to fix the upper-level decisions to  $\mathbf{x}^{\text{SM}}$  and solve the rest of the multiscale problem to obtain the “true cost” of the solution  $\mathbf{x}^{\text{SM}}$ .

$$\text{MPSS} = \min_{\mathbf{y}_s} f(\mathbf{x}^{\text{SM}}) + \sum_{s \in \mathcal{S}} q(\mathbf{x}^{\text{SM}}, \mathbf{y}_s, \boldsymbol{\theta}_s), \quad \text{s.t. } h(\mathbf{x}^{\text{SM}}, \mathbf{y}_s, \boldsymbol{\theta}_s) \leq 0 \quad \forall s \in \mathcal{S}. \quad (4)$$

It should be noted that  $\mathbf{x}^{\text{SM}}$  can be suboptimal or even infeasible when multiscale decisions are considered. The difference between MPSS and MS indicates the additional economic savings we can get by solving the MM, which is defined as VMM.

$$\text{VMM} := \text{MPSS} - \text{MM}. \quad (5)$$

We will show in our case study the VMM of our MM compared with a *0 representative day model* that ignores the hourly operating decisions.

## 5.1 | Difference with VSS

In computing VSS, an *Expected Value* problem is solved for one nominal scenario corresponding to the expected value of  $\boldsymbol{\theta}_s$ , that is,  $\bar{\boldsymbol{\theta}} = \sum_{s \in \mathcal{S}} w_s \boldsymbol{\theta}_s$

$$\text{EV} = \min_{\mathbf{x}, \bar{\mathbf{y}}} f(\mathbf{x}) + q(\mathbf{x}, \bar{\mathbf{y}}, \bar{\boldsymbol{\theta}}), \quad \text{s.t. } g(\mathbf{x}) \leq 0, \quad h(\mathbf{x}, \bar{\mathbf{y}}, \bar{\boldsymbol{\theta}}) \leq 0. \quad (6)$$

The main difference between EV and the SM defined in (3) is that EV is still a multi-scale model but just one nominal scenario is kept. In comparison, SM is a single-scale model that has a much smaller number of variables and constraints. For example, in our problem, EV is a *1 representative day model* while SM is a *0 representative day model*. Let the solution to the EV be  $\mathbf{x}^{\text{EV}}$ . We can evaluate the performance of  $\mathbf{x}^{\text{EV}}$  over all the scenarios by computing the so-called *expected result of using the EV solution* (EEV).<sup>50</sup>

$$\text{EEV} = \min_{\mathbf{y}_s} f(\mathbf{x}^{\text{EV}}) + \sum_{s \in \mathcal{S}} q(\mathbf{x}^{\text{EV}}, \mathbf{y}_s, \boldsymbol{\theta}_s), \quad \text{s.t. } h(\mathbf{x}^{\text{EV}}, \mathbf{y}_s, \boldsymbol{\theta}_s) \leq 0 \quad \forall s \in \mathcal{S}. \quad (7)$$

EEV and MPSS only differ in the way the upper-level decisions are obtained. VSS is defined by

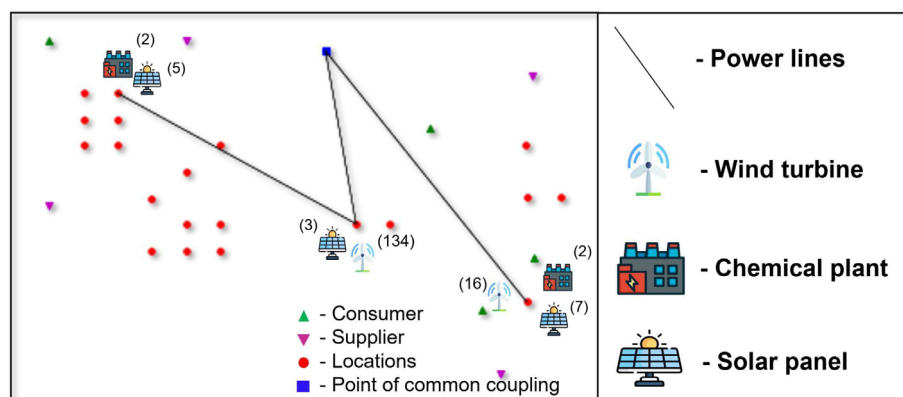
$$\text{VSS} := \text{EEV} - \text{MM}. \quad (8)$$

Empirically, VMM is usually larger than VSS because the model complexity of the SM is lower than EV.

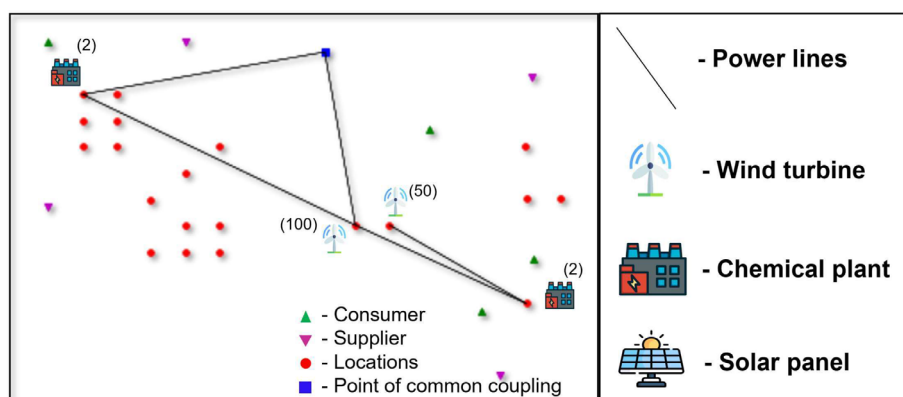
## 6 | CASE STUDY

The MILP model and the proposed algorithm are implemented in a case study in Western Texas with 20 candidate locations whose coordinates are known. We are given 15 1500-kW solar panels, 150 100-kW wind turbines, modular chlorine plants operating in three modes, and 12 kV power lines. Additionally, the location of the point of common coupling and the location of four consumers and four suppliers are given. The demand for each consumer is generated randomly from a uniform distribution.

For the chemical plant, we consider a chloralkali process, an industrial process to produce chlorine and sodium hydroxide by the electrolysis of sodium chloride solutions. In this article, we use a chlorine plant that operates in three modes - standard cathodes (STCs/ST), oxygen-depolarized cathodes (ODCs/OD), and Shut down.<sup>26</sup> The reaction in ST mode producing  $\text{H}_2$  as by-product is:  $2\text{NaCl} + 2\text{H}_2\text{O} \rightleftharpoons 2\text{NaOH} + \text{Cl}_2 + \text{H}_2$ . The net reaction of the chloralkali electrolysis in the OD mode is  $2\text{NaCl} + \text{H}_2\text{O} + 0.5\text{O}_2 \rightleftharpoons 2\text{NaOH} + \text{Cl}_2$ . The energy requirement and the capacity of the chlorine plant are obtained from Reference 26. We get the capital costs of the plant and the capital costs and energy requirement of compressors and turbine from Aspen Plus and add a cost of \$160,000 for making the electrolyzer into bi-mode. A storage cost that is 5% of



**FIGURE 6** Solution Representation from the algorithm for the investment decisions.



**FIGURE 7** Solution representation from 0 representative day model for the investment decisions.

**TABLE 2** Results summary.

Statistics	Value
Upper bound from LP relaxation (\$)	19.50 M
Total profit from proposed algorithm (\$)	18.94 M
Time for aggregation (h)	7.12
Time for disaggregation (h)	0.35
Time for solving operation decisions (h)	0.03
Profit obtained using the model with 0 representative days (\$)	18.52 M
VMM (\$)	0.42 M
Average profit from centralized production (\$)	18.72 M
Maximum profit from centralized production (\$)	18.90 M
Profit from proposed algorithm with constraints on investment decisions (described in Appendix E) (\$)	18.76 M

the total capital cost for each plant is further added to the capital cost. We assume that the plant remains in one mode for at least 2 h after switching to it each day and has a negligible cleaning time while switching modes.

The power output for the wind turbines and solar panels at the candidate locations for three historical years (2011–2013), as well

**TABLE 3** Breakdown of profit.

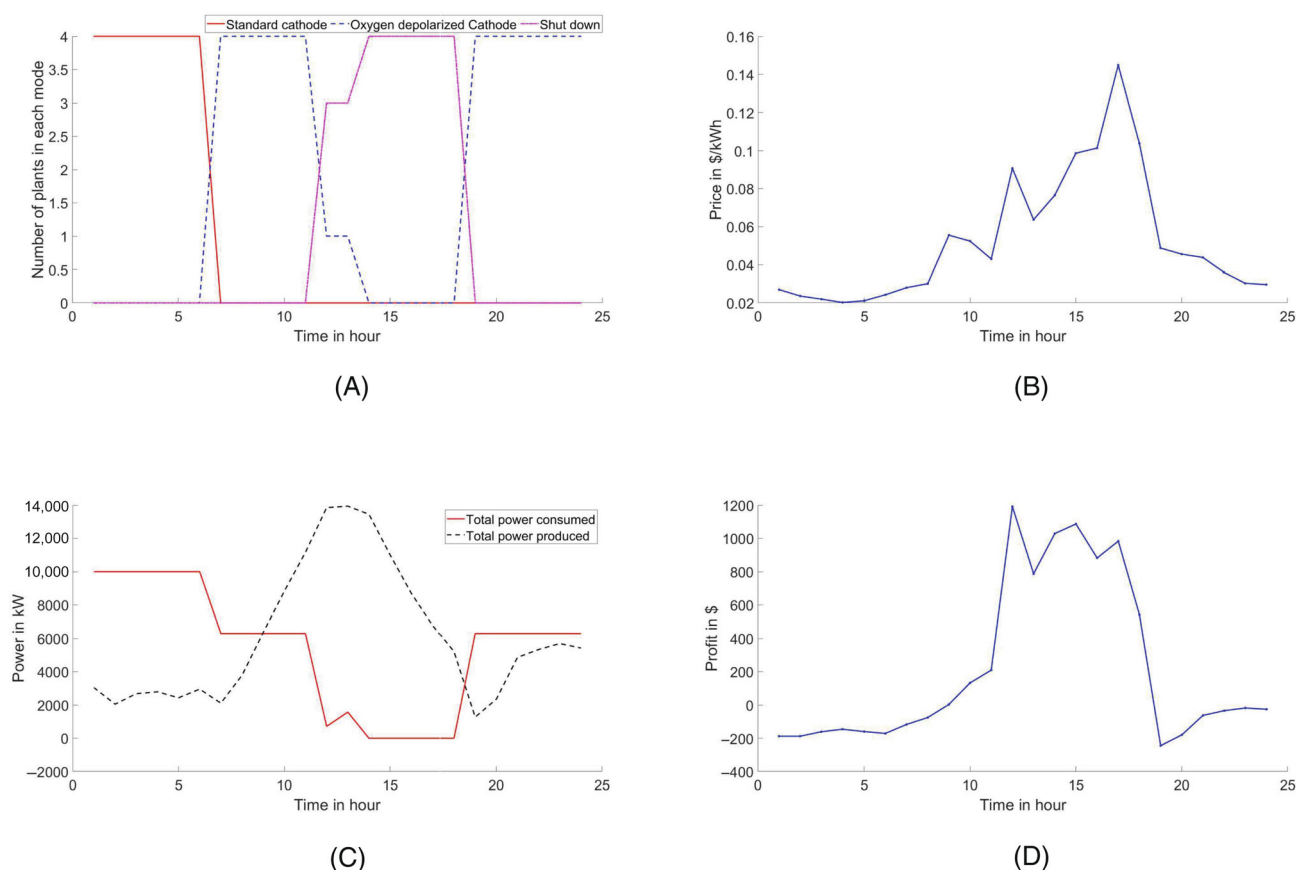
Breakdown of annual profit	Cost/revenue in \$M
Net revenue from materials	28.22
Net transportation cost	0.23
Net profit from electricity	3.16
Total fixed operating cost	5.98
Total amortized capital cost	6.23

as the capital costs of these power-generating units, are obtained from the software SAM (System Advisor Model)<sup>51</sup> after obtaining the weather-related data from NREL (National Renewable Energy Laboratory) website (National Solar Radiation Database<sup>\*</sup> and Wind Integration National Dataset Toolkit<sup>†</sup>). We assume that there are incentives for wind turbines. The electricity price for West Texas for three historical years (2011–2013) is obtained from the website Energy Online<sup>‡</sup> and adjusted for inflation. The parameters of the power lines such as resistance and inductance, are obtained from DERCAM (Distributed Energy Resource Customer Adoption Model).<sup>52</sup> Five representative days per month are chosen based on

<sup>\*</sup><https://nsrdb.nrel.gov/>

<sup>†</sup><https://www.nrel.gov/grid/wind-toolkit.html>

<sup>‡</sup><http://www.energyonline.com/Data/GenericData.aspx?DataId=4>



**FIGURE 8** Operating decisions on representative day 1 of month 9. (A) Hourly mode decisions on representative day 1 of month 9; (B) Hourly electricity prices on representative day 1 of month 9; (C) Hourly power produced and consumed by the microgrid on representative day 1 of month 9; (D) Hourly profit from electricity on representative day 1 of month 9.

the data using k-means clustering. The power lines are used in bundles of size 20 while implementing the algorithm. More data for the case study is given in section F of the Data S1.

## 6.1 | Results

The proposed algorithm and the corresponding models are implemented in Julia/JuMP. All the MILPs are solved using Gurobi version 10.0 on a Linux cluster with 48 AMD EPYC 7643 2.3GHz CPUs and 1 TB RAM. The total annual profit obtained at the end of the algorithm is \$18.94 M and the total time taken for all the steps of the algorithm is 7.5 h. An upper bound for the profit of the problem is obtained by solving the LP relaxation of the full-scale model using the barrier method without crossover and it is \$19.50 M. The original full space model has 10,111,090 constraints, 2,094,336 continuous variables, and 346,080 integer variables.

## 6.2 | The value of the MM

In order to understand the VMM, it is compared with a model that does not consider temporal variations. To this end, a model

ignoring hourly variations is formulated where the hourly operating variables are aggregated by month. The new model only has investment and monthly variables and thus has no representative day in each month. Therefore, it is called a *0 representative day model* and outputs the investment decisions. This investment decision can then be fixed in the MM to obtain the hourly operating variables and overall profit. Thus through this, the planning and scheduling are separated, and the planning does not take into account the hourly temporal variations. This profit is compared to the profit obtained from the algorithm. It has been found that the profit obtained using the *0 representative day model* is lesser than the profit obtained from the model and that the *0 representative day model* does not install any solar panels, as without the hourly variations taken into account, the solar panels are not profitable. The VMM is \$0.42 M<sup>§</sup>. Figures 6 and 7 show the optimal investment decisions obtained from the MM and the *0 representative day model*, respectively. The dots represent the candidate locations, the blue square represents the location of the point of common coupling, and the triangles represent consumers/suppliers.

<sup>§</sup>Note that the matheuristic did not solve the model to global optimality, this calculated VMM is an approximation.

The algorithm provides a configuration that favors distributed manufacturing. To further demonstrate the value of distributed manufacturing, it is compared with centralized manufacturing, where we calculated the profit by installing all the plants, solar panels, and wind turbines at each one of the 20 locations. The installed facilities are connected to the point of common coupling through sufficient number of power lines. The maximum profit obtained from centralized manufacturing across all 20 locations is around \$18.90 M, around \$0.04 M less than the profit obtained from the algorithm. However, land-based constraints may limit the number of plants or renewable resources that can be installed in a particular location. We have implemented the algorithm under such conditions, with further details and the associated results provided in Appendix E. The profit obtained from the algorithm with these constraints, is \$18.76 M and is lesser than the profit obtained without constraints.

Table 2 shows a summary of the algorithm's computing time per step and compares the profit obtained with the profit obtained from the model with 0 representative days and the average and maximum profit obtained from centralized production.

The breakdown of the profit is shown in Table 3. An important observation to note from the breakdown of the profit is that a major part of the revenue comes from the sales of chlorine and other chemicals, and the major cost is from the capital cost. The profit from the electricity makes a considerable contribution to the profit and thus the location of the plant and the power-generating units could influence the profit.

Figure 6 is a representation of the optimal configuration obtained from solving the MILP model using the algorithm proposed.

In order to understand the trends on an hourly basis and the effect of the power produced and electricity price on hourly decisions, several hourly decisions and parameters of representative day 1 in month 9 are plotted and shown in Figure 8A–D. Figure 8A shows the dynamics of the mode switching. When the electricity price is low, the STC mode is mostly preferred, when the price is moderately high the ODC mode is mostly preferred and when the price is extremely high the shutdown mode is mostly preferred. This is because the STC mode consumes high power but does not consume any oxygen and produces hydrogen, while the ODC mode consumes relatively lower power and consumes oxygen with no hydrogen produced. Thus, these two competing effects (consumption/production of oxygen/hydrogen and power required) help choose the mode for each hour.

Power is sold or bought from the electric utility depending on the net effect of the power consumed by the plant, the power generated by the solar panels and wind turbines, and the power loss through the power lines. It can be seen from Figure 8B that there is a peak in the electricity price in hour 17. The difference in power produced and power consumed in hour 17 is moderate, as seen in Figure 8C. Thus, all the plants run in the Shut down mode in hour 17, as seen in Figure 8A, and the profit from electricity is high, as seen in Figure 8D.

Another interesting observation is in hour 12 when the profit from electricity is at its peak for the day. The electricity price is moderately high in hour 12, and hence the Shut down mode is chosen for 3 of the plants and OD mode for the other plant as seen in Figure 8A. In the first few hours, the power produced is negligible. However, the

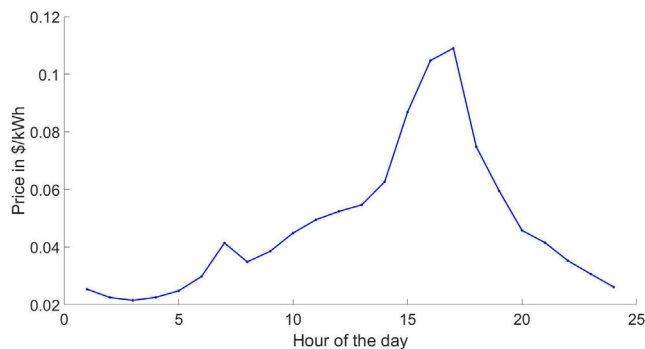


FIGURE 9 Average electricity price in each hour.

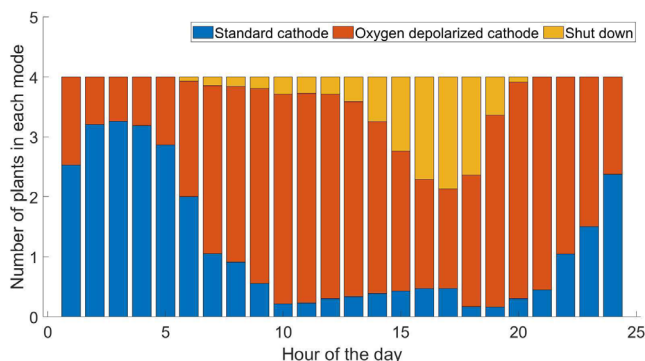


FIGURE 10 Average number of plants in each mode per hour.

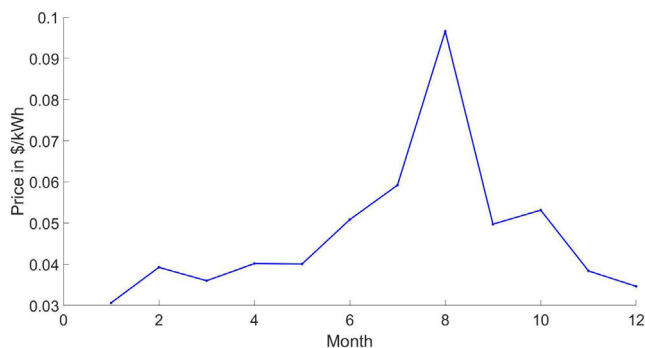


FIGURE 11 Average electricity price in each month.

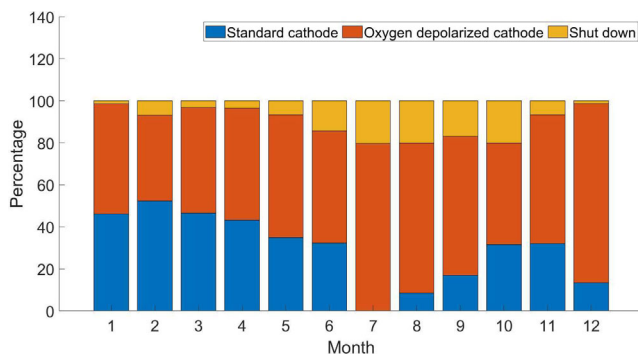
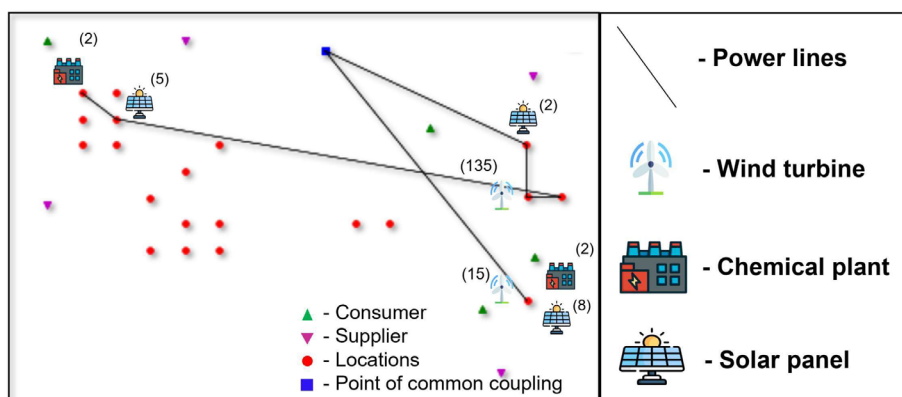


FIGURE 12 Mode decisions in a month.

**FIGURE 13** Solution representation from the algorithm for investment decisions in Scenario 2.



**TABLE 4** Split up of profit for Scenario 2.

Split up of annual profit	Cost/revenue in \$M in Scenario 2	Cost/revenue in \$M in base case
Net revenue from materials	28.13	28.22
Net transportation cost	0.23	0.23
Net profit from electricity	3.25	3.16
Total fixed operating cost	5.71	5.98
Total amortized capital cost	4.53	6.23

plants operate in the SC mode during the first few hours of the day. This is because the electricity price is very low.

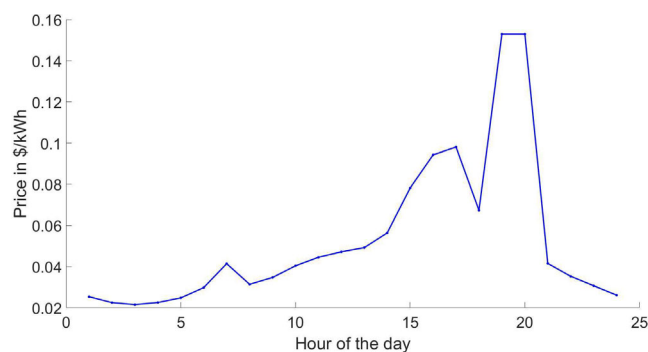
The weighted average of electricity price over all the representative days for each hour and the average number of plants in each mode for each hour is further plotted in Figures 9 and 10 and analyzed. An observation that can be made is that when the electricity price increases, the number of plants in the shutdown mode majorly increases. This is consistent with the trends.

### 6.2.1 | Monthly trends

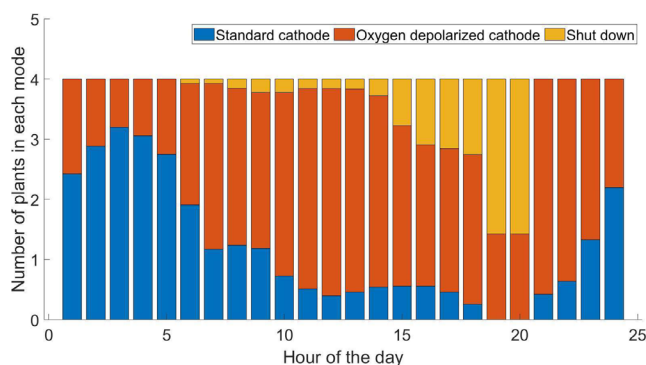
From the results obtained, an observation that can be made is that most of the demand is met by the plants and that the slack variable for each month is very small. Figure 11 shows the average electricity price for each month whereas Figure 12 depicts the average percentage of plants on each mode for each month. While the OD mode is predominantly chosen for plants on average, as seen in Figure 12, the percentage of shutdown mode mostly increases as the price of electricity increases, which is consistent with the hourly trends as well.

### 6.2.2 | Effect of more renewable electricity generation

In the future, when the renewable electricity generation capacity becomes more abundant, electricity prices are expected to be depressed



**FIGURE 14** Average electricity price in each hour in Scenario 2.



**FIGURE 15** Average number of plants in each mode per hour in Scenario 2.

during hours of peak PV output and increase sharply at sundown.<sup>53</sup> Let us assume that the sundown time is from 6:00 to 7:00 p.m. We reduce the price by 10% for all hours between 7:00 a.m. to 5:00 p.m. and assign 10% more of the current highest price to the electricity price between hours 6:00 p.m. to 7:00 p.m. For other hours, we keep the prices the same. This is done for each representative day of each month. Additionally, we expect that the costs of installing solar panels and wind turbines are going to reduce.<sup>54,55</sup> We reduce the capital and operating costs of solar panels by 50% and wind turbines by 40%.

For this scenario, the MILP model and the proposed algorithm are implemented. The total profit obtained at the end of the algorithm is



\$20.91 M. Figure 13 depicts the optimal configuration obtained from the MILP model for this scenario. The optimal configuration is different from the base case, with the plants, wind turbines, and solar panels relocated. The dots represent the candidate locations, the blue square represents the location of the point of common coupling and the triangles represent consumers and suppliers.

The split of the profit is shown in Table 4.

While the profit from electricity has increased in scenario 2 as compared to the base case, the capital cost and fixed operating cost in Scenario 2 are less than in the base case. The net effect is that the profit in Scenario 2 is more than the profit obtained in the base case.

The plots of the average electricity price for each hour and the average number of plants in each mode for each hour are further analyzed in Figures 14 and 15. It is found that in the daytime, the average number of plants in the shutdown mode is lesser than that in the base case, while in the hours 19 and 20, which represent 6:00 p.m. and 7:00 p.m., the average number of plants in the shutdown mode is more than that in the base case. This is because, in the daytime, the electricity price is lesser in this scenario, while at 6:00 p.m. and 7:00 p.m., the electricity price is at its peak and is more than those in the base case.

## 7 | CONCLUSIONS

Electrification is a solution being explored to tackle the problem of greenhouse gas emissions by the chemical industry. Electrification using renewable sources of energy includes spatial and temporal variations, which can affect plant production. An MILP model was proposed to determine a feasible near-optimal configuration of a network of modular plants, power-generating units, and power lines connected by a microgrid considering spatial and temporal variations in electricity price and weather conditions. The model takes decisions in three-time scales: one-time investment decisions, monthly decisions like transportation as well as hourly operating decisions. A spatial aggregation and disaggregation algorithm based on k-means clustering was developed to solve the model efficiently. We propose a new metric the VMM to quantify the economic savings of the MM.

The model was tested on a case study with 20 candidate locations in Western Texas with data obtained from various sources. The mode of the plant was chosen depending on the power produced and the electricity price. The major contributor to the profit was found to be the materials (products and raw materials). The profit obtained from electricity was found to have a significant contribution to the total profit and thus, the spatial location can affect the profit. The mode switching and the profit from electricity were found to be consistent with the theoretical trends. The VMM was inferred by comparing it with the net annual profit obtained from a model with 0 representative days, and we found that the profit from the 0 representative day model was \$0.42 M lesser than the profit obtained from our model. The value of distributed manufacturing was inferred by comparing it with centralized manufacturing and it was found that the configuration with distributed manufacturing gave more profit. Further, we investigated the case study in the context of a scenario in the

future, where there will be more renewable electricity generation, and found that the profit increases in this scenario.

Although the case study is on the chloralkali process, we expect that as technologies for green hydrogen, green ammonia, and other chemicals which can be produced electrochemically, get more mature, the model can be used for multiscale planning of these new technologies. We also expect the proposed approach can have a broader impact as the cost of renewable power-generating resources reduces, and microgrids become more widely adopted. In addition, the proposed metaheuristic algorithm is general and can be adapted to solve any multiscale facility location problem, which has been understudied by the Operations Research community. While bundling of power lines was used to speed up the algorithm, it adds inherent constraints to the number of power lines placed between two locations. Additionally, the number of lines in the bundle is heuristically determined based on data. In the future, we will develop novel methods that do not require bundling the power lines to speed up the algorithm.

## AUTHOR CONTRIBUTIONS

**Asha Ramanujam:** conceptualization (equal); data curation (lead); investigation (lead); methodology (lead); software (lead); writing – original draft (lead). **Gonzalo E. Constante-Flores:** investigation (equal); visualization (equal); writing – review and editing (equal). **Can Li:** conceptualization (equal); funding acquisition (equal); writing – review and editing (equal).

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## DATA AVAILABILITY STATEMENT

All the raw data and the code for reproducing the results are distributed through our GitHub repository <https://github.com/li-group/EDCheM.jl>. The figures in the result sections are generated based on the results obtained from running the code.

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## SUPPORTING INFORMATION

Additional supporting information can be found online in the Supporting Information section at the end of this article.

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