



CASSYS v. 0.9.3 Reference Guide

Physical Models and C# Engine Guide

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1 Introduction

The following document describes the physical models and used to develop the C#-source code available at <u>CASSYS</u>.

Please Note: This document is currently a work in progress, and is updated as new methods are added to the program.



2 General Program Flow

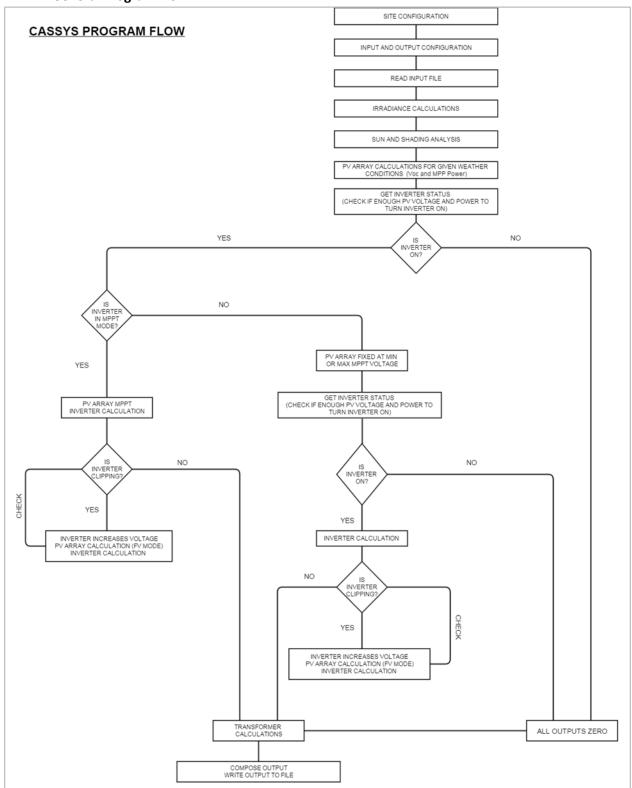


Figure 1: CASSYS v.1 Program Flow



3 List of Classes

A typical simulation flow is shown in Figure 1. Version 1.0 of CASSYS uses 16 classes to complete a simulation:

The following classes simulate physical objects or devices:

- 1) Inverter.cs
- 2) PVArray.cs
- 3) Shading.cs
- 4) Simulation.cs
- 5) Splitter.cs
- 6) Sun.cs
- 7) Tilter.cs
- 8) Tracker.cs
- 9) Transformer.cs

Classes that contain mathematical constructs:

- 1) Daily Astronomical Calculations: Astro.cs
- 2) Linear and Quadratic Interpolation: Interpolate.cs
- 3) Solar Radiation on a Tilted Surface: Tilt.cs

Classes that support program function, configuration and error checking:

- 1) Input File Reading: MetReader.cs
- 2) Site and Simulation Settings: ReadFarmSettings.cs
- 3) Error Logging: ErrorLogger.cs
- 4) Batch or Interface Mode initialization: CASSYS.cs
- 5) Utilities and Unit Conversions: Utilities.cs



4 Classes and Physical Model Guide

Parameters for each class are obtained from the .CSYX file which is defined by the user through the CASSYS MS Excel-based interface. Parameters remain unchanged during the entirety of the simulation, and provide their relevant classes (i.e. their devices or models) with key defining characteristics. The inputs are then processed and reported to an output file selected by the user. The physical models, the parameters used, and the treatment of the input values to obtain relevant outputs are discussed in this section.

4.1 Inverter Inverter.cs

An Inverter converts DC power from a Photovoltaic (PV) Array to AC power, which is then transferred to the grid.

4.1.1 Inputs

 $\begin{array}{ccc} DCPwr_{ln} & & \textit{Input power from the photovoltaic array} \\ V_{in} & & \textit{Voltage dictated by the Inverter (V)} \end{array}$

4.1.2 Outputs

 $\begin{array}{ll} ACPwr_{OUT} & \textit{Input power from the photovoltaic array} \\ V_{InDC} & \textit{Voltage dictated by the Inverter (V)} \\ \end{array}$

Efficiency Efficiency of the Inverter

Losses Losses from the Inverter (Efficiency related)
I_{Out} Current produced (A, AC Single Phase)

ACWiringLoss Losses due to wiring resistance between Inverter and

Transformer

4.1.3 Parameters

PNom AC Nominal AC Power delivered by the Inverter (can be changed

to reflect de-rating)

MPPT Tracking Boolean - specifies If the inverter performs max. power point

tracking, or if the inverter is operating in fixed-voltage mode

MPPT Window Min. Voltage
MPPT Window Max. Voltage

Mum Inverters

Minimum value for MPPT (V) Window

Num Inverters

Number of Inverters in the Sub-Array

Num. Inverters

Number of Inverters in the Sub-Array
Power required to turn the Inverter ON

Min. Voltage Min. DC-side voltage required to turn the Inverter ON (user

defined)

Max. Voltage Max. DC-voltage specification of the Inverter

Output Voltage Output Voltage of the Inverter (dictated by the Grid or step-up

transformer)

OutputPhases Number of phases (AC) at inverter output

Three Efficiency Curves

Boolean - denotes either Single or Three Efficiency Curves

Low VoltageVoltage threshold for low voltage efficiency curve [V]Med VoltageVoltage threshold for medium voltage efficiency curve [V]High VoltageVoltage threshold for high voltage efficiency curve [V]



LowEff MedEff HighEff Single Efficiency Curve Nom. Output Power Wiring Resistance Threshold Power	Jagged Array $[P_{in}][P_{AC}]$, Low Voltage Efficiency Curve Jagged Array $[P_{in}][P_{AC}]$, Medium Voltage Efficiency Curve Jagged Array $[P_{in}][P_{AC}]$, High Voltage Efficiency Curve Jagged Array $[P_{in}][P_{AC}]$, used if Three Efficiency Curve is false Nominal Output Power (W AC) AC wiring resistance(Ω) translated from STC % Loss Minimum power required to turn the Inverter ON given sufficient Voltage (Min. Voltage)
ON Bipolar Clipping	Boolean - if the inverter is ON or OFF Boolean - if the inverter uses bipolar inputs or not Boolean - if the inverter is currently demonstrating power limitation behaviour

These parameters are used to simulate the behaviour and output of the inverter. This information can be exported from an .OND file to the CASSYS database, or by using the manufacturer's datasheet in conjunction with the "Add an Inverter" button in the database (see CASSYS Interface User Manual).

4.1.4 Equations and Model Description

Inverters are responsible for the conversion of DC power into AC power that is transferred to the grid. To achieve this in a safe and controlled manner, the inverter controls the voltage of the PV array based on its operation mode. The inverter must first determine if it has sufficient voltage and power to turn on. Hence the ON or OFF state of the inverter is determined first:

4.1.4.1 Determining ON or OFF State of the Inverter

The following flow chart (Figure 2) summarizes the process to determine if the Inverter has sufficient voltage and Power to turn ON.

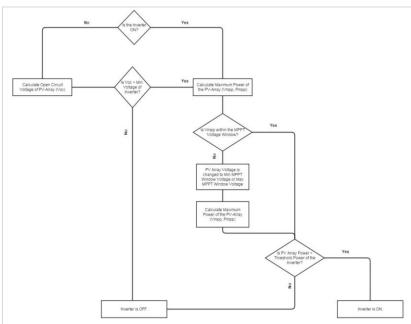


Figure 2: Determining the ON or OFF State of the Inverter



4.1.4.2 DC-Side Voltage Control

The DC-side voltage is controlled by the Inverter based on the operation mode of the Inverter. The impact on DC-side voltage for each operation mode is explained below. For all of these cases, the voltage from the array is divided by two if the inverter uses bipolar inputs.

If the Inverter is OFF

Based on Figure 2, if the Inverter is OFF resulting from insufficient voltage from the PV Array (i.e. V_{oc} < Min. Voltage of Inverter), the Inverter will report the V_{oc} as the DC-side voltage. If the Inverter has sufficient voltage to turn ON, a maximum power point tracking (MPPT) voltage determination is made. This is explained in the next section.

Maximum Power Point Tracking Voltage

If the Inverter has sufficient voltage to turn on, the maximum voltage (V_{MPP}) for given meteorological conditions is calculated. If the V_{MPP} is within the MPPT Voltage Window (V_{MPPmin}, V_{MPPmax}) the DC-side voltage remains at V_{MPP} . If $V_{MPP} < V_{MPPmin}$ or $V_{MPP} > V_{MPPmax}$, the voltage of the DC-array is shifted to V_{MPPmin} or V_{MPPmax} respectively; this value is then used to calculate the power produced by the array.

Power Limiting (or Clipping) Mode

If the calculated output power exceeds the PNom AC of the Inverter for a given input power, the limitation behaviour of the Inverter is activated. The Inverter decreases the power of the PV array to achieve an output power that does not exceed PNom AC; it increases the voltage of the PV Array and the corresponding efficiency is then re-calculated (as long as it does not exceed the maximum voltage of the inverter). The final adjusted PV Array voltage is the voltage at which the Inverter limits power output to its nominal value. The voltage for which the input power is sufficiently reduced to no longer activate the power limitation mode is found using the bisection method along the PV array's Power-Voltage curve.

4.1.4.3 Modelling Efficiency

Inverter efficiency is the ratio of the AC output power (P_{OUT}) and the DC input power (P_{IN}). An inverter's efficiency varies based on input power, the DC voltage, and the inverter temperature (heat related de-rating of Inverters is commonly observed).

The efficiency curve below is provided for some inverters based on the California Energy Commission (CEC) which was adopted from the Sandia and BEW (now DNV-KEMA) test protocol. For more information regarding the test protocol and a list of test results for various inverters, please see [1].



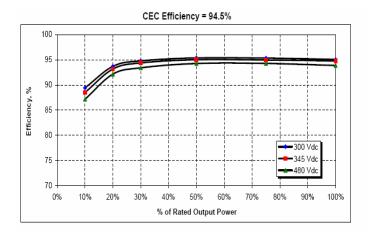


Figure 3: Voltage dependent Efficiency Curve for a sample Inverter [1]

The inverter efficiency curves used in CASSYS are defined by the efficiency measured at 8 different input power points. The inverter output is determined by using a single or a voltage-dependent (8-points each for three voltage levels: Low, Medium and High) efficiency curve based on the information available in the database.

For Single 8-point Efficiency Curve Inverters:

The curve is first translated to a $P_{OUT} = f(P_{IN})$ array using the efficiency values given. The efficiency value for a given input power is then calculated using linear interpolation (see 5.2.1.1).

For Voltage-Dependent Efficiency Curve Inverters:

For a given P_{IN} , the resultant efficiency value from the efficiency curve of each voltage level is calculated using linear interpolation similar to the previous case. This information is then used to create a voltage level vs efficiency curve (at given P_{IN}). The operating voltage of the PV array is then used as the interpolant to determine the efficiency level from the new curve using quadratic interpolation (see 5.2.1.2).

4.2 Photovoltaic Array

PVArray.cs

The PV Array Class evaluates the performance of a solar module using the "standard" or one-diode model as described in Equations and Model Description 4.2.4. The STC condition parameters for the module are obtained from module data-sheets or a .PAN file. Module behaviour is calculated for a number of non-STC operating conditions such as open circuit, fixed voltage, and maximum point tracking. Values are then converted from Module to Array level and losses are applied in accordance with user input values.

4.2.1 Inputs

Shaded POA Beam Component
Shaded POA Diffuse Component
Shaded POA Ground-Reflected
Component

Beam component of plane of array irradiance ($W \cdot m^{-2}$) Diffuse component of plane of array irradiance ($W \cdot m^{-2}$) Ground reflected component of plane of array irradiance ($W \cdot m^{-2}$)



Incidence Angle Angle of Incidence of the Beam Component (Radians)

Wind Speed $(m \cdot s^{-1})$ if provided by user

Measured Module Temperature (°C) if provided by user

Month of the Year For Soiling Percentage to be applied on irradiance

4.2.2 Outputs

Effective Global and Components of Global, Beam, Diffuse and Ground reflected irradiance in POA

POA Irradiance after Soiling and IAM have been applied (W·m⁻²)

Vout Voltage produced by (MPP mode) or dictated by the Inverter

(Fixed-Voltage mode) of the array (V)

lout Current produced by the array under MPP or Fixed-Voltage

Mode (A)

Pout Power produced by the DC Array (W)

TModule Temperature of the array (Calculated/Measured based, °C)

Soiling Loss Power lost due to soiling of the array (W)

Mismatch Loss | Power lost to mismatch of module I-V curves in the array (W)

Module Quality Loss Power lost to LID or aging of modules(W)

Ohmic Losses Power lost to resistance in the wires from array to inverter (W)

Nominal DC Array Power Power of the array under STC conditions

4.2.3 Parameters

Due to the contextual and extensive nature of the parameters required for the modelling of the PV Array, the description of each variable is presented alongside the appropriate equation.

4.2.4 Equations and Model Description

A photovoltaic module is a non-linear DC electrical device which converts the energy of light into electricity by the photovoltaic effect. An equivalent circuit model, the single diode model (SDM), is extensively used to determine the performance of a non-ideal solar cell under various illumination and temperature conditions. Figure 4 shows the equivalent circuit for the model.

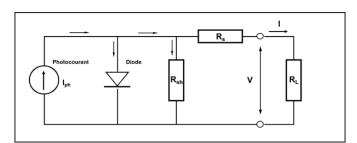


Figure 4: Equivalent circuit for the Single Diode Model (SDM) of a Solar Cell

I-V characteristics of the solar module can be completely described by equation (1).

$$I = I_{\Phi} - I_0 \left[e^{q \frac{(V + IR_S)}{N_{cells} \gamma k T_c}} - 1 \right] - \frac{V + IR_S}{R_{Sh}}$$
 (1)

Where,

 I_{Φ} : Photocurrent of the module [A]

 I_0 : Reverse saturation current of the module [A]

 R_s : Series Resistance of the module $[\Omega]$



 R_{sh} : Shunt Resistance of the module $[\Omega]$

 γ : The diode ideality factor

 T_c : Temperature of the cell [K]

 N_{cells} : Number of cells in the module V: Operating voltage of the module [V] I: Current produced by the module [A]

q: Elementary Charge [C], Constant: $1.602 \times 10^{-19} C$

Parameters of the module are obtained from the module database provided as part of the user interface. For details on adding modules that are not in the database, please see the CASSYS User Manual. The configuration of the panels occurs in the *void Config(..)* method, which then determines the missing parameters required to simulate array performance using the SDM equivalent circuit (see 4.2.5).

4.2.5 SDM Parameter Determination

void CalcGammalPhilrsRef(..)

The first five parameters listed above depend upon the type of module selected for simulation. The only available information to determine these parameters is the I-V curve obtained under standard test conditions (STC). Since the modules do not always operate under STC conditions, the unknown parameters are solved for operation at reference conditions (lending a *Ref* subscript to each parameter).

The values for $R_{series,Ref}$ and $R_{sh,Ref}$ are obtained directly from the database included in CASSYS and can also be specified from other data sources (e.g. .PAN files for modules).

The remaining three variables $(I_{0,Ref},I_{\Phi,Ref},\gamma_{Ref})$ are determined by solving the SDM equation for the three known operating points of the module at STC, i.e. at open-circuit (V_{oc}, 0), at short-circuit (0, I_{SC}), and the maximum power point (V_{MPP},I_{MPP}). These yield three equations and three unknowns which are easily reduced to a function of γ_{Ref} through substitution and elimination. Once γ_{Ref} is obtained using the Newton-Raphson root-finding algorithm, it is substituted back into the previous equations and a solution for each parameter $(I_{0,Ref},I_{\Phi,Ref},\gamma_{Ref})$ is obtained. For more details see 4.2.11.

The dependence on temperature and irradiance of each of these factors is discussed in a later section. First, the method used to determine the effective irradiance reaching a panel and the cell temperature model are discussed.

4.2.6 Effective irradiance on panel surface

void CalcEffectiveIrradiance(..)

The effective irradiance available for electricity conversion is the plane-of-array irradiance after incidence angle effects and soiling have been taken into account. It is therefore:

$$H_{T,eff} = \left(IAM_{dir} \cdot H_{T,dir} + IAM_{dif} \cdot H_{T,dif} + IAM_{dif} \cdot H_{T,ref}\right) \cdot (1 - L_{soil}) \tag{2}$$

Where,



 IAM_x : Incidence Angle Modifier [unitless], with the subscript x indicating the direct, diffuse and reflected components of irradiance (see section 4.2.6),

 $H_{T,x}$: plane of array irradiance [W/m²], with the subscript x indicating the direct, diffuse and reflected components, after shading has been taken into account,

 L_{soil} : soiling loss for the current month, expressed as a fraction (see 4.2.8).

4.2.7 Incidence Angle Modifier (IAM)

4.2.7.1 ASHRAE Model:

The incidence angle of the beam component of the irradiance affects the amount of light reaching the cell due to reflective losses. ASHRAE has proposed a convenient one parameter method of describing the efficiency of transmission for any incidence angle of incoming light [2]. This parameter (b_0) is specified by the user (based on module-specific measurements) and the Incidence Angle Modifier (IAM) is calculated using the relationship shown in (3):

$$IAM = 1 - b_0 \left(\frac{1}{\cos(IA)} - 1 \right) \tag{3}$$

Where,

IAM: Incidence Angle Modifier [unitless]

 b_0 : Single defining parameter for the IAM curve (ASHRAE)

IA: Incidence Angle of the Plane of Array Incidence Component (radians)

The Incidence Angle for the Plane of Array Beam Component is calculated based on the sun's position for a given time step. To see how the Incidence Angle for the Plane of Array Beam Component is calculated in detail, please see 5.2.1.3. Due to the scattered nature of the diffuse and ground-reflected components of the plane of array irradiance, an "averaged" incidence angle is used to determine the incidence angle modifier for these components. CASSYS uses the same angle of 60° to calculate IAM for the diffuse and ground-reflected components in accordance with [3].

4.2.7.2 User-defined IAM Profile:

For some panels, the ASHRAE IAM profile is inadequate. It is then possible for users to define their own IAM profile, by defining the IAM vs. incidence angle curve through a series of points. Equation (3) is then replaced with a Bezier interpolation between the user-defined points.

4.2.8 Soiling Losses

Soiling losses account for the accumulation of dirt, snow, or sand on the panels. Users can specify values on a yearly or monthly basis. The corresponding IAM is applied to every component of plane of array irradiance and after which the user specified soiling loss percentage is applied to the resultant irradiance. This is the irradiance used in further calculations.



4.2.9 Effective Cell Temperature

void CalcTemperature(..)

Cell temperature is modelled using the equation provided below. The equation finds its basis in the Faiman Temperature Model for module temperature [4] but is modified with module adsorption and efficiency to determine the cell temperature. The equation requires an assumption regarding the adsorption of the modules which is assigned to 0.9 in the program.

$$T_c = T_a + \frac{\alpha H_{POA}(1 - \eta_{module})}{U_0 + U_1 * WS} \tag{4}$$

Where,

 T_c : Cell temperature [°C]

 T_a : Ambient air temperature [°C]

lpha : Adsorption coefficient of the module [default value of 0.9 is used]

 H_{POA} : Incident irradiance after soiling and IAM losses are applied [W m⁻²]

 η_{module} : Efficiency of the module in the sub-array (see (5))

 U_0 : Constant Convective heat transfer coefficients [W m $^{-2}$ K $^{-1}$]

 U_1 : Wind Dependent Convective heat transfer coefficient [W m $^{ ext{-}3}$ s $^{ ext{-}1}$]

WS: Wind speed [m/s]

The efficiency of the module is calculated at reference conditions using the following equation:

$$\eta_{module} = \frac{P_{ref}}{H_{ref} * A_{module}} \tag{5}$$

Where,

 P_{ref} : Rated power of the module at reference conditions (W)

 H_{ref} : Irradiance at reference conditions (W·m²)

 A_{module} : Individual module area (m²)

4.2.10 I-V Curve Parameters at Effective Conditions

void CalcIVCurveParameters(...)

4.2.10.1 Diode Ideality Factor

void CalcGammaCoeff()

The diode ideality factor varies with temperature and is determined in order to best match the temperature correction factor of the maximum power point defined the module database (or PAN file). The determination is done using the Power at reference conditions and by assuming a temperature of 25°C higher than reference. This evaluation of the gamma coefficient assumes a linear dependence of the ideality factor on temperature. The following equation is used to adjust the ideality factor at reference conditions to a calculated cell temperature, T_C :

$$\gamma = \gamma_{ref} - \gamma_{coeff}(T_c - T_{ref}) \tag{6}$$

4.2.10.2 Reverse Saturation Current

The reverse saturation current of the module is dependent upon cell temperature T_c and the relationship is defined using physical principles as below [3]:



$$I_0 = I_{0,ref} \left(\frac{T_c}{T_{c,ref}} \right)^3 \exp \left[\frac{qE_g}{\gamma k} \left(\frac{1}{T_{c,ref}} - \frac{1}{T_c} \right) \right]$$
 (7)

Where,

 I_0 : Reverse Saturation Current

 $I_{0,ref}$: Reverse Saturation Current at reference conditions

 T_c : Calculated cell temperature [K] (see 4.2.9)

 $T_{c,ref}$: Cell temperature at reference conditions (or at T_{ref}) [K]

q: Elementary Charge [C], Constant: $1.602 \times 10^{-19} C$

 γ : Temperature adjusted diode ideality factor [1/K]

 E_q : Band-gap of the cell material (CASSYS only simulation Si based solar modules, 1.12 eV)

k: Boltzmann Constant, 1.381 x 10^{-23} m² kg s⁻² K⁻¹

4.2.10.3 Shunt Resistance

CASSYS uses the PVsyst irradiance-dependent shunt resistance model (8) which requires the definition of an exponential decay constant and a shunt resistance value at 0 irradiance, $R_{sh}(0)$. Review of prior work [5] shows that the best exponential parameter for any technology is 5.5 whereas, the $R_{sh}(0)$ is typically $4 \times R_{sh,ref}$. CASSYS uses the values in the database for both of these parameters and uses the $R_{sh}(0) = 4 * R_{sh,ref}$ rule as a default if the value is not defined for a selected module.

$$R_{sh} = R_{sh,base} + \left[R_{sh}(0) - R_{sh,base} \right] \exp \left[-R_{sh,exp} \frac{H}{H_{ref}} \right]$$
 (8)

Where,

 R_{sh} : Irradiance adjusted shunt resistance of the module $[\Omega]$

 $R_{sh,base}$: Fitting parameter [Ω] defined as,

$$R_{sh,base} = R_{sh,ref} + R_{sh}(0) * \exp(-R_{sh,exp})/(1 - \exp[-R_{sh,exp}])$$
(9)

 $R_{sh.exp}$: Exponential decay rate fixed to 5.5 in the program

H: Effective Plane of Array Irradiance [Wm⁻²]

 H_{ref} : Irradiance used at Reference Conditions [Wm⁻²]

4.2.10.4 Photo-generated Current

Photo-generated current is affected by temperature which is calculated using the current temperature coefficient ($I_{sc,T-coeff}$) listed in the database for the module selected) and the irradiance through a proportionality relationship. The temperature coefficient is typically specified by module manufacturers in module datasheets. The equation to calculate effective photo-generated current at given temperature and irradiance takes the following form:

$$I_{\Phi} = \frac{H}{H_{ref}} \left[I_{\Phi, \text{ref}} + I_{sc, T-coeff} (T_c - T_{ref}) \right]$$
(10)



Where,

 I_{Φ} : Temperature and irradiance adjusted photo-current [A]

 $I_{\Phi, ref}$: Photo-current determined at reference conditions [see 4.2.54.2.5]

 $I_{T-coeff}$: Current temperature coefficient [A/°C]

 T_c : Calculated cell temperature [K] (see 4.2.9)

 T_{ref} : Cell temperature at reference conditions (or at T_{ref}) [K]

4.2.10.5 Open-Circuit Voltage

Open-circuit voltage is affected by temperature and the relationship is best summarized by the voltage temperature coefficient ($V_{oc,T-coeff}$). To calculate the effective open-circuit voltage at given cell temperature one can use the following:

$$V_{oc} = V_{oc,ref} + V_{oc,T-coeff} * (T_c - T_{ref})$$

$$(11)$$

Where,

 V_{oc} : Temperature adjusted open-circuit voltage of the module [V]

 $V_{oc,ref}$: Open-circuit voltage at reference conditions [V]

 $V_{T-coeff}$: Open-circuit voltage temperature coefficient [V/°C]

 T_c : Calculated cell temperature [K] (see 4.2.9)

 T_{ref} : Cell temperature at reference conditions (or at T_{ref}) [K]

H: Effective Plane of Array Irradiance [Wm⁻²]

 H_{ref} : Irradiance used at Reference Conditions [Wm⁻²]

4.2.11 Array to Inverter Wiring Resistance

The wiring resistance is specified by the user for the entire sub-array in terms of a percentage loss at maximum production by the modules in the sub-array ($R_{\%,STC}$). This loss percentage is translated to an equivalent wiring resistance R_{w} 'seen' by each module, using the following equation:

$$R_w = \frac{N_S}{N_p} R_{\%,STC} \left(\frac{P_{mpp}}{I_{mpp}^2} \right) \tag{12}$$

Where,

 N_s : Number of modules in series in each string of the sub-array

 N_p : Number of modules in parallel in the sub-array

 P_{mnn} : Maximum power the module can produce [W]

 I_{mvv} : Current of the module at the maximum power point [A]

This resistance is treated as an additional resistance in series with the series resistance. The effective equation for the SDM is then changed to:

$$I = I_{\Phi} - I_0 \left[e^{q \frac{[V + I(R_S + R_W)]}{N_{cells} \gamma k T_C}} - 1 \right] - \frac{V + I(R_S + R_W)}{R_{sh}}$$
 (13)



4.2.12 Calculating Module Performance

void CalcAtMaximumPowerPoint()

After the effective I-V curve parameters and the revised SDM equations are established, the module performance can be calculated based on the operating mode of the array (i.e. if the array is allowed to operate at its maximum power point (MPP) or at a fixed-voltage).

Due to the implicit nature of the revised SDM equation, the Newton-Raphson root-finding algorithm is used to determine the current produced by the module at any voltage V. For more information on how this algorithm is implemented, please see [6] and [7].

The maximum power of the module is then determined by the golden-ratio search algorithm [7].

4.2.13 Calculating Array Performance

void CalcModuleToArray(...)

The calculations in 4.2.12 are done at the module level and must be translated to the array using the configuration of the modules. The current produced by the number of modules in parallel will add, whereas voltage for number of modules in series will add. The effective current and voltage are determined after applying the following losses to the array performance. The losses currently accepted by CASSYS (v 0.9) are discussed briefly in the next few sub-sections.

4.2.13.1 Module Quality Loss

The user provides a percentage loss ($L_{\%,modquality}$) at standard conditions reflecting losses in module quality due to LID and module aging, etc. The loss is calculated using the following:

$$L_{modquality} = I_{array} \cdot L_{\%,modquality} \cdot V_{array}$$
 (14)

This percentage is then applied to the current produced by the array and a new current value is determined:

$$I_{array,1} = I_{array} \left(1 - L_{\%,modquality} \right) \tag{15}$$

4.2.13.2 Mismatch Loss

The user provides a percentage loss occurring due to the mismatch of module current-voltage characteristics results. The losses resulting from this mismatch would be different if the array is operating at its maximum power point (MPP) or if it forced by the inverter to operate at a fixed voltage (FV). Hence, the user can provide a percentage loss at each condition. Typically the fixed voltage operating mode incurs a higher performance penalty. The percentage loss is applied to the current produced by the array based on the operating mode.

$$L_{mismatch} = I_{array} \cdot L_{\% \ mismatch,FV/MPP} \cdot V_{array}$$
 (16)

This percentage is then applied to the current produced by the array and a new current value is determined:

$$I_{array,2} = I_{array,1} \left(1 - L_{\% \, mismatch,FV/MPP} \right) \tag{17}$$



4.2.13.3 Ohmic Losses

Given the effective wiring resistance (R_w) for the entire sub-array (see 4.2.11), the ohmic loss is calculated using ohms law:

$$L_{ohmic} = I_{array,2}^2 \cdot R_w \tag{18}$$

4.2.13.4 Soiling Losses

As discussed earlier (4.2.13.4), the soiling loss percentage specified by the user is directly applied to the incident irradiance. To estimate the power lost to soiling, the program calculates the losses using the following:

$$L_{soiling} = I_{array} \cdot \frac{L_{\%,soiling}}{(1 - L_{\%,soiling})} \cdot V_{array}$$
 (19)

4.2.13.5 Power Produced by the Array

Since all other losses are accounted for by reducing the effective current produced by the array, the ohmic loss is applied in the end. The total power produced by the array after all is then given by:

$$P_{array} = V_{array} \cdot I_{array} - L_{ohmic}$$
 (20)

4.3 Shading Shading.cs

This class calculates the shading factors on the beam, diffuse and ground-reflected components of incident irradiance based on the sun position throughout the day resulting from a near shading model. Shading models are available for panels arranged in an unlimited rows or a fixed tilt configuration. If the unlimited row model is to be used, the model can be further customized to use a linear shading model or a cell based (step-wise) shading model.

4.3.1 Inputs

Sun Zenith

Sun Azimuth

POA Beam Irradiance

POA Diffuse Irradiance

POA Ground-Reflected

Irradiance

Zenith angle of the sun (rad)

Azimuth angle of the sun (rad)

Beam component of POA irradiance (W·m⁻²)

Diffuse component of POA irradiance (W·m⁻²)

Ground reflected component of POA Irradiance (W·m⁻²)

4.3.2 Outputs

Beam Shading Factor (SF)

Diffuse SF

Ground-Reflected SF

Profile Angle

Shading factor applied to POA Diffuse Irradiance

Profile Angle

Shading factor applied to POA Ground-Reflected Irradiance

Profile angle of the sun [see (21)]

Sum of all components after respective shading factors are applied (W·m²²)

Shaded Beam POA Irradiance

Shading factor applied to POA Beam Irradiance

Profile angle of the sun [see (21)]

Sum of all components after respective shading factors are applied (W·m²²)

POA Beam Irradiance with SF applied (W·m²²)

POA Diffuse Irradiance with SF applied (W·m²²)



Shaded Ground-Reflected POA	POA Ground-Reflected Irradiance with SF applied (W·m ⁻²)
Irradiance	

4.3.3 Parameters

Fixed-Tilt Configuration:

Plane of Array Tilt

Tilt of the modules installed relative to the ground (rad)

Plane of Array Azimuth

Azimuth angle of the modules relative to True South (rad)

For the Unlimited Rows Configuration, the following are required in addition to the above (see Figure 5):

SLA Shading Limit Angle
Width of Active Area See Figure 5 (m)
Pitch Distance between consecutive ro

Pitch Distance between consecutive rows of modules (m)
Number of Rows Number of rows in the far, Unlimited Rows Configuration

The above parameters allow for the calculation of a linear shading model (with respect to Profile Angle), for the non-linear shading model, the following additional parameters are required (see Figure 5):

Number of Modules

Cell Size

Number of modules in width of active area

Size of the cell in the transverse direction (cm)

4.3.4 Shading Model for Unlimited Rows Configuration

The unlimited row configuration is an array configuration in which panels are placed on racking with a fixed tilt with rows of such racks placed behind one another. CASSYS considers the length of such rows to be long enough to not consider any edge effects in its shading model. This assumption reduces the calculation of the shading factor at different times of the day to a simple geometrical construct. The user can specify the following parameters regarding the row orientation summarized in the image below:

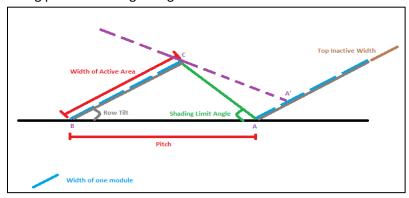


Figure 5: Unlimited Rows Orientation and Shading Analysis

The shading limit angle (SLA) is the angle formed by the top inactive width (if defined as shown in row 2) to the bottom of the active area for the following row. It is determined using the cosine law (two sides and an angle of the triangle ABC are known). This calculation is done in the interface and provided to the user. The second useful angle is the profile angle of the sun at a given time. The profile angle (PA) is defined as the projection of the solar altitude angle (complement of zenith angle) on a vertical plane perpendicular to the array [3]. For a given Sun Zenith (S_Z) and Azimuth (S_A) and for a Collector Azimuth (S_A), the PA is calculated with equation (21).



$$PA = \arctan\left[\frac{\tan\left(\frac{\pi}{2} - S_Z\right)}{\cos(S_A - C_A)}\right]$$
 (21)

4.3.4.1 Linear Shading Factor on the POA Beam Component

For shading to occur, the profile angle of the sun must be lower than the shading limit angle. If this is true, the length of AA' is the portion of a row shaded by the preceding row. To determine the length of the shaded portion, the following equations (22)-(83) are used:

$$AC = \frac{\sin(Row \, Tilt)}{\sin(SLA)} Collector \, Width \tag{22}$$

$$\angle CAA' = \pi - Row \ Tilt - SLA$$
 (23)

$$\angle CA'A = \pi - CAA' - (SLA - PA)$$
 (24)

$$AA' = \frac{AC \cdot \sin(SLA - PA)}{\sin(CA'A)}$$
 (25)

The shaded fraction for the beam component is given by the ratio of the collector width and the AA' calculated from equation (83).

4.3.4.2 Cell-based Shading Model on the POA Beam Component

In the cell-based shading model, the entire section (modules placed alongside in the length of the row) is considered inactive as soon as the first cell of that module is completely shaded. Once the length of the shaded section is calculated from (25), the model determines the number of cells under this section (26).

$$N_{cells \, shaded} = \frac{AA'}{Cell \, Size} \tag{26}$$

When the last cell of section *S* is shaded by the preceding row, the shading fraction is the ratio of the section number and the total number of sections (or modules) in the active area width.

$$SF_S = \frac{S}{N_{modules,Active\ Area}}$$
 (27)

The shading fraction maximizes for a given section at SF_s once a module is completely shaded, and follows a linear pattern until the first cell in each module section is completely shaded.

4.3.4.3 Shading factor on the POA Diffuse Component

The shaded fraction for the diffuse component is calculated using the view factor of the sky for a tilted surface obstructed by the row in front of it. For more information regarding view factor integrals, please see [8].

$$Diffuse Shading Fraction = \frac{1 + \cos(SLA)}{2}$$
 (28)



4.3.4.4 Shading factor on the POA Ground-Reflected Component

Due to the arrangement of the rows, only the rows other than the first row will experience shading from preceding rows. CASSYS adjusts for this by scaling the shading factors based on a row block factor. The row block factor is given by (29). This is applied to the diffuse and beam shading factor as above in the linear shading case. This adjustment is not applied to the beam shading factor calculated using the cell based shading model.

$$Row\ Block\ Factor = \frac{Number\ of\ Rows - 1}{Number\ of\ Rows}$$
 (29)

Using the above, the shading factor for the ground-reflected component is given by (29)(83).

Ground Reflected Shading Factor =
$$1 - Row Block Factor$$
 (30)

From the definition of the diffuse and ground-reflected shading factor, it is clear that these remain constant over the year, and hence are calculated only once by the program.

4.4 Trackers Tracker.cs

This class is responsible for determining the array orientation when trackers are used in solar plants. The tracking mode depends on the inputs provided by the user. The effect of backtracking strategies is also calculated in this class.

4.4.1 Inputs

Tracker Axis Tilt Angle between tracking axis and horizontal (°) Angle of proj. horizontal tracker axis rel. to true South (°) Tracker Axis Azimuth Minimum Tilt Minimum slope of tracker surface wrt. horizontal (°) Maximum slope of tracker surface wrt. horizontal (°) Maximum Tilt Minimum angle of rotation of surface about tracker axis (°) Minimum Rotation Angle Maximum Rotation Angle Maximum angle of rotation of surface about tracker axis (°) Minimum Azimuth Minimum angle of horizontal proj. of normal to module surface and true South (°) Maximum angle of horizontal proj. of normal to module Maximum Azimuth surface and true South (°) Angle between horizontal proj. of a ray from sun and true Sun Azimuth South (°) Angle between elevation of sun and vertical (°) Sun Zenith Tracker Pitch Distance between two rows of trackers (m) Tracker Bandwidth Width of single tracker array (m)

4.4.2 Outputs

Tracker Azimuth
Angle of proj. horizontal axis relative to true South (°)
Angle between tracking axis and horizontal (°)
Surface Azimuth
Angle between horizontal proj. of normal to module surface and true South (°)



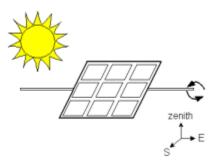
Surface Slope Rotation Angle Angle of tracker surface wrt. horizontal (°)
Angle of rotation of surface about tracker axis (°)

4.4.3 List of Methods

public void Calculate(...)
public void Config()

4.4.4 Equations and Model Descriptions

4.4.4.1 E-W Elevation Tracker



E-W elevation trackers allow the panel to track the sun's movement vertically throughout the day. The tracker's tilt angle β is given by the following equation, where θ_z is sun zenith, γ_s is sun azimuth, γ_a and is axis azimuth.

$$\beta = \arctan(\tan(\theta_z) * \cos(\gamma_s - \gamma_a))$$
(31)

If the calculated slope is negative, an angle of 180 degrees is added.

If the sun azimuth is greater than the axis azimuth, then the surface azimuth γ is given by

$$\gamma = \gamma_a + \frac{\pi}{2} \tag{32}$$

If the sun azimuth is less that the axis azimuth, then the surface azimuth γ is given by

$$\gamma = \gamma_a - \frac{\pi}{2} \tag{33}$$

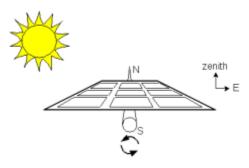
When backtracking is selected, the outputted surface slope is adjusted by the backtracking correction angle, ω_c , which is calculated from the tracker pitch, TP, and the tracker bandwidth, TW. The equation for finding the correction angle is found below



$$\omega_c = \arccos\left(TP * \frac{\cos(\beta)}{TW}\right) \tag{34}$$

The outputted surface angle β is then adjusted by the correction angle.

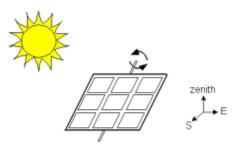
4.4.4.2 N-S Axis Tracker



N-S axis trackers allow the panel to track the sun's movement from east to west, rotating on an axis from north to south (axis azimuth of 0°). The model used to calculate the tilt angle is the same as with the E-W elevation tracker, except that the axis azimuth value is 0.

With backtracking enabled, the same correction angle from the E-W tracker is calculated and applied.

4.4.4.3 Tilt and Roll Tracker



Tilt and Roll trackers allow the panel to follow the sun by rotating on a tilted axis with a user defined azimuth, γ_a , and tilt angle, β_a . The rotation angle, R, of the tracker is given by the equation

$$R = \arctan\left[\frac{\sin(\theta_z) * \sin(\gamma_s - \gamma_a)}{\cos(\theta_z) * \cos(\beta_a) + \sin(\theta_z) * \sin(\beta_a) * \cos(\gamma_s - \gamma_a)}\right]$$
 (35)

The slope of the module, β , is calculated with the equation

$$\beta = \arccos(\cos(R) * \cos(\beta_a)) \tag{36}$$



The surface azimuth, γ , is calculated using one of the three equations below depending on the rotation angle. If the rotation angle is between -180 degrees and -90 degrees then the azimuth is calculated with

$$\gamma = \gamma_a - \arcsin\left(\frac{\sin(R)}{\sin(\beta)}\right) - \pi \tag{37}$$

If the rotation angle is between 180 degrees and 90 degrees then the azimuth is calculated with

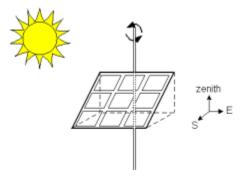
$$\gamma = \gamma_a - \arcsin\left(\frac{\sin(R)}{\sin(\beta)}\right) + \pi \tag{38}$$

If the rotation angle is outside either of those ranges then the azimuth is calculated with

$$\gamma = \gamma_a + \arcsin\left(\frac{\sin(R)}{\sin(\beta)}\right) \tag{39}$$

In the reference papers [9] for these equations, an azimuthal angle was defined between 0 and 360 degrees clockwise from true north, whereas CASSYS uses an azimuthal angle of -180 through 180 degrees, with \pm 180 degrees being true north. Due to this difference of angle convention, 360 degrees will be added or subtracted to the CASSYS angle in order to rectify this difference.

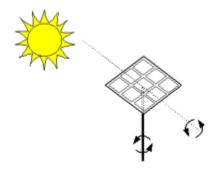
4.4.4.4 Azimuth Tracking



Azimuth trackers follow the sun's azimuth exactly. With this type of tracker, the slope of the panel is fixed but the surface azimuth is equal to that of the sun within the limits on the surface azimuth defined by the user.



4.4.4.5 Two Axis Tracking



Two axis trackers follow both the sun's zenith and azimuth. The tilt of the surface is equal to the zenith of the sun and the surface azimuth is equal to the azimuth of the sun, which keeps the incidence angle of the beam at 0 degrees to the normal within the azimuthal and tilt limits defined by the user.

4.5 Simulation Simulation.cs

This class is responsible for determining the various interactions between the other classes and has methods that are used to control behaviour of certain components.

4.5.1 Inputs

4.5.2 Outputs

4.5.3 List of Methods

4.5.4 Equations and Model Descriptions

4.6 Splitter Splitter

This class calculates beam and diffuse irradiance, given global horizontal irradiance (or its components).

4.6.1 Inputs

Sun Zenith	Zenith angle of the sun [radians]
Global Horizontal Irradiance	Measured/Calculated (W·m ⁻²)
Diffuse Horizontal Irradiance	Measured (W·m⁻²)
Direct Normal Irradiance	Measured (W·m⁻²)
Direct Horizontal Irradiance	Measured (W·m⁻²)
Normal Extraterrestrial Irradiance	Measured (W·m⁻²)

4.6.2 Outputs

Global Horizontal Irradiance $(W \cdot m^{-2})$



Diffuse Horizontal Irradiance	(W·m ⁻²) (W·m ⁻²) (W·m ⁻²)
Direct Normal Irradiance	(W·m ⁻²)
Direct Horizontal Irradiance	(W·m ⁻²)

4.6.3 List of Methods

public void Calculate (...)
double GetClearnessIndex (...)
double GetDiffuseFraction (...)

4.6.4 Equations and Model Description

The algorithm used by the Splitter class depends on the solar radiation components (e.g. global, diffuse or direct) provided as input.

4.6.4.1 When only global irradiance is provided

When only global irradiance is provided, the first step of the algorithm is to calculate the beam and diffuse components of irradiance. This is done through the use of Orgill and Hollands' formula (see [3], p. 81). The diffuse fraction k_d is defined as the ratio of horizontal diffuse irradiance to horizontal global irradiance:

$$\begin{array}{cccc} k_d = & 1.0 - 0.249 \cdot k_t & \text{if } k_t < 0.35 \\ k_d = & 1.557 - 1.84 \cdot k_t & \text{if } 0.35 < k_t < 0.75 \\ k_d = & 0.177 & \text{if } k_t > 0.75 \end{array} \tag{40}$$

where k_t is the clearness index defined as:

$$k_t = \frac{H_g}{H_{0,n} \cdot \cos(z)} \tag{41}$$

with H_g the global irradiance on the horizontal, $H_{0,n}$ the normal extraterrestrial irradiance measured perpendicularly to the rays of the sun, and z the zenith angle. Then diffuse and beam irradiance on the horizontal, H_d and H_b , are calculated as:

$$H_d = H_g \cdot k_d \tag{42}$$

$$H_b = H_g - H_d \tag{43}$$

Finally, normal beam irradiance $H_{b,n}$ is calculated as:

$$H_{h,n} = H_h/\cos(z) \tag{44}$$

In early morning or late afternoon, the formulae above may lead to very large values of beam irradiance. To circumvent that issue, the program sets H_b to zero and $H_d = H_g$ whenever the zenith angle exceeds 87.5°.



Finally, to prevent possible issues, particularly when the program is used with radiation data measured in the field, beam normal irradiance is limited its clear sky value $H_{b,cs}$. This latter value is calculated using the ASHRAE model ([10], ch. 14) as

$$H_{b,cs} = H_0 \cdot \exp(-\tau_b \cdot m^{ab}) \tag{45}$$

where m is the air mass. The beam pseudo optical depth τ_b and the airmass exponent ab receive the values 0.245 and 0.668. These values were derived for Flagstaff, AZ, for the month of June, and correspond to one of the highest beam/extraterrestrial ratios that can be reasonably expected worldwide.

4.6.4.2 When both global and diffuse irradiances are provided

This is the easiest case. Beam irradiance is simply calculated through eqs. (43) and (44).

4.6.4.3 When both global and beam horizontal irradiances are provided

This is again an easy case. Diffuse irradiance is calculated as:

$$H_d = H_g - H_b \tag{46}$$

Other formulae such as (44) are unchanged.

4.6.4.4 When both global and beam normal irradiances are provided

This case is similar to the previous one, except that beam horizontal irradiance is first calculated as:

$$H_b = H_{b,n} \cdot \cos(z) \tag{47}$$

4.6.4.5 When both global and beam rizontal irradiances are provided

The same equations are used, the first step being now the calculation of global irradiance:

$$H_a = H_b + H_d \tag{48}$$

4.6.4.1 When both global and beam normal irradiances are provided

This is the same case as the previous one, with the addition of equ. (47).

4.7 Sun Sun.cs

The Sun class is an object used to compute solar zenith and azimuth angles, and other quantities related directly to earth-sun geometry. For the conventions used throughout CASSYS for solar angles, please refer to Section 0, "



Appendix: Angle Conventions".

4.7.1 Inputs

Day of the year 1 to 365 (Leap Year: 29 Feb and March 1 is treated as the

same day)

24-Hour Decimal Format (11.75 is 11:45) Hour of the Day

4.7.2 Outputs

Zenith Zenith angle of sun [rad]

Azimuth Azimuth of sun [rad, >0 facing E]

AirMass Air mass [unitless]

Extraterrestrial normal Irradiance [W/m2] **NExtra** AppSunsetHour Apparent sunset hour (given array tilt) Apparent sunrise hour (given array tilt) AppSunriseHour

TrueSunsetHour True sunset hour TrueSunriseHour True sunrise hour

4.7.3 Parameters and Cached Variables

Cached variables are used to speed up some calculations.

Site Lat Latitude of the site (°N is positive, °S is negative)

Site Long Longitude of the site (°E is positive, °W is negative)

Site Meridian Longitude Reference Meridian for Local Standard Time at Site (°E is

Positive), required when doing calculatons is in local time

Slope of the plane of array (radian) Slope of Collector

Cached, Current day of year (to speed up daily calculations) Current Day

Current Declination Cached, Declination for Current Day

Current extraterrestrial irradiance | Cached, Extra-terrestrial radiation for current day

4.7.4 Equations and Model Descriptions

This class is mostly a wrapper for methods found in the Astro.cs class (for calculation of declination, sun position, etc.) and in the Tilt.cs class (for calculation of apparent sunrise and sunset). Please refer to sections 5.1 and 5.2.1.3 for a description of the mathematical models used.

Note that internally all the angular parameters and variables are stored in radians. This makes it straightforward to make use of trigonometric equations without having to convert angles between degrees and radians.

4.8 **Transposition models**

Tilter.cs

The Tilter class is used to calculate plane of array irradiance knowing horizontal irradiance (i.e. solar radiation transposition). It includes two widely used models, the Hay model and the Perez model.

4.8.1 Inputs

Normal Direct Irradiance Beam normal irradiance incident upon the array (W/m^2) Horizontal Diffuse Irradiance

Horizontal diffuse irradiance (W/m²) Normal Extraterrestrial Irr.

Extraterrestrial irradiance measured perpendicularly to the

rays of the sun (W/m^2)

Zenith angle of the sun (radians) Sun Zenith



Sun Azimuth Azimuth angle of the sun (radians)
Air Mass Air mass (-)
Month number Month (1-12)

4.8.2 Outputs

Global Irradiance in Tilted Plane

Beam Irradiance in Tilted Plane

Diffuse Irradiance in Tilted Plane

Plane-of-array global irradiance (W/m²)

Plane-of-array beam irradiance (W/m²)

Plane-of-array diffuse irradiance (W/m²)

Plane-of-array ground-reflected irradiance (W/m²)

Reflected Irradiance in Tilted Plane-of-array graphiane

Angle of Incidence

Angle of incidence of beam irradiance on the array (radians)

4.8.3 Parameters and Cached Variables

Tilt Algorithm

Surface Slope

Surface Azimuth

Monthly Albedo

HAY or PEREZ

Slope of the array (radians)

Azimuth of the array (radians, 0 = S, W > 0)

Average albedo value for each month [0-1]

4.8.4 Equations and Model Descriptions

Both models calculate plane-of-array radiation as the sum of three components: beam, diffuse and ground-reflected. The models differ only in the way they calculate plane-of-array diffuse irradiance. The calculation of beam and ground-reflected irradiances is identical in both models.

4.8.4.1 Beam and ground-reflected irradiances in the plane of array

Beam irradiance in the plane of the array $H_{b,t}$ is calculated from beam normal irradiance $H_{b,n}$ through a simple geometrical relationship:

$$H_{b,t} = H_{b,n} \cdot \cos \theta \tag{49}$$

where θ is the angle of incidence of beam irradiance on the array.

4.8.4.2 Diffuse irradiance in the plane of array – Hay model

The Hay model [3] calculates diffuse irradiance in the plane of array as:

$$H_{d,t} = H_d \cdot \left[(1 - AI) \cdot \frac{1 + \cos \beta}{2} + AI \cdot \frac{\cos \theta}{\cos z} \right]$$
 (50)

where H_d is the diffuse irradiance on the horizontal, β is the slope of the array, θ is the angle of incidence of beam irradiance on the array, and z is the zenith angle. AI is the anisotropy index defined as:

$$AI = \frac{H_{b,n}}{H_{0,n}} \tag{51}$$

where $H_{0,n}$ is the extraterrestrial normal irradiance.



4.8.4.1 Diffuse irradiance in the plane of array – Perez model

The Perez model [11] is slightly more complicated than the Hay model. It calculates diffuse irradiance in the plane of array as:

$$H_{d,t} = H_d \cdot \left[(1 - F_1) \cdot \frac{1 + \cos \beta}{2} + F_1 \cdot \frac{a}{b} + F_2 \cdot \sin \beta \right]$$
 (52)

a and b are two empirical coefficients defined as

$$a = \max(0, \cos \theta) \tag{53}$$

$$b = \max(\cos 85^{\circ}, \cos z) \tag{54}$$

where θ is the incidence angle and z is the zenith angle.

 F_1 and F_2 are also empirical coefficients. Their definition relies on the concepts of clearness ε and brightness Δ , defined as:

$$\epsilon = 1 + \frac{H_{b,n}/H_d}{1 + \kappa \cdot z^3} \tag{55}$$

$$\Delta = m \frac{H_d}{H_{0n}} \tag{56}$$

where $H_{b,n}$ is the beam normal irradiance, H_d is the diffuse horizontal irradiance, κ is a constant equal to 5.535 10^{-6} , z is the zenith angle, m is the air mass, and $H_{0,n}$ is the extraterrestrial normal irradiance. F_1 and F_2 are calculated as:

$$F_1 = \max[0, f_{11} + f_{12} \cdot \Delta + f_{13} \cdot z]$$
 (57)

$$F_2 = f_{21} + f_{22} \cdot \Delta + f_{23} \cdot z \tag{58}$$

where coefficients f_{11} to f_{23} are defined through a look-up table based on the value of ϵ :

Range of ϵ	f_{11}	f_{12}	f_{13}	f_{21}	f_{22}	f_{23}
0.000 to 1.065	-0.008	0.588	-0.062	-0.060	0.072	-0.022
1.065 to 1.230	0.130	0.683	-0.151	-0.019	0.066	-0.029
1.230 to 1.500	0.330	0.487	-0.221	0.055	-0.064	-0.026
1.500 to 1.950	0.568	0.187	-0.295	0.109	-0.152	-0.014
1.950 to 2.800	0.873	-0.392	-0.362	0.226	-0.462	0.001
2.800 to 4.500	1.132	-1.237	-0.412	0.288	-0.823	0.056
4.500 to 6.200	1.060	-1.600	-0.359	0.264	-1.127	0.131
above 6.200	0.678	-0.327	-0.250	0.156	-1.377	0.251

4.8.4.1 Ground-reflected irradiance in the plane of array

Ground-reflected irradiance in the plane of the array $H_{r,t}$, it is approximated by



$$H_{r,t} = H_g \cdot \rho \cdot \frac{1 - \cos \beta}{2} \tag{59}$$

where H_g is the global irradiance on the horizontal, β is the slope of the array, and ρ is the albedo.

4.8.4.2 Global irradiance in the plane of array

Once beam, diffuse and reflected components of irradiance $H_{b,t}$, $H_{d,t}$ and $H_{r,t}$, are calculated through equations (49), (50) or (52) (depending whether the Hay or Perez model is used), and (59), plane-of-array global irradiance H_t is calculated by summing all three components:

$$H_t = H_{b,t} + H_{d,t} + H_{r,t} {(60)}$$

4.9 Transformer Transformer.cs

CASSYS models two types of losses for the grid-connected transformer, the core or iron losses and the ohmic losses.

4.9.1 Inputs

Input Power	Power going from Inverters to the low-side of the
	transformer (W)
Global Loss	Total loss of the transformer at Rated Transformer Power
	(W), calculated (see 4.9.4)
Core or Iron-Loss	Loss under no-load conditions (see 4.9.3)
Nightly Disconnected	Boolean, if the transformer is designed to disconnect at
	night

4.9.2 Outputs

Power Produced	Power delivered to the grid by the transformer (W)
Ohmic Losses	Losses due to internal resistance of the windings (see
Total Losses	4.9.3.2)
	Losses due to the core and ohmic losses

4.9.3 Parameters

4.9.3.1 Core Losses

Some of the input power on the primary side of the transformer is used to compensate for the core losses (composed of hysteresis and eddy currents) occurring within the transformer. The user can specify the power lost to core losses for a grid-connected transformer (or a combination of inverter transformers and grid-connected transformers) directly. Since this loss occurs under no-load conditions, this is modelled as a constant loss by CASSYS as long as the transformer is not disconnected.

4.9.3.2 Ohmic Losses

Input power is also lost to the internal resistance of the primary and secondary windings. This loss is also called the copper loss of the transformer. This is typically dissipated as heat and can be modelled with an effective resistance. Users can specify the percentage loss expected when the array is subject to STC conditions ($L_{\%,OhmicT,STC}$) which is interpreted to an STC Loss of the transformer using (61).



$$L_{OhmicT,STC} = L_{\%,OhmicT,STC} \cdot \eta_{Inv} \cdot PDC_{STC}$$
 (61)

Where,

 η_{Inv} : Efficiency of the Inverters (assumed to be 95%)

 PDC_{STC} : STC rated capacity of the farm

4.9.3.3 Nightly Disconnect

Core losses of the transformer could add up to a substantial amount over a year (~1% of annual production). Hence, some sites are designed to disconnect the transformer at night. CASSYS models this by disconnecting the transformer when the *sun sets for the day under simulation* when the user selects the night disconnection option.

4.9.4 Modelling Transformer Loss

Transformer losses are the sum of the iron and resistive/inductive losses. The core losses are constant and the ohmic losses are quadratic. The following definition of the global loss of the transformer at its nominal rated power can be used:

$$L_{Global,Nom} = L_{IronLoss,Nom} + L_{OhmicLoss,Nom}$$
 (62)

From the above, the ohmic losses at nominal transformer power are unknown. The ohmic losses at nominal conditions are calculated by scaling down the losses in (61) to the transformer rated power using the quadratic relationship:

$$L_{OhmicLoss,Nom} = L_{OhmicLoss,STC} \cdot \left(\frac{P_{Nom,T}}{\eta_{Inv} \cdot PDC_{STC}}\right)^{2}$$
 (63)

This provides the Global losses at nominal power of the transformer. This relationship is then used to determine the power loss from an input power, P_{Input} using

$$L_{OhmicLoss,P_{Input}} = \left(L_{Global,Nom} - L_{IronLoss,Nom}\right) \cdot \left(\frac{P_{Input}}{P_{Nom,T}}\right)^{2}$$
(64)

The loss at any input power is then calculated using the relationship in (62) as the iron losses remain constant.

5 Classes with Mathematical Constructs

The following classes are static classes and contain mathematical constructs that enable the calculation of several different values that are used in the main classes above.

5.1 Daily Astronomical Calculations

Astro.cs

The Astro class contains a set of methods to calculate sun position, air mass, day length, etc. This class is a static class and does not require any parameters from the user.

5.1.1 List of Methods

private static double _GetDayAngle(...)



```
public static double GetDeclination(...)
public static double GetHourAngle (...)
public static void CalcSunPosition (...)
public static void CalcSunPositionHourAngle (...)
public static double GetEccentricityCorrFactor (...)
public static double GetSunEarthDistance (...)
public static double GetATmsST (...)
public static double GetLATime (...)
public static double GetNormExtra (...)
public static double GetAirMass (...)
public static double GetSunsetHourAngle (...)
public static double GetDayLength (...)
```

5.1.2 Physical Model and Methods Description

5.1.2.1 GetDayAngle: calculation of the day angle

The day angle is an auxiliary quantity use in the calculation of declination. It is defined as:

$$DA = \frac{2 \cdot \pi \cdot (n-1)}{365} \tag{65}$$

where n is the day of year (January 1 = 1, February 1 = 32, etc.).

5.1.2.1 GetDeclination: calculation of declination

Declination is the angular position of the sun at solar noon with respect to the plane of the equator ([3], p. 13). North is positive. It is given as [12]:

$$\delta = 0.006918 - 0.399912 \cdot \cos(DA) + 0.070257 \cdot \sin(DA) - 0.006758 \cdot \cos(2 \cdot DA) + 0.000907 \cdot \sin(2 \cdot DA) - 0.002697 \cdot \cos(3 \cdot DA) + 0.00148 \cdot \sin(3 \cdot DA)$$
(66)

where DA is the day angle.

5.1.2.1 GetHourAngle: calculation of hour angle

The hour angle HA is the angular displacement of the sun east or west of the local meridian due to the rotation of the earth, and has a value of 15° per hour. It is expressed in degrees as:

$$HA = 15 \cdot (t - 12) \tag{67}$$

where t is the solar time. The hour angle is negative in the morning and positive in the afternoon. The Astro.cs class also includes the reciprocal function, GetTimeHA, which calculates the time given the hour angle.

5.1.2.1 CalcSunPosition: calculation of the sun's position (zenith and azimuth angle)

CalcSunPosition is a wrapper function. It calculates the sun declination and hour angle and calls CalcSunPositionHourAngle.



5.1.2.1 CalcSunPositionHourAngle: calculation of the sun's position (zenith and azimuth angle)

The function calculates the sun zenith and azimuth given declination and hour angle. The zenith angle z is the angle between the vertical and a line to the sun. Its cosine is given by [3]:

$$\cos(z) = \cos(\phi) \cdot \cos(\delta) \cdot \cos(HA) - \sin(\phi) \cdot \sin(\delta) \tag{68}$$

where ϕ is the latitude, δ is the declination, and HA is the hour angle.

The azimuth angle γ is the angular displacement from south of the projection, on the horizontal plane, of the earth/sun line. It is positive for afternoon hours and negative for morning hours. It is defined by its sine and cosine [13] [14]:

$$\sin(\gamma) = \sin(HA) \cdot \cos(\delta) / \sin(z) \tag{69}$$

$$\cos(\gamma) = (\cos(HA) \cdot \cos(\delta) \cdot \sin(\phi) - \sin(\delta) \cdot \cos(\phi)) / \sin(z) \tag{70}$$

where z is the zenith angle.

5.1.2.1 GetEccentricityCorrFactor: calculation of the sun's eccentricity factor

The eccentricity correction factor describes the eccentricity of the earth's orbit around the sun. It is approximated by [12]:

$$\varepsilon = 1.000110 + 0.034221 \cdot \cos(DA) + 0.00128 \cdot \sin(DA) + 0.000719 \cdot \cos(2 \cdot DA) + 0.000077 \cdot \sin(2 \cdot DA)$$
(71)

where DA is the day angle.

5.1.2.1 GetSunEarthDistance: calculation of the distance between the sun and the earth

The earth-sun distance d is simply the average sun-earth distance (also known as the Astronomical Unit or AU) divided by the eccentricity correction factor:

$$d = AU/\varepsilon \tag{72}$$

5.1.2.1 GetATmsST: Calculation of the solar to standard time difference

GetATmsST is a function that calculates the <u>apparent time minus</u> standard time, that is, the difference between the solar time (the time based on the apparent motion of the sun across the sky, with noon corresponding to the time when the sun reaches its zenith) and the clock time (exclusive of daylight savings time). It is given in minutes by the following equation:

Solar time – Standard time =
$$4 \cdot (\lambda_{st} - \lambda_{loc}) + E$$
 (73)

where λ_{st} is the longitude of the standard meridian (corresponding to the standard time zone), expressed in degrees, λ_{loc} is the local longitude, also expressed in degrees, and E is the equation of time:

$$E = 229.18 * (0.000075 + 0.001868 \cdot \cos(DA) - 0.032077 \cdot \sin(DA)$$
 (74)



$$-0.014615 \cdot \cos(2 \cdot DA) - 0.04089 \cdot \sin(2 \cdot DA)$$

with DA the day angle.

5.1.2.1 GetLATime and GetLSTime: conversions between standard and solar time

These functions simply calculate the Local Apparent Time (a.k.a. solar time) or the Local Standard Time, given the other quantity and the difference between solar and standard time.

5.1.2.2 GetNormExtra: calculation of normal extraterrestrial irradiance

Normal extraterrestrial irradiance $H_{0,n}$ is the irradiance at the top of the atmosphere, measured perpendicularly to the rays of the sun. It is given by

$$H_{0,n} = H_x \cdot \varepsilon \tag{75}$$

where H_x is the solar constant (1367 W/m²) and ε is the eccentricity correction factor, given by equation (71).

5.1.2.3 GetAirMass: calculation of the air mass

Air mass is the ratio of the length of the optical path through the atmosphere to the path length vertically upwards. It is given by Kasten's formula [15]:

$$AM = \frac{1}{\cos(z) + 0.15 \cdot (93.885 - z)^{-1.253}}$$
 (76)

where z is the zenith angle [expressed in degrees].

5.1.2.4 GetSunsetHourAngle: calculation of the sunset or sunrise hour angle

This function calculates the hour angle at sunset (or sunrise, since the day is symmetrical with respect to solar noon). The sunset hour angle ω_s is simply given by its cosine [3]:

$$\cos(\omega_s) = -\tan(\phi) \cdot \tan(\delta) \tag{77}$$

where ϕ is the latitude and δ is the declination

5.1.2.5 GetDayLength: calculation of day length

The length of the day can be directly calculated from the sunset hour angle through:

$$L = 2 \cdot \omega_s / 15 \tag{78}$$

where L is the day length in hours and ω_{s} is the sunset hour angle expressed in degrees.

5.1.2.6 GetDistance: calculation of the distance between two points on the surface of the earth This function first calculates the angular distance ξ between the two points according to [16]:

$$\cos(\xi) = \sin(\phi_1) \cdot \sin(\phi_2) + \cos(\phi_1) \cdot \cos(\phi_2) \cdot \cos(\lambda_1 - \lambda_2) \tag{79}$$



Then the distance d between the two points is calculated as:

$$d = R \cdot \xi \tag{80}$$

where R is the mean earth radius (6,371 km).

5.2 Interpolate Interpolate.cs

This class contains 2 methods that enable Linear and Quadratic Interpolation for arrays of varied lengths. This class is used exclusively to model Inverter Efficiency (see: 4.1.4).

5.2.1 Equations and Methods Description

5.2.1.1 Linear Interpolation

public static double Linear (...)

For a given interpolant x_v , CASSYS uses linear interpolation using two arrays x and y each with n entries to determine y_v . First, the program determines the interval number k, such that $x_k < x_v < x_{k+1}$. The following formulae can then be used.

$$y_v = y_k \frac{(x_{k+1} - x_v)}{(x_{k+1} - x_k)} + y_{k+1} \frac{(x_v - x_k)}{(x_{k+1} - x_0)}$$
(81)

If x_v lies outside of these bounds, an extrapolation formula is used, ensuring the continuity and smoothness of the overall curve. The following formula is used with k = 0 when extrapolating to the left and k = n-1 when extrapolating to the right:

$$y_v = y_i + (x_v - x_{k+1}) \cdot \frac{(y_{k+1} - y_k)}{(x_{k+1} - x_k)}$$
(82)

5.2.1.2 Quadratic Interpolation

public static double Quadratic (...)

CASSYS only allows the use of quadratic interpolation [7] for three input values (see Inverter.cs). This allows for the use of the Lagrange interpolating polynomial of degree 2 to obtain P(x) as below:

$$P(x) = \frac{(x - x_2)(x - x_2)}{(x_1 - x_2)(x_1 - x_3)} y_0 + \frac{(x - x_1)(x - x_3)}{(x_2 - x_1)(x_2 - x_3)} y_1 + \frac{(x - x_1)(x - x_2)}{(x_3 - x_1)(x_3 - x_2)} y_2$$
 (83)

5.2.1.3 Bezier Interpolation

public static double Bezier (...)

CASSYS allows users to specify a variable number of incidence angles and incidence angle modifiers for a given PV system. The interpolation between the points provided is done using the Bezier interpolation method (see PVArray.cs). For succinctness, the reader is advised to follow the description of this method provided in [7] which explains the process of obtaining the curves in good detail.

5.3 Tilt Tilt.cs

The Tilt class contains a set of methods to calculate solar radiation on tilted surfaces, as well as the object to encapsulate them. For the conventions used throughout CASSYS for solar angles, please refer to Section 0, "



Appendix: Angle Conventions".

5.3.1 List of Methods

public static double GetCosIncidenceAngle (...)
public static double GetIncidenceAngle (...)
public static double GetProfileAngle (...)
public static double GetApparentSunsetHourAngleEquator (...)
public static void CalcApparentSunsetHourAngle (...)

5.3.2 Physical Models and Descriptions

5.3.2.1 GetCosIncidenceAngle: calculation of the cosine of the incidence angle

The incidence angle θ is the angle between the beam radiation on the array and the normal to the array. Its cosine is calculated as [3]:

$$\cos(\theta) = \cos(z) \cdot \cos(\beta) + \sin(z) \cdot \sin(\beta) \cdot \cos(\gamma - \gamma_s)$$
(84)

where z is the solar zenith angle, β is the slope of the array, γ is the solar azimuth angle and γ_s is the azimuth of the surface.

5.3.2.2 GetIncidenceAngle: calculation of the incidence angle

This function simply calls GetCosIncidenceAngle and takes the arc cosine of the result.

5.3.2.3 GetProfileAngle: calculation of the profile angle

The profile angle α_p is the projection of the solar altitude angle (i.e. the complement of the zenith angle) on a vertical plane perpendicular to the array. Its tangent is calculated as [3]:

$$\tan(\alpha_{p)} = \frac{\tan(\pi/2 - z)}{\cos(\gamma - \gamma_s)} \tag{85}$$

Where z is the zenith angle, γ is the solar azimuth angle and γ_s is the azimuth of the surface

5.3.2.1 GetApparentSunsetHourAngleEquator: calculation of the apparent sunset or sunrise hour angle for a tilted surface facing the equator

The apparent sunset hour angle ω_{ss} is the hour angle at which direct rays from the sun strike the front of the array. It is calculated as ([3], p. 109):

$$\omega_{ss} = \min \begin{cases} a\cos(-\tan\phi \cdot \tan\delta) \\ a\cos(-\tan(\phi - s \cdot \beta) \cdot \tan\delta) \end{cases}$$
 (86)

Where ϕ is the latitude, δ the declination, β the slope of the surface, and s is equal to +1 in the Northern hemisphere and -1 in the Southern hemisphere.



5.3.2.2 CalcApparentSunsetHourAngle: calculation of the apparent sunset and sunrise hour angles for a tilted surface of any orientation

This function computes the apparent sunrise and sunset hour angles on a tilted surface of any orientation, i.e. the hour angle at which direct rays from the sun first strike the surface during the morning and last strike it in the evening. This is a generalization of the formula above, although it is much more complicated. The algorithm is as follows ([3], eqn [3], eqn [3]). First, calculate quantities [3], and [3] defined as:

$$A = \cos \beta + \tan \phi \cdot \cos \gamma \cdot \sin \beta \tag{87}$$

$$B = \cos \omega_s \cdot \cos \beta + \tan \delta \cdot \cos \gamma \cdot \sin \beta \tag{88}$$

$$C = \frac{\sin \beta \cdot \sin \gamma}{\cos \phi} \tag{89}$$

where β is the slope of the array, ϕ is the latitude, γ is the solar azimuth angle, δ is the declination, and ω_s is the true sunset angle (see equ. (78)). Then sunrise and sunset hour angles ω_{sr} and ω_{ss} are calculated as:

$$\omega_{sr} = s \cdot min \left[\omega_s, a\cos \frac{AB + C\sqrt{A^2 - B^2 + C^2}}{A^2 + C^2} \right]$$
 (90)

with

$$s=-1$$
 if $(A>0$ and $B>0)$ or $(A \ge B)$
 $s=+1$ otherwise (91)

and

$$\omega_{SS} = s \cdot min \left[\omega_S, a\cos \frac{AB - C\sqrt{A^2 - B^2 + C^2}}{A^2 + C^2} \right]$$
 (92)

with

$$s = +1 \text{ if } (A > 0 \text{ and } B > 0) \text{ or } (A \ge B)$$

$$s = -1 \text{ otherwise}$$
(93)

These expressions can only be calculated when the discriminant appearing in the square root is positive. If this is not the case, then it's either a case where the surface is always or never illuminated during the day. The calculation of the angle of incidence at noon enables to distinguish between these two possibilities: if the incidence angle is greater than $\pi/2$ then the surface is never illuminated, otherwise it is always illuminated from true sunrise to true sunset.



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7 Appendix: Angle Conventions

This appendix summarizes angle conventions used throughout the CASSYS program. All angles (including latitudes and longitudes) are expressed in radians:

7.1 General angles

- Latitude: angular location north or south of the equator, north positive; $[-\pi/2, \pi/2]$.
- Longitude: angular location east of Greenwich meridian; $[-\pi, \pi]$.
- Declination: angular position of the sun at solar noon, with respect to the plane of the equator, north positive; [-0.4093, 0.4093] (i.e. [-23.45, 23.45] in degrees).

7.2 Solar angles

- Hour Angle: the angular displacement of the sun east or west of the local meridian (15 degrees per hour); morning negative, afternoon positive; $[-\pi, \pi]$.
- Zenith Angle: angle between the vertical and the line to the sun, i.e. the angle of incidence of beam radiation on a horizontal surface; $[0, \pi]$. Values greater than π /2 indicate that the sun is below the horizon.
- Solar Azimuth Angle: the angular displacement from south of the projection of beam radiation on the horizontal plane; displacements east of south are negative and west of south are positive; $[-\pi, \pi]$.

7.3 Orientation of a receiving surface

- Slope: angle between the normal to the surface and the zenith; [0, [(slope > π /2 means surface is facing the ground).
- Collector Azimuth Angle: the deviation of the projection on a horizontal plane of the normal to the surface from the local meridian, with zero due south, east negative, and west positive; $[-\pi, \pi]$.
- Angle Of Incidence: the angle between the beam radiation on a surface and the normal to that surface; $[0, \pi]$ (greater than 2/2 means the rays of the sun strike the back of the surface).