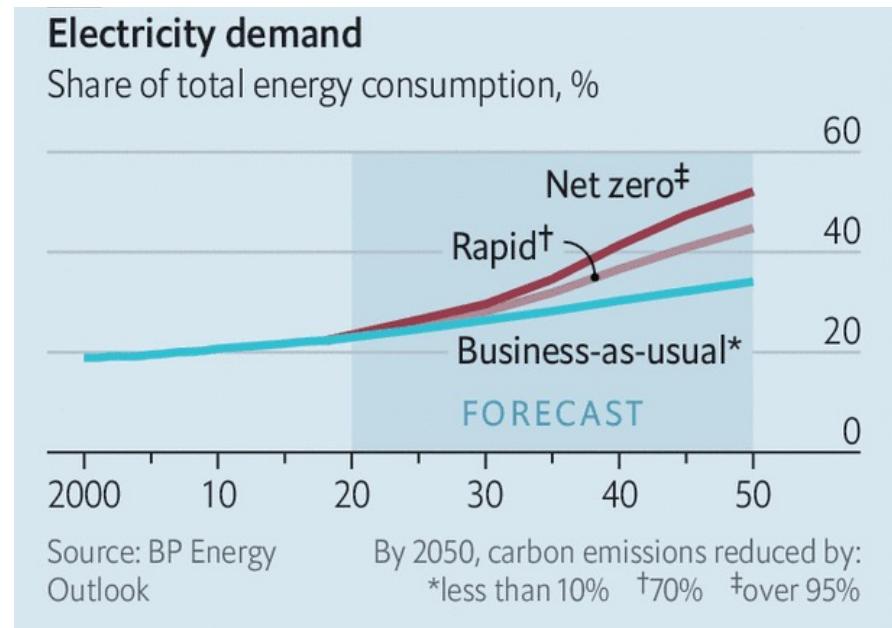
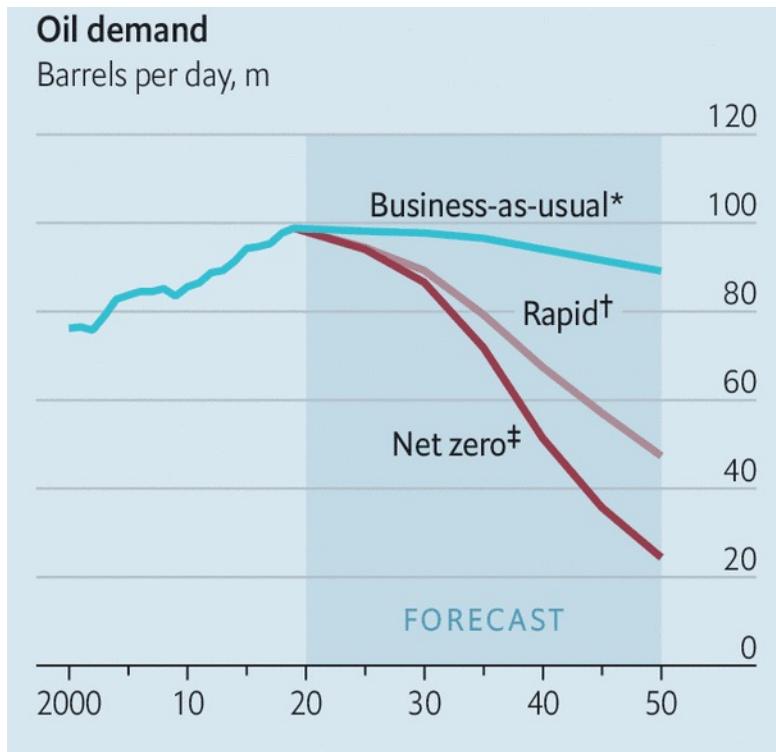


# Capacity Expansion Planning of Power Systems under High Renewables Penetration

Can Li  
Fifth year PhD candidate  
Advised by Prof. Ignacio Grossmann

# Energy Transition from Oil to Electricity

- **Electricity** demand would account for over 50% of total energy demand if we were to achieve **net zero carbon** emission in 2050

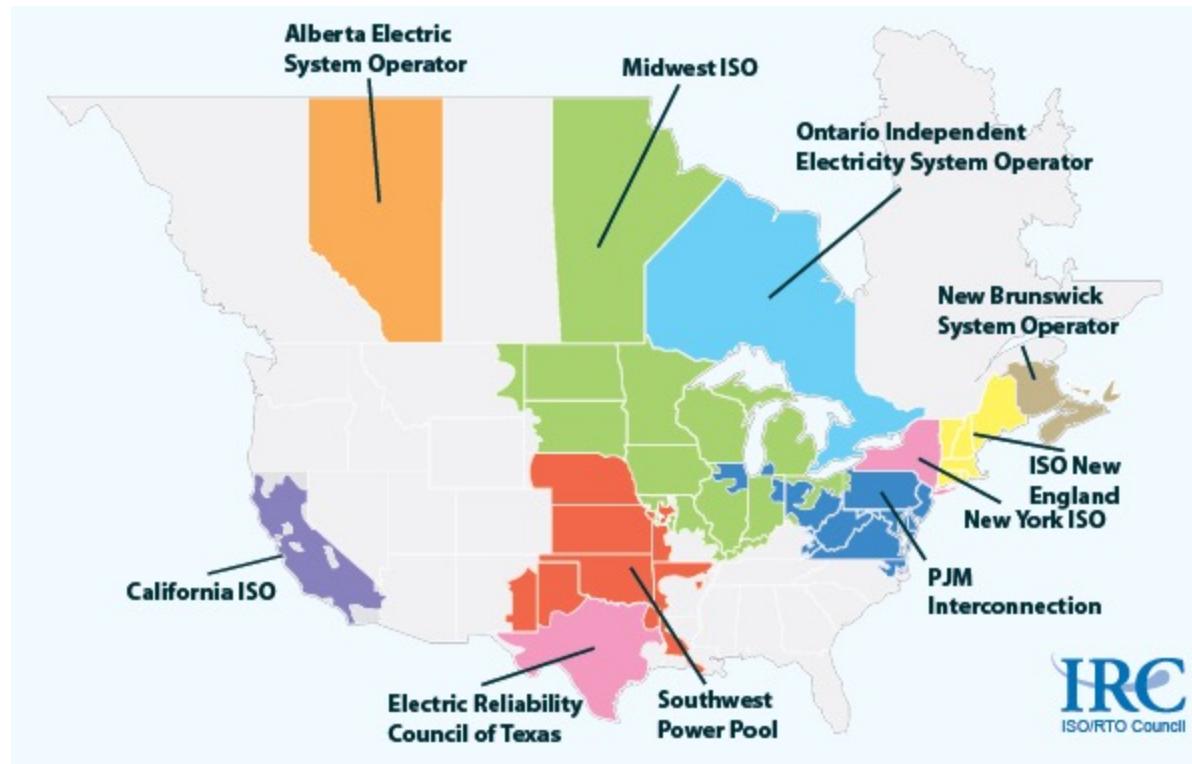


The Economist

BP Energy Outlook 2020

# Electricity Market in the US

- The electricity transmission network is controlled by **Independent System Operators** (ISOs). An ISO coordinates, controls, and monitors a multi-state electric grid.
- Create **a competitive wholesale electricity market** where all generators can compete on an equal basis and have equal access to the grid.

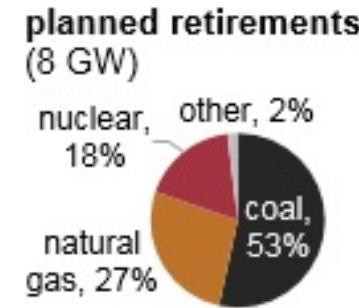
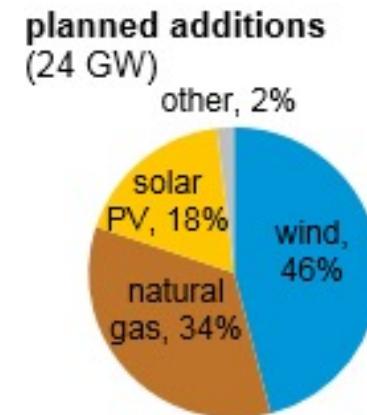
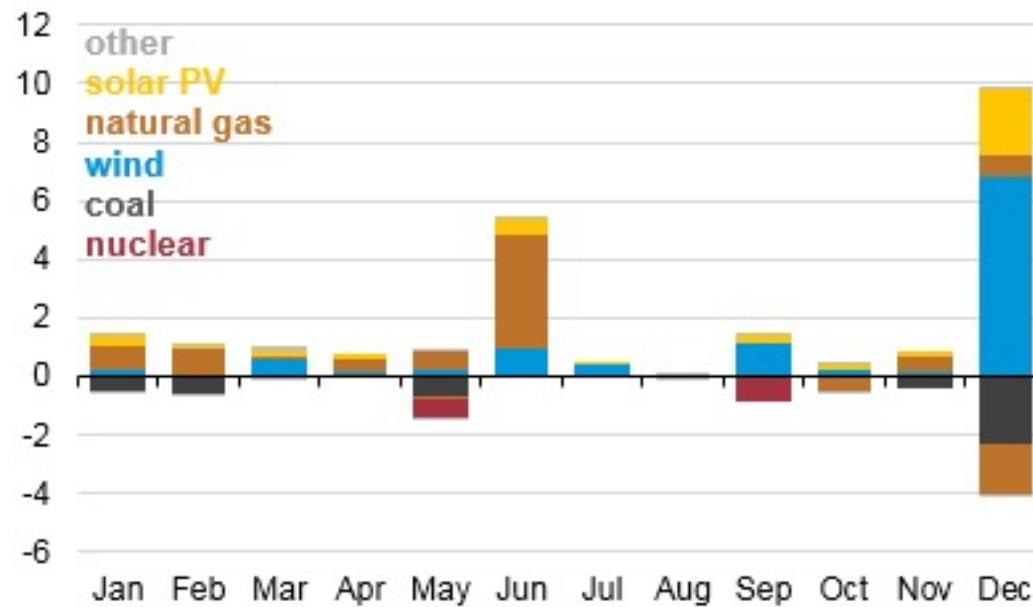


ISOs in North America

# Current Capacity Additions

- Most electric capacity additions come from **renewables**
  - In 2019, 64% capacity additions in the US are from renewables. 34% from natural gas

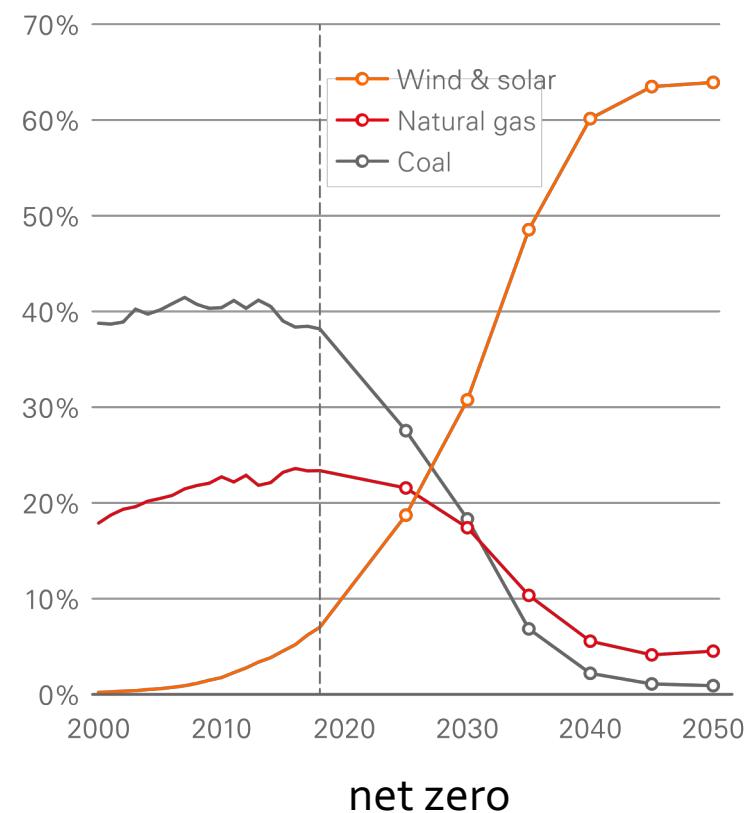
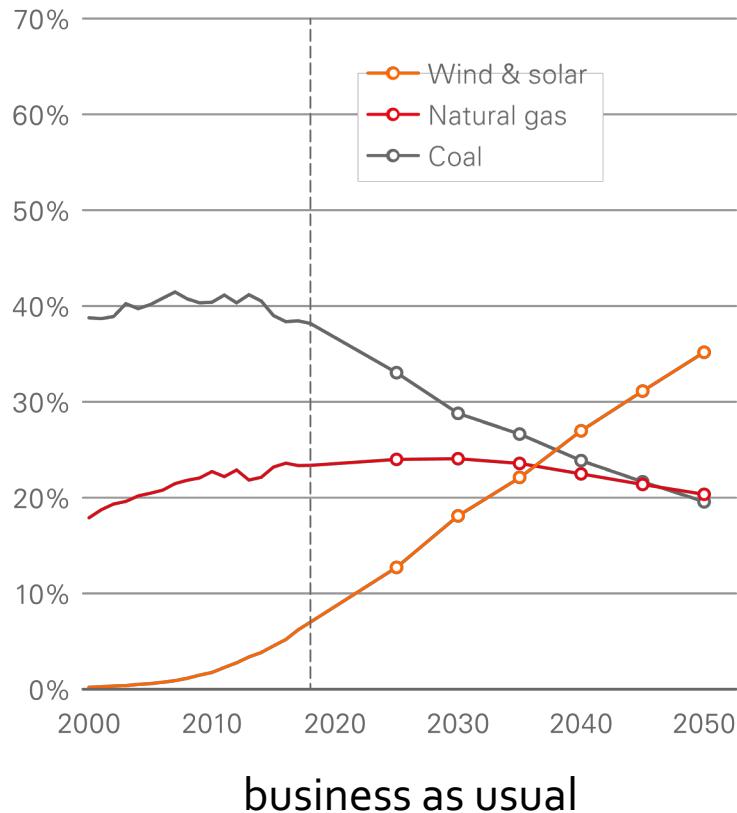
**U.S. electric capacity additions and retirements, 2019**  
gigawatts (GW)



eria

# Renewable Generation

- Share of global power generation from **wind&solar** is expected to **increase**

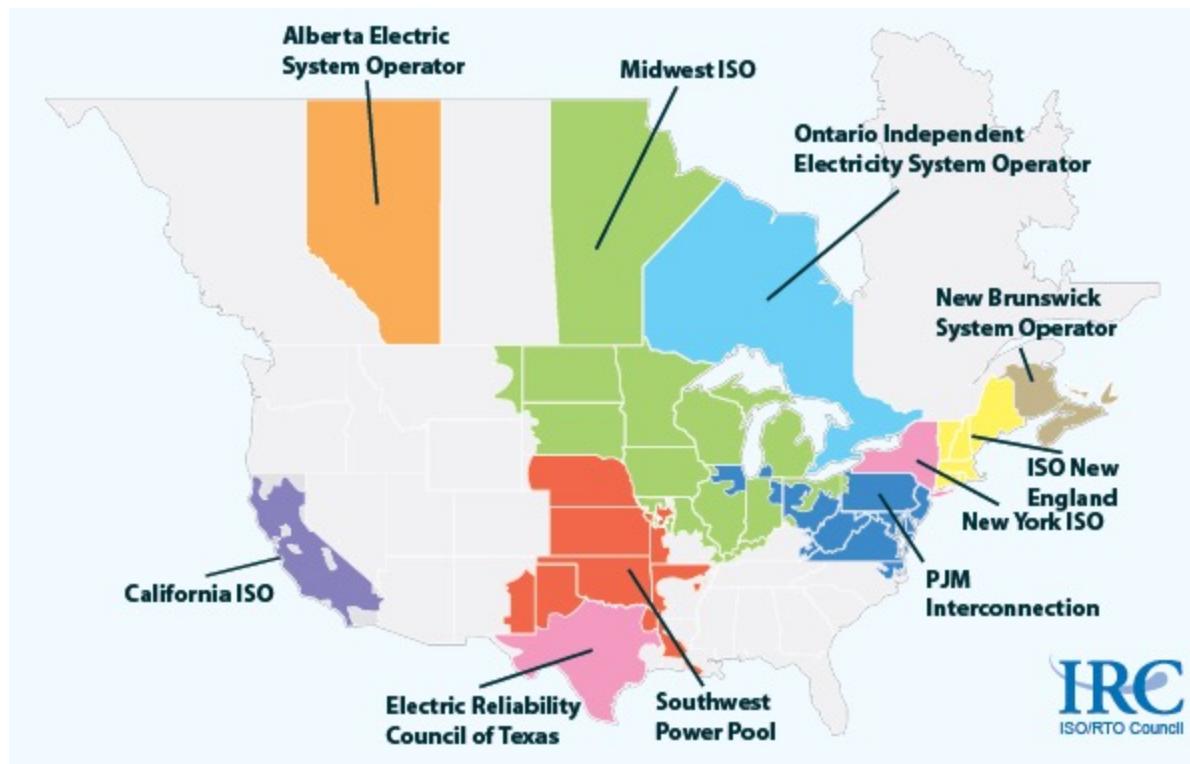


BP Energy Outlook 2020

# Problem Addressed in This Presentation

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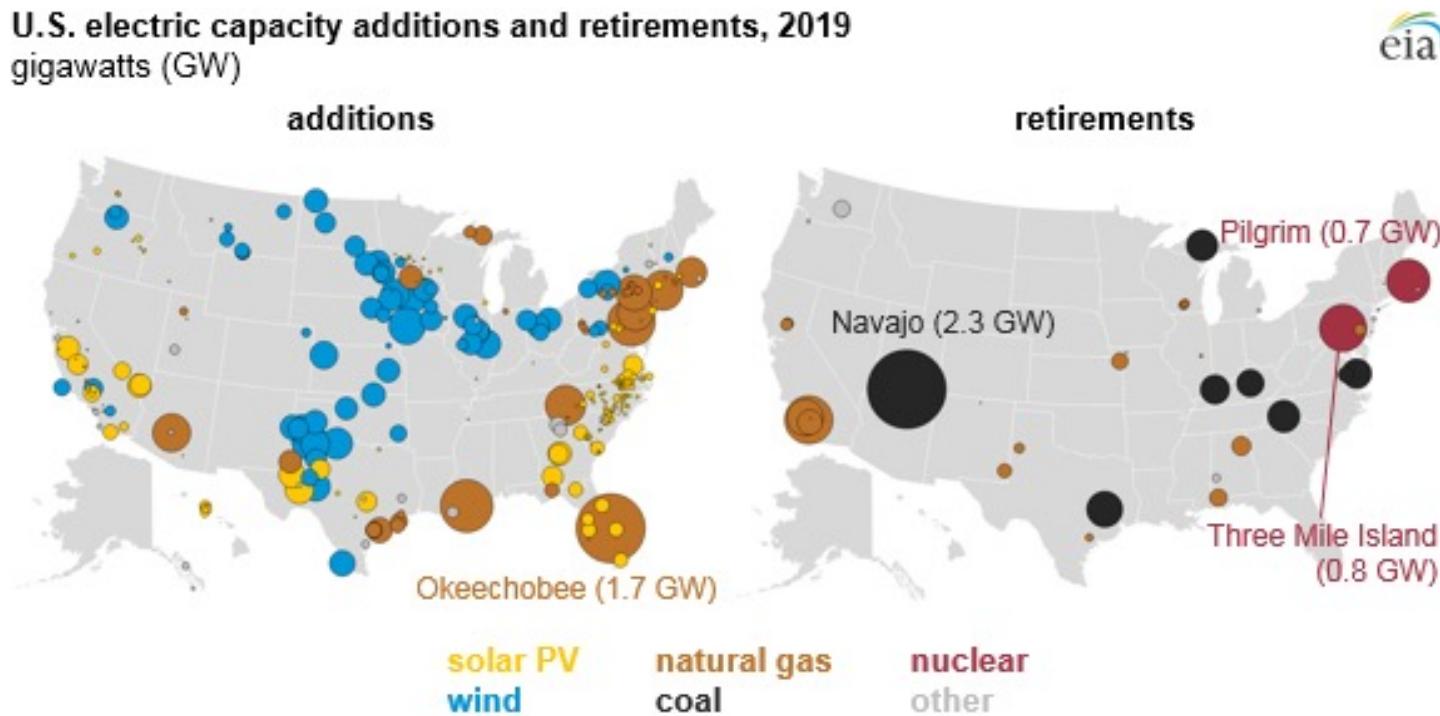
- We take the role of a **central planner** on the **capacity expansion of generating units and transmission lines** to satisfy the increase in demand within a geographical region, like a region corresponding to an Independent System Operator (ISO)



ISOs in North America

# Research Challenges in Transitioning to Renewables

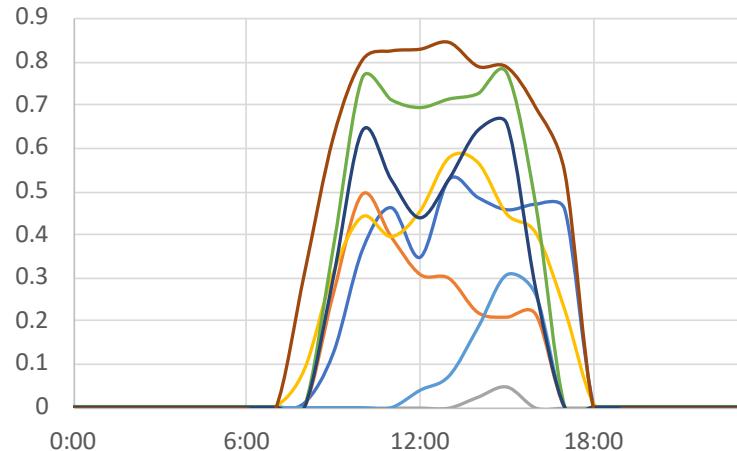
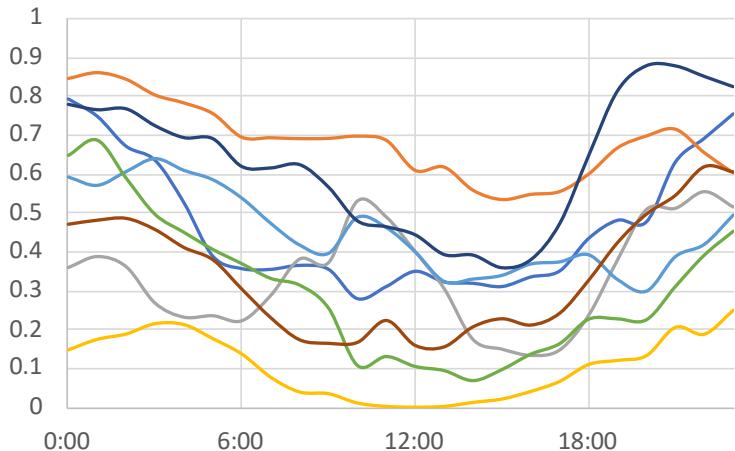
- Renewables concentrate in **remote areas** not well connected to load demand. The model needs to **coordinate transmission and generation** expansion.



# Research Challenges in Transitioning to Renewables

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- Power systems need to be able to adjust to the **volatile** power generation from renewables. The model has to capture the **hourly** variations.



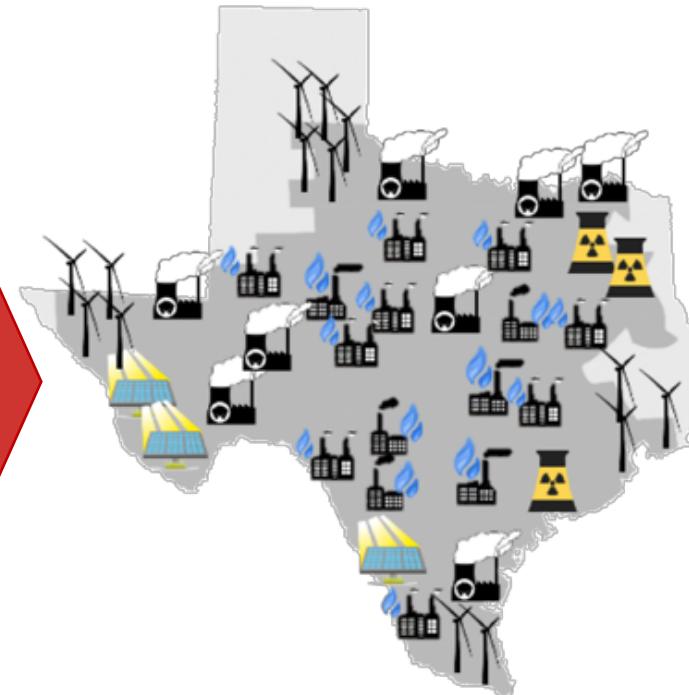
Hourly wind and solar generator output in 8 days

# Generation Transmission Expansion Planning + Unit Commitment

## INPUT

- Energy source (**coal, natural gas, nuclear, solar, wind\***);
- **Generation and storage** technology;
- Location of existing generators;
- Nameplate capacity;
- Age and expected lifetime
- Potential transmission lines
- Emissions
- Operating and investment costs
- **Ramping rates, operating limits, maximum operating reserve.**
- Renewable generation profile.
- Load demand

Minimize the **net present cost** (operating, investment, and environmental).



## OUTPUT

- **Location, year, type and number of generators, transmission lines and storage units** to install;
- When to retire them;
- Whether or not to extend their lifetime;
- Approximate power flow between locations;
- Approximate operating schedule

## Research Challenges

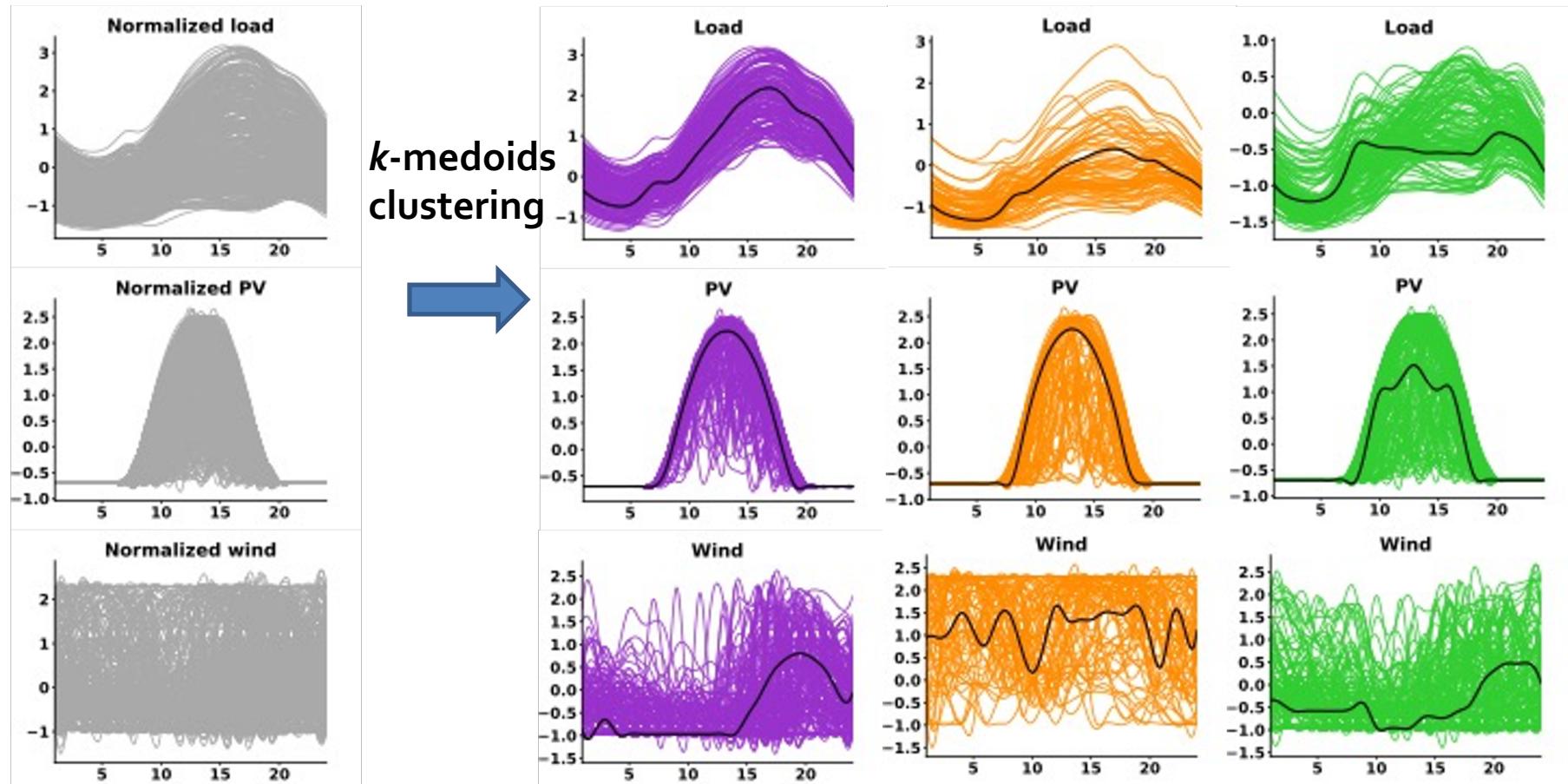
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- **Temporal** complexity:  $20 \text{ years} \times 365 \text{ days} \times 24 \text{ hours} = 175,200 \text{ hours}$
- **Spatial** complexity: Around 500-2,000 individual generators depending on the region
- Complexity of the **optimization problem** with hourly decisions can be easily over **1 billion** variables.

**Intractable. Need simplification**

# Temporal Aggregation

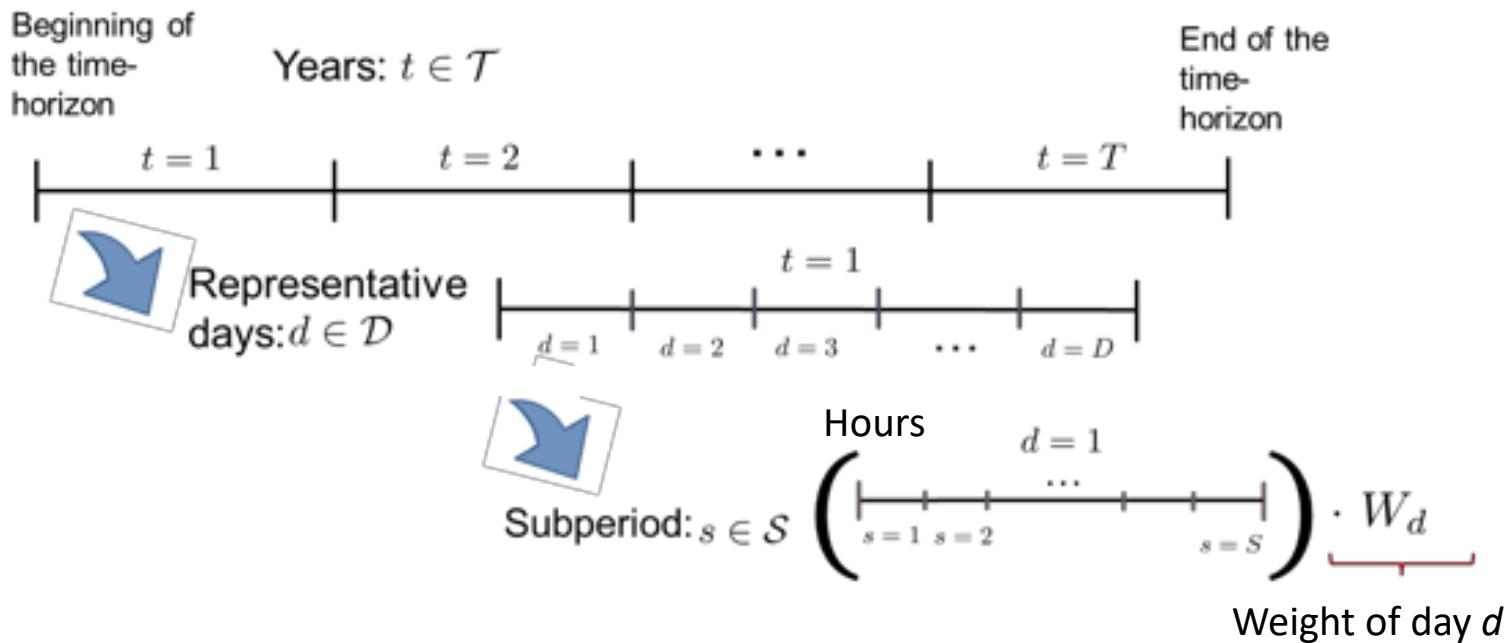
- Aggregate the days with **similar load and renewable output time series** using **machine learning-based clustering algorithms.**



Li, C., A.J. Conejo, J.D. Siirola, I.E. Grossmann. On representative day selection for capacity expansion planning of power systems under extreme events. Working paper.

# Temporal Aggregation

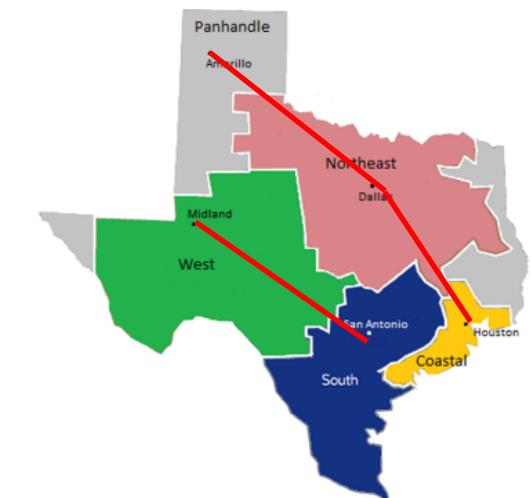
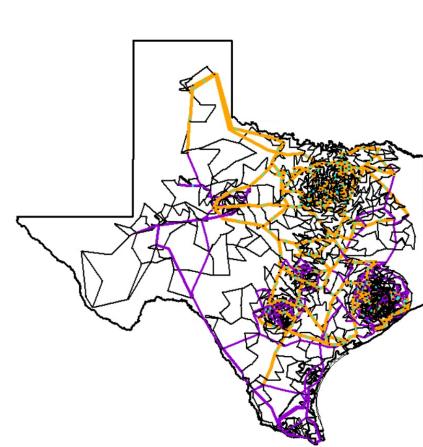
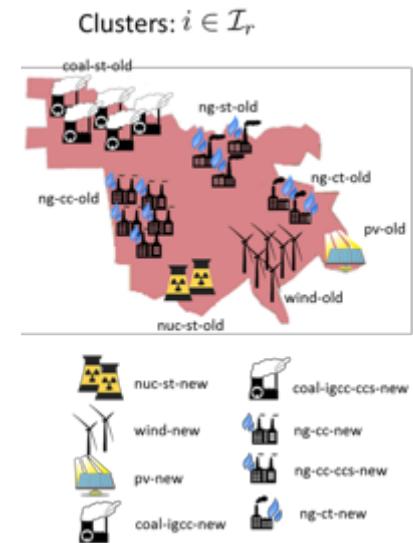
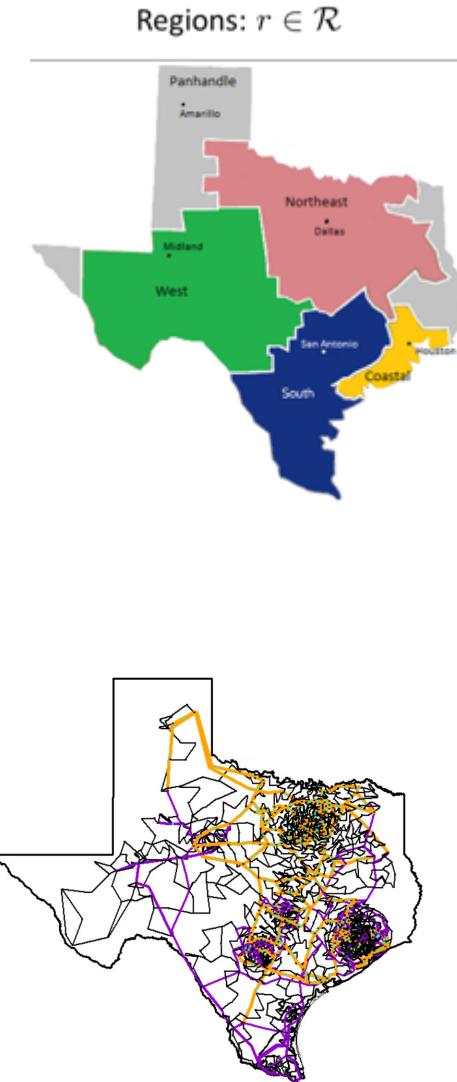
- $d$  **representative days** per year to account for unit commitment and power flow in the **hourly** level



# Spatial Aggregation

## Region and cluster representation

- Area represented by a few **zones**
- Potential locations are the **midpoint** in each zone
- Center for each region:
  - Panhandle (Amarillo), West (Midland), South (San Antonio), Coastal (Houston), Northeast (Dallas).
- Clustering of generators and storage units
- Only consider the **tielines** that connect the centers of two neighboring regions



# Overview of Mixed-integer Linear Programming (MILP) Model

## Objective function:

### **Continuous variables:**

- Power output at sub-period  $s$
- Curtailment generation slack at  $s$
- Power flow between regions at  $s$
- Deficit from renewable quota at  $t$
- Spinning reserve at  $s$
- Quick-start reserve at  $s$
- Voltage angle of region  $r$  at  $s$
- Power level and power charged or discharged at storage cluster  $j$

### **Discrete variables:**

- no. of generators installed at period  $t$
- no. of generators built at  $t$
- no. of generators retired at  $t$
- no. of generators with life extended at  $t$
- whether transmission line  $l$  is installed at  $t$
- whether transmission line  $l$  exists at  $t$
- no. of generators ON at sub-period  $s$
- no. of generators starting up at  $s$
- no. of generators shutting down at  $s$

Minimization of the **net present cost** over the planning horizon comprising:

- Variable operating cost
- Fixed operating cost
- Startup costs
- Cost of investments in new generators, transmission lines and storage units
- Cost to extend the life of generators that achieved their expected lifetime
- Fuel consumption
- Carbon tax for CO<sub>2</sub> emission
- Penalty for not meeting the minimum renewable annual energy production requirement

Lara, C. L., Mallapragada, D. S., Papageorgiou, D. J., Venkatesh, A., & Grossmann, I. E. (2018). Deterministic electric power infrastructure planning: Mixed-integer programming model and nested decomposition algorithm. *European Journal of Operational Research*, 271(3), 1037-1054.  
Li, C., A.J. Conejo, P. Liu, B.P. Omell, J.D. Siirola, I.E. Grossmann. Mixed-integer Linear Programming Models and Algorithms for Generation and Transmission Expansion Planning of Power Systems. Under review in European Journal of Operations Research.

# Overview of Mixed-integer Linear Programming (MILP) Model

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## Summary of constraints:

- **Energy balance** in each region  $r$ .
- **DC power flow** calculate the power flow between any two nodes at each subperiod  $s$
- **Capacity factor** of renewable generators .
- **Unit commitment constraints** to compute the startup and shutdown, operating limits and ramping rates for thermal generators.
- **Operating reserve constraints** to determine the maximum contribution per thermal generator for spinning and quick-start reserves, and the minimum total operating reserves.
- **Investment constraints** to ensure that the planning reserve and renewable energy contribution requirements are satisfied, and to limit the yearly installation per generation type.
- **Balance of generators** to define the number of generators that are **operational**, **built**, **retired**, and have their life **extended** in each time period  $t$ .

# DC v.s. AC Power Flow Equations

---

DC power flow

$$P_i = \sum_{k=1}^N B_{ik}(\delta_i - \delta_k) \quad \forall i \in N$$

Real power only  
Linear equations

AC power flow

$$\begin{aligned} P_i(V, \delta) &= V_i \sum_{k=1}^N V_k (G_{ik} \cos(\delta_i - \delta_k) \\ &\quad + B_{ik} \sin(\delta_i - \delta_k)) \quad \forall i \in N, \end{aligned}$$

$$\begin{aligned} Q_i(V, \delta) &= V_i \sum_{k=1}^N V_k (G_{ik} \sin(\delta_i - \delta_k) \\ &\quad - B_{ik} \cos(\delta_i - \delta_k)) \quad \forall i \in N. \end{aligned}$$

Real and reactive power  
nonlinear equations  
(trigonometric functions)

DC is a good approximation for AC if

- 1) All system branch resistances are approximately zero
- 2) The differences between adjacent bus voltage angles are small
- 3) The system bus voltages are approximately equal to the 1.0 per unit
- 4) Reactive power flow is neglected

# Comparison of Formulations of Transmission Expansion

## Generalized Disjunctive Programming

Grossmann, I.E. and F. Trespalacios, "Systematic Modeling of Discrete-Continuous Optimization Models through Generalized Disjunctive Programming," *AIChE J.* **59**, 3276-3295 (2013).

$$\left[ \begin{array}{c} NTE_{l,t} \\ p_{l,t,d,s}^{\text{flow}} = B_l(\theta_{sr(l),t,d,s} - \theta_{er(l),t,d,s}) \\ -F_l^{\max} \leq p_{l,t,d,s}^{\text{flow}} \leq F_l^{\max} \end{array} \right] \vee \left[ \begin{array}{c} \neg NTE_{l,t} \\ p_{l,t,d,s}^{\text{flow}} = 0 \end{array} \right] \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s$$

## Big M reformulation

$$\begin{aligned} -(1-n_{te_{l,t}})M &\leq p_{l,t,d,s}^{\text{flow}} - B_l(\theta_{sr(l),t,d,s} - \theta_{er(l),t,d,s}) \leq (1-n_{te_{l,t}})M \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s \\ -F_l^{\max}n_{te_{l,t}} &\leq p_{l,t,d,s}^{\text{flow}} \leq F_l^{\max}n_{te_{l,t}} \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s \end{aligned}$$

## Hull formulation

$$\begin{aligned} p_{l,t,d,s}^{\text{flow}} &= B_l \Delta \theta_{l,t,d,s}^1 \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s \\ \theta_{sr(l),t,d,s} - \theta_{er(l),t,d,s} &= \Delta \theta_{l,t,d,s}^1 + \Delta \theta_{l,t,d,s}^2 \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s \\ -\pi \cdot n_{te_{l,t}} &\leq \Delta \theta_{l,t,d,s}^1 \leq \pi \cdot n_{te_{l,t}} \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s \\ -\pi(1 - n_{te_{l,t}}) &\leq \Delta \theta_{l,t,d,s}^2 \leq \pi(1 - n_{te_{l,t}}) \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s \end{aligned}$$

**Tighter formulation, also has more variables**

# Comparison of Formulations of Transmission Expansion

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## Alternative big M formulation

Bahiense, L., Oliveira, G. C., Pereira, M., & Granville, S. (2001). A mixed integer disjunctive model for transmission network expansion. *IEEE Transactions on Power Systems*, 16(3), 560-565.

$$p_{l,t,d,s}^{\text{flow+}} - B_l \Delta\theta_{l,t,d,s}^+ \leq 0 \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s$$

$$p_{l,t,d,s}^{\text{flow-}} - B_l \Delta\theta_{l,t,d,s}^- \leq 0 \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s$$

$$p_{l,t,d,s}^{\text{flow+}} - B_l \Delta\theta_{l,t,d,s}^+ \geq -M_l(1 - nte_{l,t}) \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s$$

$$p_{l,t,d,s}^{\text{flow-}} - B_l \Delta\theta_{l,t,d,s}^- \geq -M_l(1 - nte_{l,t}) \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s$$

$$p_{l,t,d,s}^{\text{flow}} = p_{l,t,d,s}^{\text{flow+}} - p_{l,t,d,s}^{\text{flow-}} \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s$$

$$\theta_{sr(l),t,d,s} - \theta_{er(l),t,d,s} = \Delta\theta_{l,t,d,s}^+ - \Delta\theta_{l,t,d,s}^- \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s$$

$$p_{l,t,d,s}^{\text{flow+}} \leq F_l^{\max} nte_{l,t} \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s$$

$$p_{l,t,d,s}^{\text{flow-}} \leq F_l^{\max} nte_{l,t} \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s$$

$$p_{l,t,d,s}^{\text{flow+}}, p_{l,t,d,s}^{\text{flow-}}, \Delta\theta_{l,t,d,s}^+, \Delta\theta_{l,t,d,s}^- \geq 0 \quad \forall l \in \mathcal{L}^{\text{new}}, t, d, s$$

The authors claim that alternative big M formulation is **tighter** than big M formulation

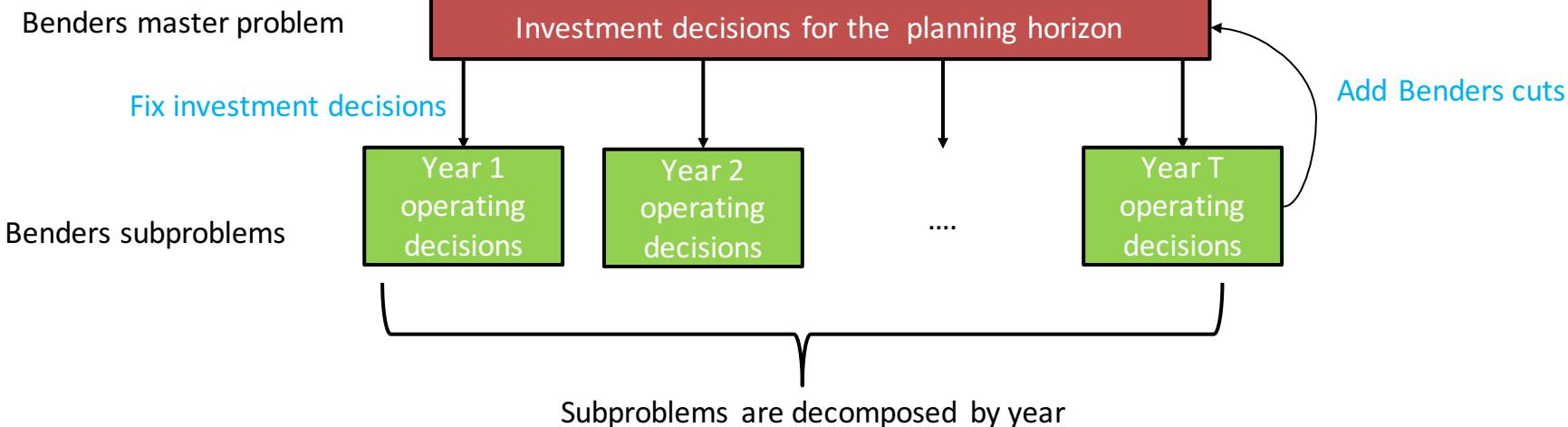
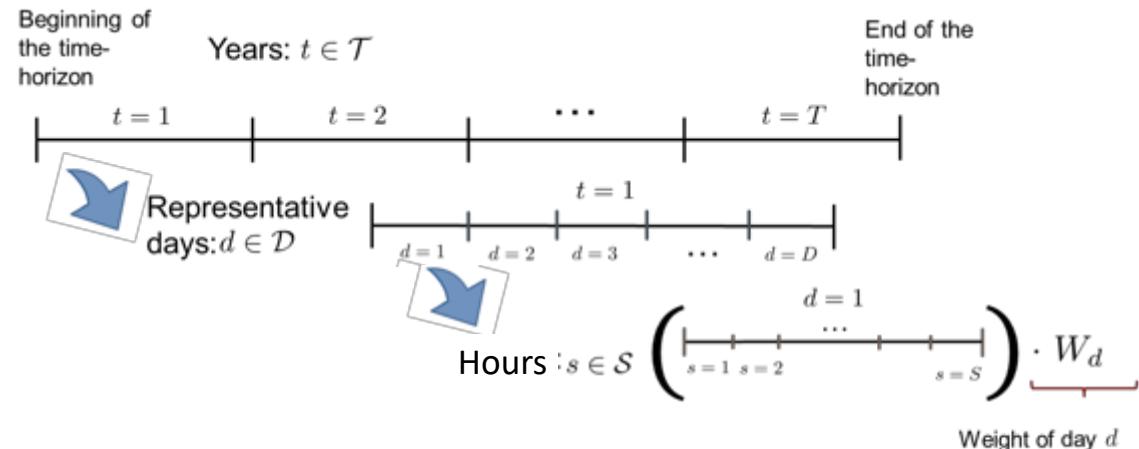
Theorem: The two formulations have **the same feasible region** when project on the original variable space

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# Solution Techniques-Benders Decomposition

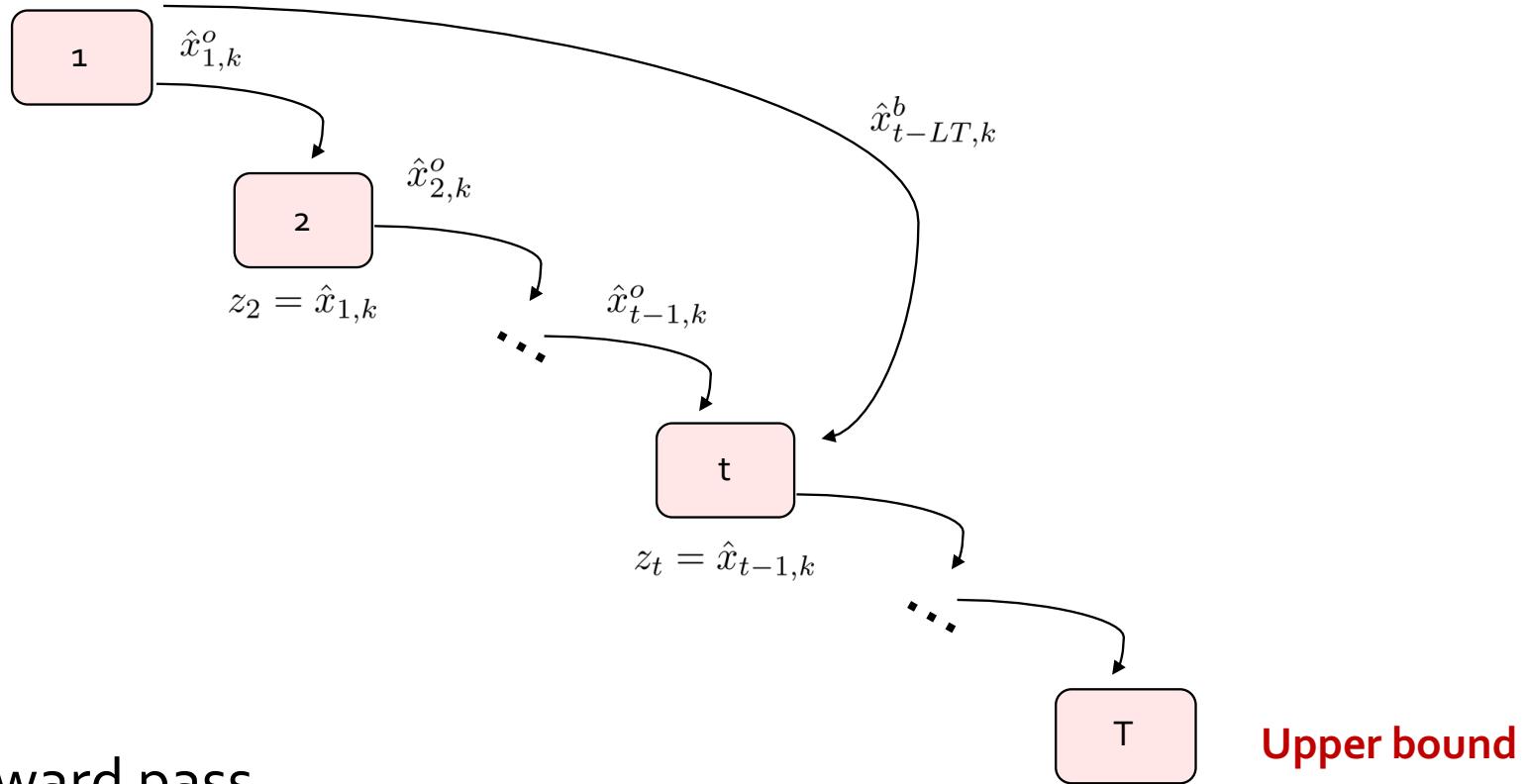
Time scale approach:

**$d$  representative days** per year to account for unit commitment in the **hourly** level



# Solution Techniques-Nested Benders Decomposition

Time period  
 $t = \{1, \dots, T\}$

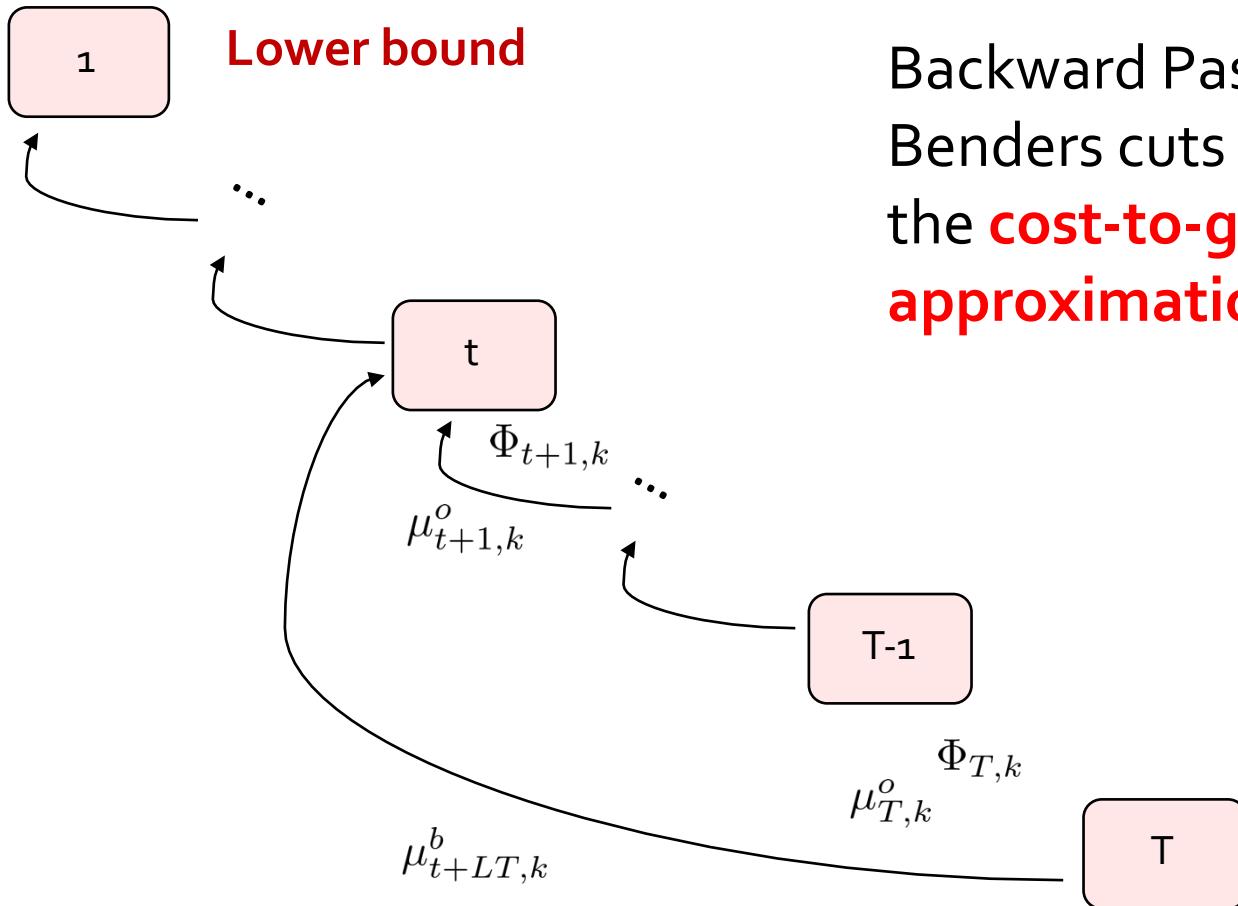


The forward pass  
solves the model in a  
**myopic fashion.**

Lara, C.L. et al., "Electric Power Infrastructure Planning: Mixed-Integer Programming Model and Nested Decomposition Algorithm," *European Journal of Operational Research* **271**, 1037–1054 (2018).  
Birge, J. R. (1985). Decomposition and partitioning methods for multistage stochastic linear programs. *Operations research*, 33(5), 989–1007.

# Solution Techniques-Nested Benders Decomposition

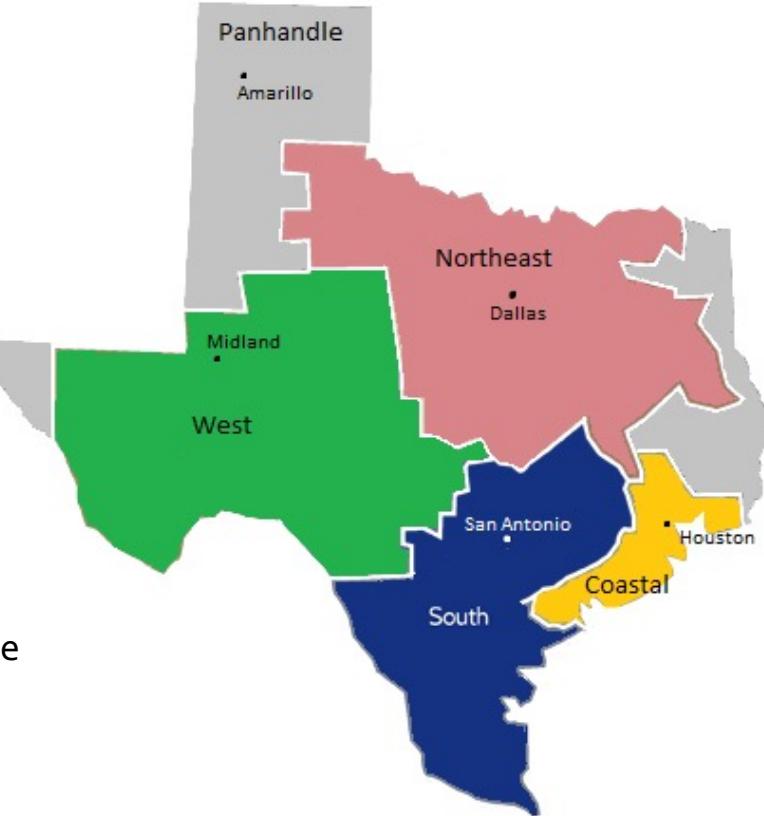
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# ERCOT Case Study

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- 20 year time horizon (1<sup>st</sup> year is 2019)
- **Load** Data from ERCOT database
- **Solar and wind capacity factor** data from NREL
- **Generator cost** information from NREL (Annual Technology Baseline (ATB))
- **Storage data** from Schmidt et al. (2017) Nature Energy.
- **Transmission line** data from Texas Synthetic Grid. Only 500 kV tielines between two neighboring regions are considered
- All costs in 2019 USD
- Regions: Northeast, West, Coastal, South, Panhandle
- **Fuel price** data from EIA Annual Energy Outlook 2016 (reference case)
- **Carbon tax** is zero in the first year and grows linearly across years to \$0.325/kg CO<sub>2</sub>.



# 4 representative days, 15 years results

## Fullspace mixed-integer linear programming (MILP) models

formulation	Integer Var	Binary Var	Continuous Var	Constraints	UB	LB	Wall time
big-M	274,920	2,800	564,826	1,543,966	-	21.13	36,000
alternative big M	274,920	2,800	1,102,426	2,081,566	-	21.13	36,000
hull	274,920	2,800	833,626	2,081,566	-	281.73	36,000

All the problems are solved with Cplex v 12.9.0.0 from Pyomo. **The fullspace model cannot be solved directly. No feasible solution can be found within 10 hours**

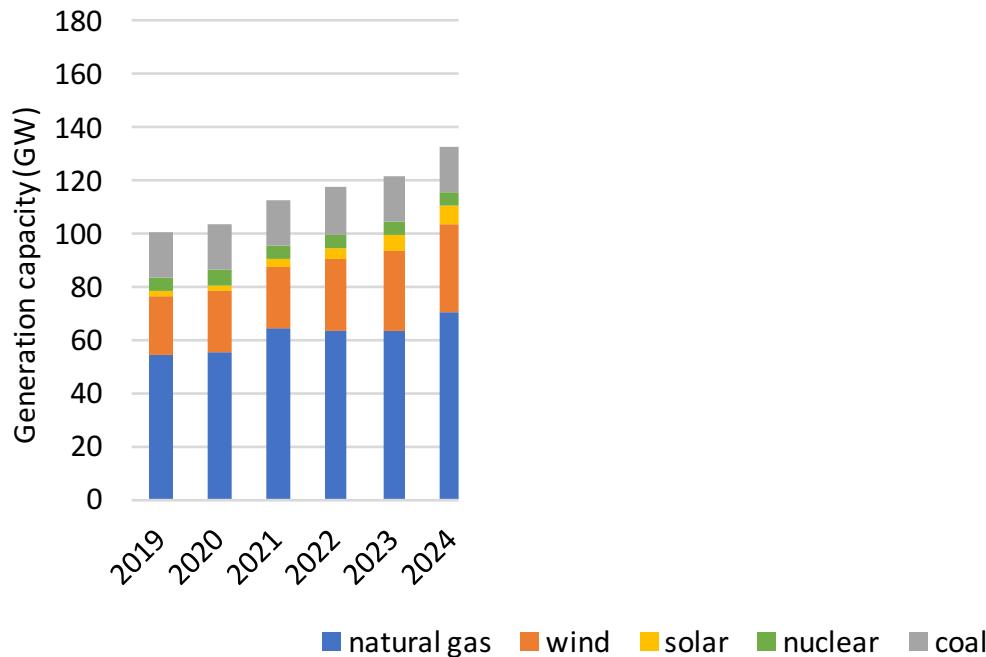
## Decomposition algorithms

algorithm	formulation	ub	lb	gap	Wall time (secs)
Benders	big-M	283.7	282.6	0.38%	5,115
<b>Benders</b>	<b>alternative big M</b>	<b>283.9</b>	<b>281.6</b>	<b>0.82%</b>	<b>3,693</b>
Benders	hull	282.6	280.6	0.71%	8,418
nested Benders	big-M	295.7	268.9	9.98%	53,682
nested Benders	alternative big M	294.2	265.5	10.81%	43,389
nested Benders	hull	288.0	269.3	6.97%	37,577

The **Benders decomposition algorithm with the alternative big-M formulation** has the **best computational performance**

# 20-year Generation Expansion

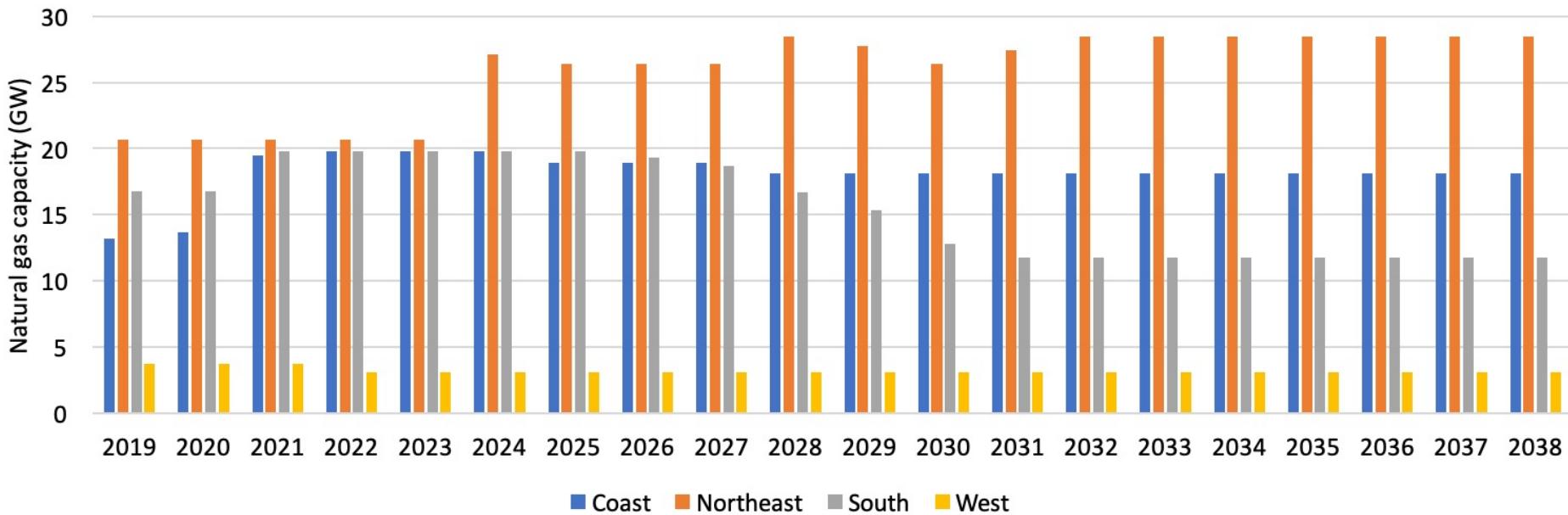
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- Natural gas capacity increases in the beginning and then decreases due to the increase in carbon tax
- Most projected capacity expansion is in wind and solar. **27-fold** increase in **solar** and **87%** increase in **wind**.

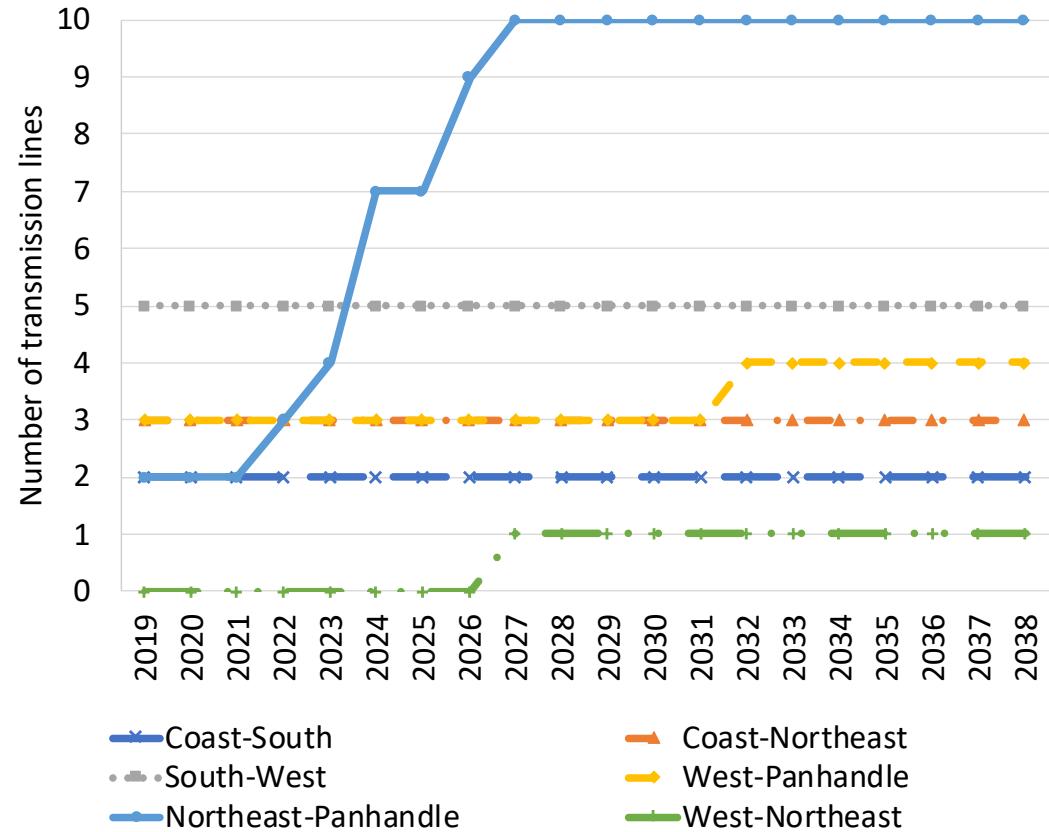
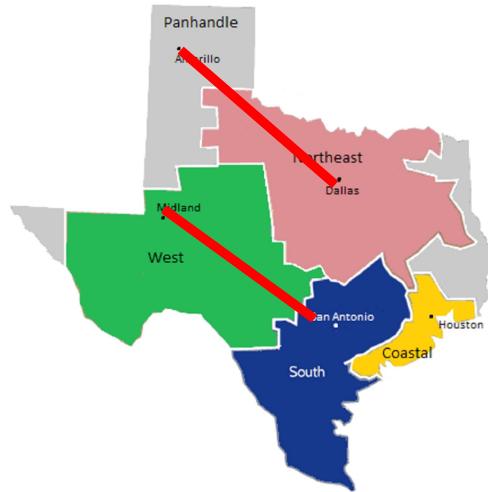
# Geographical Distribution of Natural Gas Capacity

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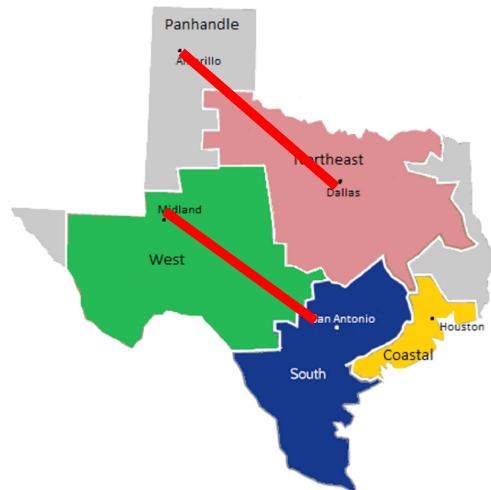
- Most natural gas expansions are expected to take place in the **Northeast** and **Coast** regions where the absolute increase in **load** is **high** and capacity factors for **renewables** are relatively **low**.

# Transmission Expansion

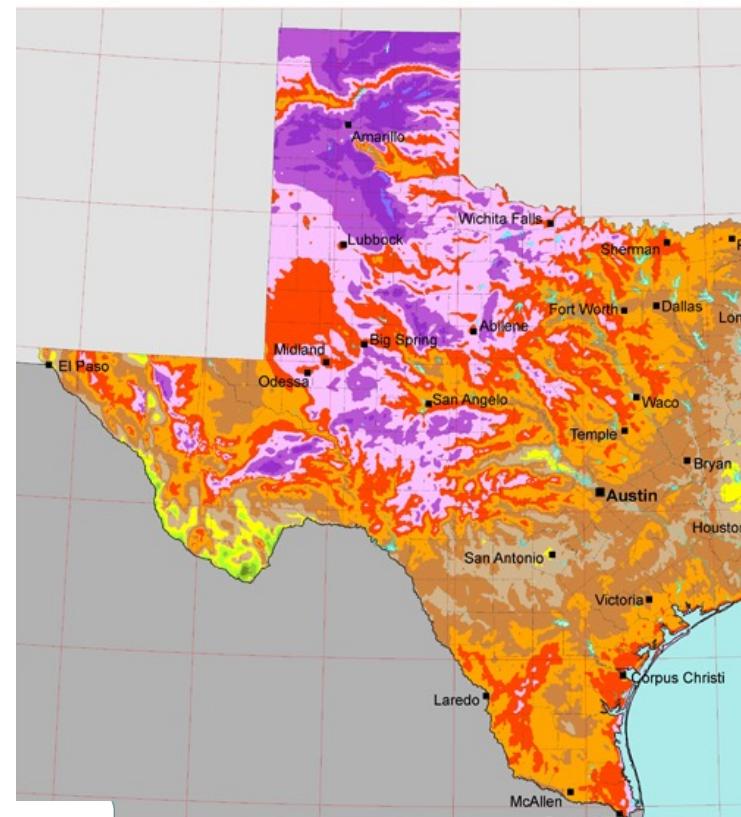


- Most of the transmission lines are built for **Northeast-Panhandle** and **South-West** in order to transfer the power generated by the **renewables** in West and Panhandle to other regions

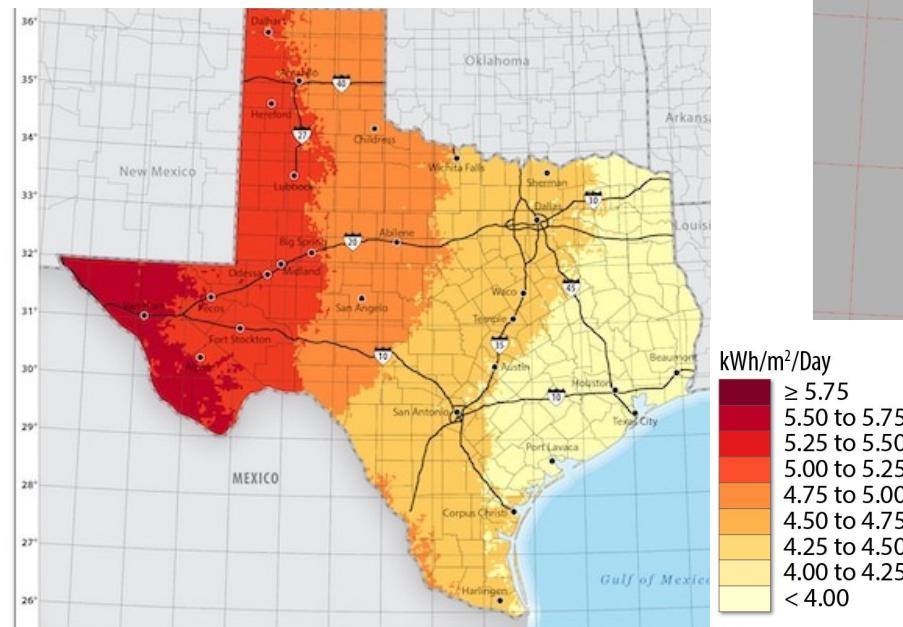
# Transmission Expansion



Average annual wind speed at 80 meter

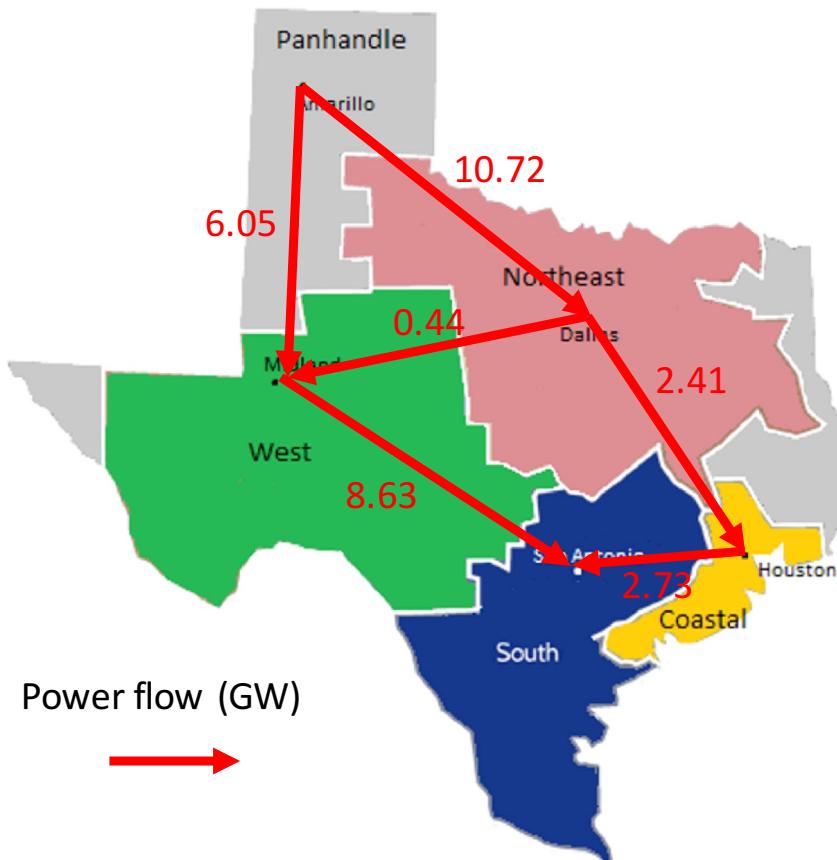


Average annual solar irradiance



Data source: NREL

# Power Flow in ERCOT



The largest power flow magnitudes are **Panhandle-Northeast, West-South** due to the surplus of their renewable energy generation

There are potential benefits in **integrating generation** and **transmission** expansion

Year 20 (2038), representative day 15, 11pm

# Acknowledgment

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- Advisor: Prof. Ignacio E. Grossmann
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  - Prof. Antonio Conejo (OSU)
  - Dr. John Siirola (Sandia)
  - Dr. Benjamin Omell (NETL)
  - Dr. Peng Liu (NETL)
- Acknowledgment
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  - Dr. Dimitri Papageorgiou (ExxonMobil)

