INDIAN INSTITUTE OF TECHNOLOGY ROORKEE



Sparsh Mittal

Logical Operations (for bitwise manipulation)

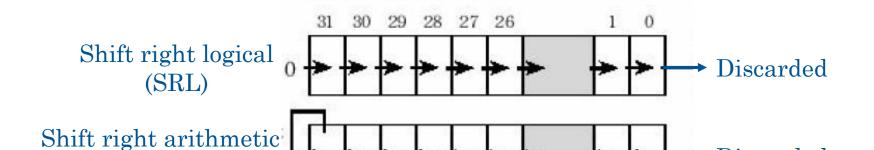
Operation	С	Java	RISC-V
Shift left	<<	<<	sll, slli
Shift right	>>	>>>	srl, srli, sra, srai
Bit-by-bit AND	&	&	and, andi
Bit-by-bit OR			or, ori
Bit-by-bit XOR	^	^	xor, xori
Bit-by-bit NOT	~	~	not

srl = shift-right logical. "i" refers to immediate

Arithmetic and logical shifts

Here, we show 32b registers. Same applies to a 64b register also

n = #shifted bits

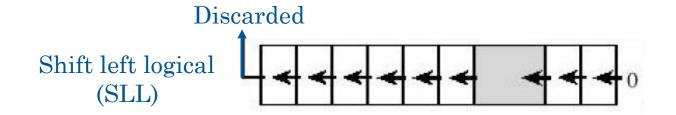


Equivalent to

Unsigned divide by 2ⁿ

Signed divide by 2ⁿ

Discarded



Multiply by 2ⁿ (both signed and unsigned)

(SRA)

Examples

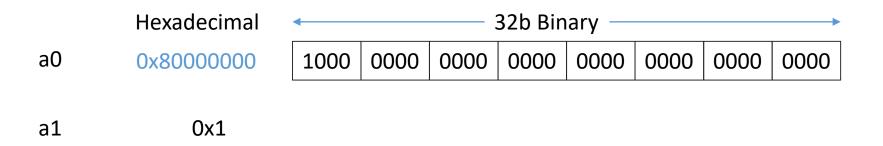
- Q1. Shift-left register x10 by the number stored in x11. Store result in x9.
- sll x9, x10, x11
- So, if x11 stores 5, then x10 shifted by 5 will be stored in x9.
- Q2. Shift-left register x10 by 3 times. Store result in x9.
- slli x9, x10, 3

Shift Instructions (SLL, SRL, SRA)

```
li a0, 0x80000000 # a0 \leftarrow 0x80000000 li a1, 1 # a1 \leftarrow 1 (We want to shift by 1 position) sll a2, a0, a1 # a2 \leftarrow 0 (The MSB bit is discarded, so the number becomes zero) srl a3, a0, a1 # a3 \leftarrow 0x40000000. New bit filled =0 sra a4, a0, a1 # a4 \leftarrow 0xC00000000. New bit filled =1
```

Visual explanation is shown on the next slide.

Visual explanation



On doing, "sll a2, a0, a1", we are shifting a0 left by 1. So now, the value of a2 is:

On doing, "srl a3, a0, a1", we are shifting a0 right by 1. It's logical shift, so new bit filled will be 0. a3 will be

On doing, "sra a4, a0, a1", we are shifting a0 right by 1. It's arithmetic shift, so new bit filled will be the same as the sign bit, which is 1. a4 will be

Corner case

- NOTE: div always rounds towards zero, whereas srai rounds towards negative infinity. Hence, srai is not exactly equivalent to division.
- Srai fails for Odd Negative Numbers.

There is no SLA operation. Why? Answer: Two's complement ensures that SLA and SLL lead to same effect.

- ☐ Right shift requires both logical and arithmetic modes
 - Assuming 4 bits
 - $(4_{10})>>1=(0100_2)>>1=0010_2=2_{10}$ Correct!
 - $(-4_{10})>>_{logical}1 = (1100_2)>>_{logical}1 = 0110_2 = 6_{10}$ For signed values, Wrong!
 - \circ (-4₁₀)>>_{arithmetic}1 = (1100₂)>>_{arithmetic}1 = 1110₂ = -2₁₀ Correct!
 - Arithmetic shift replicates sign bits at MSB
- Left shift is the same for logical and arithmetic
 - Assuming 4 bits
 - $(2_{10}) << 1 = (0010_2) << 1 = 0100_2 = 4_{10}$ Correct!
 - \circ $(-2_{10}) <<_{logical} 1 = (1110_2) <<_{logical} 1 = 1100_2 = -4_{10}$ Correct!

Understanding left-shift

- Consider a 4-bit number -6, which is 1010.
- On left-shifting, we should get -12. But we get 0100, which is just 4. Is this an error?
- **Explanation:** With 4 bits, we can represent only -8 to 7. The number -12 is outside the range, so overflow happens.
- We have to use 5-bit number system. Here, -6 is 11010.
- On left-shifting, we get 10100, which is -12, the correct answer.

Solved example

Multiplication by 4

	C code	RISC-V code
Left-shift by 2 = Multiplication by 4	a=64; b=2; c = a< <b; /*Final value of c becomes 256 */</b; 	li a0, 64 li a1, 2 sll a2, a0, a1
Right-shift by 2 = Division by 4	a=64; b=2; c = a>>b; /*Final value of c becomes 16 */	li a0, 64 li a1, 2 sra a2, a0, a1
Right-shift by 2 = Division by 4. Floor(50/2) = 12	a=50; b=2; c = a>>b; /*Final value of c becomes 12 */	li a0, 50 li a1, 2 sra a2, a0, a1

Solved Exercise

- Program to (unsigned) divide register a0 by 8. Result in a1
- Srli a1 a0 3

- Program to (signed) divide register a0 by 8. Result in a1
- Srai a1 a0 3

- Program to multiply register a0 by 8. Result in a1
- Slli a1 a0 3

Solved Exercise

- Program to multiply register a0 by 10. Result in a3
- Slli a1 a0 3 # y = x*8
- Slli a2 a0 1 $\# z = x^2$
- Add a3 a1 a2 #v = y+z = x*10

AND Operations

- Useful to mask bits in a word
 - Select some bits, clear others to 0

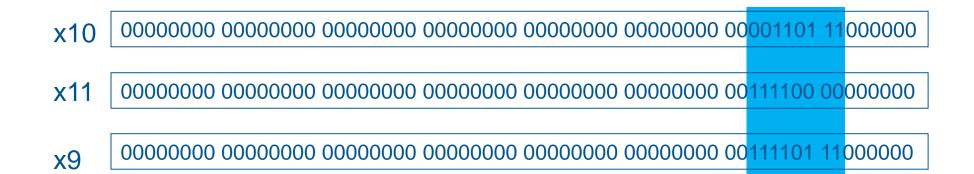
```
and x9, x10, x11
```

- Clear a register:
- andi t0, t0, 0 # Clear register t0

OR Operations

- Useful to include bits in a word
 - Set some bits to 1, leave others unchanged

```
or x9, x10, x11
```



XOR Operations

- Differencing operation
 - Set some bits to 1, leave others unchanged

```
xor x9, x10, x12
```

Negate

Negate (NEG) instruction computes two's complement of a value.

neg x6, x5
$$\#$$
 x6 \leftarrow -x5

If value of x5 was 1, then above instruction would store -1 in x6.

Logical instructions

```
li a0, 6  # a0 <- 0110 (in binary)

li a1, 10  # a1 <- 1010 (in binary)

and a2, a0, a1  # a2 <- 0010 (in binary) or 2 (in decimal)

or a3, a0, a1  # a3 <- 1110 (in binary) or 14 (in decimal)

not a4, a0  # a4 <- 0xFFFFFFF9 (1's complement of 6 in 32bits)

neg a5, a0  # a5 <- 0xFFFFFFFA (2's complement of 6 in 32bits)
```

```
Compute 1's complement of 0110 in 32 bits.

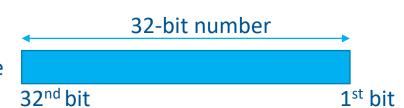
Answer: Original number is 0000 0000 0000 0000 0000 0000 0110

1's complement is 1111 1111 1111 1111 1111 1111 1001

In hexa, this is same as F F F F F F F F 9 , that means 0xFFFFFFF9
```

Solved question

- Let x5 = 0x00000000AFAFAFAF
- x6 = 0x1234567812345678
- Then, what is the value of x7 after these instructions?
- slli x7, x5, 4
- or x7, x7, x6
- Remember: the shift of "4" is at bit-level, whereas the number is specified as a hexadecimal number. Hence, 4-bit shift will lead to shift of one hex symbol.
- Answer:
- Explanation: After slli, x7 becomes 0x0000000AFAFAFAF0
- Finally, x7 is 0x1234567AFAFEFEF8.



How counting is done

Solved Question

• Assume RV32. Register a0 currently stores some non-zero value.

Set its 29th bit to 1.

li a1 1 slli a2 a1 28 or a0 a0 a2

Reset its 29th bit

li a1 1 slli a2 a1 28 not a3 a2 and a0 a0 a3

Flip its 29th bit

li a1 1 slli a2 a1 28 xor a0 a0 a2

C code

```
int a;

//a="some value";

a = a | 0x10000000;
```

C code

```
int a;
//a="some value";
a = a & Oxefffffff;
```

C code

```
int a;

//a="some value";

a = a^0x10000000;
```

Solved Question

- Assume RV32. Check whether the lowest 4 bits of register a0 are 1010. If so, put 1 in a5
- li a1 0b1010
- li a2 0b1111
- and a3 a0 a2
- xor a4 a3 a1 # if a3 was 1010, then a4 should be all zeros.
- Seqz a5 a4

Solved Question [Case 1: 1010 is there]

• Assume RV32. Check whether the lowest 4 bits of register a0 are 1010. If so, put 1 in a5

• li a1 0b1010

a1 = 0000 0000 0000 0000 0000 0000 1010

• li a2 0b1111

• and a3 a0 a2

a3 = 0000 0000 0000 0000 0000 0000 1010

• xor a4 a3 a1 # if a3 was 1010, then a4 should be all zeros.

a4 = 0000 0000 0000 0000 0000 0000 0000

• Seqz a5 a4

a5 = 0000 0000 0000 0000 0000 0000 0001

a5 becomes 1

Solved Question [Case 2: 1010 is not there]

• Assume RV32. Check whether the lowest 4 bits of register a0 are 1010. If so, put 1 in a5

• li a1 0b1010

a1 = 0000 0000 0000 0000 0000 0000 1010

• li a2 0b1111

a2 = 0000 0000 0000 0000 0000 0000 1111

• and a3 a0 a2

a3 = 0000 0000 0000 0000 0000 0000 1110

• xor a4 a3 a1 # if a3 was 1010, then a4 should be all zeros.

a4 = 0000 0000 0000 0000 0000 0000 0100

• Seqz a5 a4

a5 = 0000 0000 0000 0000 0000 0000 0000

a5 becomes 0

Instruction	Туре	Example	Meaning
AND	R	and rd, rs1, rs2	R[rd] = R[rs1] & R[rs2]
OR	R	or rd, rs1, rs2	$R[rd] = R[rs1] \mid R[rs2]$
XOR	R	xor rd, rs1, rs2	$R[rd] = R[rs1] ^ R[rs2]$
AND immediate	I	andi rd, rs1, imm12	R[rd] = R[rs1] & SignExt(imm12)
OR immediate	I	ori rd, rs1, imm12	R[rd] = R[rs1] SignExt(imm12)
XOR immediate	I	xori rd, rs1, imm12	R[rd] = R[rs1] ^ SignExt(imm12)
Shift left logical	R	sll rd, rs1, rs2	R[rd] = R[rs1] << R[rs2]
Shift right logical	R	srl rd, rs1, rs2	R[rd] = R[rs1] >> R[rs2] (logical)
Shift right arithmetic	R	sra rd, rs1, rs2	R[rd] = R[rs1] >> R[rs2] (arithmetic)
Shift left logical immediate	I	slli rd, rs1, shamt	R[rd] = R[rs1] << shamt
Shift right logical imm.	I	srli rd, rs1, shamt	R[rd] = R[rs1] >> shamt (logical)
Shift right arithmetic immediate	I	srai rd, rs1, shamt	R[rd] = R[rs1] >> shamt (arithmetic)