## Poker as a Testbed for AI Research<sup>1</sup>

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Abstract. For years, games researchers have used chess, checkers and other board games as a testbed for artificial intelligence research. The success of world-championship-caliber programs for these games has resulted in a number of interesting games being overlooked. Specifically, we show that poker can serve as an interesting testbed for machine intelligence research related to decision making problems. Poker is a game of imperfect knowledge, where multiple competing agents must deal with risk management, agent modeling, unreliable information and deception, much like decision-making applications in the real world. The heuristic search and evaluation methods successfully employed in chess are not helpful here. This paper outlines the difficulty of playing strong poker, and describes our first steps towards building a world-class poker-playing program.

## 1. Introduction

Why study computer games? By writing programs that play games, some insights can be gained about machine intelligence. These lessons can then be used to develop useful non-game programs. Researchers have invested a lot of effort researching board games such as chess and checkers. These games all share the property that high performance can be achieved by brute-force search. This search emphasis was taken to the extreme by *Deep Blue*, which analyzed 200 million positions per second in its May 1997 match against World Chess Champion Garry Kasparov. This achievement only confirmed the effectiveness of brute-force search for some application domains. Can computer games give us any fresh insights into machine intelligence, beyond brute-force search?

We believe that the answer to this question is yes. However, real progress can only be made if we study games in which search is not the major criteria for success. Instead, we need to mimic real-world applications that are perceived to require intelligent behaviour. Activities such as financial trading, business negotiations, and

<sup>&</sup>lt;sup>1</sup> This research is supported by the Natural Sciences and Engineering Research Council of Canada.

forecasting (from weather to politics) meet this criteria. The first column of Table 1 shows some of the characteristics of these applications from the AI point of view. We are not claiming that these are the only activities of interest, just that they are important considerations for a wide range of interesting problem domains. Unfortunately, games like chess and checkers do not have these characteristics, or involve them only in limited ways. Can these activities be studied in the context of computer games, and if so, what games?

Table 1. Characteristics of AI problems and how they are exhibited by poker.

General problem	Problem realization in poker		
imperfect knowledge	opponents' hands are hidden		
multiple competing agents	many competing players		
risk management	betting strategies and their consequences		
agent modeling	identifying opponent patterns and exploiting them		
deception	bluffing and varying style of play		
unreliable information	handling your opponents' deceptive plays		

We are currently studying the game of poker and are attempting to build a high-performance poker program that is capable of beating the best human players. As shown in the second column of Table 1, poker exhibits all of the activities we are interested in studying.

Certain aspects of poker have been extensively studied by mathematicians and economists but, surprisingly, very little work has been done by computing scientists. There are two main approaches to poker research. One approach is to use simplified artificial variants [1] or simplified real variants [2] [3] that are easier to analyze. For example, one could use only two players or constrain the betting rules. The other approach is to pick a real variant, but to combine mathematical analysis, simulation and ad-hoc expert experience. Expert players with a penchant for mathematics are usually involved in this approach [4].

Simplification is a common technique for solving difficult problems. However, we must be careful that simplification does not remove the complex activities that we are interested in studying. For example, Findler worked on and off for 20 years on a poker-playing program for 5-card draw poker [5]. His approach was to model human cognitive processes and build a program that could learn. Unfortunately his simplified approach nullified many of the potential benefits of his research [6].

Recently, Koller and Pfeffer have been investigating poker from a theoretical point of view [7]. They implement the first practical algorithm for finding optimal randomized strategies in two-player imperfect information competitive games. This is done in their *Gala* system, a tool for specifying and solving problems of imperfect information. Their system builds trees to find the game-theoretic optimal (but not maximal) strategy, however only vastly simplified versions of poker can be solved due to the size of trees being built. The authors state that "...we are nowhere close to being able to solve huge games such as full-scale poker, and it is unlikely that we will ever be able to do so."

We have chosen to study the game of Texas Hold'em, the poker variation used in the annual World Series of Poker Championships. It is considered to be the most strategically difficult poker variant that is widely played, and requires all of the complex activities listed in Table 1. This paper describes our first steps towards building a strong poker program, called *Loki*. Section 2 gives the rules of Texas Hold'em. Section 3 discusses the requirements of a strong Hold'em program and provides evidence that all of the activities listed in Table 1 are necessary to play strong poker. Section 4 describes the *Loki* program and Section 5 gives some initial performance assessments. Section 6 discusses ongoing work on this project.

The research contributions of this paper include:

- · showing that poker can be a testbed of real-world decision making,
- identifying the major requirements of high-performance poker,
- · presenting new enumeration techniques for hand-strength and potential, and
- · demonstrating a working program that successfully plays "real" poker.

## 2. Texas Hold'em

A hand of Texas Hold'em begins with the *pre-flop*, where each player is dealt two *hole* cards, face down, followed by the first round of betting. Then three community cards are dealt face up on the table, called the *flop*, and the second round of betting occurs. On the *turn*, a fourth community card is dealt face up and another round of betting ensues. Finally, on the *river*, a fifth community card is dealt face up and the fourth (final) round of betting occurs. All players still in the game turn over their two hidden cards for the *showdown*. The best five card poker hand formed from the two hole cards and the five community cards wins the pot. If a tie occurs, the pot is split. Typically Texas Hold'em is played with 8 to 10 players.

Limit Texas Hold'em uses a structured betting system, where the order and amount of betting is strictly controlled on each betting round<sup>2</sup>. There are two denominations of bets, called the small bet and the big bet. For simplicity, we will use a value of \$10 for the small bet and \$20 for the big bet. In the first and second betting rounds (preflop and flop), all bets and raises are \$10, while in rounds three and four (turn and river), they are \$20. In general, when it is a player's turn to bet, one of three options is available: fold (withdraw from the hand, leaving all previously wagered money in the pot), call (match the current outstanding bet; if there is no current bet, one is said to check), or raise one bet (put the current bet plus one into the pot; if there is no current bet, one is said to bet). There is usually a maximum of three raises allowed per betting round. The betting option rotates clockwise until each player that has not folded has put the same amount of money into the pot for the current round, or until there is only one player remaining. In the latter case, this player is the winner and is awarded the pot without having to reveal their cards.

There is a strategic advantage to being the last bettor in any given round, so to maintain fairness, the order of betting is rotated clockwise after each hand.

<sup>&</sup>lt;sup>2</sup> In No-limit Texas Hold'em, there are no restrictions on the size of bets.

# 3. Requirements for a World-Class Poker Player

We have identified several key components (modules) that incorporate some of the required activities of a strong poker player and address most of the six characteristics listed in Table 1. However, these components are not independent. They must be continually refined as new activities are supported.

- Hand strength: assesses how strong your hand is in relation to what other players may hold. Hand strength is computed on the flop, turn and river. At a minimum, hand strength is a function of your cards and the community cards that have been dealt. A better hand strength computation takes into account the number of players still in the game, position at the table, and history of betting in the hand. An even better model considers different probabilities for each hidden hand, based on the relative chance of each hand being played to the current point in the game. This may be improved by varying the hidden hand probabilities for each player depending on a learned model of that opponent's play.
- Hand potential: assesses the probability of the hand improving (or being overtaken) as additional community cards appear. For example, having four cards in the same suit does not count toward hand strength, but has good potential to become a winning flush as more community cards are dealt. At a minimum, hand potential is a function of your cards and the community cards that have already been dealt. However, a better model can be evolved as capabilities are added to the program, similar to the hand strength computation described above.
- Betting strategy: determines whether to fold, call/check, or bet/raise in any given situation. A minimum model is based on hand strength. Refinements consider hand potential, pot odds (your winning chances compared to the expected return from the pot), bluffing, opponent modeling and unpredictability. Note that an accurate computation of your winning chances is necessary. This requires a sophisticated assessment of hand strength, as described above. Even with an accurate hand strength computation, the game-theoretic optimal folding/calling strategy may not be the best decision in practice, where bluffing, opponent modeling and unpredictability may be used to improve your betting strategy.
- Bluffing<sup>3</sup>: allows you to make a profit from weak hands. Even if you only break even on the bluffing plays, the false impression created about your play may improve the profitability of subsequent hands. Thus, bluffing is critical to successful play. Game theory can be used to compute a theoretical optimal bluffing frequency in certain situations. The minimal bluffing system merely bluffs this percentage of hands. In practice, you need to be able to predict the probability that your opponent will call in order to identify profitable bluffing opportunities. The better your opponent models are, the better your bluffing strategy will be.
- Opponent modeling: allows you to determine a likely probability distribution
  for your opponent's hidden cards or betting strategy. A minimal opponent model
  might use a single model for all opponents in a given hand. This can be improved

<sup>&</sup>lt;sup>3</sup> Other forms of bluffing (semi-bluffing and betting a strong hand weakly) are not considered here.

by modifying the probabilities based on a classification of each opponent (e.g. weak/strong, passive/aggressive), betting history, and collected statistics. Opponent modeling has been attempted in two-player games but with limited success [8]. In poker, however, it is essential to success.

Unpredictability: makes it difficult for opponents to form an accurate model of
your strategy. By varying playing strategy over time (e.g. pre-flop hand selection,
variable bluffing rate), opponents may be induced to make mistakes based on an
incorrect model.

In addition, there are a number of less immediate concerns which may not be necessary to play reasonably strong poker, but may be required for world-class play.

This paper focuses on the issues of hand strength, hand potential and betting strategy. Other issues are the subject of on-going research.

## 4. Loki

Loki handles its play differently at the pre-flop, flop, turn and river. The play is controlled by two components: an evaluation of the hand and a betting strategy. The strategy is influenced both by the pot odds and our model of the opponent.

## 4.1. Pre-flop Evaluation

The hand strength for pre-flop play has been extensively studied in the poker literature [4]. These works attempt to explain the play in human understandable terms, by classifying all the initial two-card pre-flop combinations into nine betting categories. For each hand category, a suggested betting strategy is given, based on the strength of the hand, the number of players in the game, the position at the table, and the type of opponents (e.g. aggressive or conservative). For a poker program, these ideas could be implemented as an expert system, but a more general approach would be preferable.

For the initial two cards, there are {52 choose 2} = 1326 possible combinations, but only 169 distinct hand types. For each one of the 169 possible hand types, a simulation of 1,000,000 poker games was done against nine random opponents. This produced a statistical measure of the approximate *income rate* for each starting hand. A pair of aces had the highest income rate; a 2 and 7 (of different suits) had the lowest income rate for a 10-player simulation. There is a strong correlation between our simulation results and the pre-flop card ordering given in [4] (although there are a few interesting differences).

#### 4.2. Hand Evaluation

Critical to the program's performance on the flop, turn and river is an assessment of the current strength of the program's hand. Enumeration techniques can provide an accurate estimate of the probability of currently holding the strongest hand.

For example, suppose our starting hand is A - Q and the flop is 3 - 4. There are 47 remaining unknown cards and there are  $\{47 \text{ choose } 2\} = 1,081$  possible hands an opponent might hold. To estimate hand strength, the enumeration technique gives a percentile ranking of our hand. We simply count the number of possible hands that are better than ours (any pair, two pair, A-K, or three of a kind: 444 hands), how many hands are equal to ours (9 possible remaining A-Q combinations), and how many hands are worse than ours (628). Counting ties as half, this corresponds to a percentile ranking, or hand strength (HS), of 0.585. In other words there is a 58.5% chance that our hand is better than a random hand. This measure is with respect to one opponent but can be extrapolated to multiple opponents by raising it to the power of the number of active opponents. Against five opponents with random hands, the adjusted hand strength (HS<sub>5</sub>) is .585<sup>5</sup> = .069. Hence, the presence of additional opponents has reduced the likelihood of our having the best hand to only 6.9%.

In practice, hand strength alone is insufficient to assess the quality of a hand. Consider the hand 8 + 7 with a flop of 9 + 6 + 2. The probability of having the strongest hand is very low, even against one random opponent. On the other hand, there is tremendous potential for improvement. With two cards yet to come, any +, 10, or 5 will give us a straight or a flush. Hence there is a high probability that this hand will improve substantially in strength, so the hand has a lot of value. We need to be aware of the potential changes of hand strength.

In addition to this positive potential (Ppot) of pulling ahead when we are behind, enumeration can also compute the negative potential (Npot) of falling behind if we are ahead. For each of the possible 1,081 opposing hands, we consider the {45 choose 2} = 990 combinations of the next two cards. For each subcase we count how many combinations of upcoming cards result in us being ahead, behind or tied.

The potential for A◆-Q♣ / 3♥-4♣-J♥ is shown in Table 2. The table shows, for cases where we were ahead, tied or behind after five cards, what the result would be after seven cards. For example, if we did not have the best hand after five cards, then there are 91,981 combinations of cards (pre-flop and two cards to come) for the opponents that will give us the best hand. Of the remaining hands, 1,036 will leave us tied with the best hand, and 346,543 will leave us behind. In other words, if we are behind we have roughly a 21% chance of winning against one opponent.

We use these values to generate Ppot and Npot. If  $T_{\text{trow,col}}$  refers to the values in the table (for brevity we use B, T, A, and S for Behind, Tied, Ahead, and Sum) then Ppot and Npot are calculated by:

5 Cards	7 Cards						
	Ahead	Tied	Behind	Sum			
Ahead Tied	449,005	3,211	169,504	621,720	=	628 <b>x</b> 990	
Tied	0	8,370	540	8,910	=	9x990	
Behind	91,981	1,036	346,543	439,560	=	444×990	
Sum	540,986	12,617	516,587	1,070,190	=	1,081x990	

Table 2.  $A \leftarrow -Q + / 3 \lor -4 + -J \lor$  potential.

$$P_{pot} = (T_{\{B,A\}} + T_{\{B,T\}} / 2 + T_{\{T,A\}} / 2) / (T_{\{B,S\}} + T_{\{T,S\}} / 2)$$
 (1)

$$N_{pot} = (T_{\{A,B\}} + T_{\{A,T\}}/2 + T_{\{T,B\}}/2)/(T_{\{A,S\}} + T_{\{T,S\}}/2)$$
 (2)

In the example Ppot is .208 and Npot is .274. The calculation for one card look-ahead is exactly the same as the above calculation, except there are only 45 possible upcoming cards instead of 990 (or 44 if we are on the turn). With only one card to come on the turn, Ppot is .108 and Npot is .145.

By enumerating all possible card combinations, the program uses a brute-force approach to calculating hand strength and potential. The calculations are easily done in real-time and provide accurate probabilities that take into account every possible scenario. Hence the calculation gives smooth and robust results.

## 4.3 Weighting the Enumeration

So far our calculations assume that all opponent hands are equally likely. In reality, this is not the case. Many weak hands like  $4\Psi$ -J\* would have been folded before the flop. However, with the example flop of  $3\Psi$ -4\*-J\$, these hidden cards make a strong hand that skews the hand evaluations.

Accuracy of the estimates also depends strongly on models of our opponents. Ultimately, we want a different set of weights for each possible starting hand for each opponent. These weights could then be adjusted depending on the opponent's playing style. For example, raising on the flop probably indicates a strong hand that should be reflected in the weightings. We would then apply the appropriate weight for each of the 1,081 possible subcases when calculating hand strength and potential.

Although Loki treats all opponents the same, it was designed to support generalized opponent modeling. Currently the common weights are based on the simulations of the 169 different starting hand types, providing a reasonable starting template for unknown players.

### 4.4 Betting Strategy

Hand strength and potential are combined into effective hand strength (EHS):

$$EHS = HS_n + (1 - HS_n) \times P_{pot}$$
 (3)

where  $\mathrm{HS}_n$  is the adjusted hand strength for n opponents and Ppot is the positive potential. This formula means that EHS is the probability that we are ahead, and in those cases where we are behind there is a Ppot chance that we will pull ahead. Currently, EHS is compared to some thresholds to determine when to bet. For example, with an EHS greater than 0.5 we can say there is a reasonable chance we are ahead of our opponents and will bet if no other opponent has bet. This is an optimistic estimate because we only consider positive potential. Npot is not considered for two reasons. First, we do not know if our opponent will play. Second,

in many situations where we calculate a high Npot, it is often a better strategy to bet/raise to scare the opponent out of the hand.

Determining if the pot is large enough and whether we have enough equity to warrant calling a bet is different than deciding when to bet. This decision is made by comparing Ppot against the pot odds, where

$$pot\_odds = bets\_to\_us / (bets\_in\_pot + bets\_to\_us).$$
 (4)

We call when Ppot  $\geq pot\_odds$ . Note that even on the flop we use only one card look ahead for Ppot. If we examine the situation two cards in the future we must consider whether we will face another bet (or more) after the first card.  $Pot\_odds$  is based on the immediate situation. With the example hand of A + Q + / 3 - 4 + J + J + I, if there are five opponents and we are first to act, EHS is  $0.069 + (1 - 0.069) \times 0.108 = 0.17$  (assuming one-card Ppot) so we check. Assume the pot has \$125 in it. If the first opponent behind us bets \$10, two others call, and the fourth raises \$10, then it is \$20 to us and the pot is \$175. Therefore  $pot\_odds$  is 20 / (175 + 20) = 0.103, so we call (Ppot =  $0.108 \ge 0.103$ ).

## 5. Experiments

A variety of different experimental methods have been used to evaluate *Loki* during its development. These include self-play simulations, play against human opposition, and play against other computer programs. Each type of evaluation has limitations, reinforcing the need for a wide range of experiments and testing methods.

Self-play simulations offer a convenient method for the comparison of two or more versions of the program. The simulations use a duplicate tournament system, based on the same principle as duplicate bridge. Since each hand can be played with no memory of preceding hands, it is possible to re-play the same deal, but with the participants holding a different set of hole cards. Our tournament system simulates a ten-player game, where each deal is replayed ten times, shuffling the seating arrangement each time so that every participant has the opportunity to play each set of hole cards once. This arrangement greatly reduces the "luck element" of the game, since each player will have the same number of good and bad hands. The differences in the performance of players will therefore be based more strongly on the quality of the decisions made in each situation. This large reduction in natural variance means that meaningful results can be obtained with a smaller number of trials than a typical game setting.

One simple application of a self-play simulation would be to play five copies of a new version against five copies of an older version, differing only in the addition of one new feature. If the new component improves the program, then that version will win against the older one. The margin of victory, in terms of expected number of bets per hand, can also give an indication of the relative value of the new enhancement.

However, there are limitations to how much can be concluded from a single experiment, since it is representative of only one particular type of game and style of opponent. It is quite possible that the same feature will perform much worse (or much better) in a game against human opposition, for example. A wider variety of testing is

necessary to get an accurate assessment of the new feature. One approach is to change the context of the simulated game. The next self-play experiment might include a number of players who employ a different style of play, such as a more liberal selection of starting hands. If the new feature is successful over a wide variety of game types, we will have a more reliable indication of the value of that concept, with a metric to quantify its contribution.

As an example of a self-play experiment, Figure 1 shows the results of a tournament with five different versions of *Loki*. The average bankroll size (profit) is plotted against the number of hands played. Player A is the most advanced version of the program, including three major components that the most basic player does not have. Player E is a basic player, having no advanced features. The other three versions are the same as Player A, but with one of the major components removed. Player B lacks an appropriate weighting of subcases, using a uniform distribution for all possible opponent hands. Player C uses a simplistic pre-flop hand selection method, rather than the advanced system which accounts for player position and number of opponents. Player D lacks the computation of hand potential, which is used in modifying the effective hand strength and calling with proper pot odds.

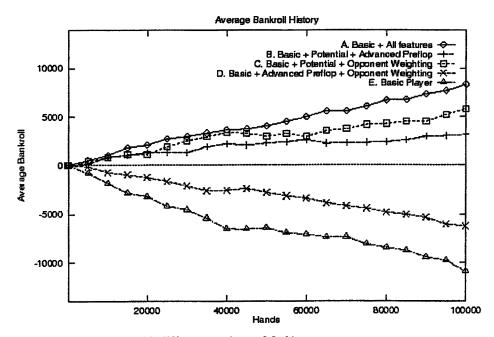


Fig. 1. A Tournament with different versions of Loki.

As expected, the complete system performs the best, while the basic system loses the most. The best program earned approximately +0.08 small bets per hand, while the worst lost at a rate of -0.11 small bets per hand.

Within the context of this particular experiment, the use of hand potential had the greatest impact on the strength of the program, since Player D, which lacked that component, performed poorly. Player B, missing the appropriate weighting of

subcases, was still able to win against this field of opponents, but did not perform nearly as well as the version having this feature. Player C, differing only in the use of the advanced pre-flop hand selection method, did not lose much compared to the other weakened versions.

Loki must also be tested in more realistic games against human opposition. For this purpose, the program participates in an on-line poker game, running on IRC (Internet Relay Chat). Human players connect to the server and participate in games. No real money is at stake, but statistics on each player are maintained. Certain games are reserved for players who have earned enough virtual dollars to qualify, and those games are usually taken more seriously than the games open to all players. This provides an environment with several games, differing in styles of play and skill level.

Early versions of *Loki* had mixed results on the IRC server, but played at about the same level as the average human participant in the open games, roughly breaking even over the course of about 12,000 hands. When it qualified for the stronger game it lost slowly, averaging about -0.05 small bets per hand dealt (2,000 hands). This is not a large enough sample size for conclusive results, but strongly suggests it was a losing player overall in these games. Recent versions of *Loki* have performed much better, averaging about +0.20 small bets per hand (3,500 hands), which is comparable to a solid human player (probably in the top 10% of IRC players).

A third form of competition was introduced against other computer programs on the IRC server. Four programs participated, using three copies of each in a 12-player game. Two programs, R00lbot and Loki, were clearly dominant over the other two, Xbot and Replicat, with the more established R00lbot winning overall. Over 10,000 hands, Loki averaged about +0.03 small bets per hand. It should be noted, however, that this competition is representative of only one type of game, where all the players are quite conservative. Replicat in particular performs much better in the open games against human opposition than in this closed experiment.

# 6. Work in Progress

Loki still suffers from some obvious problems. Most importantly, it is a predictable player that reacts the same in a given situation irrespective of any historical information. This leaves it open to exploitation by an opponent who has deduced its simplistic playing style. The two major areas requiring improvement are opponent modeling and betting strategy. Both of these topics are open-ended, and will provide interesting challenges for future work.

When Loki is better able to infer likely holdings for the opponent, it will be capable of much better decisions. The hand strength and potential calculations will use a different table of weights for each particular opponent. Now the specific actions of that opponent can be taken into consideration, as well as historical and statistical information gathered on this opponent from previous games. A wide variety of properties can be measured and applied, such as betting frequencies, known bluffs, recent trends, etc. Additionally for each opponent we will also compute statistics to measure the betting strategy and thresholds for the various betting actions.

The current betting strategy is simplistic and predictable. A better betting system would bluff with high potential hands and occasionally bet a strong hand weakly. It would also predict opponent responses in order to choose the best practical action. Unpredictability and other advanced betting strategies can be incorporated.

The infrastructure is in place to incorporate these features. Loki is changing on a daily basis. It is only six months old and already at a level that exceeds our initial expectations. We understand many of the weaknesses in the program, but do not yet know if all of them can be addressed sufficiently to produce a world-class poker player.

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