

Fuzzy

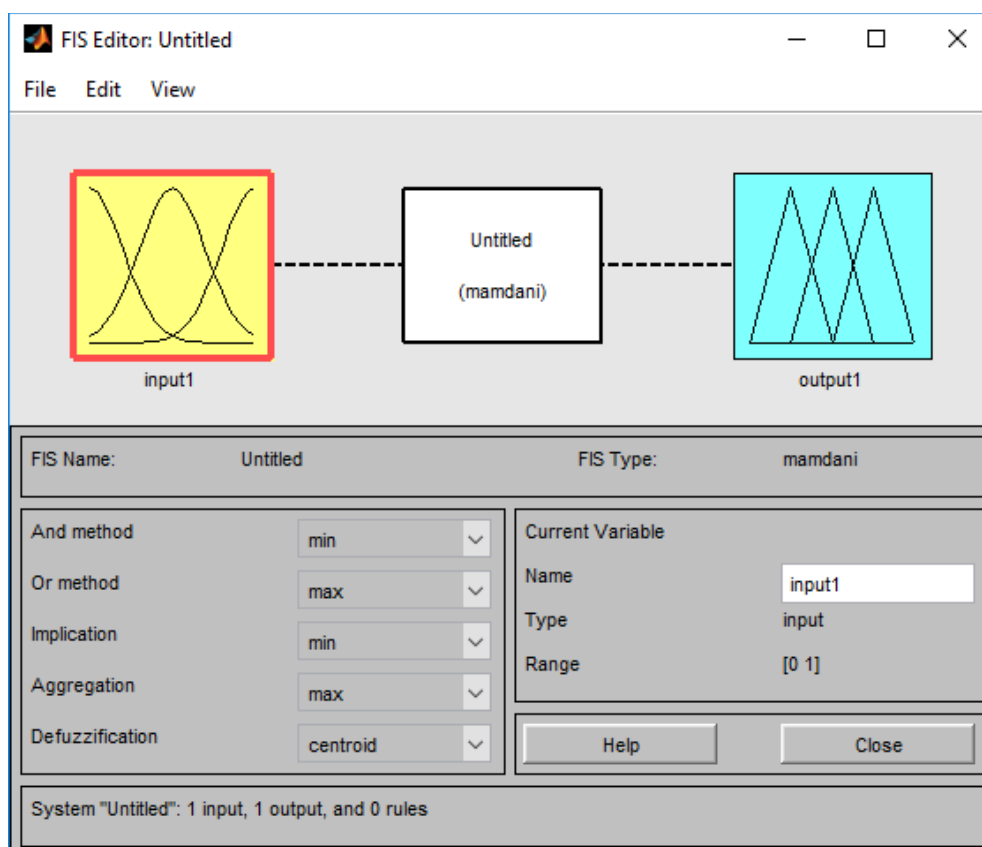
1. Upravlja se kočenjem automobila u odnosu na brzinu kretanja i udaljenost objekta ispred. Objekt ispred automobila može biti neki drugi automobil, neka prepreka na putu i sl. Ulazni skupovi imaju varijable: velika, srednja i mala, dok izlazni skup kočenja ima varijable: lagano, umjereno, snažno i jako snažno. Raspon udaljenosti je od 10 do 150 m. Raspon brzine je od 10 do 100 $\frac{km}{h}$. Kočenje na raspodijeljeno na rasponu od 0 do 10.

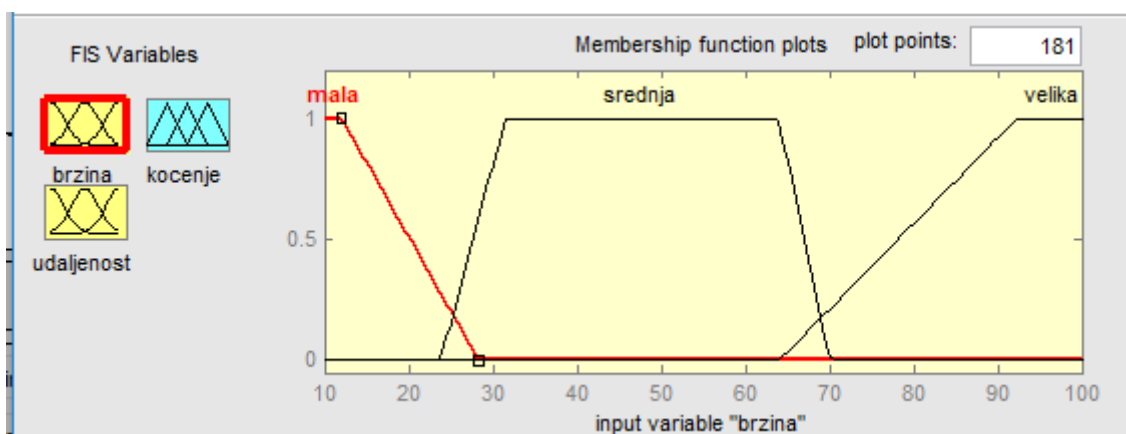
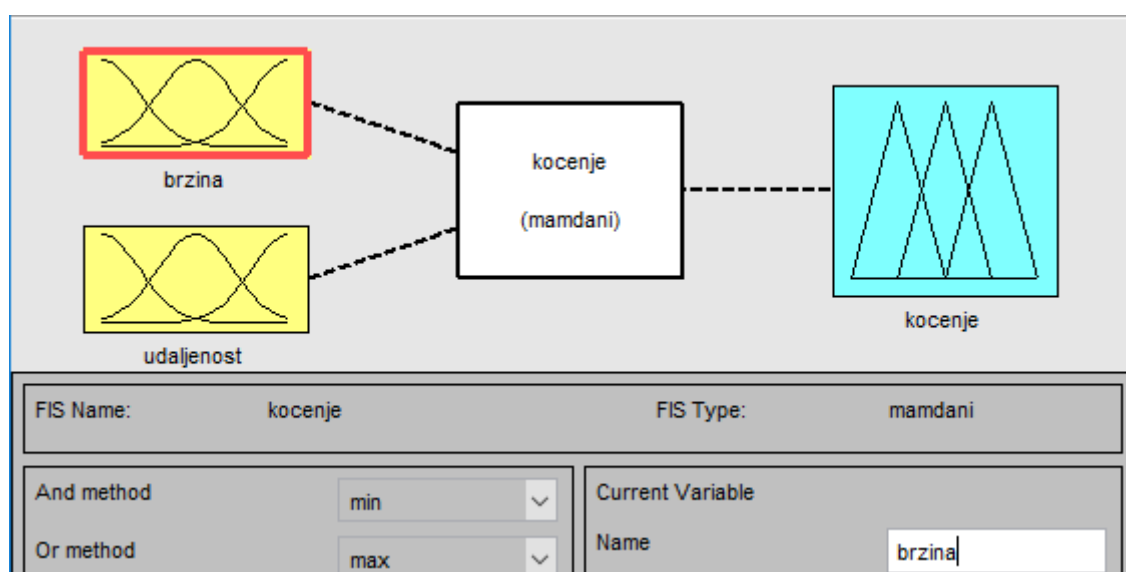
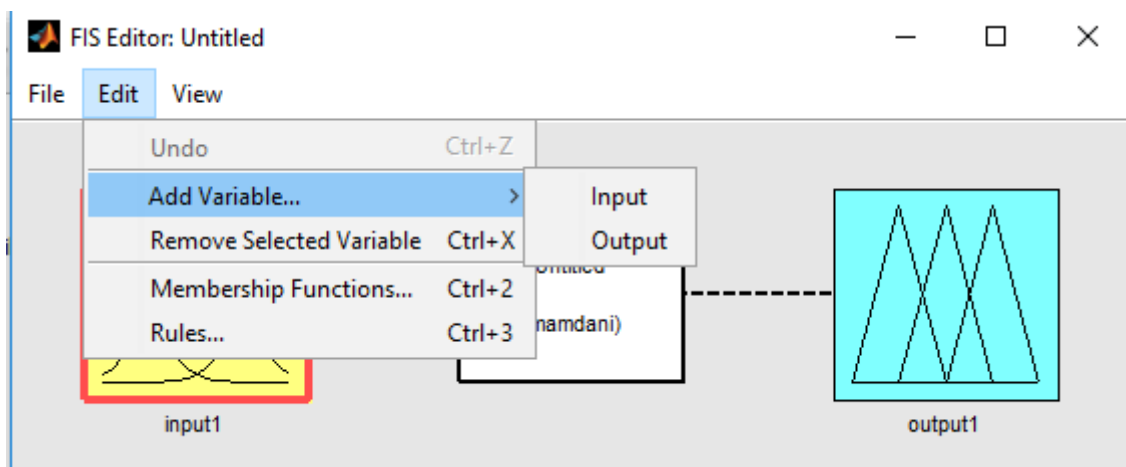
Tabela pravila:

| KOČENJE | | BRZINA | | |
|------------|---|--------|---|---|
| | | V | S | M |
| UDALJENOST | V | U | U | L |
| | S | S | U | U |
| | M | JS | S | U |

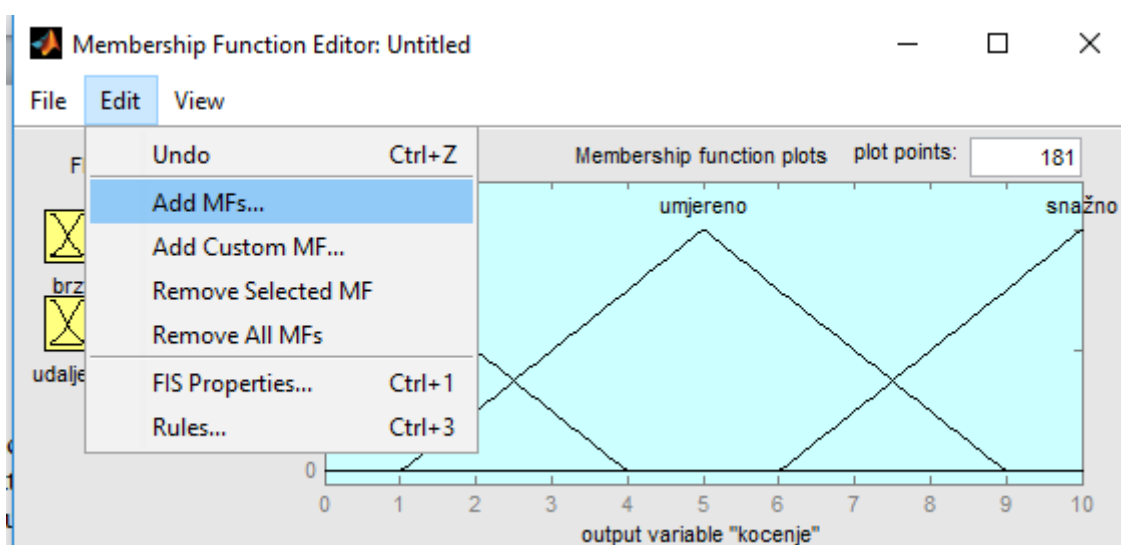
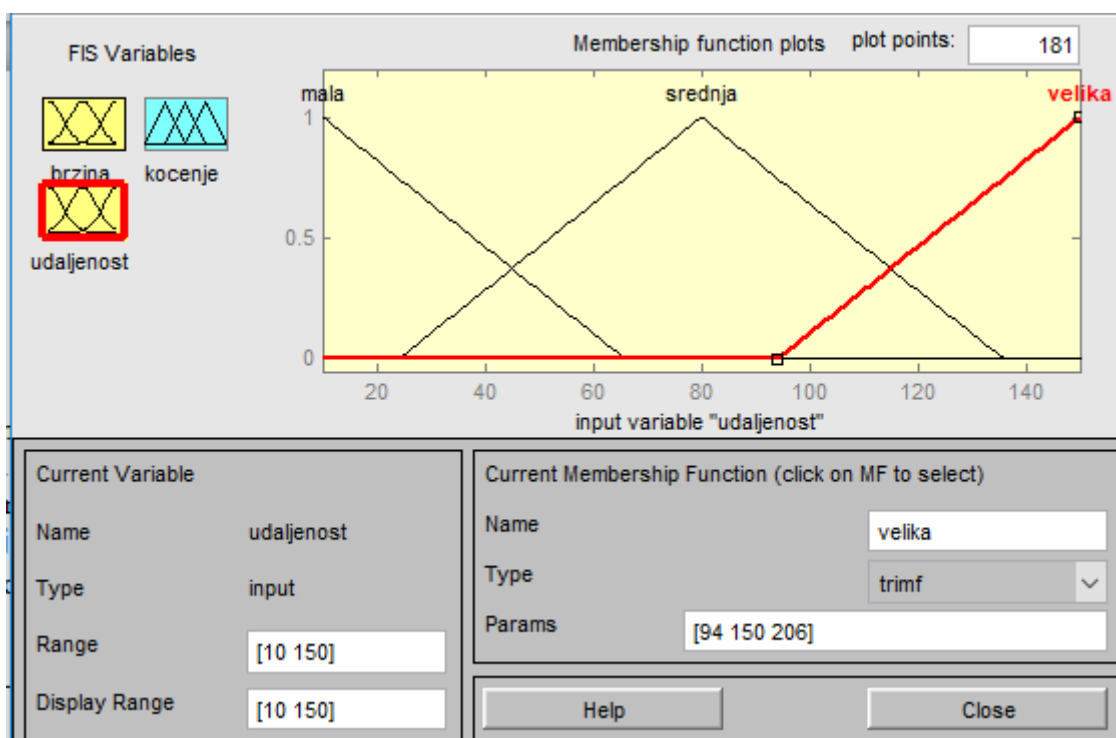
Kuca se u komadni prozor:

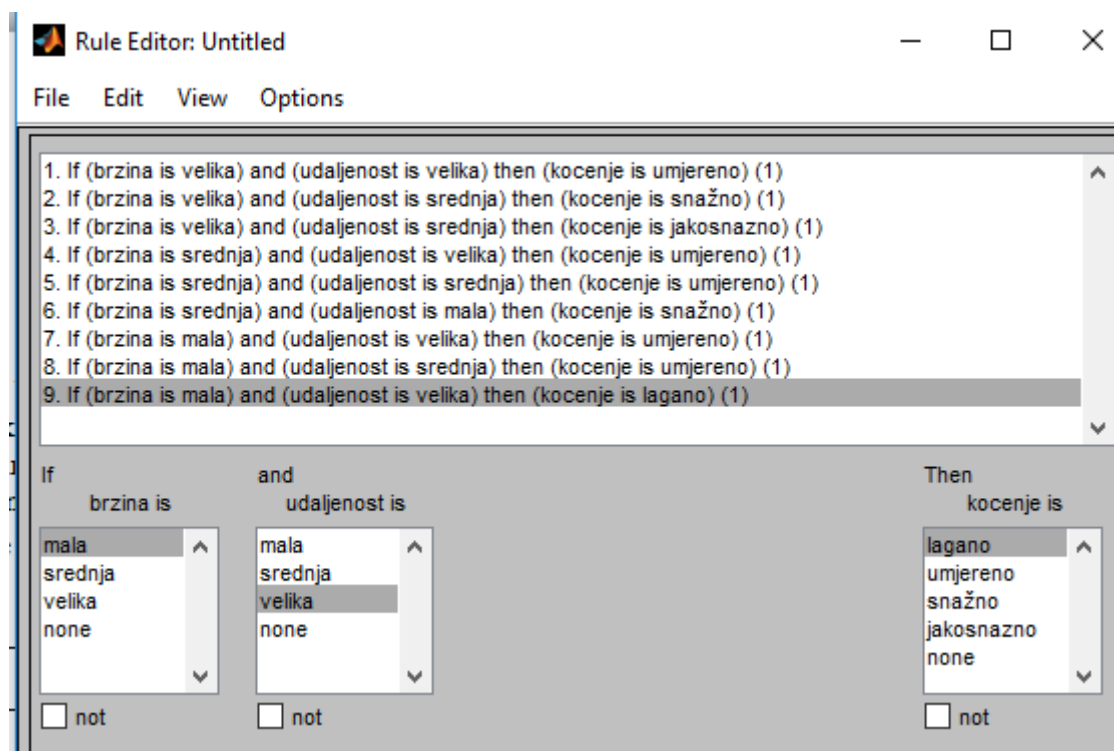
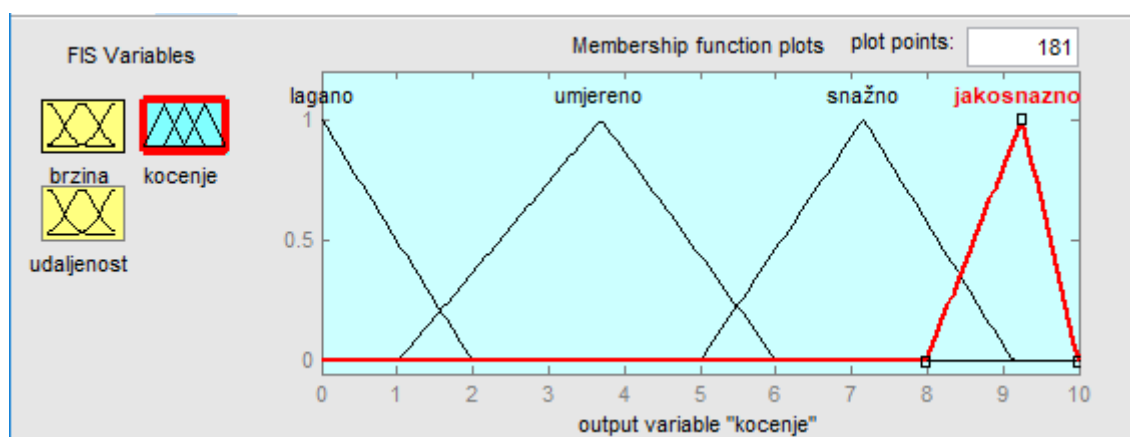
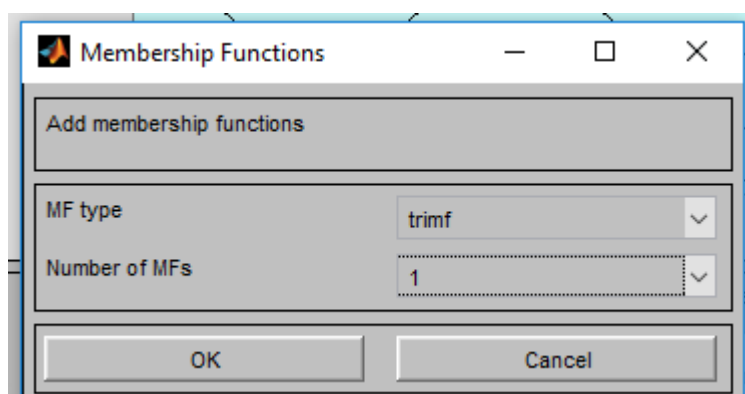
fuzzy

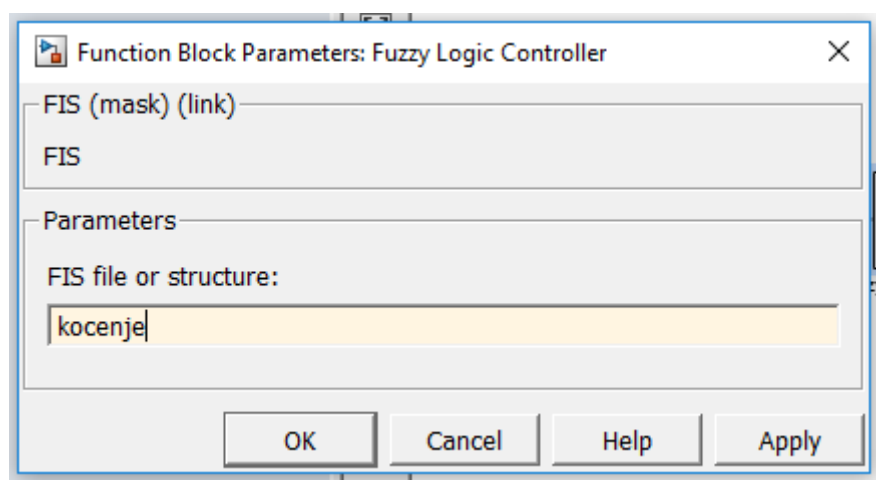
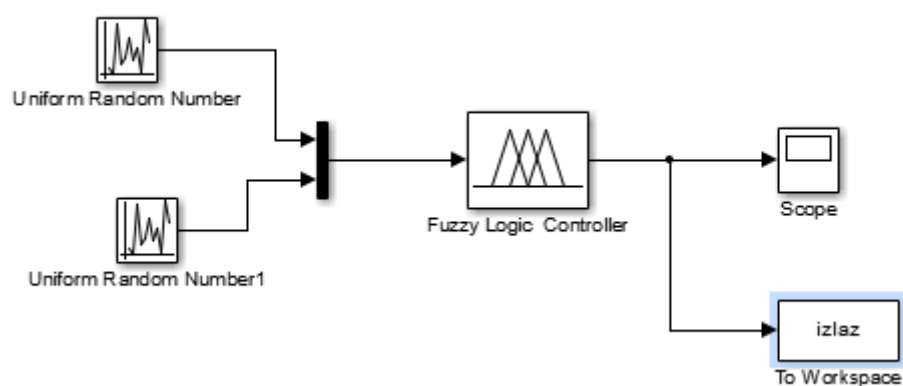
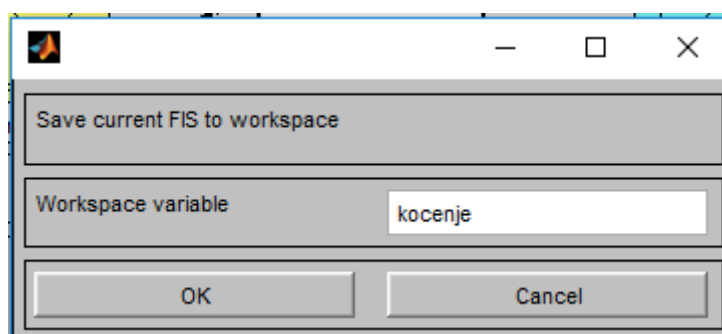
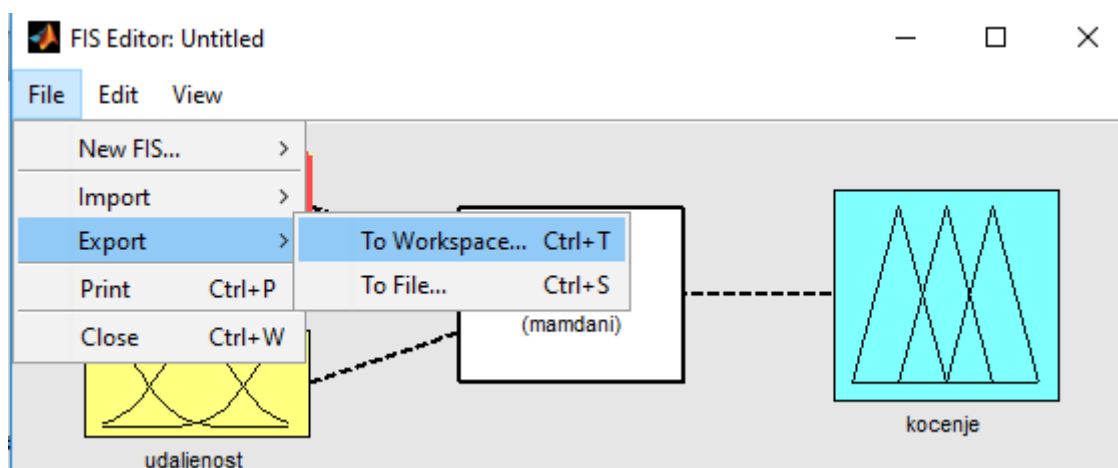


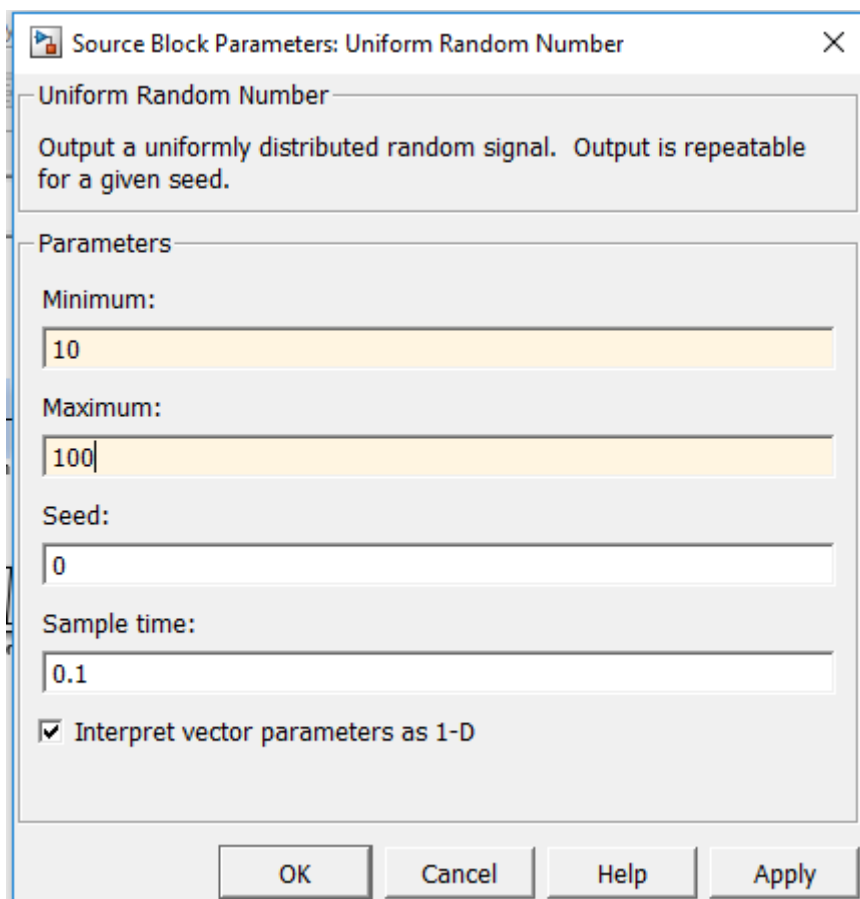


| Current Variable | |
|------------------|----------|
| Name | brzina |
| Type | input |
| Range | [10 100] |
| Display Range | [10 100] |









Source Block Parameters: Uniform Random Number

Uniform Random Number

Output a uniformly distributed random signal. Output is repeatable for a given seed.

Parameters

Minimum:
10

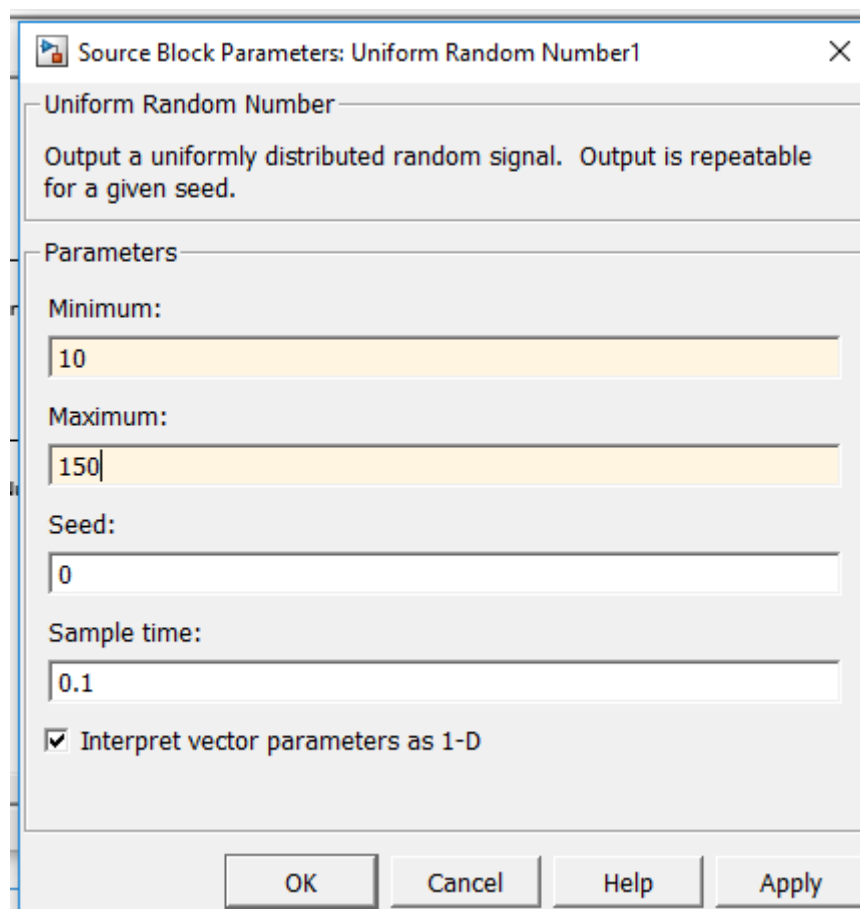
Maximum:
100

Seed:
0

Sample time:
0.1

☒ Interpret vector parameters as 1-D

OK Cancel Help Apply



Source Block Parameters: Uniform Random Number1

Uniform Random Number

Output a uniformly distributed random signal. Output is repeatable for a given seed.

Parameters

Minimum:
10

Maximum:
150

Seed:
0

Sample time:
0.1

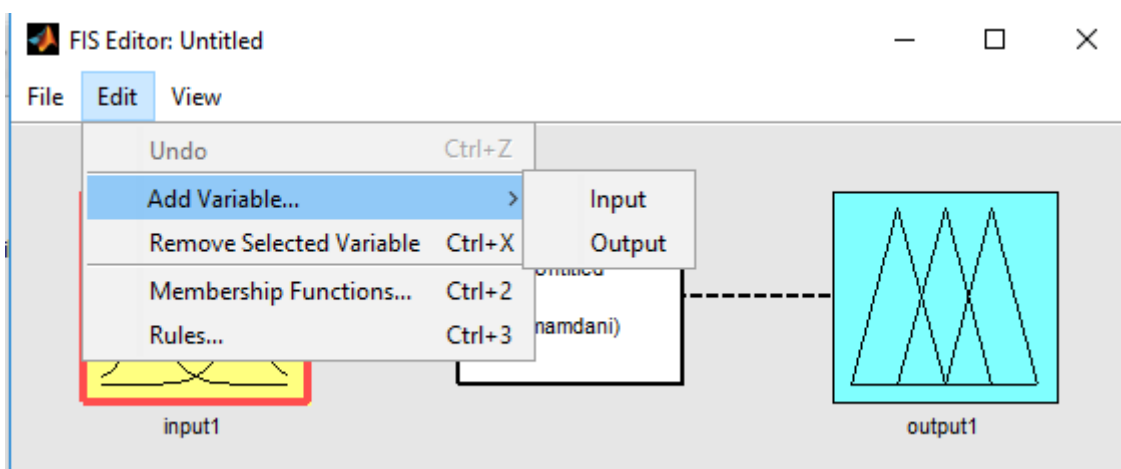
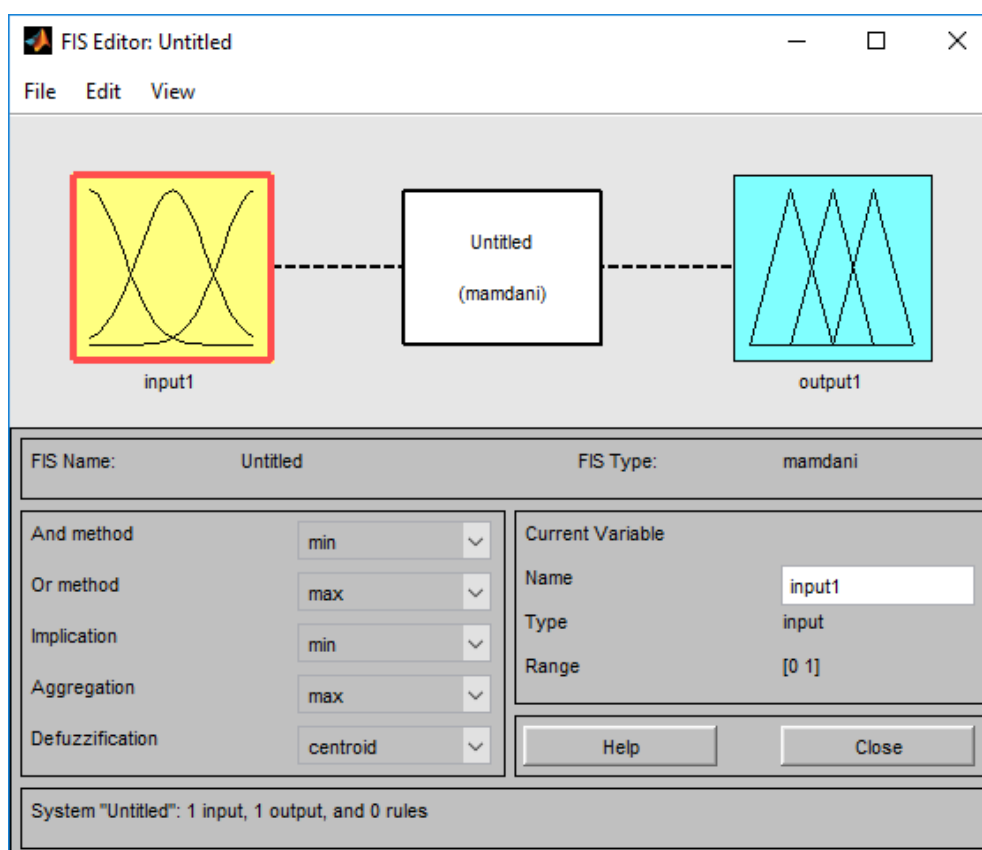
☒ Interpret vector parameters as 1-D

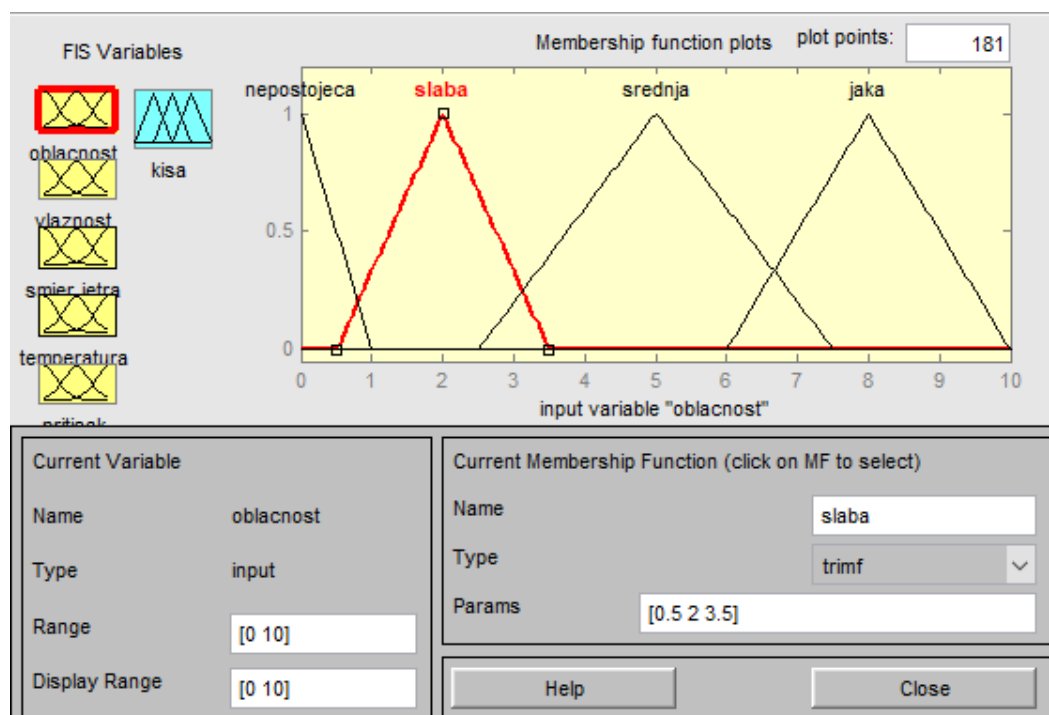
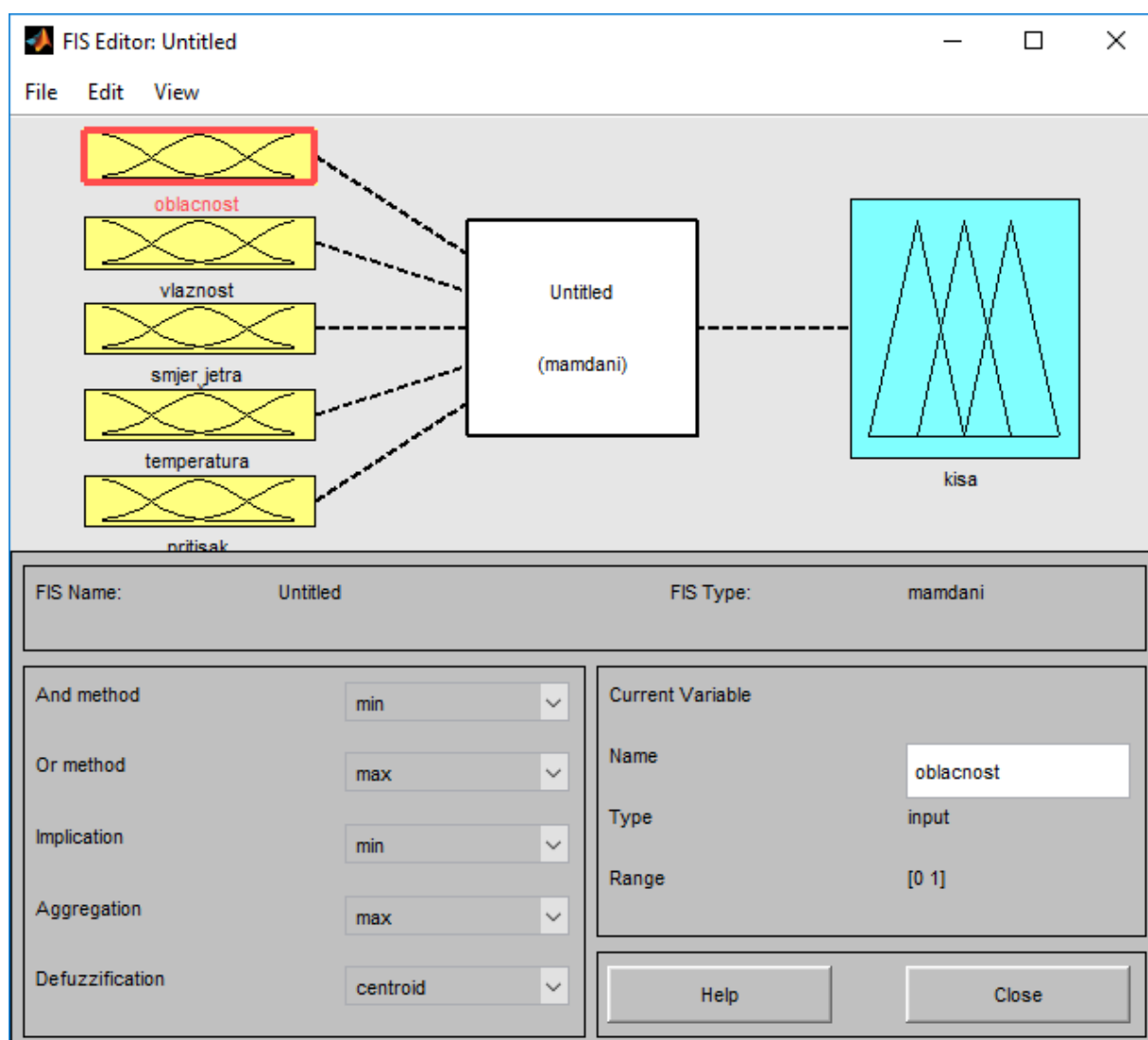
OK Cancel Help Apply

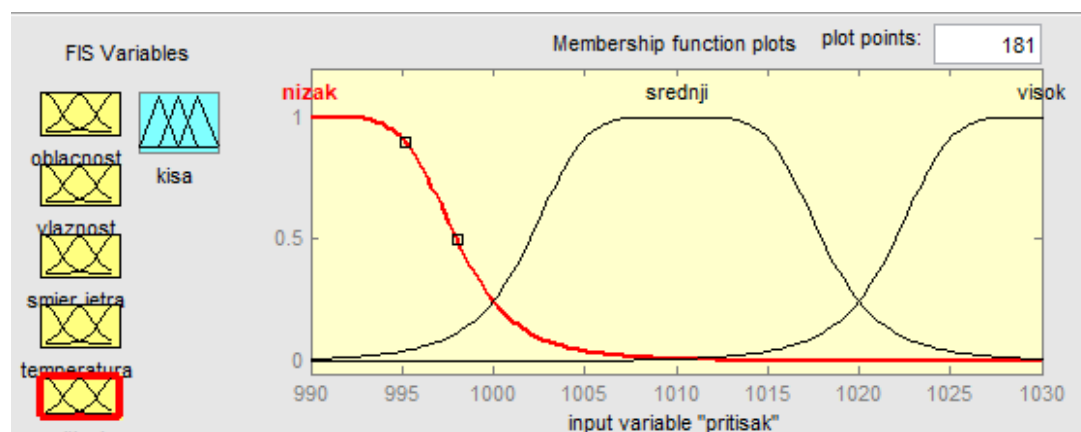
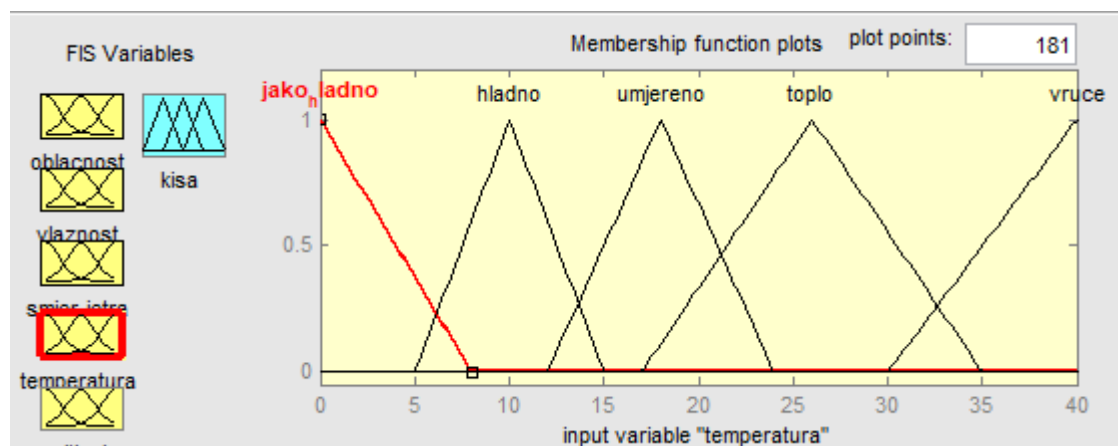
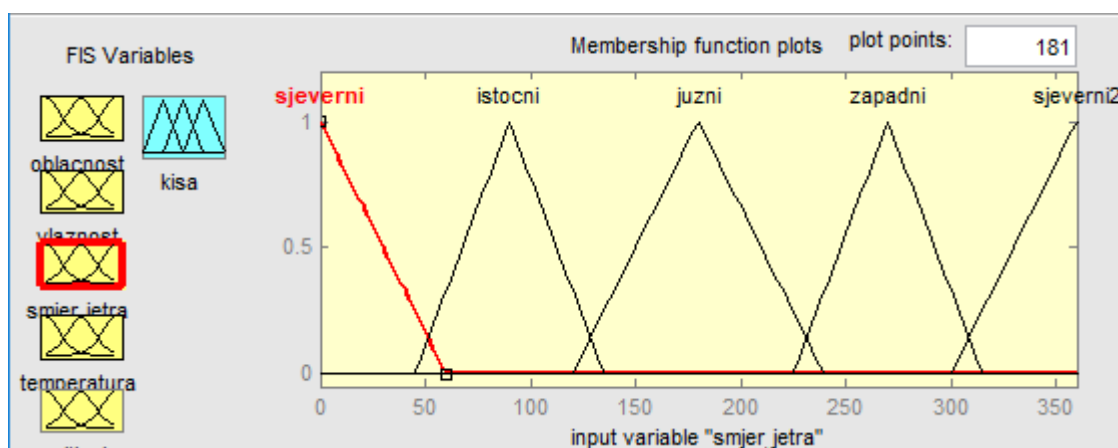
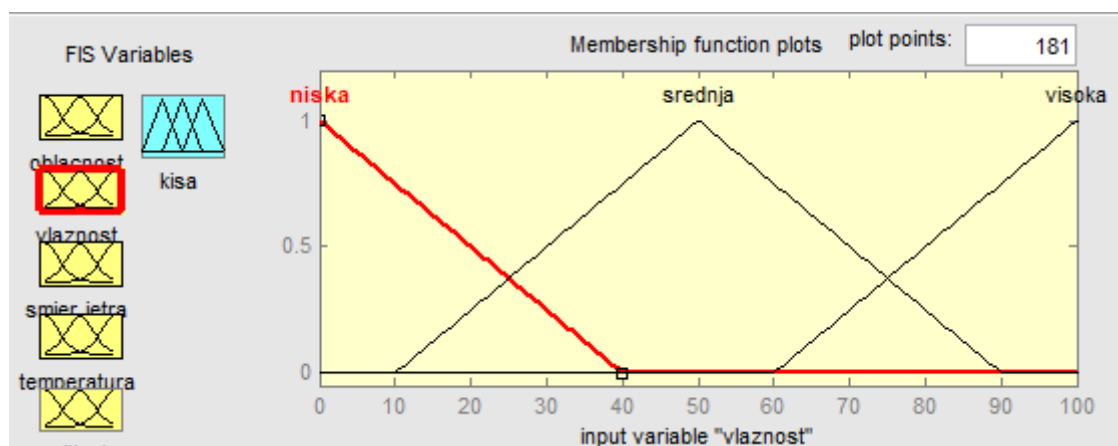
2. Na osnovu 5 ulaznih varijabli potrebno je odrediti da li će kiša padati. Za procjenu se koristi: relativna vlažnost, oblačnost, smjer vjetra, te temperatura i pritisak. Oblaci su u rasponu od 0 do 10, vlažnost od 0 do 100, smjer vjetra od 0 do 360, temperatura od 0 do 40, pritisak od 990 do 1030. Izlazna varijabla je u rasponu od 0 do 100. Napisati bazu pravila i rezultate provjeriti u Simulinku.

Komadni prozor:

fuzzy







Rule Editor: zzz

File Edit View Options

1. If (oblacnost is nepostojeca) then (kisa is ne_pada) (1)
 2. If (oblacnost is slaba) and (vlaznost is niska) then (kisa is ne_pada) (1)
 3. If (temperatura is jako_hladno) then (kisa is ne_pada) (1)
 4. If (oblacnost is slaba) and (vlaznost is srednja) and (smjer_vjetro is juzni) and (pritisak is srednji) then (kisa is slaba) (1)
 5. If (oblacnost is slaba) and (vlaznost is srednja) and (smjer_vjetro is juzni) and (pritisak is visok) then (kisa is slaba) (1)
 6. If (oblacnost is jaka) and (vlaznost is srednja) and (temperatura is hladno) and (pritisak is srednji) then (kisa is umjerena) (1)
 7. If (oblacnost is jaka) and (vlaznost is srednja) and (temperatura is umjereno) and (pritisak is srednji) then (kisa is umjerena) (1)
 8. If (oblacnost is jaka) and (vlaznost is srednja) and (temperatura is toplo) and (pritisak is srednji) then (kisa is umjerena) (1)
 9. If (oblacnost is jaka) and (vlaznost is srednja) and (smjer_vjetro is juzni) then (kisa is jaka) (1)
 10. If (oblacnost is jaka) and (vlaznost is visoka) then (kisa is jaka) (1)
 11. If (oblacnost is jaka) and (vlaznost is niska) and (smjer_vjetro is juzni) and (pritisak is visok) then (kisa is slaba) (1)
 12. If (oblacnost is srednja) and (vlaznost is visoka) and (smjer_vjetro is juzni) and (pritisak is visok) then (kisa is umjerena) (1)
 13. If (oblacnost is srednja) and (vlaznost is visoka) and (smjer_vjetro is juzni) and (pritisak is srednji) then (kisa is umjerena) (1)
 14. If (oblacnost is srednja) and (vlaznost is niska) and (smjer_vjetro is sjeverni) then (kisa is ne_pada) (1)

If and and and and Then

oblacnost is vlaznost is smjer_vjetro is temperatura is pritisak is kisa is

slaba niska sjeverni jako_hladno nizak ne_pada

srednja srednja juzni hladno srednji slaba

jaka visoka zapadni umjereno visok umjerena

nepostojeca none istocni toplo none jaka

none none sjeverni2 vruce none jaka

not not not not not not

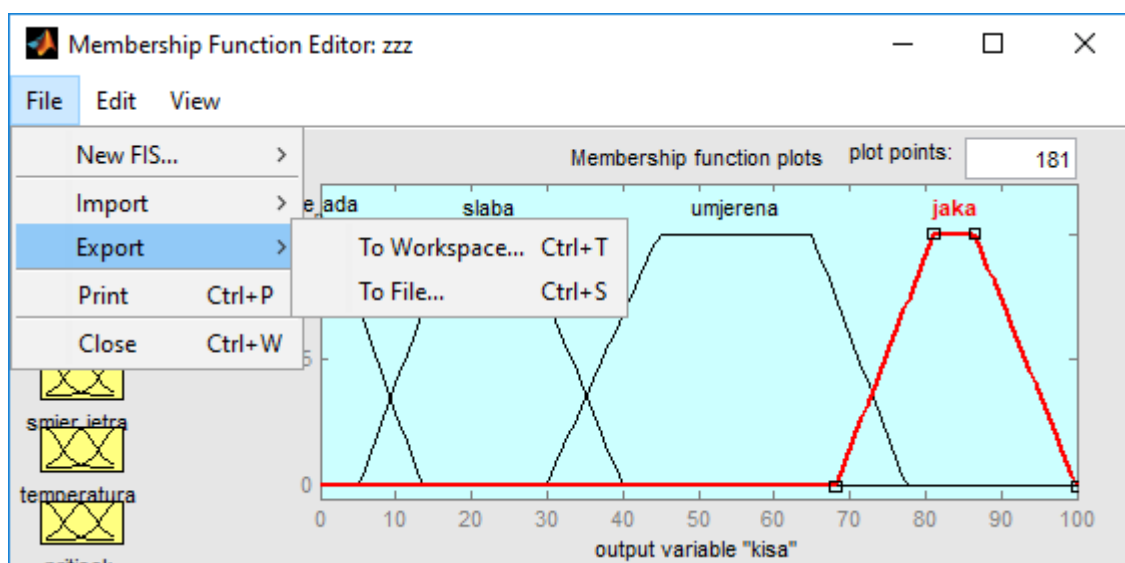
Connection Weight:

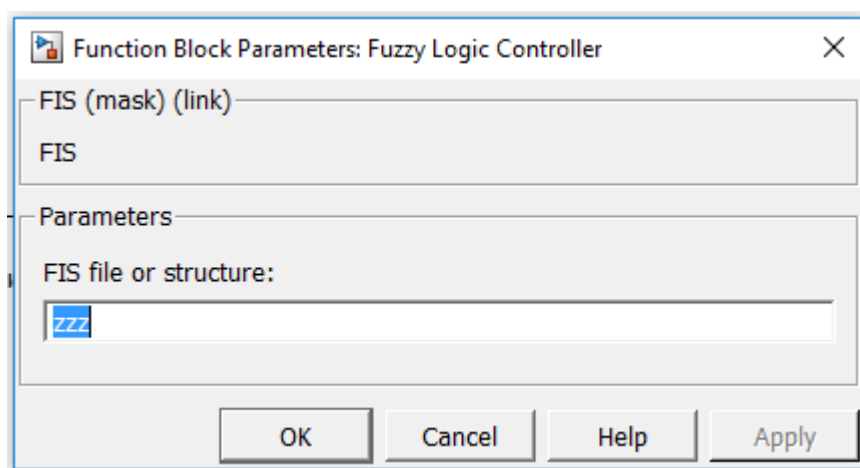
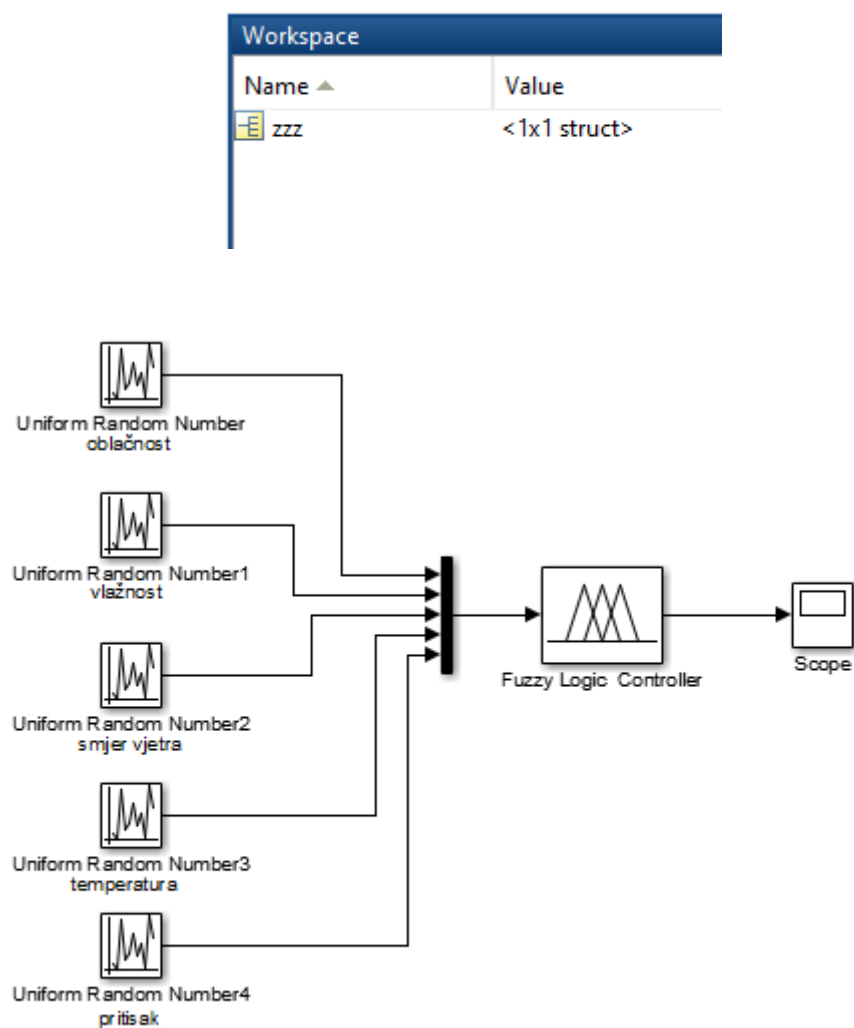
or and 1 Delete rule Add rule Change rule << >>

Renamed FIS to "zzz"

Help Close

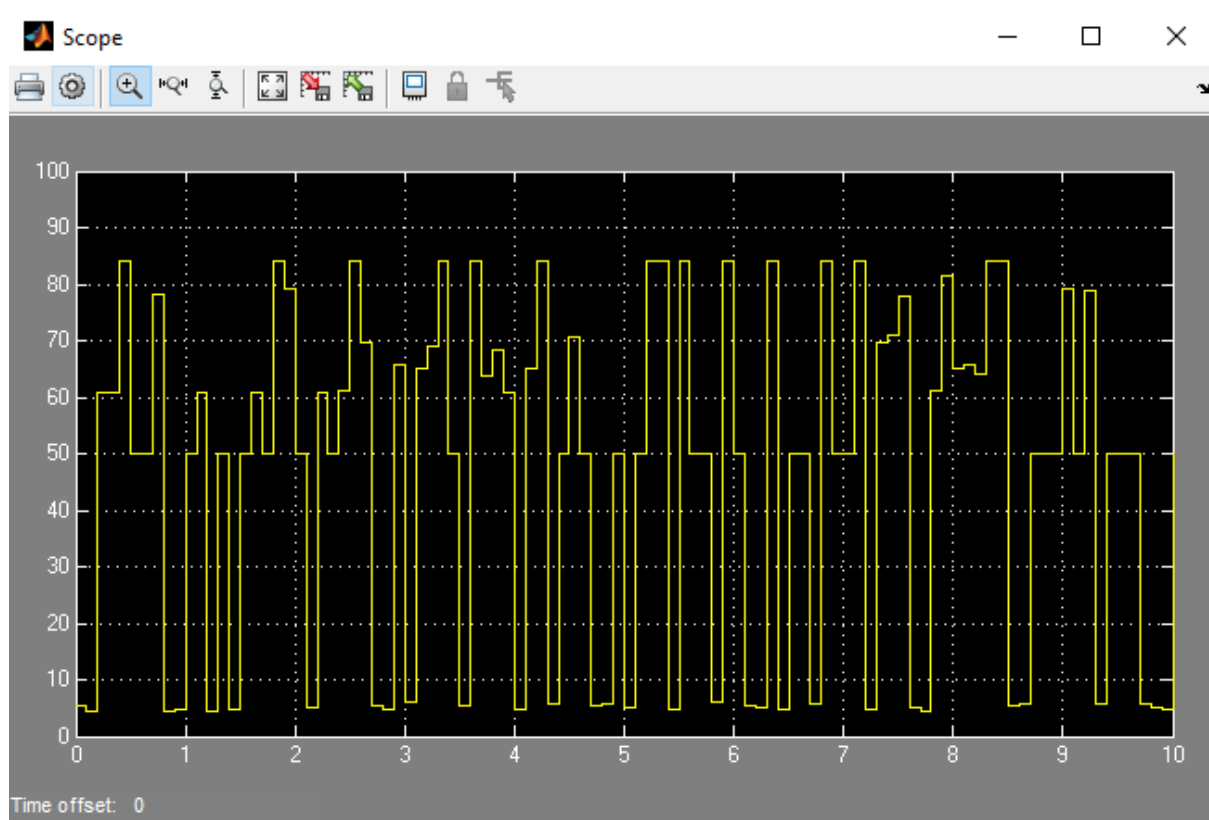
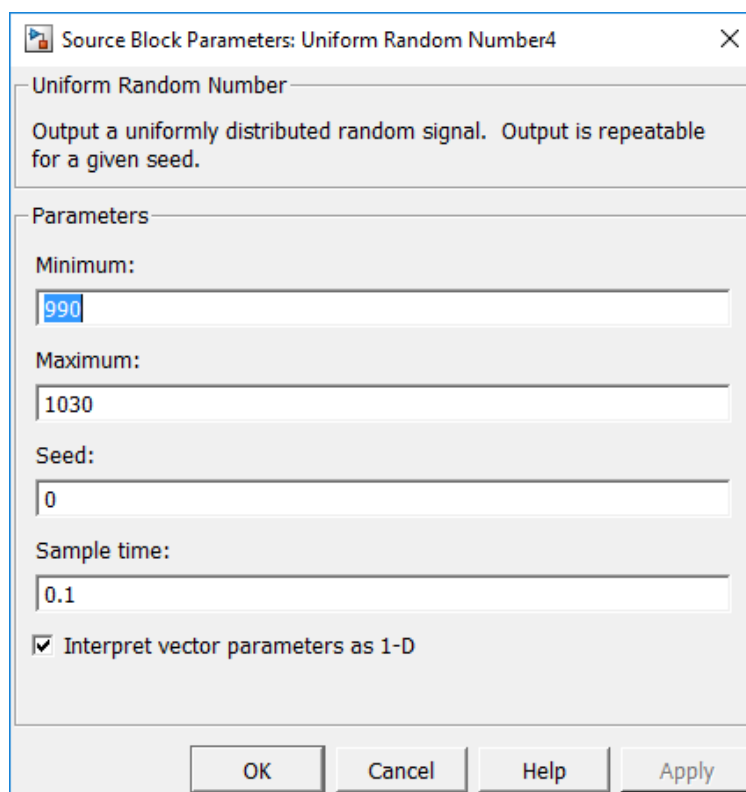
1. If (oblacnost is nepostojeca) then (kisa is ne_pada) (1)
2. If (oblacnost is slaba) and (vlaznost is niska) then (kisa is ne_pada) (1)
3. If (temperatura is jako_hladno) then (kisa is ne_pada) (1)
4. If (oblacnost is slaba) and (vlaznost is srednja) and (smjer_vjetro is juzni) and (pritisak is srednji) then (kisa is slaba) (1)
5. If (oblacnost is slaba) and (vlaznost is srednja) and (smjer_vjetro is juzni) and (pritisak is visok) then (kisa is slaba) (1)
6. If (oblacnost is jaka) and (vlaznost is srednja) and (temperatura is hladno) and (pritisak is srednji) then (kisa is umjerena) (1)
7. If (oblacnost is jaka) and (vlaznost is srednja) and (temperatura is umjereno) and (pritisak is srednji) then (kisa is umjerena) (1)
8. If (oblacnost is jaka) and (vlaznost is srednja) and (temperatura is toplo) and (pritisak is srednji) then (kisa is umjerena) (1)
9. If (oblacnost is jaka) and (vlaznost is srednja) and (smjer_vjetro is juzni) then (kisa is jaka) (1)
10. If (oblacnost is jaka) and (vlaznost is visoka) then (kisa is jaka) (1)
11. If (oblacnost is jaka) and (vlaznost is niska) and (smjer_vjetro is juzni) and (pritisak is visok) then (kisa is slaba) (1)
12. If (oblacnost is srednja) and (vlaznost is visoka) and (smjer_vjetro is juzni) and (pritisak is visok) then (kisa is umjerena) (1)
13. If (oblacnost is srednja) and (vlaznost is visoka) and (smjer_vjetro is juzni) and (pritisak is srednji) then (kisa is umjerena) (1)
14. If (oblacnost is srednja) and (vlaznost is niska) and (smjer_vjetro is sjeverni) then (kisa is ne_pada) (1)





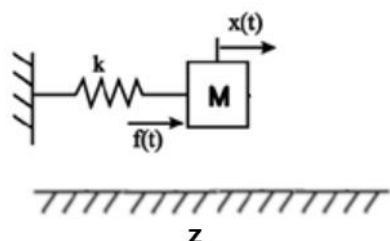
The image shows two side-by-side dialog boxes titled "Source Block Parameters: Uniform Random Number" and "Source Block Parameters: Uniform Random Number1". Both dialogs have a description: "Output a uniformly distributed random signal. Output is repeatable for a given seed." Below the description is a "Parameters" section with four input fields: "Minimum:" (set to 0), "Maximum:" (set to 10 for the first and 100 for the second), "Seed:" (set to 0), and "Sample time:" (set to 0.1). At the bottom of the parameters section is a checked checkbox labeled "Interpret vector parameters as 1-D". Each dialog has four buttons at the bottom: "OK", "Cancel", "Help", and "Apply".

The image shows two side-by-side dialog boxes titled "Source Block Parameters: Uniform Random Number2" and "Source Block Parameters: Uniform Random Number3". Both dialogs have a description: "Output a uniformly distributed random signal. Output is repeatable for a given seed." Below the description is a "Parameters" section with four input fields: "Minimum:" (set to 0), "Maximum:" (set to 360 for the first and 40 for the second), "Seed:" (set to 0), and "Sample time:" (set to 0.1). At the bottom of the parameters section is a checked checkbox labeled "Interpret vector parameters as 1-D". Each dialog has four buttons at the bottom: "OK", "Cancel", "Help", and "Apply".



Fuzzy 2

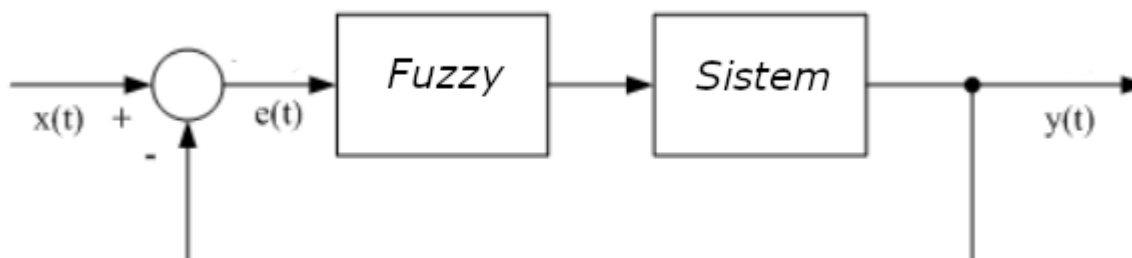
1. Za sistem fuzzy upravljanja mehaničkim sistemom na slici i za dani mehanički sistem na drugoj slici i na osnovu fuzzy modela iz tabele prikazati izlaze sistema ako se na ulaze dovodi proizvoljni ulazni signal koji odgovara danom fuzzy sistemu.



$$m = 10$$

$$k = 1$$

$$z = 0,5$$



$$m \cdot x''(t) + z \cdot x'(t) + kx(t) = f(t)$$

ULAZ1 → GREŠKA

| NAZIV | TIP | PARAMETRI | OPSEG |
|---------|--------|------------|-------|
| mala | trimf | -3.5 0 3.5 | 0-100 |
| srednja | trimf | 5 6.5 10.5 | |
| velika | trapmf | 4 8 10 100 | |

ULAZ2 → PREKORAČENJE

| NAZIV | TIP | PARAMETRI | OPSEG |
|-----------|--------|---------------|-------|
| nisko | trimf | 3 8 10 | 0-100 |
| prosječno | trimf | 5.5 10 20 | |
| visoko | trapmf | 8 17.5 10 100 | |

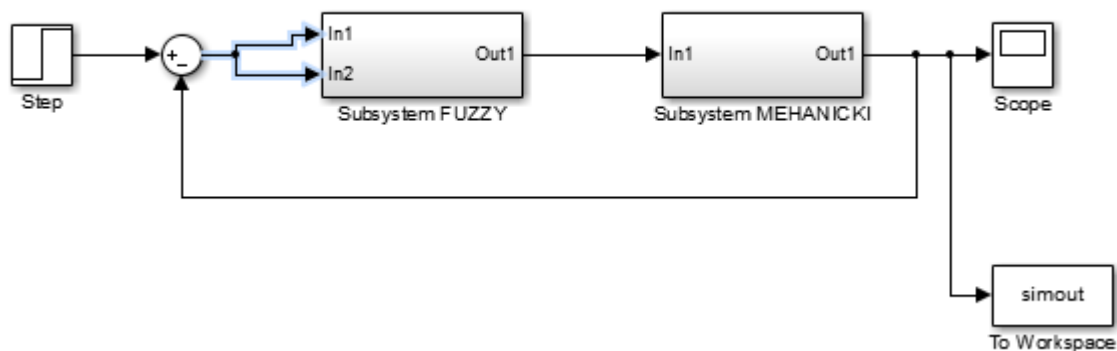
IZLAZ → SILA

| NAZIV | TIP | PARAMETRI | OPSEG |
|-------|-----|-----------|-------|
|-------|-----|-----------|-------|

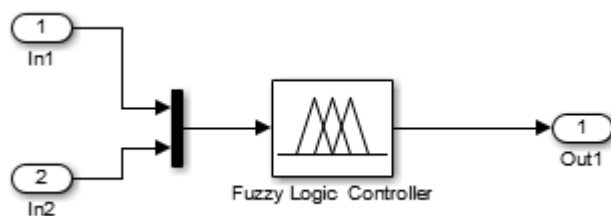
| | | | |
|----------|--------|--------------------|-------|
| slaba | trimf | -60 10 60 | 0-200 |
| normalna | trimf | 60 85 100 | |
| jaka | trapmf | 100 125 200 200 | |

PRAVILA

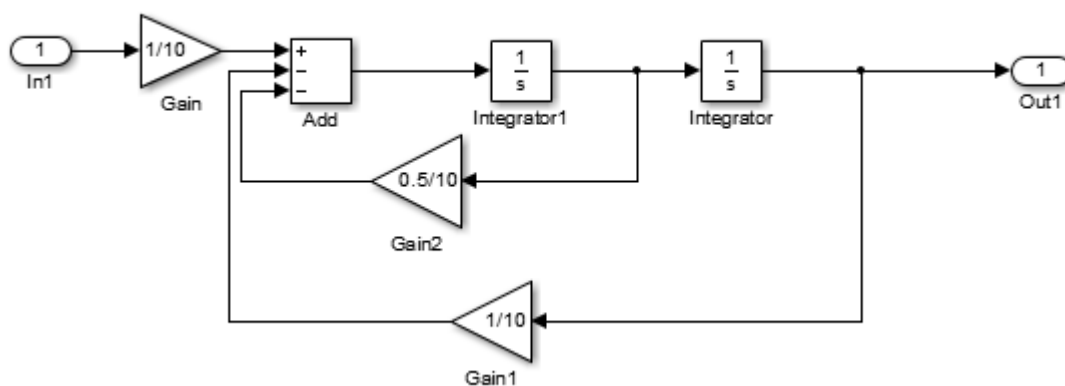
| | | | | | | | |
|----|--------------|---------|-----|--------------|-----------|--------------------|----------|
| 1. | IF GREŠKA | mala | OR | PREKORAČENJE | veliko | THEN SILA IS | slaba |
| 2. | | srednja | AND | | prosječno | | normalna |
| 3. | | velika | OR | | visoko | | jaka |



Fuzzy podsistem (može i bez podsistema sa jednim ulazom):

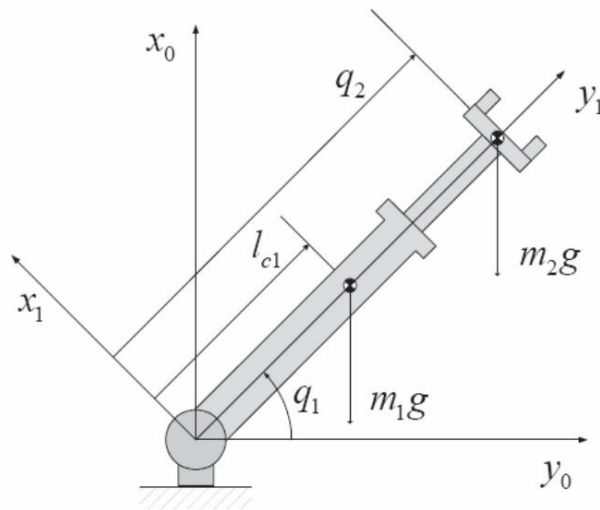


Mehanički podsistem:



2. Izvršiti upravljanje RT robotom koje je prikazano na slici koristeći fuzzy logiku. Potrebno je prikazati poziciju 1, poziciju 2, brzinu 1, brzinu 2, moment 1 i silu 2. (sa infoservisa)

RT robot



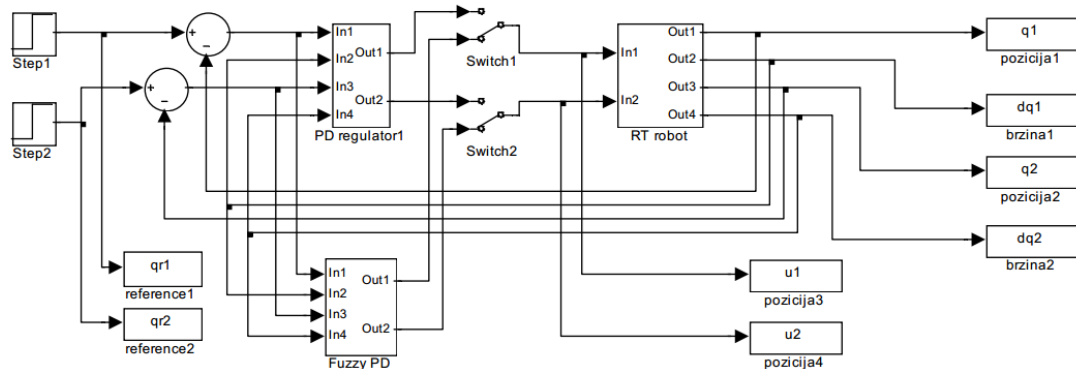
$$M(q)\ddot{q} + C(q, \dot{q})\dot{q} + g(q) = u,$$

$$M(q) = \begin{bmatrix} m_1 l_{c1}^2 + m_2 q_2^2 + I_1 + I_2 & 0 \\ 0 & m_2 \end{bmatrix},$$

$$C(\dot{q}, q) = \begin{bmatrix} m_2 \dot{q}_2 q_2 & m_2 \dot{q}_1 q_2 \\ -m_2 \dot{q}_1 q_2 & 0 \end{bmatrix},$$

$$g(q) = \begin{bmatrix} m_1 l_{c1} g \cos q_1 + m_2 g q_2 \cos q_1 \\ m_2 g \sin q_1 \end{bmatrix},$$

Simulink model



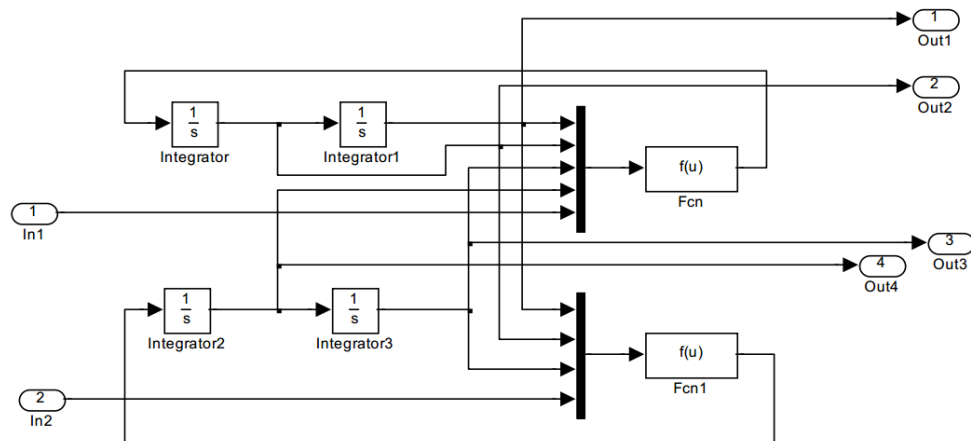
Simulation time
Start time: 0.0 Stop time: 5.0

Solver options
Type: Fixed-step ode4 (Runge-Kutta)

Fixed step size: 0.01 Mode: Auto

Output options
Refine output Refine factor: 1

RT robot blok



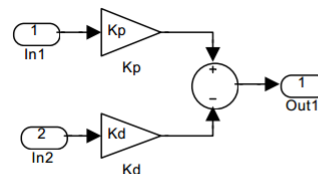
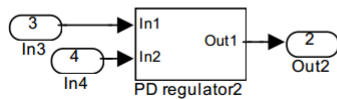
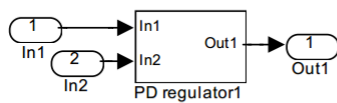
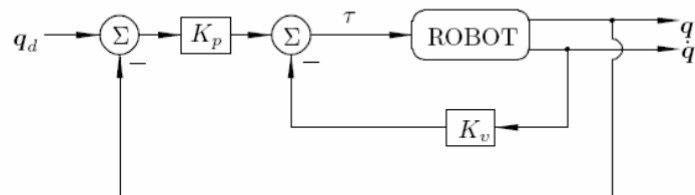
$$(-2*m2*u(3)*u(2)*u(4)-m1*lc1*g*cos(u(1))-m2*g*u(3)*cos(u(1))+u(5))/(m0+m2*u(3)*u(3))$$

$$u(3)*u(2)*u(2)-g*sin(u(1))+u(4)/m2$$

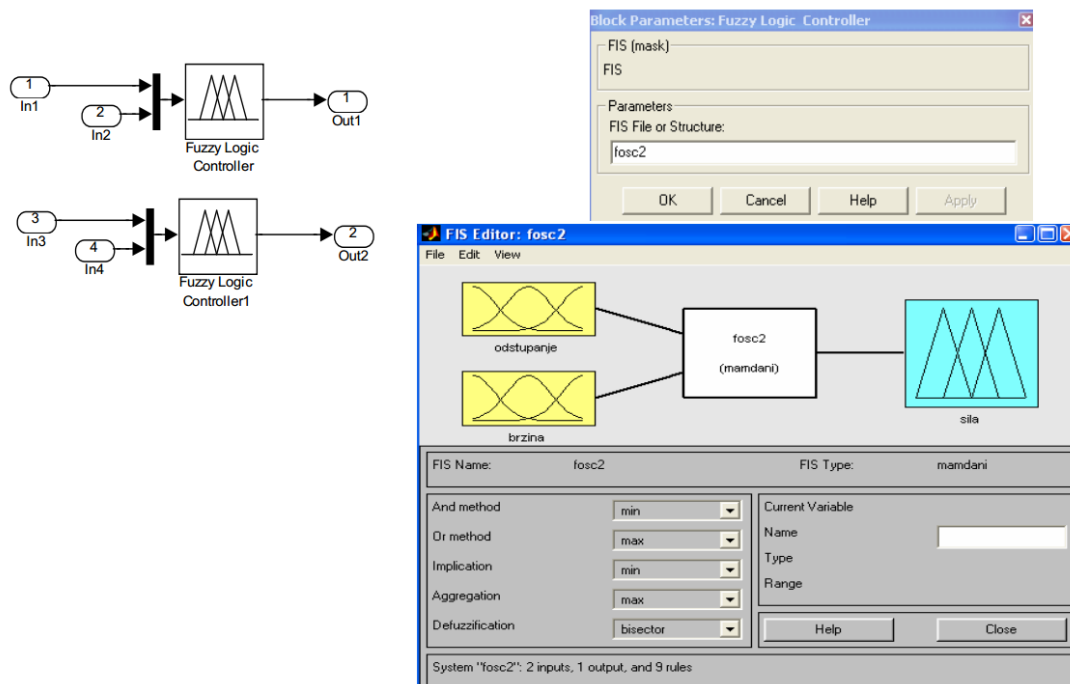
PD regulator blok

$$\tilde{q}(t) := q_d - q(t).$$

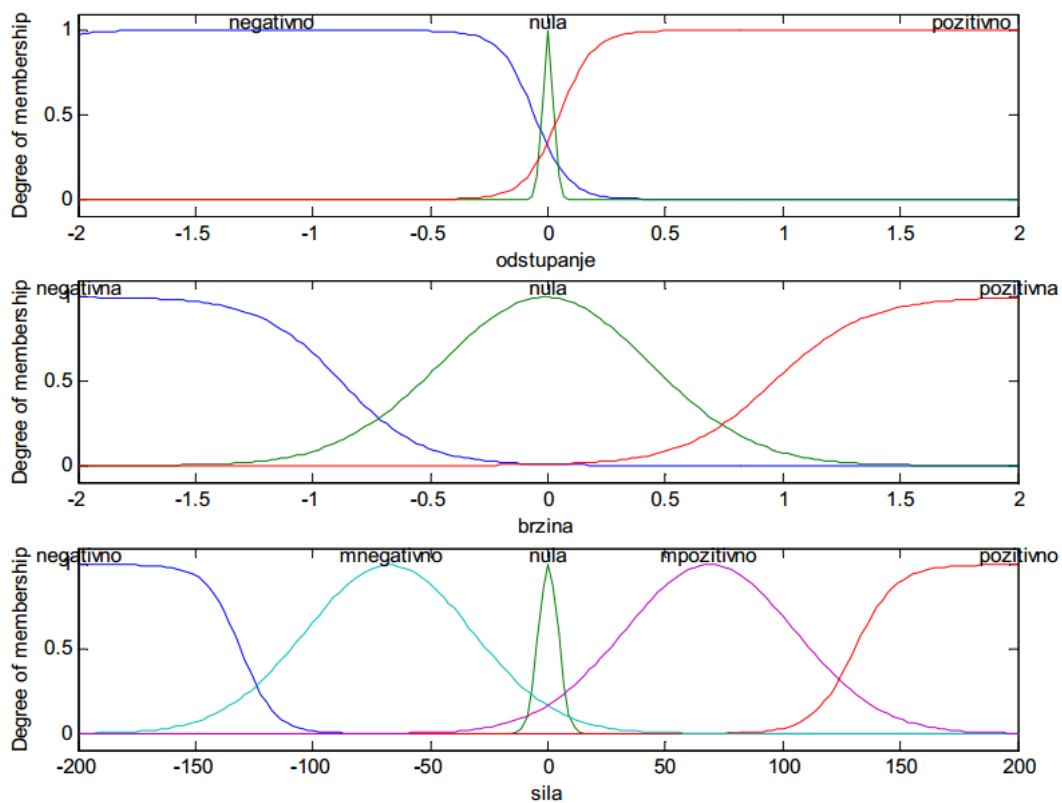
$$\tau = K_p \tilde{q} - K_v \dot{q},$$



Fuzzy PD regulator blok



Funkcije pripadnosti



Baza pravila ponašanja

1. If (odstupanje is nula) and (brzina is nula) then (sila is nula) (1)
2. If (odstupanje is nula) and (brzina is negativna) then (sila is mpozitivno) (1)
3. If (odstupanje is nula) and (brzina is pozitivna) then (sila is mnegativno) (1)
4. If (odstupanje is negativno) and (brzina is nula) then (sila is negativno) (1)
5. If (odstupanje is pozitivno) and (brzina is nula) then (sila is pozitivno) (1)
6. If (odstupanje is pozitivno) and (brzina is negativna) then (sila is pozitivno) (1)
7. If (odstupanje is pozitivno) and (brzina is pozitivna) then (sila is negativno) (1)
8. If (odstupanje is negativno) and (brzina is pozitivna) then (sila is negativno) (1)
9. If (odstupanje is negativno) and (brzina is negativna) then (sila is pozitivno) (1)

| <i>de</i> \ <i>e</i> | N | Z | P |
|----------------------|---|----|---|
| N | P | MP | P |
| Z | N | Z | P |
| P | N | MN | N |

MATLAB KOD:

```

m2 = 10;
m1 = 10;
lc1 = 0.8;
Il2 = 0.1;
m0 = m1*lc1*lc1+Il2;
g = 9.81;
q10 = 0;
dq10 = 0;
q20 = 0;
dq20 = 0;
Kp = 900; Kd = 200;

figure(1)
subplot(221); plot(tout, q1, 'b', tout, qr1, 'r');
xlabel('vrijeme'); ylabel('pozicija 1');
legend('odziv', 'referentni signal');

subplot(222); plot(tout, q2, 'b', tout, qr2, 'r');
xlabel('vrijeme'); ylabel('pozicija 2');
legend('odziv', 'referentni signal');

subplot(223); plot(tout, dq1, 'b');

```

```
xlabel('vrijeme'); ylabel('brzina 1');

subplot(224); plot(tout, dq2, 'b');
xlabel('vrijeme'); ylabel('brzina 2');

figure(2)
subplot(221); plot(tout, u1, 'b');
xlabel('vrijeme'); ylabel('moment 1');

subplot(222); plot(tout, u2, 'b');
xlabel('vrijeme'); ylabel('sila 2');

% (-2*m2*u(3)*u(2)*u(4)-m1*lc1*g*cos(u(1))-
m2*g*u(3)*cos(u(1))+u(5))/(m0+m2*u(3)*u(3))

% u(3)*u(2)*u(2)-g*sin(u(1))+u(4)/m2
```

Fuzzy – zadaća

Na slici 1 je prikazan model dva međusobno povezana rezervoara, gdje su prikazani ventili (μu_1 , μi_1 , μu_2 i μi_2) i površine A_1 i A_2 , kao i nivoi h_1 i h_2 . Potrebno je prikazati nivoe rezervoara 1 i 2 (h_1 i h_2) koristeći:

- Direktan način (Jednačina kola za nivoe h_1 i h_2)
- Korištenjem PID regulatora
- Korištenjem Fuzzy regulatora
- Na jednom modelu i jednom dijagramu prikazati razlike dobijenih rezultata
- Napraviti GUI aplikaciju u Matlabu koja izgleda kao na slici 2

Poznato je:

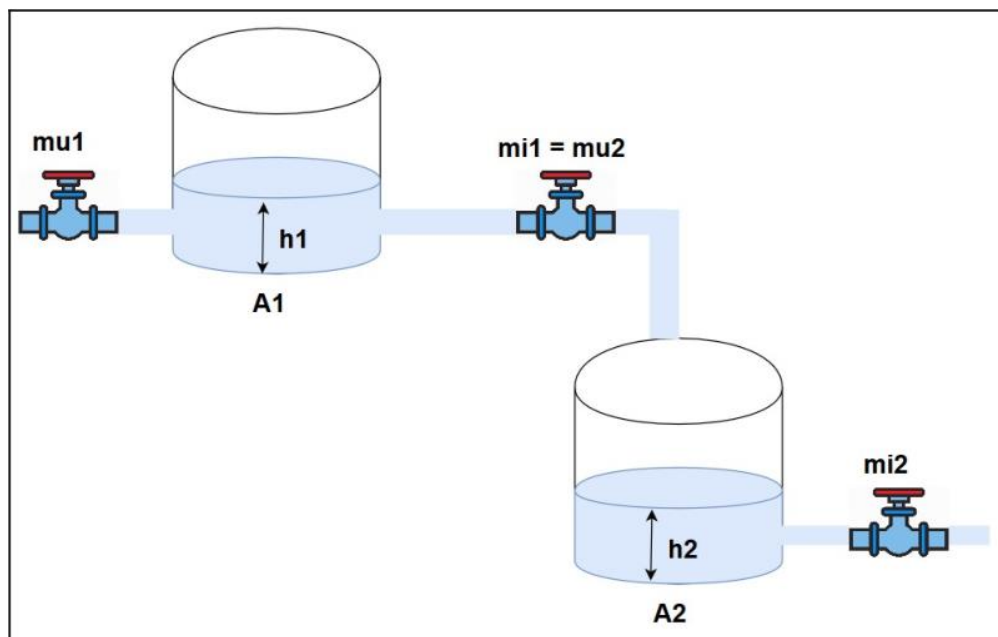
Pumpa: $H=12$ [m]

Površina prvog rezervoara: $A_1 = 2 \text{ m}^2$

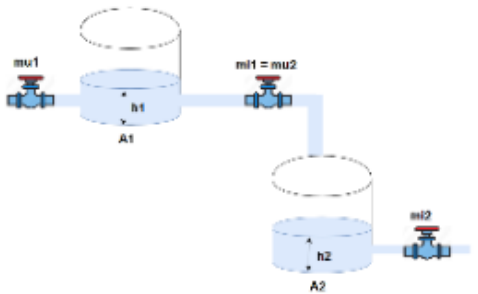
Površina drugog rezervoara: $A_2 = 3 \text{ m}^2$

Ventili: $\mu u_1 = \mu i_1 = \mu u_2 = 40 \text{ [m m}^2\text{s}^{-1}]$

$\mu i_2 = 30 \text{ [m m}^2\text{s}^{-1}]$



Simulacija razine vode u rezervoarima



Model dva povezana rezervoara

REZERVOAR A1

REZERVOAR A2

DIREKTNO

PID

FUZZY

POKRENI SIMULACIJU

Otvorenost ventila

Prvi ventil mu1:

Drugi ventil mi1 = mu2:

Treci ventil mi2:

Površina baze rezervoara

A rezervoar:

B rezervoar:

DIREKTNO
PID
FUZZY

DIREKTNO
PID
FUZZY

ME I PREZIME , BROJ INDEKSA

$$A1 = \frac{dh_1(t)}{dt} = \left[\frac{(\Delta H - h_1(t))}{mv_1} - \frac{h_1(t)}{mv_1} \right]$$

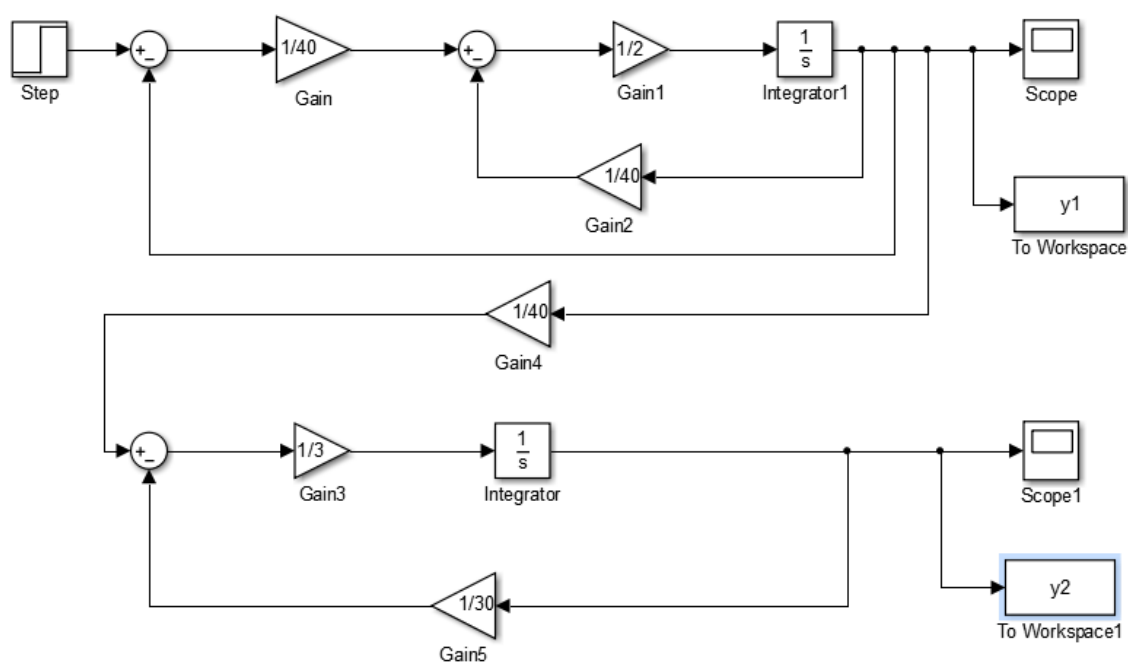
$$A2 = \frac{dh_2(t)}{dt} = \left[\frac{(h_1(t))}{mi_1} - \frac{h_2(t)}{mi_2} \right]$$

$$\frac{dh_1(t)}{dt} = \frac{1}{A_1} \cdot \left[\frac{(\Delta H - h_1(t))}{mv_1} - \frac{h_1(t)}{mi_1} \right]$$

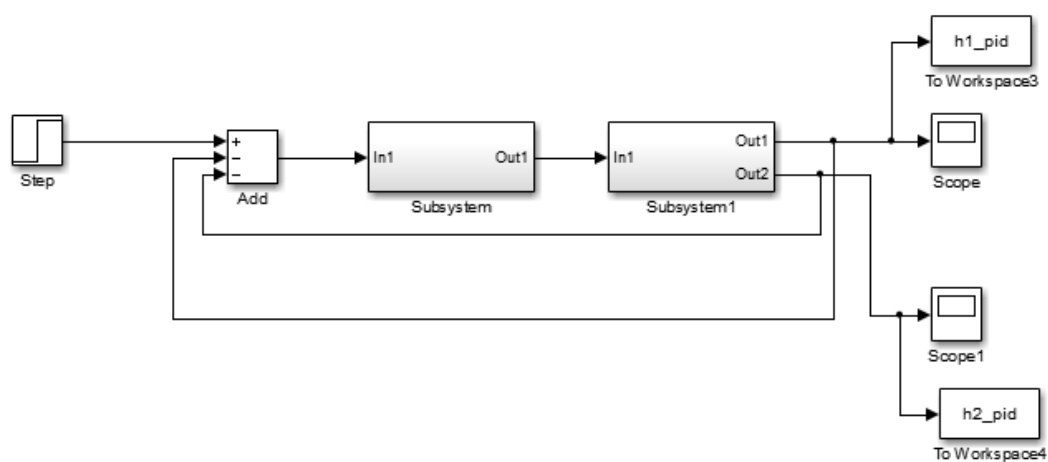
$$\frac{dh_2(t)}{dt} = \frac{1}{A_2} \cdot \left[\frac{(h_1(t))}{mi_1} - \frac{h_2(t)}{mi_2} \right]$$

$$G(s) = \frac{1}{9600s^2 + 316.6s + 2.66}$$

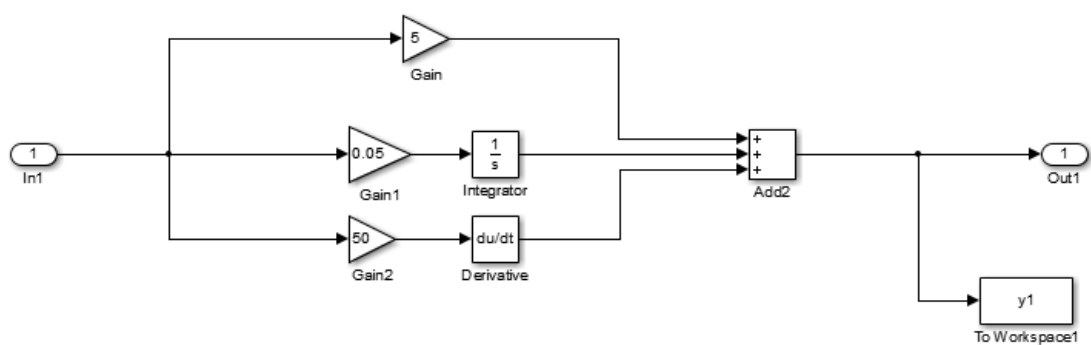
a)



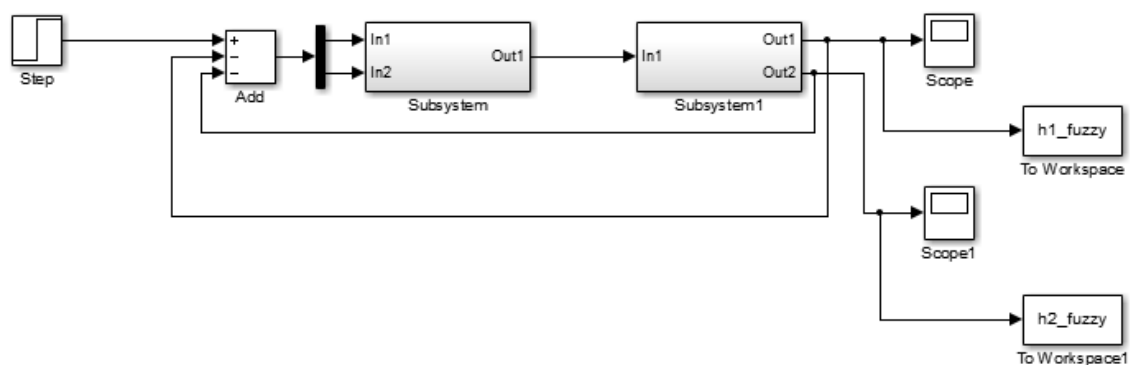
b)



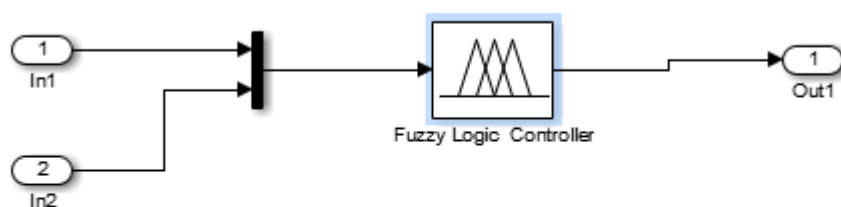
Prvi podsistem:



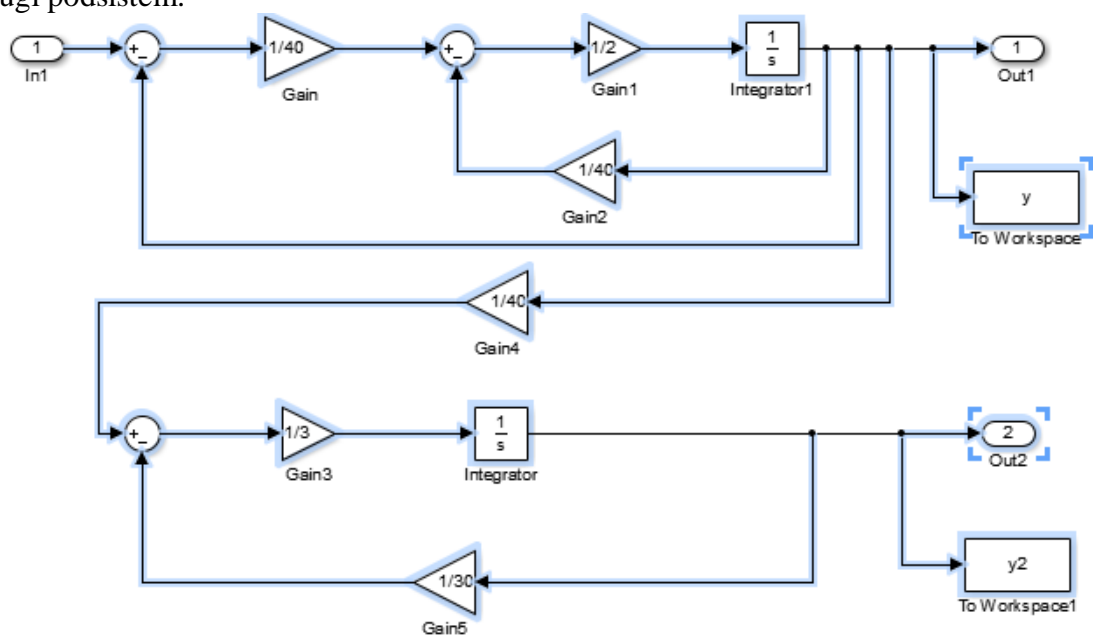
c)



Prvi podsistem:



Drugi podsistem:



Tabele za fuzzy:

NIVO

| | | | |
|------------|-------------|---------------------|------|
| Nizak | Trapezoidal | -2 -1 -0.9 0 | -1 1 |
| Malo_nizak | Trapezoidal | -0.8 -0.6 -0.4 -0.2 | |
| Dobar | Triangular | -0.3 0 0.3 | |
| Malo_visok | Triangular | 0.2 0.4 0.6 0.8 | |
| Visok | Triangular | 0 0.9 1 0 | |

Promjena

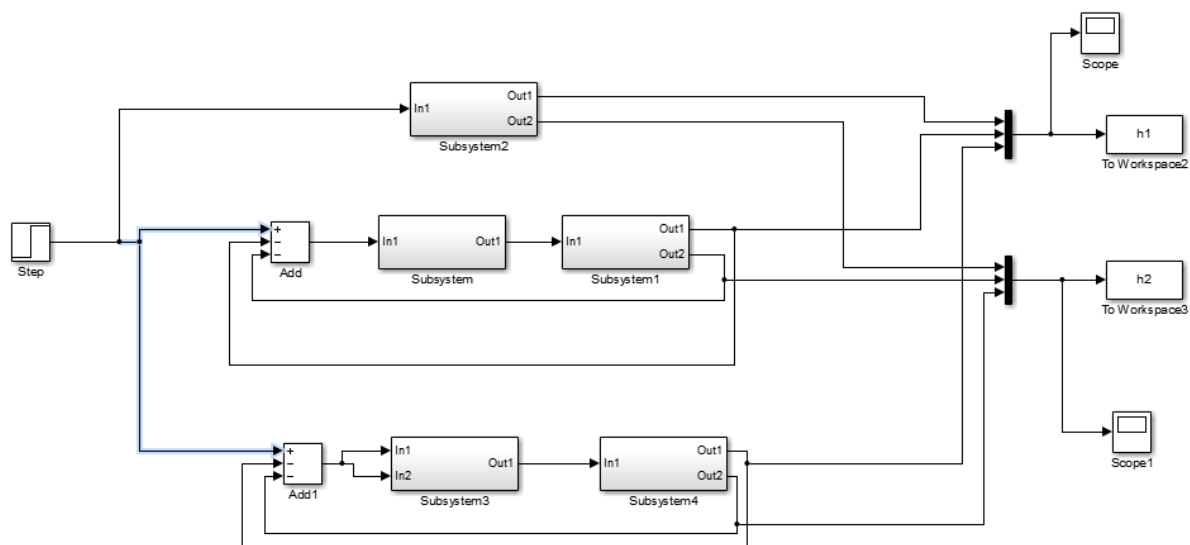
| | | | |
|-----------|-------------|---------------------------|--------------|
| Negativna | Trapezoidal | -0.3987 -0.27 -0.2077 0.1 | [-0.27 0.27] |
| Neznatna | Triangular | -0.1 0 0.1 | |
| Pozitivna | Trapezoidal | 0.1 0.2077 0.27 0.3738 | |

Ventil

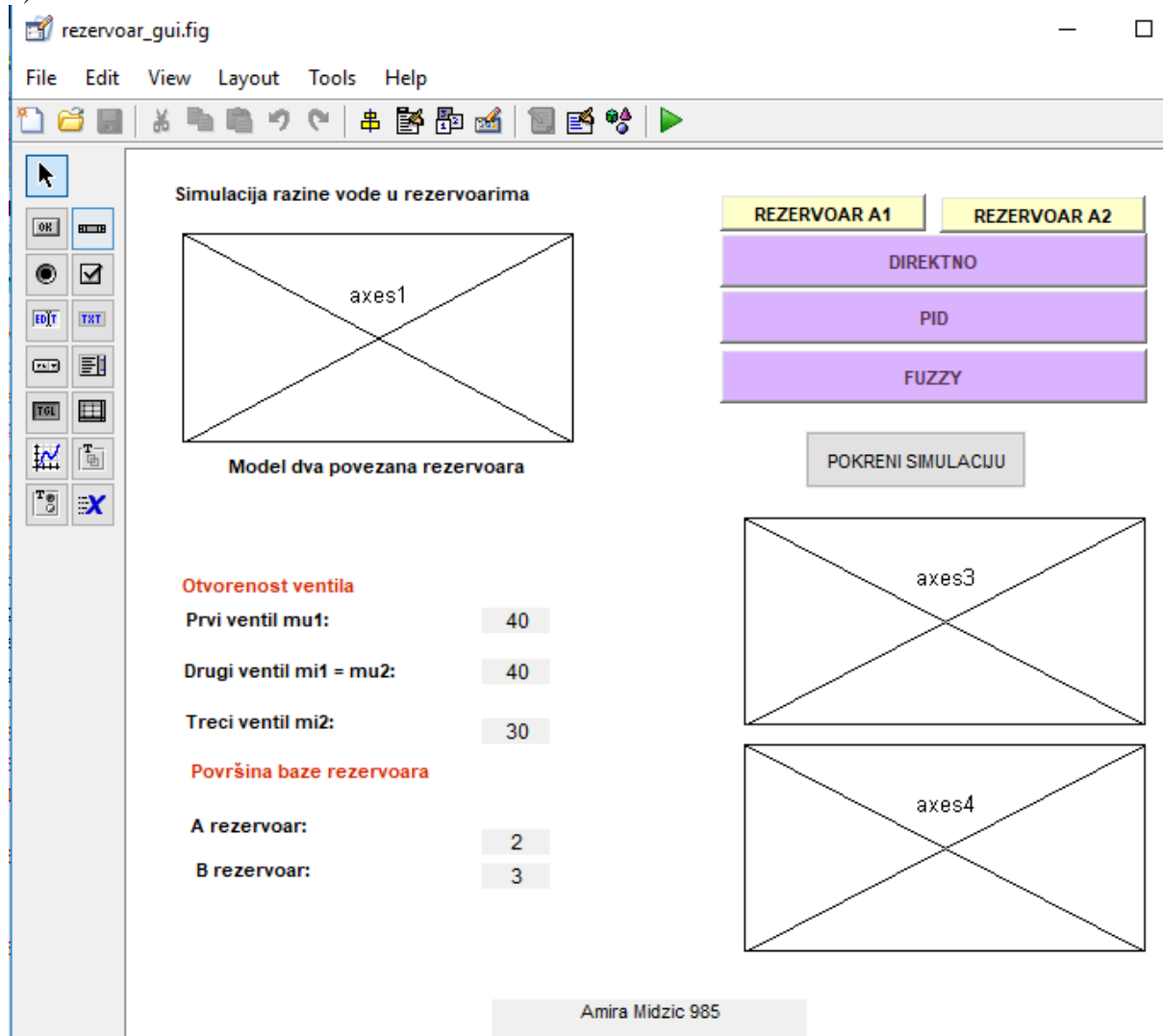
| | | | |
|----------------|------------|---------------------|--------------|
| Zatvori brzo | Triangular | -0.825 -0.55 -0.275 | [-0.55 0.55] |
| Zatvori polako | | -0.55 -0.4 -0.25 | |
| Malo_zatvori | | -0.35 -0.2 -0.05 | |
| Bez promjene | | -0.1375 0 0.1375 | |
| Malo otvori | | 0.05 0.2 0.35 | |
| Otvori polako | | 0.25 0.4 0.55 | |
| Otvori brzo | | 0.275 0.55 0.825 | |

| | | | |
|---------|------------|----------------------------|--------------------------|
| IF NIVO | VISOK | THEN VENTIL IS OTVORI BRZO | |
| | NIZAK | | THEN VENTIL ZATVOIR BRZO |
| | DOBAR | AND PROMJENA IS NEGATIVNA | OTVRI POLAKO |
| | DOBAR | AND PROMJENA IS POZITIVNA | ZATVORI POLAKO |
| | DOBAR | AND PROMJENA IZ NEZNATNA | BEZ PROMJENE |
| | MALO NIZAK | AND PROMJENA IZ NEZNATNA | MALO ZATVORI |
| | MALO VISOK | AND PROMJENA IZ NEZNATNA | MALO OTVORI |

d)



e)



```

function pokreni_Callback(hObject, eventdata, handles)
% hObject      handle to pokreni (see GCBO)
% eventdata    reserved - to be defined in a future version of MATLAB
% handles      structure with handles and user data (see GUIDATA)

% Hint: get(hObject,'Value') returns toggle state of pokreni

set_param('rezervoar_a','SimulationCommand','Start')
set_param('rezervoar_b_pid','SimulationCommand','Start')
set_param('rezervoar_c_fuzzy','SimulationCommand','Start')
set_param('rezervoar_d_sve','SimulationCommand','Start')

r1 = get(handles.rezervoar1, 'Value');
r2 = get(handles.rezervoar2, 'Value');
dir = get(handles.direktno, 'Value');
p = get(handles.pid, 'Value');
f = get(handles.fuzzy, 'Value');
prvi = evalin('base', 'h1');
drugi = evalin('base', 'h2');
y1 = evalin('base', 'y1');
h1_pid = evalin('base', 'h1_pid');
h1_fuzzy = evalin('base', 'h1_fuzzy');
y2 = evalin('base', 'y2');
h2_pid = evalin('base', 'h2_pid');
h2_fuzzy = evalin('base', 'h2_fuzzy');

if(r1==1)
axes(handles.axes3)
if(dir==1 && p ==0 && f==0)
    plot(y1), legend('Jednaccine'), grid on;
end
if(dir==0 && p ==1 && f==0)
    plot(h1_pid), legend('PID'), grid on;
end
if(dir==0 && p ==0 && f==1)
    plot(h1_fuzzy), legend('Fuzzy'), grid on;
end
if(dir==1 && p ==1 && f==0)
    plot(0:length(y1)-1, y1, 0:length(h1_pid)-1, h1_pid),
    legend('Jednaccine', 'PID'), grid on;
end
if(dir==1 && p ==0 && f==1)
    plot(0:length(y1)-1, y1, 0:length(h1_fuzzy)-1, h1_fuzzy),
    legend('Jednaccine', 'Fuzzy'), grid on;
end
if(dir==0 && p ==1 && f==1)
    plot(0:length(h1_pid)-1, h1_pid, 0:length(h1_fuzzy)-1, h1_fuzzy),
    legend('PID', 'Fuzzy'), grid on;
end
if(dir==1 && p ==1 && f==1)
    plot(0:length(prvi)-1, prvi), legend('Jednaccine', 'PID', 'Fuzzy'),
    grid on;
end
end
end

if(r2==1)
axes(handles.axes4)

if(dir==1 && p ==0 && f==0)
    plot(y2), legend('Jednaccine'), grid on;

```

```
end
if(dir==0 && p ==1 && f==0)
    plot(h2_pid), legend('PID'), grid on;
end
if(dir==0 && p ==0 && f==1)
    plot(h2_fuzzy), legend('Fuzzy'), grid on;
end
if(dir==1 && p ==1 && f==0)
    plot(0:length(y2)-1, y2, 0:length(h2_pid)-1, h2_pid),
    legend('Jednachine', 'PID'), grid on;
end
if(dir==1 && p ==0 && f==1)
    plot(0:length(y2)-1, y2, 0:length(h2_fuzzy)-1, h2_fuzzy),
    legend('Jednachine', 'Fuzzy'), grid on;
end
if(dir==0 && p ==1 && f==1)
    plot(0:length(h2_pid)-1, h2_pid, 0:length(h2_fuzzy)-1, h2_fuzzy),
    legend('PID', 'Fuzzy'), grid on;
end
if(dir==1 && p ==1 && f==1)
    plot(0:length(drugi)-1, drugi), legend('Jednachine', 'PID', 'Fuzzy'),
    grid on;
end
end
```

Genetski algoritam 1

1. Napisati program koji će predstavljati određivanje optimuma funkcije pod a, b i c upotrebom integrisane funkcije genetskog algoritma u MATLAB-u.

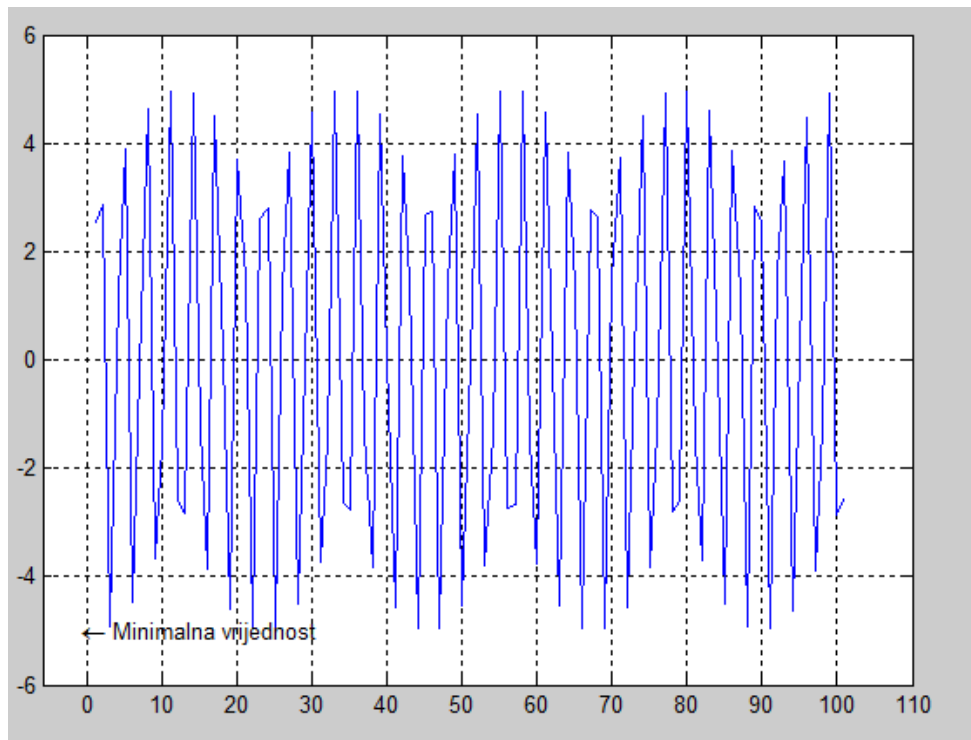
a) $z = 5 \sin(2x)$

b) $z = y^2 + x^2$

c) $z = \sin(x^2) + y^2$

a)

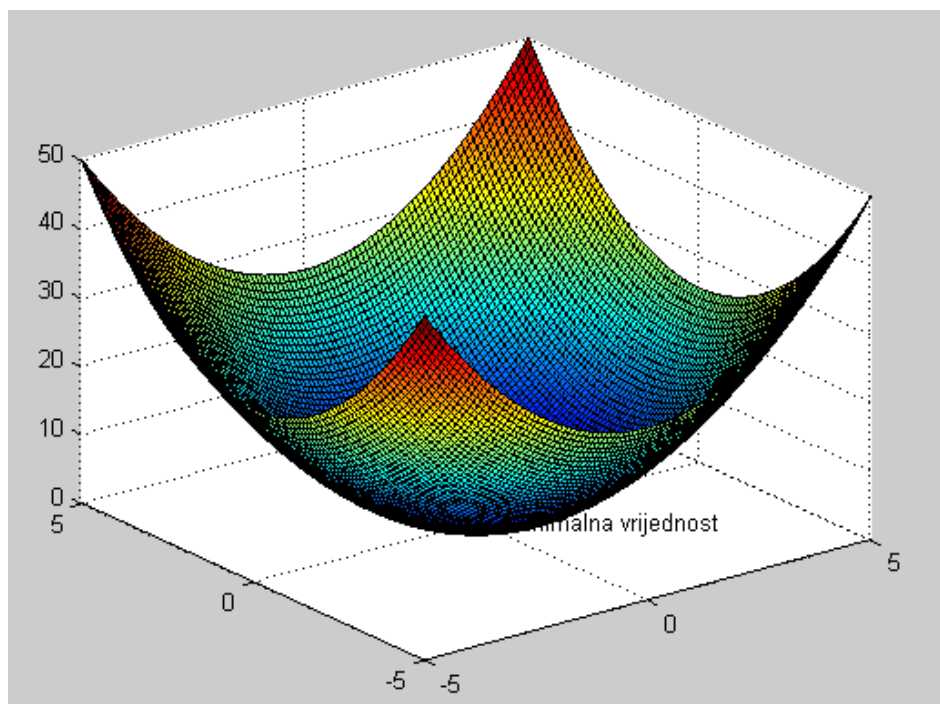
```
x = -50:1:50;
z = 5*sin(2*x); %FUNKCIJA
plot(z);
[x, f, m, n, k, v] = ga(@(x) 5*sin(2*x(1)), 1); %NAREDBA ZA POKRETANJE
text(x, f, '\leftarrow Minimalna vrijednost');
axis([-6 110 -6 6]);
grid ON
```



b)

```
[x, y] = meshgrid(-5:0.1:5, -5:0.1:5);
z = y.^2+x.^2;
surf(x, y, z);
[x, f, m, n, k, v] = ga(@(x) x(2).^2+x(1).^2,2);
text(x(1), x(2), f, '\leftarrow Minimalna vrijednost');

%KLASIFIKACIJA NA?IN TRAŽENJA MINIMUMA FUNKCIJE
r = min(z)
disp('Minimum funkcije');
h = min(r)
```

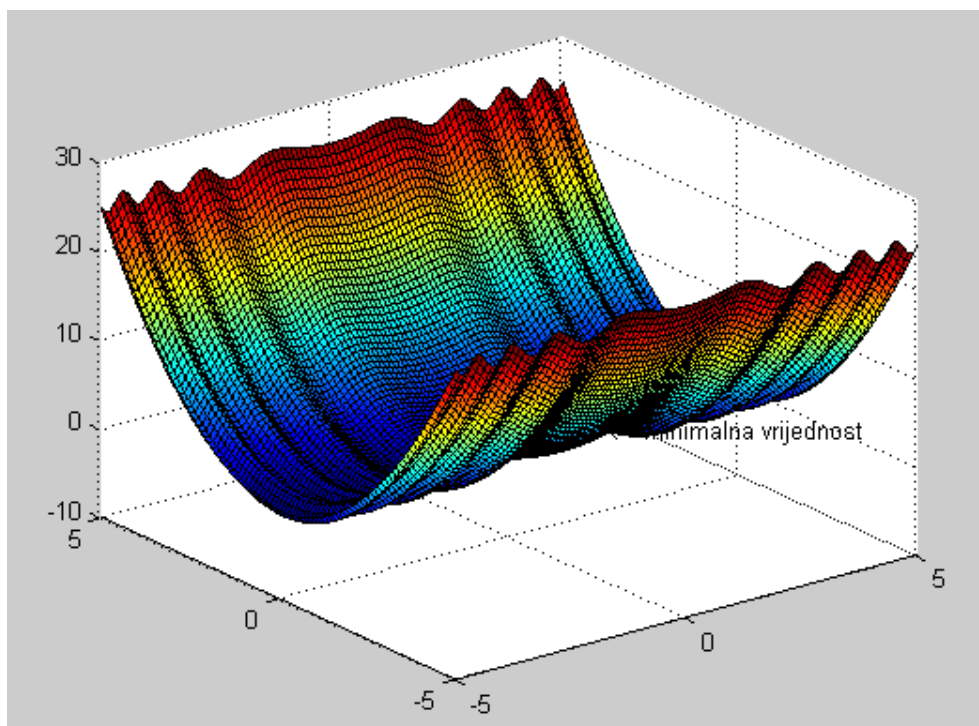


c)

```
[x, y] = meshgrid(-5:0.1:5, -5:0.1:5);
z = sin(x.^2)+y.^2;
surf(x, y, z);
[x, f, m, n, k, v] = ga(@(x) sin(x(1).^2)+x(2).^2,2);
text(x(1), x(2), f, '\leftarrow Minimalna vrijednost');
```

```
%KLASIFIKACIJA NA?IN TRAŽENJA MINIMUMA FUNKCIJE
```

```
r = min(z)
disp('Minimum funkcije');
h = min(r)
```



2. Napisati programski kod u MATLAB-u koji će pronaći maksimum funkcije $\frac{3}{2} \cos(t)$ koristeći mutacijsko-seleksijski algoritam (simulirano kaljenje)

```

period = 0:0.1:3;
funkcija = (3/2)*cos(period); %FUNKCIJA U KOJOJ SE TRAŽI MAKSIMUM
plot(period, funkcija);
axis([-4 4 -2 2]);

%PRVI KORAK: IZBOR SLUŽAJNOG HROMOSOMA X
xx = randi([1 30]); %NASUMICNI INTEGER

%DRUGI KORAK: ODREĐIVANJE FUNKCIJE SPOSOBNOSTI POCETNOG HROMOSOMA
funkcija_sposobnosti_xx = funkcija(xx)

uslov = 1;
zastavica = true;

%PETLJA KOJA OMOGUĆAVA POVRATAK SA 7. NA 3. KORAK
while zastavica == true
    % TREĆI KORAK: PROMJENA X U X' (MUTACIJA)
    ni = 0.01;
    z = randi([-1 1]);
    delta = ni*z;
    xPrim = int8(xx+delta);

    %ČETVRTI KORAK: ODREĐIVANJE FUNKCIJE SPOSOBNOSTI OD X'
    funkcija_sposobnosti_xPrim = funkcija(xPrim);

    %PETI KORAK: ODREĐIVANJE d
    d = funkcija_sposobnosti_xPrim-funkcija_sposobnosti_xx;

    %SESTI KORAK: a) računanje p(d)
    T = 0.1;
    p = 1/1+exp(-d/T);

    %SESTI KORAK: b) NOVO z
    z_novo = randi([0 1]);

    %SESTI KORAK: c) z_novo<p
    if z_novo<p
        xx = xPrim;
    end

    %SESTI KORAK: d) T-ni
    T = 0.1-0.01;

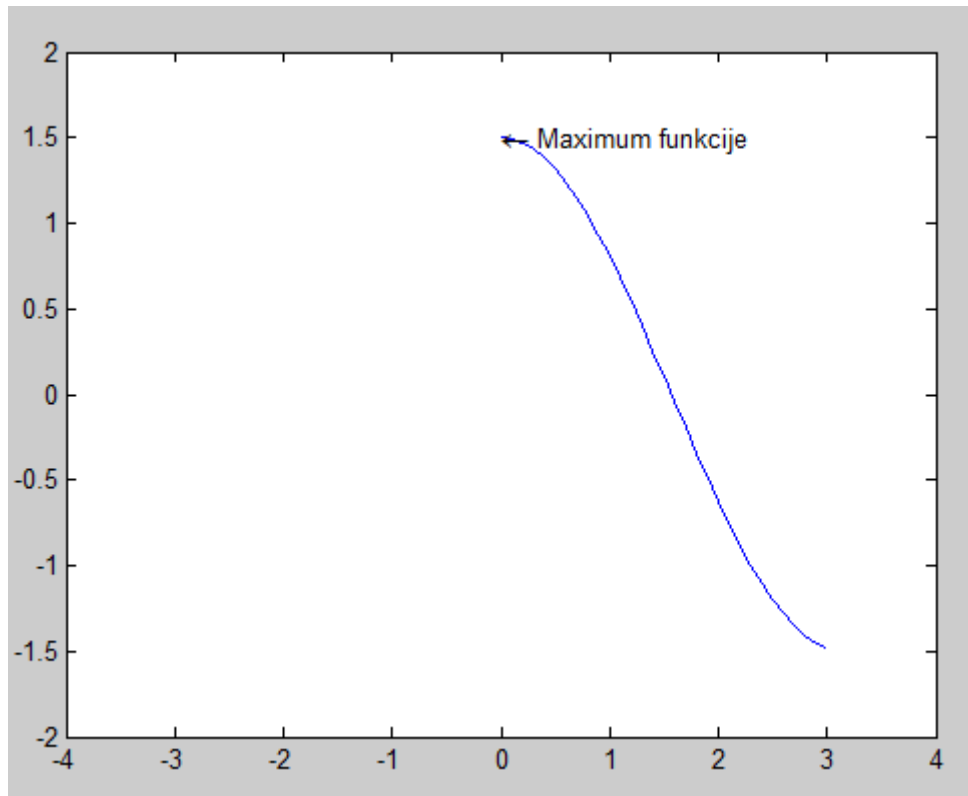
    %SEDMI KORAK: USLOV PREKIDA
    if uslov == 1000
        zastavica =false;
    end

    uslov = uslov+1;
end
koordinata1 = double(xx)/1000;

```



```
koordinata2 = 3/2;
text(koordinata1, koordinata2, '\leftarrow Maximum funkcije');
```



3. Za funkciju $2\cos(t)$ napisati program koji će predstavljati određivanje maksimuma funkcije upotrebom mutacijsko-seleksijskog algoritma

```
clc
clear all
t = 0:0.01:2*pi;
f = 2*cos(t);
plot(t,f,'k','linewidth',2); grid on;
axis([-0.9 6.5 -2.5 2.5]);

% 1. Izbor slučajnog hromosoma x
x = randi([1 length(f)]);

% 2. Funkcija sposobnosti x
fx = f(x);

uslov = 1;
zast = true;

while zast == true

% 3. Mutacija (x->x')
ni = length(f)*rand(1);
z = randi([-1 1]);
delta = ni*z;
xp = int8(x+delta);

zast1 = true;
while zast1 == true
```

```

    zast1 = false;
    if (xp>length(f) || xp<=0)
        ni = length(f)*rand(1)
        delta = ni*z;
        xp = int8(x+delta);
        zast1 = true;
    end
end

% 4. Funkcija sposobnosti x'
fxp = f(xp);

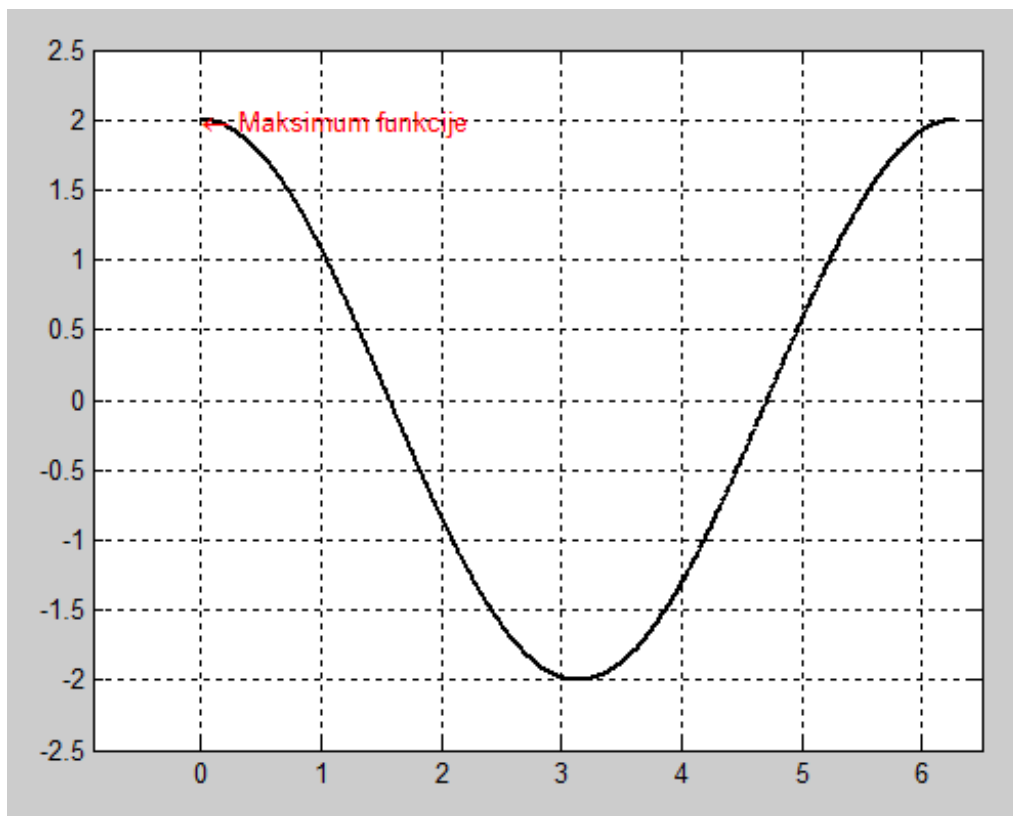
% 5. Razlika funkcija sposobnosti (određivanje boljeg hromosoma)
d = fxp - fx;

% 6. Odabiranje hromosoma
if d>0
    x = xp;
end

% 7. Izlaz iz petlje
if uslov == 50
    zast = false;
end
uslov = uslov+1;
end

k1 = double(x)/50;
k2 = 2;
text(k1, k2, '\leftarrow Maksimum funkcije','color','r');

```



4. Napisati programski kod kojim će se odrediti maksimum funkcije od kreirane slučajne populacije upotrebom genetskog algoritma

```

clear all
clc
tic %POCETAK TAJMERA
tekst = 'Tekst';

popDuzina = 1000;
genome = length(tekst);
stopaMutacije = 0.001;
brojac = 1;
S = 4;
najbolji = Inf;
maxVrijednost = max(double(tekst));
idealno = double(tekst);

selekcija=0;
krizanje = 1;
iscrtavanje = 1;

%POSTAVLJANJE POCETKA SLUCAJNE POPULACIJE
Pop = round(rand(popDuzina, genome)*(maxVrijednost-1)+1);

initF = min(sum(abs(bsxfun(@minus, Pop, idealno)), 2);

for Gen = 1:1e6
    F = sum(abs(bsxfun(@minus, Pop, idealno)), 2);
    [trenutni, trenutniGen] = min(F);

    if trenutni < najbolji
        najbolji=trenutni;
        najboljiGen = Pop(trenutniGen);

        if iscrtavanje == 1
            B(brojac) = najbolji;
            G(brojac) = Gen;
            brojac = brojac+1;
        end

        fprintf('Gen: %d Sposobnost: %d', Gen, najbolji);
        disp(char(najboljiGen));
    elseif najbolji == 0
        break
    end

    %ODABIR PAROVA RODITELJA
    if selekcija == 0
        T = round(rand(2*popDuzina, S)*(popDuzina-1)+1);
        [~, idx] = min(F(T), [], 2);
        W = T(sub2ind(size(T), (1:2*popDuzina)', idx));
    elseif selekcija == 1
        [~, V] = sort(F, 'descend');
        V = V(popDuzina/2+1:end);
        W = V(round(rand(2*popDuzina, 1)*(popDuzina/2-1)+1));
    end

    %KRIZANJE

    if krizanje == 0

```

```

    idx = logical(round(rand(size(P))));
    Pop2 = Pop(W(1:2:end), :);
    P2A = Pop(W(2:2:end), :);
    Pop2(idx) = P2A(idx);

elseif krizanje==1
    Pop2 = Pop(W(1:2:end), :);
    P2A = Pop(W(2:2:end), :);
    Ref = ones(popDuzina, 1)*(1:genome);
    idx = (round(rand(popDuzina, 1) * (genome-1)+1)*ones(1, genome)) >
Ref;
    Pop2(idx) = P2A(idx);
elseif krizanje == 2
    Pop2 = Pop(W(1:2:end), :);
    P2A = Pop(W(2:2:end), :);
    Ref = ones(popDuzina, 1)*(1:genome);
    CP = sort(round(rand(popDuzina, 2) * (genome-1)+1), 2);
    idx = CP(:, 1)*ones(1, genome)<Ref&CP(:, 2)*ones(1, genome)>Ref;
end

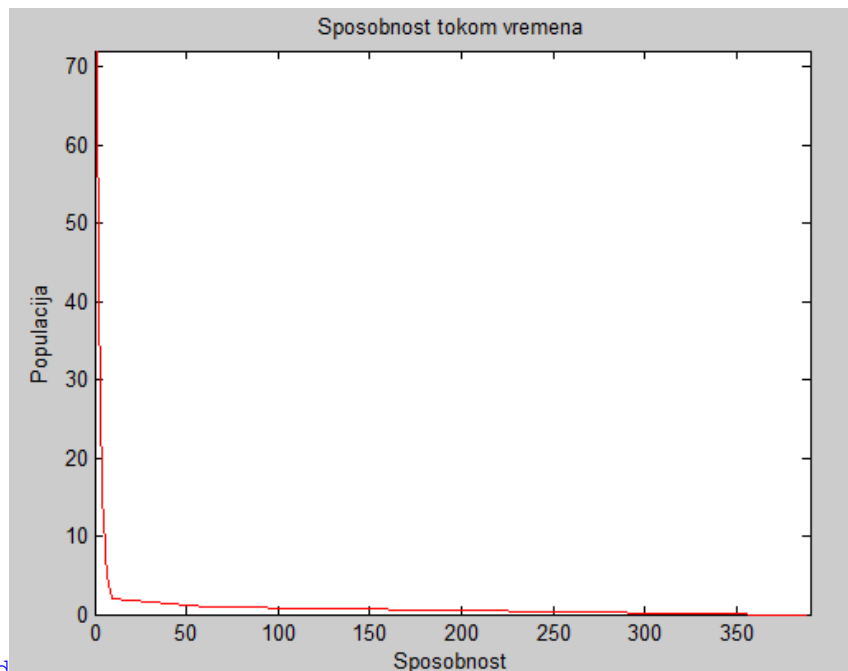
%MUTACIJA
idx = rand(size(Pop2))<stopaMutacije;
Pop2(idx) = round(rand([1, sum(sum(idx))])*(maxVrijednost-1)+1);

%RESETOVANJE POPULACIJE
Pop = Pop2;
end

toc

if iscrtavanje ==1
    figure(1)
    plot(G(:), B(:), '-r');
    axis([0 Gen 0 initF]);
    xlabel('Sposobnost'); ylabel('Populacija'), title('Sposobnost tokom
vremena');
end

```

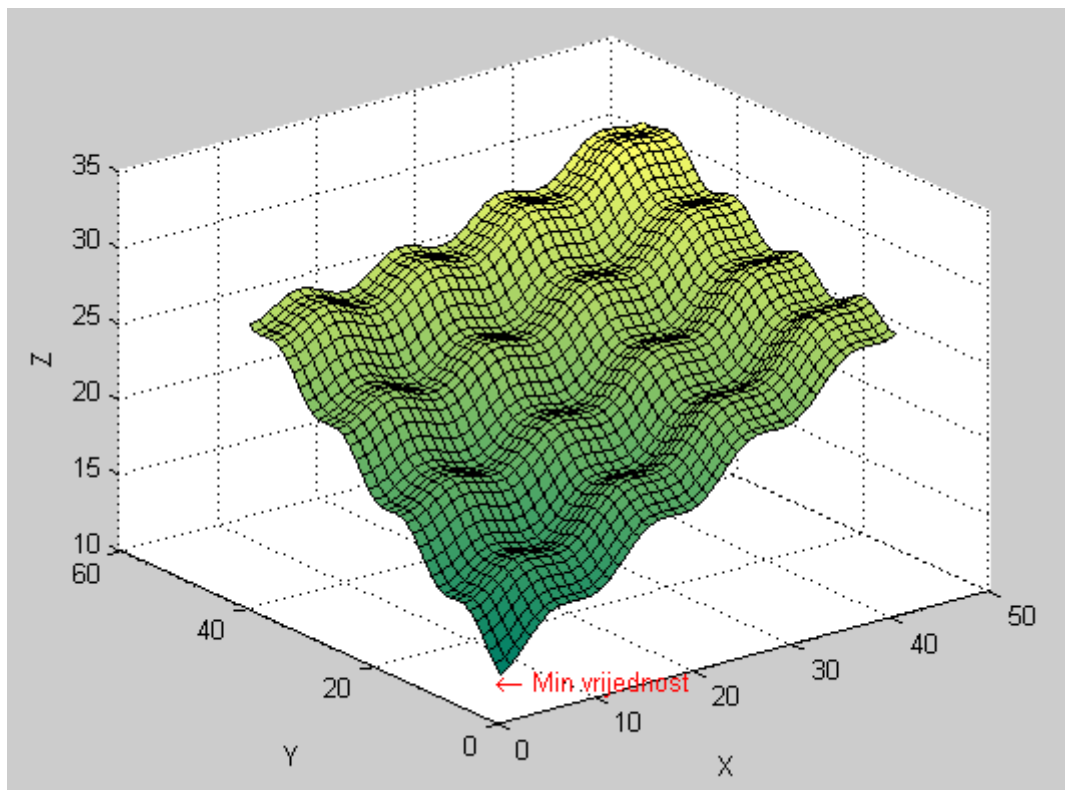


Genetski algoritam 2

1. Nadi minimum funkcije na intervalu 0-5, 0-5.

```
close all
%zadatak 1
%naciminimum funkcije naintervalu 0-5, 0-5
[x,y] = meshgrid (0:0.1:4, 0:0.1:4);
c=2.*pi;
z=1/2.*(-20.*exp(1).*(-0.20.*sqrt(1/2.*(x.^2+y.^2)))-
exp(1).*(1/2.*(cos(c.*x)+cos(c.*y)))+20+exp(1)+5.7);
disp('Minimalna vrijednost rucno: ')
b=min(min(z));
[x,f]=ga(@(x) 1/2.*(-20.*exp(1).*(-0.20.*sqrt(1/2.*(x(1).^2+x(2).^2)))-
exp(1).*(1/2.*(cos(c.*x(1))+cos(c.*x(2)))+20+exp(1)+5.7),2,[],[],[],...
[],[0 0], [4 4]));
x
x(1)
x(2)
disp('Minimalna vrijednost ga: ')
f
figure

surf(z)
colormap summer
xlabel('X');
ylabel('Y');
zlabel('Z');
text(x(1),x(2),f,'\leftarrow Min
vrijednost','FontSize',10,'Color','red','linewidth',2.5);
```



2. Nađi minimum funkcije:

$$f(x) = \begin{cases} -\exp\left(-\left(\frac{x}{20}\right)^2\right) & \text{za } x \leq 20 \\ -\exp(-1) + (x-20)(x+22) & \text{za } x > 20 \end{cases}$$

```
close all
clc
clear
x=0:0.1:22; %proizvoljno stavljamo

if max(x)<=20
    y1=-exp(-(x./20).^2);
    plot(x,y1);
    a=min(y1)

[x,f]=ga(@(x) -exp(-x(1)./20).^2,1,[],[],[], ...
    [],[0],[20]);
x
f
elseif max(x)>20
    y=-exp(-1)+(x-20).*(x+22);

    plot(x,y);
    b=min(y)
    [x,f]=ga(@(x) -exp(-1)+(x(1)-20).*(x(1)+22),1,[],[],[], ...
    [],[0],[21]);
x
f
end
text(x(1),f,'\leftarrow Min
vrijednost','FontSize',10,'Color','red','linewidth',2.5)
```

