Classifing Fish

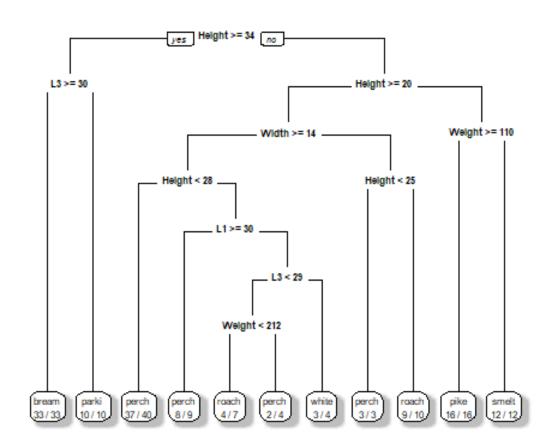
Charles

Table of Contents

Classification Tree	2
Linear Discriminant Analysis	12
Quadratic Discriminant Analysis	18
Nearest Neighbor Methods	21
Logistic Discrimination	23

Classification Tree

```
fish <- read.table("file:///C:/Users/Asus/Documents/GitHub/classifng_fi</pre>
sh/fish.data.txt", header = T)
library(rpart)
require(rpart.plot)
## Loading required package: rpart.plot
fish.control <- rpart.control(minisplit = 10, minbucket = 3, xval = 0)</pre>
fish.treeorig <- rpart(Species~Weight+L1+L2+L3+Height+Width,data=fish,m
ethod="class",control=fish.control)
#Let's now plot the tree:
plot(fish.treeorig)
text(fish.treeorig)
prp(fish.treeorig,
                  # 模型
   faclen=0,
                      # 呈現的變數不要縮寫
   fallen.leaves=TRUE, # 讓樹枝以垂直方式呈現
    shadow.col="gray", # 最下面的節點塗上陰影
   extra=2 )
                       # number of correct classifications / number of
observations in that node
```



```
#Also check out the complexity parameter (CP):
printcp(fish.treeorig)
##
## Classification tree:
## rpart(formula = Species ~ Weight + L1 + L2 + L3 + Height + Width,
##
       data = fish, method = "class", control = fish.control)
##
## Variables actually used in tree construction:
## [1] Height L1
                    L3
                            Weight Width
##
## Root node error: 94/148 = 0.63514
##
## n= 148
##
           CP nsplit rel error
## 1 0.351064
                       1.00000
                   0
## 2 0.170213
                   1
                       0.64894
## 3 0.127660
                   2
                       0.47872
## 4 0.106383
                   3
                       0.35106
## 5 0.053191
                   4
                       0.24468
## 6 0.031915
                   5
                       0.19149
## 7 0.010638
                   6
                       0.15957
## 8 0.010000
                  10
                       0.11702
summary(fish.treeorig)
## Call:
## rpart(formula = Species ~ Weight + L1 + L2 + L3 + Height + Width,
       data = fish, method = "class", control = fish.control)
##
     n = 148
##
##
             CP nsplit rel error
## 1 0.35106383
                     0 1.0000000
                     1 0.6489362
## 2 0.17021277
## 3 0.12765957
                     2 0.4787234
## 4 0.10638298
                     3 0.3510638
## 5 0.05319149
                     4 0.2446809
## 6 0.03191489
                     5 0.1914894
## 7 0.01063830
                     6 0.1595745
## 8 0.01000000
                    10 0.1170213
##
## Variable importance
## Height
              L3
                     L2
                            L1 Weight
                                       Width
##
       26
              16
                     15
                            15
                                   15
                                          13
##
## Node number 1: 148 observations,
                                       complexity param=0.3510638
     predicted class=perch expected loss=0.6351351 P(node) =1
## class counts: 33 10 54 16 18 12
```

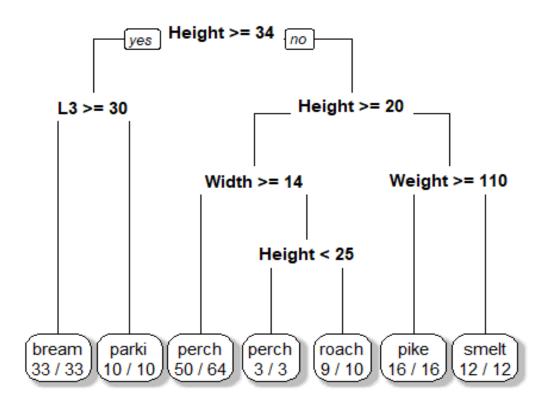
```
##
      probabilities: 0.223 0.068 0.365 0.108 0.122 0.081 0.034
##
     left son=2 (43 obs) right son=3 (105 obs)
##
     Primary splits:
##
         Height < 33.9
                         to the right, improve=29.75863, (0 missing)
         Width < 11.85 to the right, improve=17.98385, (0 missing)
##
##
                < 29.7
                         to the right, improve=13.80398, (0 missing)
         L3
##
         L2
                < 28.85
                         to the right, improve=12.96300, (0 missing)
                         to the right, improve=12.56245, (0 missing)
##
         L1
                < 26.1
##
## Node number 2: 43 observations,
                                      complexity param=0.106383
     predicted class=bream expected loss=0.2325581
##
                                                      P(node) =0.2905405
##
       class counts:
                                     0
                                           0
                        33
                              10
                                                        0
      probabilities: 0.767 0.233 0.000 0.000 0.000 0.000 0.000
##
##
     left son=4 (33 obs) right son=5 (10 obs)
##
     Primary splits:
##
         L3
                < 29.5
                         to the right, improve=15.348840, (0 missing)
                         to the right, improve=13.530660, (0 missing)
##
         L2
                < 26.15
##
                         to the right, improve=13.407660, (0 missing)
         L1
                < 23.1
                         to the right, improve=12.015500, (0 missing)
##
         Weight < 331.5
##
         Width < 14.85
                         to the right, improve= 1.063123, (0 missing)
##
     Surrogate splits:
##
                         to the right, agree=0.977, adj=0.9, (0 split)
         L1
                < 23.1
##
                < 25.2
                         to the right, agree=0.977, adj=0.9, (0 split)
         L2
##
         Weight < 221
                         to the right, agree=0.953, adj=0.8, (0 split)
##
## Node number 3: 105 observations,
                                       complexity param=0.1702128
     predicted class=perch expected loss=0.4857143 P(node) =0.7094595
##
##
                         0
                                    54
                                                       12
                                                              5
       class counts:
                               0
                                          16
                                                 18
##
      probabilities: 0.000 0.000 0.514 0.152 0.171 0.114 0.048
##
     left son=6 (77 obs) right son=7 (28 obs)
##
     Primary splits:
##
         Height < 20.1
                         to the right, improve=21.78355, (0 missing)
##
         Width < 12.45
                         to the right, improve=20.93000, (0 missing)
##
         Weight < 25.95 to the right, improve=13.35778, (0 missing)
                         to the right, improve=10.68888, (0 missing)
##
         L3
                < 15.6
##
                         to the right, improve=10.63876, (0 missing)
         L1
                < 12.3
##
     Surrogate splits:
##
         Width < 12.45 to the right, agree=0.990, adj=0.964, (0 split)
##
         Weight < 25.95 to the right, agree=0.838, adj=0.393, (0 split)
##
                < 12.3
                         to the right, agree=0.819, adj=0.321, (0 split)
         L1
                         to the right, agree=0.819, adj=0.321, (0 split)
##
         L2
                < 13.35
##
         L3
                < 14.25
                         to the right, agree=0.819, adj=0.321, (0 split)
##
## Node number 4: 33 observations
     predicted class=bream expected loss=0 P(node) =0.222973
##
##
       class counts:
                        33
                               0
                                     0
                                           0
                                                  0
                                                        0
##
      probabilities: 1.000 0.000 0.000 0.000 0.000 0.000 0.000
##
## Node number 5: 10 observations
     predicted class=parki expected loss=0 P(node) =0.06756757
```

```
##
       class counts: 0 10 0 0 0
##
      probabilities: 0.000 1.000 0.000 0.000 0.000 0.000 0.000
##
## Node number 6: 77 observations,
                                     complexity param=0.05319149
     predicted class=perch expected loss=0.2987013 P(node) =0.5202703
##
##
       class counts:
                                    54
                         0
                               0
                                           0
                                                18
##
      probabilities: 0.000 0.000 0.701 0.000 0.234 0.000 0.065
##
     left son=12 (64 obs) right son=13 (13 obs)
##
     Primary splits:
##
        Width < 14.4
                         to the right, improve=5.777691, (0 missing)
##
        Height < 25.25
                        to the left, improve=4.275974, (0 missing)
                         to the right, improve=2.872913, (0 missing)
##
               < 25.1
##
                < 27.15 to the right, improve=2.872913, (0 missing)
         L2
##
         Weight < 548
                         to the right, improve=2.448383, (0 missing)
##
     Surrogate splits:
##
         L1 < 13.35 to the right, agree=0.844, adj=0.077, (0 split)
##
         L2 < 14.55 to the right, agree=0.844, adj=0.077, (0 split)
##
## Node number 7: 28 observations,
                                      complexity param=0.1276596
##
     predicted class=pike
                            expected loss=0.4285714 P(node) =0.1891892
                                          16
##
       class counts:
                               0
                                     0
                                                      12
##
      probabilities: 0.000 0.000 0.000 0.571 0.000 0.429 0.000
##
     left son=14 (16 obs) right son=15 (12 obs)
##
     Primary splits:
##
        Weight < 109.95 to the right, improve=13.714290, (0 missing)
                        to the right, improve=13.714290, (0 missing)
##
         L1
                < 21.9
##
         L2
                < 23.65 to the right, improve=13.714290, (0 missing)
##
         L3
                < 25.5
                         to the right, improve=13.714290, (0 missing)
##
        Height < 16.05 to the left, improve= 4.571429, (0 missing)
##
     Surrogate splits:
##
         L1
                < 21.9
                         to the right, agree=1.000, adj=1.000, (0 split)
##
         L2
                < 23.65
                        to the right, agree=1.000, adj=1.000, (0 split)
                         to the right, agree=1.000, adj=1.000, (0 split)
##
                < 25.5
##
                         to the left, agree=0.786, adj=0.500, (0 split)
         Height < 16.05
##
        Width < 9.45
                         to the right, agree=0.714, adj=0.333, (0 split)
##
## Node number 12: 64 observations,
                                       complexity param=0.0106383
##
     predicted class=perch expected loss=0.21875 P(node) =0.4324324
##
       class counts:
                               0
                                    50
                                           0
##
      probabilities: 0.000 0.000 0.781 0.000 0.141 0.000 0.078
     left son=24 (40 obs) right son=25 (24 obs)
##
##
     Primary splits:
##
                        to the left, improve=3.314583, (0 missing)
        Height < 27.55
                        to the right, improve=1.557526, (0 missing)
##
        Width < 15.65
##
         L1
                < 30
                         to the right, improve=1.174970, (0 missing)
##
         L2
                < 32.25 to the right, improve=1.174970, (0 missing)
##
         Weight < 548
                         to the right, improve=1.058472, (0 missing)
##
     Surrogate splits:
##
         Width < 17.4
                         to the left, agree=0.719, adj=0.250, (0 split)
##
        Weight < 267.5 to the left, agree=0.688, adj=0.167, (0 split)
```

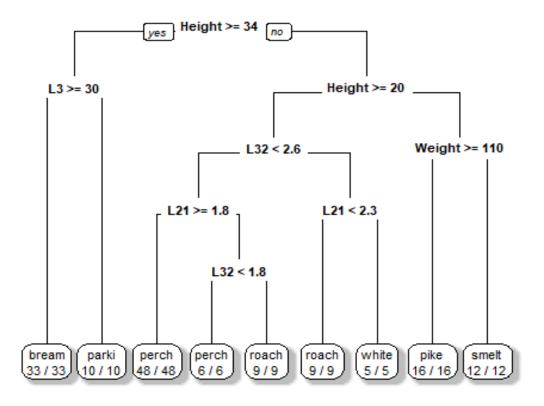
```
##
                < 29.05 to the left, agree=0.656, adj=0.083, (0 split)</pre>
##
## Node number 13: 13 observations,
                                       complexity param=0.03191489
     predicted class=roach expected loss=0.3076923 P(node) =0.0878378
4
##
       class counts:
                         0
                               0
                                     4
                                           0
##
      probabilities: 0.000 0.000 0.308 0.000 0.692 0.000 0.000
##
     left son=26 (3 obs) right son=27 (10 obs)
##
     Primary splits:
##
         Height < 24.8
                         to the left, improve=3.7384620, (0 missing)
##
         Weight < 174.5 to the right, improve=1.0051280, (0 missing)
##
                < 22.5
                         to the right, improve=1.0051280, (0 missing)
                         to the right, improve=1.0051280, (0 missing)
##
         L2
                < 24.5
##
         L3
                < 21.1
                         to the left, improve=0.4273504, (0 missing)
##
## Node number 14: 16 observations
     predicted class=pike
                            expected loss=0 P(node) =0.1081081
##
       class counts:
                         0
                               0
                                     0
                                          16
                                                 0
##
      probabilities: 0.000 0.000 0.000 1.000 0.000 0.000 0.000
##
## Node number 15: 12 observations
     predicted class=smelt expected loss=0 P(node) =0.08108108
##
##
       class counts:
                         0
                               0
                                     0
                                           0
                                                       12
##
      probabilities: 0.000 0.000 0.000 0.000 1.000 0.000
##
## Node number 24: 40 observations
     predicted class=perch expected loss=0.075 P(node) =0.2702703
##
##
                                    37
                                                  3
                                                        0
       class counts:
                         0
                               0
                                           0
                                                              0
##
      probabilities: 0.000 0.000 0.925 0.000 0.075 0.000 0.000
##
## Node number 25: 24 observations,
                                       complexity param=0.0106383
     predicted class=perch expected loss=0.4583333 P(node) =0.1621622
##
       class counts:
                         0
                               0
                                    13
                                           0
                                                 6
                                                        0
##
      probabilities: 0.000 0.000 0.542 0.000 0.250 0.000 0.208
##
     left son=50 (9 obs) right son=51 (15 obs)
##
     Primary splits:
##
         L1
                < 29.5
                         to the right, improve=2.772222, (0 missing)
##
         L2
                < 31.9
                         to the right, improve=2.772222, (0 missing)
##
         Width < 16.45 to the right, improve=2.772222, (0 missing)
##
         Weight < 295
                         to the right, improve=2.583333, (0 missing)
                         to the right, improve=2.216667, (0 missing)
##
         L3
                < 32.4
##
     Surrogate splits:
##
                < 31.9
         L2
                         to the right, agree=1.000, adj=1.000, (0 split)
                         to the right, agree=0.958, adj=0.889, (0 split)
##
         Weight < 410
##
                         to the right, agree=0.958, adj=0.889, (0 split)
         L3
                < 32.4
##
         Width < 16.45
                         to the right, agree=0.833, adj=0.556, (0 split)
##
         Height < 29.35
                         to the right, agree=0.667, adj=0.111, (0 split)
##
## Node number 26: 3 observations
     predicted class=perch expected loss=0 P(node) =0.02027027
```

```
##
       class counts: 0 0 3 0 0
##
      probabilities: 0.000 0.000 1.000 0.000 0.000 0.000 0.000
##
## Node number 27: 10 observations
     predicted class=roach expected loss=0.1 P(node) =0.06756757
##
##
       class counts:
                        0
                              0
                                     1
                                           0
##
      probabilities: 0.000 0.000 0.100 0.000 0.900 0.000 0.000
##
## Node number 50: 9 observations
##
     predicted class=perch expected loss=0.1111111 P(node) =0.0608108
1
##
      class counts:
                                     8
                                                 0
                                                             1
      probabilities: 0.000 0.000 0.889 0.000 0.000 0.000 0.111
##
##
## Node number 51: 15 observations,
                                       complexity param=0.0106383
     predicted class=roach expected loss=0.6 P(node) =0.1013514
##
##
       class counts:
                               0
                                     5
                                           0
                                                 6
      probabilities: 0.000 0.000 0.333 0.000 0.400 0.000 0.267
##
     left son=102 (11 obs) right son=103 (4 obs)
##
##
     Primary splits:
##
         L3
                < 29.25 to the left,
                                       improve=2.003030, (0 missing)
##
                                       improve=1.866667, (0 missing)
        Weight < 247.5 to the left,
##
               < 22.85 to the left,
                                       improve=1.866667, (0 missing)
         L1
##
         L2
                < 25
                        to the left,
                                       improve=1.866667, (0 missing)
##
         Height < 28.45 to the left,
                                       improve=1.088889, (0 missing)
##
     Surrogate splits:
##
               < 24.05 to the left,
                                      agree=0.933, adj=0.75, (0 split)
         L1
         L2
##
                < 26.25 to the left,
                                       agree=0.933, adj=0.75, (0 split)
##
        Weight < 303
                        to the left,
                                      agree=0.867, adj=0.50, (0 split)
##
## Node number 102: 11 observations,
                                       complexity param=0.0106383
     predicted class=perch expected loss=0.5454545 P(node) =0.0743243
2
##
       class counts:
##
      probabilities: 0.000 0.000 0.455 0.000 0.455 0.000 0.091
##
     left son=204 (7 obs) right son=205 (4 obs)
##
     Primary splits:
##
        Weight < 212.5 to the left,
                                      improve=0.4350649, (0 missing)
##
                < 22.05 to the left,
                                       improve=0.4350649, (0 missing)
         L1
##
         L2
                < 23.75 to the left,
                                       improve=0.4350649, (0 missing)
                                       improve=0.4350649, (0 missing)
##
                < 26.15 to the left,
         Height < 28.5
##
                        to the left,
                                       improve=0.4350649, (0 missing)
##
     Surrogate splits:
##
               < 23.75 to the left,
                                      agree=1.000, adj=1.00, (0 split)
         L2
##
        Height < 28.5
                        to the left,
                                      agree=1.000, adj=1.00, (0 split)
##
         L1
               < 21.25 to the left,
                                       agree=0.909, adj=0.75, (0 split)
##
         L3
                < 25.4
                        to the left,
                                       agree=0.909, adj=0.75, (0 split)
         Width < 14.95 to the right, agree=0.727, adj=0.25, (0 split)
##
##
## Node number 103: 4 observations
```

```
predicted class=white expected loss=0.25 P(node) =0.02702703
##
                                 0
                                      0
      class counts: 0
                           0
                                          1
                                                 0
                                                      3
     probabilities: 0.000 0.000 0.000 0.000 0.250 0.000 0.750
##
##
## Node number 204: 7 observations
    predicted class=roach expected loss=0.4285714 P(node) =0.0472973
##
##
      class counts: 0 0 3
                                      0 4
                                                 0
     probabilities: 0.000 0.000 0.429 0.000 0.571 0.000 0.000
##
##
## Node number 205: 4 observations
    predicted class=perch expected loss=0.5 P(node) =0.02702703
##
##
      class counts: 0 0
                                2
                                      0
                                          1
                                                 0
     probabilities: 0.000 0.000 0.500 0.000 0.250 0.000 0.250
##
fish.prunetree <- prune.rpart(fish.treeorig,cp=0.02)</pre>
plot(fish.prunetree)
text(fish.prunetree)
prp(fish.prunetree, # 模型
   faclen=0, # 呈現的變數不要縮寫
   fallen.leaves=TRUE, # 讓樹枝以垂直方式呈現
   shadow.col="gray", #最下面的節點塗上陰影
   extra=2 ) # number of correct classifications / number of
observations in that node
```



```
L21<-fish$L2-fish$L1
L32<-fish$L3-fish$L2
L31<-fish$L3-fish$L1
newfish<-cbind(fish,L21,L32,L31)</pre>
newfish.treenew<-rpart(Species~., data=newfish,method="class",parms=lis</pre>
t(split="information"),control=fish.control)
printcp(newfish.treenew)
##
## Classification tree:
## rpart(formula = Species ~ ., data = newfish, method = "class",
##
      parms = list(split = "information"), control = fish.control)
## Variables actually used in tree construction:
## [1] Height L21
                 L3
                          L32
                                 Weight
##
## Root node error: 94/148 = 0.63514
##
## n= 148
##
##
          CP nsplit rel error
## 1 0.351064 0 1.000000
                 1 0.648936
## 2 0.170213
## 3 0.127660
                2 0.478723
                3 0.351064
## 4 0.106383
                4 0.244681
## 5 0.095745
                5 0.148936
## 6 0.053191
## 7 0.047872
                 6 0.095745
             8 0.000000
## 8 0.010000
plot(newfish.treenew)
text(newfish.treenew)
prp(newfish.treenew, # 模型
   faclen=0, # 呈現的變數不要縮寫
   fallen.leaves=TRUE, # 讓樹枝以垂直方式呈現
   shadow.col="gray", #最下面的節點塗上陰影
   extra=2 )
                      # number of correct classifications / number of
 observations in that node
```



```
#分的有點完美(有點過度配適)
fish.control <- rpart.control(minbucket=3,minsplit=10,xval=148)</pre>
newfish.treenewcv <- rpart(Species~., data=newfish,method="class",parms</pre>
=list(split="information"),control=fish.control)
printcp(newfish.treenewcv)
##
## Classification tree:
## rpart(formula = Species ~ ., data = newfish, method = "class",
##
       parms = list(split = "information"), control = fish.control)
##
## Variables actually used in tree construction:
## [1] Height L21
                  L3
                          L32
                                  Weight
##
## Root node error: 94/148 = 0.63514
##
## n= 148
##
##
          CP nsplit rel error
                                xerror
                                           xstd
## 1 0.351064
                  0 1.000000 1.000000 0.062302
                  1 0.648936 0.648936 0.063704
## 2 0.170213
                  2 0.478723 0.478723 0.059534
## 3 0.127660
                  3 0.351064 0.351064 0.053870
## 4 0.106383
## 5 0.095745 4 0.244681 0.361702 0.054442
```

```
5 0.148936 0.170213 0.040187
## 6 0.053191
                    6 0.095745 0.180851 0.041267
## 7 0.047872
## 8 0.010000
                   8 0.000000 0.031915 0.018238
newfish.test<-read.table("file:///C:/Users/Asus/Documents/GitHub/classi</pre>
fng_fish/fish_test.data.txt",h=T)
L31<-newfish.test$L3- newfish.test$L1
L32<-newfish.test$L3- newfish.test$L2
L21<-newfish.test$L2- newfish.test$L1
newfish.test<-cbind(newfish.test,L21,L32,L31)</pre>
newfish.tpred<-predict(newfish.treenewcv,newfish.test)</pre>
newfish.tpred
      bream parki perch pike roach smelt white
##
## 1
                0
                                  0
                                         0
          1
                       0
                            0
## 2
          1
                                  0
                                         0
                                               0
                0
                       0
                            0
## 3
          0
                0
                       1
                                  0
                                         0
                                               0
                            0
                                         0
## 4
          0
                0
                       1
                            0
                                  0
                                               0
          0
                0
                       0
                            1
                                  0
                                         0
                                               0
## 5
## 6
          0
                0
                       0
                            0
                                  0
                                         1
                                               0
## 7
          0
                0
                       0
                            0
                                  0
                                         1
                                               0
## 8
                1
                       0
                            0
                                  0
                                         0
                                               0
          0
## 9
          0
                0
                       0
                            0
                                  1
                                         0
                                               0
                0
                                  1
## 10
          0
                       0
                            0
                                         0
                                               0
          0
                0
                       0
                            0
                                  0
                                         0
                                               1
## 11
```

Linear Discriminant Analysis

library(MASS)

```
newfish
```

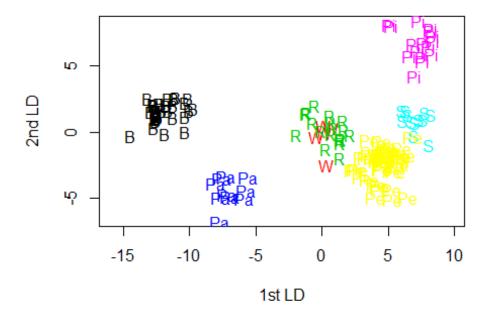
```
##
                              L2
                                   L3 Height Width L21 L32 L31
       Species Weight
                         L1
## 1
         bream
                242.0 23.2 25.4 30.0
                                         38.4
                                               13.4 2.2 4.6 6.8
## 2
                290.0 24.0 26.3 31.2
                                         40.0
                                               13.8 2.3 4.9 7.2
         bream
## 3
         bream
                363.0 26.3 29.0 33.5
                                         38.0
                                               13.3 2.7 4.5 7.2
## 4
         bream
                430.0 26.5 29.0 34.0
                                               15.1 2.5 5.0 7.5
                                         36.6
## 5
         bream
                500.0 26.8 29.7 34.5
                                         41.1
                                               15.3 2.9 4.8 7.7
## 6
         bream
                390.0 27.6 30.0 35.0
                                         36.2
                                               13.4 2.4 5.0 7.4
## 7
         bream
                450.0 27.6 30.0 35.1
                                         39.9
                                               13.8 2.4 5.1 7.5
## 8
                500.0 28.5 30.7 36.2
                                         39.3
                                               13.7 2.2 5.5 7.7
         bream
## 9
         bream
                475.0 28.4 31.0 36.2
                                         39.4
                                               14.1 2.6 5.2 7.8
## 10
         bream
                500.0 28.7 31.0 36.2
                                         39.7
                                               13.3 2.3 5.2 7.5
## 11
         bream
                500.0 29.1 31.5 36.4
                                         37.8
                                               12.0 2.4 4.9 7.3
## 12
         bream
                500.0 29.5 32.0 37.3
                                         37.3
                                               13.6 2.5 5.3 7.8
## 13
         bream
                600.0 29.4 32.0 37.2
                                         40.2
                                               13.9 2.6 5.2 7.8
## 14
         bream
                600.0 29.4 32.0 37.2
                                         41.5
                                               15.0 2.6 5.2 7.8
## 15
                700.0 30.4 33.0 38.3
                                         38.8
                                               13.8 2.6 5.3 7.9
         bream
## 16
         bream
                700.0 30.4 33.0 38.5
                                         38.8
                                               13.5 2.6 5.5 8.1
## 17
                610.0 30.9 33.5 38.6
                                        40.5
                                               13.3 2.6 5.1 7.7
         bream
                                               14.8 2.5 5.2 7.7
## 18
         bream
                650.0 31.0 33.5 38.7
                                         37.4
## 19
         bream
                575.0 31.3 34.0 39.5
                                         38.3
                                               14.1 2.7 5.5 8.2
## 20
                                               13.7 2.6 5.2 7.8
         bream
                685.0 31.4 34.0 39.2
                                         40.8
## 21
         bream
                620.0 31.5 34.5 39.7
                                         39.1
                                               13.3 3.0 5.2 8.2
## 22
         bream
                680.0 31.8 35.0 40.6
                                         38.1
                                               15.1 3.2 5.6 8.8
## 23
                700.0 31.9 35.0 40.5
                                         40.1
                                               13.8 3.1 5.5 8.6
         bream
## 24
                725.0 31.8 35.0 40.9
                                         40.0
                                               14.8 3.2 5.9 9.1
         bream
## 25
                720.0 32.0 35.0 40.6
                                         40.3
                                               15.0 3.0 5.6 8.6
         bream
## 26
         bream
                714.0 32.7 36.0 41.5
                                         39.8
                                               14.1 3.3 5.5 8.8
## 27
         bream
                850.0 32.8 36.0 41.6
                                         40.6
                                               14.9 3.2 5.6 8.8
## 28
         bream 1000.0 33.5 37.0 42.6
                                         44.5
                                               15.5 3.5 5.6 9.1
                920.0 35.0 38.5 44.1
## 29
                                               14.3 3.5 5.6 9.1
         bream
                                        40.9
## 30
         bream
                955.0 35.0 38.5 44.0
                                         41.1
                                               14.3 3.5 5.5 9.0
## 31
                925.0 36.2 39.5 45.3
                                               14.9 3.3 5.8 9.1
         bream
                                         41.4
## 32
                975.0 37.4 41.0 45.9
                                         40.6
                                               14.7 3.6 4.9 8.5
         bream
## 33
                                         37.9
         bream
                950.0 38.0 41.0 46.5
                                               13.7 3.0 5.5 8.5
## 34
         white
                270.0 23.6 26.0 28.7
                                         29.2
                                               14.8 2.4 2.7 5.1
## 35
         white
                270.0 24.1 26.5 29.3
                                         27.8
                                               14.5 2.4 2.8 5.2
## 36
         white
                306.0 25.6 28.0 30.8
                                         28.5
                                               15.2 2.4 2.8 5.2
## 37
         white
                540.0 28.5 31.0 34.0
                                         31.6
                                               19.3 2.5 3.0 5.5
## 38
         white 1000.0 37.3 40.0 43.5
                                         28.4
                                               15.0 2.7 3.5 6.2
## 39
         roach
                 40.0 12.9 14.1 16.2
                                         25.6
                                               14.0 1.2 2.1 3.3
## 40
         roach
                 69.0 16.5 18.2 20.3
                                         26.1
                                               13.9 1.7 2.1 3.8
## 41
         roach
                 78.0 17.5 18.8 21.2
                                         26.3
                                               13.7 1.3 2.4 3.7
## 42
         roach
                 87.0 18.2 19.8 22.2
                                         25.3
                                               14.3 1.6 2.4 4.0
## 43
                120.0 18.6 20.0 22.2
                                         28.0
         roach
                                               16.1 1.4 2.2 3.6
## 44
         roach
                118.0 19.0 20.5 22.8
                                         28.4
                                               14.7 1.5 2.3 3.8
## 45
         roach 110.0 19.1 20.8 23.1
                                         26.7
                                               14.7 1.7 2.3 4.0
```

```
## 46
         roach
                120.0 19.4 21.0 23.7
                                         25.8
                                               13.9 1.6 2.7 4.3
## 47
                160.0 20.5 22.5 25.3
                                               15.1 2.0 2.8 4.8
         roach
                                         27.8
## 48
         roach
                140.0 21.0 22.5 25.0
                                         26.2
                                               13.3 1.5 2.5 4.0
## 49
                160.0 21.1 22.5 25.0
                                        25.6
                                               15.2 1.4 2.5 3.9
         roach
## 50
         roach
                169.0 22.0 24.0 27.2
                                         27.7
                                               14.1 2.0 3.2 5.2
## 51
                161.0 22.0 23.4 26.7
                                         25.9
                                               13.6 1.4 3.3 4.7
         roach
## 52
                200.0 22.1 23.5 26.8
                                         27.6
                                               15.4 1.4 3.3 4.7
         roach
                180.0 23.6 25.2 27.9
                                               14.0 1.6 2.7 4.3
## 53
         roach
                                         25.4
## 54
                290.0 24.0 26.0 29.2
                                         30.4
                                               15.4 2.0 3.2 5.2
         roach
## 55
         roach
                272.0 25.0 27.0 30.6
                                         28.0
                                               15.6 2.0 3.6 5.6
                390.0 29.5 31.7 35.0
## 56
         roach
                                         27.1
                                               15.3 2.2 3.3 5.5
## 57
                 55.0 13.5 14.7 16.5
                                        41.5
                                               14.1 1.2 1.8 3.0
         parki
## 58
         parki
                 60.0 14.3 15.5 17.4
                                         37.8
                                               13.3 1.2 1.9 3.1
## 59
         parki
                 90.0 16.3 17.7 19.8
                                         37.4
                                               13.5 1.4 2.1 3.5
## 60
         parki
                120.0 17.5 19.0 21.3
                                         39.4
                                               13.7 1.5 2.3 3.8
## 61
         parki
                150.0 18.4 20.0 22.4
                                         39.7
                                               14.7 1.6 2.4 4.0
## 62
         parki
                140.0 19.0 20.7 23.2
                                         36.8
                                               14.2 1.7 2.5 4.2
## 63
         parki
                170.0 19.0 20.7 23.2
                                         40.5
                                               14.7 1.7 2.5 4.2
                                        40.1
                                               14.2 1.8 2.8 4.6
## 64
         parki
                200.0 21.2 23.0 25.8
## 65
         parki
                273.0 23.0 25.0 28.0
                                         39.6
                                               14.8 2.0 3.0 5.0
## 66
                300.0 24.0 26.0 29.0
                                         39.2
                                               14.6 2.0 3.0 5.0
         parki
## 67
         smelt
                  6.7
                      9.3 9.8 10.8
                                         16.1
                                                9.7 0.5 1.0 1.5
## 68
                  7.5 10.0 10.5 11.6
                                               10.0 0.5 1.1 1.6
         smelt
                                        17.0
## 69
         smelt
                  7.0 10.1 10.6 11.6
                                         14.9
                                                9.9 0.5 1.0 1.5
## 70
                                               11.5 0.6 1.0 1.6
         smelt
                  9.7 10.4 11.0 12.0
                                         18.3
## 71
         smelt
                 10.0 11.3 11.8 13.1
                                         16.9
                                                9.8 0.5 1.3 1.8
                  9.9 11.3 11.8 13.1
## 72
                                                8.9 0.5 1.3 1.8
         smelt
                                         16.9
## 73
                  9.8 11.4 12.0 13.2
                                                8.7 0.6 1.2 1.8
         smelt
                                        16.7
## 74
         smelt
                 12.2 11.5 12.2 13.4
                                         15.6
                                               10.4 0.7 1.2 1.9
## 75
         smelt
                 13.4 11.7 12.4 13.5
                                         18.0
                                                9.4 0.7 1.1 1.8
## 76
         smelt
                 12.2 12.1 13.0 13.8
                                        16.5
                                                9.1 0.9 0.8 1.7
## 77
         smelt
                 19.7 13.2 14.3 15.2
                                        18.9
                                               13.6 1.1 0.9 2.0
## 78
         smelt
                 19.9 13.8 15.0 16.2
                                        18.1
                                               11.6 1.2 1.2 2.4
## 79
          pike
                200.0 30.0 32.3 34.8
                                         16.0
                                                9.7 2.3 2.5 4.8
                300.0 31.7 34.0 37.8
                                               11.0 2.3 3.8 6.1
## 80
          pike
                                         15.1
                                               11.3 2.3 3.8 6.1
## 81
          pike
                300.0 32.7 35.0 38.8
                                        15.3
## 82
          pike
                300.0 34.8 37.3 39.8
                                        15.8
                                               10.1 2.5 2.5 5.0
## 83
          pike
                430.0 35.5 38.0 40.5
                                         18.0
                                               11.3 2.5 2.5 5.0
                456.0 40.0 42.5 45.5
                                                9.5 2.5 3.0 5.5
## 84
          pike
                                         16.0
## 85
          pike
                510.0 40.0 42.5 45.5
                                         15.0
                                                9.8 2.5 3.0 5.5
                                               11.2 2.9 2.8 5.7
## 86
          pike
                540.0 40.1 43.0 45.8
                                         17.0
## 87
          pike
                500.0 42.0 45.0 48.0
                                         14.5
                                               10.2 3.0 3.0 6.0
                                               10.0 2.8 2.7 5.5
## 88
          pike
                567.0 43.2 46.0 48.7
                                         16.0
                770.0 44.8 48.0 51.2
                                         15.0
                                               10.5 3.2 3.2 6.4
## 89
          pike
## 90
               950.0 48.3 51.7 55.1
                                               11.2 3.4 3.4 6.8
          pike
                                        16.2
## 91
          pike 1250.0 52.0 56.0 59.7
                                        17.9
                                               11.7 4.0 3.7 7.7
## 92
          pike 1600.0 56.0 60.0 64.0
                                         15.0
                                                9.6 4.0 4.0 8.0
                                                9.6 4.0 4.0 8.0
## 93
          pike 1550.0 56.0 60.0 64.0
                                         15.0
## 94
          pike 1650.0 59.0 63.4 68.0
                                        15.9
                                               11.0 4.4 4.6 9.0
## 95
         perch 5.9 7.5 8.4 8.8
                                        24.0 16.0 0.9 0.4 1.3
```

```
## 96
         perch
                 32.0 12.5 13.7 14.7
                                        24.0
                                               13.6 1.2 1.0 2.2
## 97
                                        23.9
                                               15.2 1.2 1.0 2.2
         perch
                 40.0 13.8 15.0 16.0
                                               15.3 1.2 1.0 2.2
## 98
         perch
                 51.5 15.0 16.2 17.2
                                        26.7
## 99
                 70.0 15.7 17.4 18.5
                                        24.8
                                               15.9 1.7 1.1 2.8
         perch
## 100
         perch
                100.0 16.2 18.0 19.2
                                        27.2
                                               17.3 1.8 1.2 3.0
## 101
                 78.0 16.8 18.7 19.4
                                               16.1 1.9 0.7 2.6
         perch
                                        26.8
## 102
                 80.0 17.2 19.0 20.2
                                        27.9
                                               15.1 1.8 1.2 3.0
         perch
## 103
                                        24.7
         perch
                 85.0 17.8 19.6 20.8
                                               14.6 1.8 1.2 3.0
## 104
                 85.0 18.2 20.0 21.0
                                        24.2
                                               13.2 1.8 1.0 2.8
         perch
## 105
         perch
                110.0 19.0 21.0 22.5
                                        25.3
                                               15.8 2.0 1.5 3.5
                                               14.7 2.0 1.5 3.5
## 106
         perch
                115.0 19.0 21.0 22.5
                                        26.3
## 107
                125.0 19.0 21.0 22.5
                                        25.3
                                               16.3 2.0 1.5 3.5
         perch
## 108
         perch
                130.0 19.3 21.3 22.8
                                        28.0
                                               15.5 2.0 1.5 3.5
## 109
         perch
                120.0 20.0 22.0 23.5
                                        26.0
                                               14.5 2.0 1.5 3.5
## 110
                120.0 20.0 22.0 23.5
                                        24.0
                                               15.0 2.0 1.5 3.5
         perch
## 111
         perch
                130.0 20.0 22.0 23.5
                                        26.0
                                               15.0 2.0 1.5 3.5
## 112
         perch
                135.0 20.0 22.0 23.5
                                        25.0
                                               15.0 2.0 1.5 3.5
## 113
                110.0 20.0 22.0 23.5
                                        23.5
                                               17.0 2.0 1.5 3.5
         perch
                                        24.4
## 114
         perch
                130.0 20.5 22.5 24.0
                                               15.1 2.0 1.5 3.5
## 115
         perch
                150.0 20.5 22.5 24.0
                                        28.3
                                               15.1 2.0 1.5 3.5
## 116
                145.0 20.7 22.7 24.2
                                        24.6
                                               15.0 2.0 1.5 3.5
         perch
                                               14.8 2.0 1.5 3.5
## 117
         perch
                150.0 21.0 23.0 24.5
                                        21.3
## 118
                170.0 21.5 23.5 25.0
                                        25.1
                                               14.9 2.0 1.5 3.5
         perch
## 119
         perch
                225.0 22.0 24.0 25.5
                                        28.6
                                               14.6 2.0 1.5 3.5
                                        25.0
## 120
                                               15.0 2.0 1.5 3.5
         perch
                145.0 22.0 24.0 25.5
## 121
         perch
                188.0 22.6 24.6 26.2
                                        25.7
                                               15.9 2.0 1.6 3.6
## 122
                180.0 23.0 25.0 26.5
                                        24.3
                                               13.9 2.0 1.5 3.5
         perch
## 123
                197.0 23.5 25.6 27.0
                                        24.3
                                               15.7 2.1 1.4 3.5
         perch
## 124
                218.0 25.0 26.5 28.0
                                        25.6
                                               14.8 1.5 1.5 3.0
         perch
## 125
         perch
                300.0 25.2 27.3 28.7
                                        29.0
                                               17.9 2.1 1.4 3.5
## 126
                260.0 25.4 27.5 28.9
                                        24.8
                                               15.0 2.1 1.4 3.5
         perch
## 127
                265.0 25.4 27.5 28.9
                                        24.4
                                               15.0 2.1 1.4 3.5
         perch
## 128
         perch
                250.0 25.4 27.5 28.9
                                        25.2
                                               15.8 2.1 1.4 3.5
## 129
                250.0 25.9 28.0 29.4
                                        26.6
                                               14.3 2.1 1.4 3.5
         perch
## 130
         perch
                300.0 26.9 28.7 30.1
                                        25.2
                                               15.4 1.8 1.4 3.2
## 131
                                        24.1
         perch
                320.0 27.8 30.0 31.6
                                               15.1 2.2 1.6 3.8
## 132
                514.0 30.5 32.8 34.0
                                        29.5
                                               17.7 2.3 1.2 3.5
         perch
## 133
         perch
                556.0 32.0 34.5 36.5
                                        28.1
                                               17.5 2.5 2.0 4.5
## 134
                840.0 32.5 35.0 37.3
                                               20.9 2.5 2.3 4.8
         perch
                                        30.8
## 135
                685.0 34.0 36.5 39.0
                                        27.9
                                               17.6 2.5 2.5 5.0
         perch
## 136
         perch
                700.0 34.0 36.0 38.3
                                        27.7
                                               17.6 2.0 2.3 4.3
                                               15.9 2.5 2.4 4.9
## 137
         perch
                700.0 34.5 37.0 39.4
                                        27.5
## 138
                                               16.2 2.4 2.3 4.7
         perch
                690.0 34.6 37.0 39.3
                                        26.9
## 139
                900.0 36.5 39.0 41.4
                                        26.9
                                               18.1 2.5 2.4 4.9
         perch
## 140
         perch 650.0 36.5 39.0 41.4
                                        26.9
                                               14.5 2.5 2.4 4.9
## 141
         perch
                820.0 36.6 39.0 41.3
                                        30.1
                                               17.8 2.4 2.3 4.7
## 142
         perch 850.0 36.9 40.0 42.3
                                        28.2
                                               16.8 3.1 2.3 5.4
## 143
         perch 820.0 37.1 40.0 42.5
                                        26.2
                                               15.6 2.9 2.5 5.4
## 144
         perch 1100.0 39.0 42.0 44.6
                                        28.7
                                               15.4 3.0 2.6 5.6
## 145
         perch 1000.0 39.8 43.0 45.2
                                        26.4 16.1 3.2 2.2 5.4
```

```
## 146
        perch 1100.0 40.1 43.0 45.5
                                     27.5 16.3 2.9 2.5 5.4
## 147
        perch 1000.0 40.2 43.5 46.0
                                     27.4 17.7 3.3 2.5 5.8
                                     26.8 16.3 2.9 2.6 5.5
## 148
        perch 1000.0 41.1 44.0 46.6
newfish.lda<-lda(Species~.,data=newfish)</pre>
## Warning in lda.default(x, grouping, ...): variables are collinear
newfish.lda<-lda(Species~Weight+L1+Height+Width+L21+L32,data=newfish)</pre>
newfish.lda
## Call:
## lda(Species ~ Weight + L1 + Height + Width + L21 + L32, data = newfi
sh)
##
## Prior probabilities of groups:
       bream
                  parki
                            perch
                                        pike
                                                  roach
## 0.22297297 0.06756757 0.36486486 0.10810811 0.12162162 0.08108108
##
       white
## 0.03378378
##
## Group means:
          Weight
                       L1
                            Height
                                     Width
                                                 L21
                                                          L32
## bream 636.1818 30.60606 39.52727 14.10000 2.8060606 5.272727
## parki 155.8000 18.62000 39.20000 14.18000 1.6100000 2.430000
## perch 360.9333 25.31852 26.17778 15.78519 2.1259259 1.650000
## pike 742.0625 42.88125 15.85625 10.48125 3.0375000 3.281250
## roach 159.1111 20.66667 26.88333 14.57222 1.6388889 2.716667
## smelt 11.5000 11.34167 16.99167 10.21667 0.6916667 1.091667
## white 477.2000 27.82000 29.10000 15.76000 2.4800000 2.960000
## Coefficients of linear discriminants:
##
                  LD1
                               LD2
                                           LD3
                                                        LD4
LD5
## Weight 0.000911022 -0.002710071 0.007553399 0.001688806 0.006182
751
## L1
          903
## Height -0.618519868 -0.332732865 -0.053863042 -0.330737436 -0.029226
039
## Width
          0.464670922 -0.341184928 -0.353062958 0.842951264 -0.201141
743
## L21
         -0.114071841 0.712452136 -2.278059990 0.277900320 2.700516
892
## L32
         -2.311243186 2.141452146 0.539501848 1.803654269 -0.461925
634
##
                  LD6
## Weight -0.003600115
## L1
         -0.119589009
## Height -0.019796935
## Width -0.159484049
```

```
## L21
           2.813216431
## L32
          -0.080912628
##
## Proportion of trace:
             LD2
                            LD4
                                    LD5
                                            LD6
##
      LD1
                     LD3
## 0.7998 0.1327 0.0473 0.0167 0.0035 0.0000
newfish.ldapred<-predict(newfish.lda,newfish[,-1])</pre>
table(newfish$Species,newfish.ldapred$class)
##
##
           bream parki perch pike roach smelt white
##
     bream
               33
                      0
                            0
                                  0
                                        0
                                              0
                            0
                                  0
                                        0
                                              0
                                                     0
##
     parki
               0
                     10
                      0
                           54
                                  0
                                              0
                                                     0
##
     perch
               0
                                        0
##
     pike
               0
                      0
                            0
                                 16
                                        0
                                              0
                                                     0
##
     roach
               0
                      0
                            0
                                  0
                                       18
                                              0
                                                     0
     smelt
##
               0
                      0
                            0
                                  0
                                        0
                                              12
                                                     0
##
     white
               0
                      0
                            0
                                  0
                                        1
                                              0
                                                     4
newfish.ldacv<-lda(Species~Weight+L1+Height+Width+L21+L32,data=newfish,
CV=T)
table(newfish$Species,newfish.ldacv$class)
##
           bream parki perch pike roach smelt white
##
##
     bream
                      0
                                  0
                                              0
                                                     0
              33
                            0
                                        0
                                              0
##
     parki
               0
                     10
                            0
                                  0
                                        0
                                                     0
##
     perch
               0
                      0
                           54
                                  0
                                        0
                                              0
                                                     0
                                                     0
##
               0
                      0
                            0
                                 16
                                        0
                                              0
     pike
##
               0
                      0
                            0
                                  0
                                       18
                                              0
                                                     0
     roach
##
     smelt
                0
                      0
                            0
                                  0
                                        0
                                              12
                                                     0
##
     white
               0
                      0
                            0
                                        1
                                              0
                                                     4
# The true error rate remains to be 0.6%
eqscplot(newfish.ldapred$x,type="n",xlab="1st LD",ylab="2nd LD")
fish.species <- c(rep("B",33),rep("W",5),rep("R",18),rep("Pa",10),rep("
S",12),rep("Pi",16),rep("Pe",54))
fish.colors \leftarrow c(rep(1,33),rep(2,5),rep(3,18),rep(4,10),rep(5,12),rep(6,
16),rep(7,54))
text(newfish.ldapred$x[,1:2],fish.species,col=fish.colors)
```



#To predict the class identities of the new data points we use:
newfish.ldatest<-predict(newfish.lda,newfish.test)
newfish.ldatest\$class</pre>

[1] bream bream perch perch pike smelt smelt parki roach roach whi te

Levels: bream parki perch pike roach smelt white

#We see that the results agree with those obtained from the classificat ion tree.

#Let us examine how to apply QDA to this dataset.

Quadratic Discriminant Analysis

```
#newfish.qda<-qda(Species~.,data=newfish)</pre>
newfish.q<-read.table("file:///C:/Users/Asus/Documents/GitHub/classifng</pre>
fish/newfish.qdata.txt",h=T)
library(MVN)
## sROC 0.1-2 loaded
#Running (i) Mardia's; (ii) Henze-Zirkler's and (iii) Royston's Multiva
riate
#Normality Test:
mvn(data = newfish.q[,-c(1,8,9,10)], mvnTest = "ma")
## $multivariateNormality
##
                Test
                            Statistic
                                                    p value Result
## 1 Mardia Skewness 426.417978948719 2.01256215659792e-58
                                                                NO
## 2 Mardia Kurtosis 1.58569973539399
                                         0.112807439232689
                                                               YES
## 3
                 MVN
                                 <NA>
                                                       <NA>
                                                                NO
##
## $univariateNormality
##
             Test Variable Statistic
                                         p value Normality
## 1 Shapiro-Wilk Weight
                                       <0.001
                               0.8780
                                                    NO
## 2 Shapiro-Wilk
                     L1
                               0.9679
                                       0.0019
                                                    NO
## 3 Shapiro-Wilk
                     L2
                               0.9702
                                       0.0033
                                                    NO
## 4 Shapiro-Wilk
                     L3
                               0.9703
                                       0.0033
                                                    NO
## 5 Shapiro-Wilk Height
                               0.9125
                                       <0.001
                                                    NO
## 6 Shapiro-Wilk
                    Width
                               0.9344
                                       <0.001
                                                    NO
##
## $Descriptives
##
                          Std.Dev Median
                                          Min
                                                        25th 75th
            n
                   Mean
                                                  Max
 Skew
## Weight 143 398.02378 360.51374 272.0 5.9 1650.0 120.00 650.0
75913
## L1
          143
               26.27692 10.16502
                                     25.2 7.5
                                                 59.0 19.00
                                                             32.6
                                                                   0.62
15598
## L2
          143
               28.44406 10.88848
                                     27.3
                                          8.4
                                                 63.4 20.90
                                                              35.0 0.57
96666
## L3
               31.25455 11.82529
                                     29.2 8.8
                                                       22.80
          143
                                                 68.0
                                                              39.6 0.43
06508
                                     26.8 14.5
## Height 143
               28.33217
                          8.39113
                                                 44.5 24.25
                                                              37.8 0.13
35468
## Width 143 14.07063
                          2.23310
                                     14.6 8.7
                                                 20.9 13.40 15.3 -0.49
62807
##
             Kurtosis
## Weight
           0.89652958
## L1
           0.35891664
## L2
           0.32535350
## L3
          -0.02200252
## Height -1.07931595
## Width
           0.27826140
```

```
mvn(data = newfish.q[,-c(1,8,9,10)], mvnTest = "hz")
## $multivariateNormality
##
              Test
                         HZ p value MVN
## 1 Henze-Zirkler 4.496681
                                  0
                                     NO
## $univariateNormality
             Test Variable Statistic
                                        p value Normality
##
                                       <0.001
## 1 Shapiro-Wilk Weight
                               0.8780
                                                   NO
## 2 Shapiro-Wilk
                     L1
                               0.9679
                                       0.0019
                                                   NO
## 3 Shapiro-Wilk
                     L2
                                                   NO
                               0.9702
                                       0.0033
## 4 Shapiro-Wilk
                     L3
                               0.9703
                                       0.0033
                                                   NO
## 5 Shapiro-Wilk Height
                               0.9125
                                       <0.001
                                                   NO
## 6 Shapiro-Wilk
                    Width
                               0.9344
                                       <0.001
                                                   NO
## $Descriptives
##
                          Std.Dev Median
                                          Min
                                                       25th 75th
            n
                   Mean
                                                 Max
Skew
## Weight 143 398.02378 360.51374 272.0 5.9 1650.0 120.00 650.0
75913
## L1
         143 26.27692 10.16502
                                    25.2 7.5
                                                59.0 19.00
                                                            32.6 0.62
15598
## L2
          143
               28.44406 10.88848
                                    27.3
                                          8.4
                                                63.4 20.90
                                                             35.0 0.57
96666
## L3
               31.25455 11.82529
                                    29.2 8.8
                                                68.0 22.80
          143
                                                             39.6 0.43
06508
                          8.39113
                                    26.8 14.5
                                                44.5 24.25
                                                             37.8 0.13
## Height 143
               28.33217
35468
## Width 143 14.07063
                          2.23310
                                    14.6 8.7
                                                20.9 13.40 15.3 -0.49
62807
             Kurtosis
## Weight 0.89652958
## L1
           0.35891664
## L2
           0.32535350
## L3
          -0.02200252
## Height -1.07931595
## Width
           0.27826140
mvn(data = newfish.q[,-c(1,8,9,10)], mvnTest = "royston")
## $multivariateNormality
##
        Test
                    Η
                           p value MVN
## 1 Royston 46.25164 2.211833e-10 NO
##
## $univariateNormality
##
             Test Variable Statistic
                                        p value Normality
## 1 Shapiro-Wilk Weight
                               0.8780
                                       <0.001
                                                   NO
## 2 Shapiro-Wilk
                                                   NO
                     L1
                               0.9679
                                       0.0019
## 3 Shapiro-Wilk
                     L2
                               0.9702
                                                   NO
                                       0.0033
## 4 Shapiro-Wilk
                     L3
                               0.9703
                                                   NO
                                       0.0033
```

```
## 5 Shapiro-Wilk Height
                               0.9125
                                       <0.001
                                                    NO
## 6 Shapiro-Wilk
                    Width
                               0.9344 < 0.001
                                                    NO
##
## $Descriptives
##
                          Std.Dev Median Min
                                                        25th 75th
            n
                   Mean
                                                  Max
 Skew
## Weight 143 398.02378 360.51374
                                   272.0 5.9 1650.0 120.00 650.0
75913
## L1
          143 26.27692 10.16502
                                    25.2 7.5
                                                 59.0 19.00
                                                             32.6 0.62
15598
          143
               28.44406 10.88848
                                          8.4
                                                63.4 20.90 35.0 0.57
## L2
                                    27.3
96666
              31.25455 11.82529
                                                68.0 22.80
## L3
          143
                                    29.2 8.8
                                                             39.6 0.43
06508
## Height 143
               28.33217
                          8.39113
                                    26.8 14.5
                                                 44.5
                                                      24.25
                                                             37.8 0.13
35468
## Width 143 14.07063
                          2.23310
                                    14.6 8.7
                                                 20.9 13.40 15.3 -0.49
62807
##
             Kurtosis
## Weight 0.89652958
## L1
           0.35891664
## L2
           0.32535350
## L3
          -0.02200252
## Height -1.07931595
## Width
           0.27826140
#資料不是多元常態
#newfish.qda<-qda(Species~.,data=newfish.q)</pre>
newfish.qda<-qda(Species~Weight+L1+Height+Width+L21+L32,data=newfish.q)</pre>
newfish.qdapred<-predict(newfish.qda,newfish.q)</pre>
predict(newfish.qda,newfish.test)$class
## [1] bream bream perch perch pike smelt smelt parki roach roach per
ch
## Levels: bream parki perch pike roach smelt
newfish.qda<-qda(Species~Weight+L1+Height+Width+L21+L32,data=newfish.q,
CV=T)
table(newfish.q$Species,newfish.qda$class)
##
##
           bream parki perch pike roach smelt
##
     bream
              33
                     0
                           0
                                0
                                      0
                                            0
##
     parki
               0
                    10
                           0
                                0
                                      0
                                            0
                          54
                                            0
##
                     0
                                0
                                      0
     perch
               0
##
     pike
               0
                     0
                           0
                               16
                                      0
                                            0
##
               0
                     0
                           1
                                0
                                     17
                                            0
     roach
                     0
                           1
##
     smelt
               0
                                0
                                           11
```

Nearest Neighbor Methods

```
library(class)
newfish.knn <- knn(newfish[,2:10],newfish[,2:10],newfish[,"Species"],k=</pre>
table(newfish$Species,newfish.knn)
##
          newfish.knn
##
           bream parki perch pike roach smelt white
##
                                   0
                                         0
                                                0
     bream
               30
                      1
                             2
                                         2
                                                0
                                                      0
##
     parki
                1
                      6
                             1
                                   0
                3
                      0
                            47
                                         2
                                                1
##
     perch
                                   0
                                                      1
##
     pike
                1
                      0
                             3
                                 11
                                         1
                                                0
                                                      0
                      0
                                   0
                                         8
                                                0
                                                      1
##
     roach
                1
                             8
                      0
                             0
                                   0
                                               12
                                                      0
##
     smelt
                0
                                         0
##
     white
                0
                      0
                             2
                                   1
                                         0
                                                0
                                                      2
#We see that the apparent error rate for k = 3 is about 21%. For k = 2,
we have:
newfish.knn<-knn(newfish[,2:10],newfish[,2:10],newfish[,"Species"],k=2,</pre>
table(newfish$Species,newfish.knn)
##
          newfish.knn
##
           bream parki perch pike roach smelt white
##
     bream
               27
                      0
                             3
                                   0
                                         2
                                                0
                                                      1
                      7
                             0
                                   0
                                         2
                                                0
                                                      0
##
     parki
                1
                3
                      0
                            45
                                   0
                                         4
                                                1
                                                      1
##
     perch
                1
                             2
                                 13
                                                0
                                                      0
##
     pike
                      0
                                         0
                                                0
                                                      1
##
     roach
                0
                      0
                             8
                                   0
                                         9
##
     smelt
                0
                      0
                             0
                                   0
                                         0
                                               12
                                                      0
                      0
                             2
##
     white
                0
                                   0
                                         0
                                                0
                                                      3
newfish.knn <- knn(newfish[,2:10],newfish[,2:10],newfish[,"Species"],k=</pre>
1, prob=T)
table(newfish$Species,newfish.knn)
##
          newfish.knn
##
           bream parki perch pike roach smelt white
##
     bream
               33
                      0
                             0
                                   0
                                         0
                                                0
                                                      0
                                   0
                                                0
                                                      0
##
     parki
                0
                     10
                             0
                                         0
                      0
                            54
                                                0
                                                      0
##
     perch
                0
                                   0
                                                0
                                                      0
##
                0
                      0
                             0
                                 16
                                         0
     pike
##
                0
                      0
                             0
                                   0
                                        18
                                                0
                                                      0
     roach
##
     smelt
                0
                      0
                             0
                                   0
                                         0
                                               12
                                                      0
##
     white
                0
                                                0
                                                      5
newfish1 <- newfish[,c(1,2,3,6,8,9)]
newfish.knncv <- knn.cv(newfish1[,2:6],newfish1[,"Species"],k=1,prob=T)</pre>
table(newfish1$Species,newfish.knncv)
```

```
newfish.knncv
##
          bream parki perch pike roach smelt white
##
##
    bream
             26
                    0
                         4
                              0
                                    2
                                          0
                                               1
##
    parki
              1
                    4
                         0
                              0
                                    4
                                          0
                                               1
##
    perch
              3
                    0
                        37
                              0
                                   11
                                          1
                                               2
##
    pike
              2
                    0
                         4
                              9
                                    0
                                          0
                                               1
                    0
                              0
                                    5
                                          0
##
    roach
              2
                        10
                                               1
##
    smelt
                    0
                         0
                              0
                                    0
                                         12
                                               0
              0
                         3
                              0
                                               2
    white
                    0
##
              0
                                          0
newfish1.test<-newfish.test[,c(1,2,5,7,8)]</pre>
newfish.knntest<-knn(newfish1[,2:6],newfish1.test,newfish1[,"Species"],</pre>
k=1,prob=T)
newfish.knntest
## [1] bream bream perch white perch smelt smelt parki perch per
ch
## attr(,"prob")
## Levels: bream parki perch pike roach smelt white
```

Logistic Discrimination

```
library(nnet)
newfish.logd<-multinom(Species~.,data=newfish,maxit=250)</pre>
## # weights: 77 (60 variable)
## initial value 287.994702
## iter 10 value 189.100680
## iter 20 value 82.739762
## iter 30 value 15.668415
## iter 40 value 0.165377
## iter 50 value 0.003851
## final value 0.000000
## converged
newfish.logd
## Call:
## multinom(formula = Species \sim ., data = newfish, maxit = 250)
## Coefficients:
##
        (Intercept)
                         Weight
                                        L1
                                                   L2
                                                              L3
Height
## parki
          -29.45533 0.02917110
                                6.349592 17.8259067 -23.500970
                                                                   9.
645257
## perch
          -80.11405 0.16021628
                                3.267803 56.6489218 -53.765483
684178
           15.22567 -0.05874368
                                 8.093673
                                            0.9753102 -3.095179 -13.
## pike
084687
## roach -277.16410 -0.51539078 54.195310 -43.6844449
                                                        4.362472 -2.
952463
## smelt 455.64639 0.18459382 29.363751 -20.5072505 -10.290211 -13.
228223
## white
          -57.01255 0.19991067 -17.467222 31.7667561 -20.454096 -4.
118171
##
            Width
                         L21
                                     L32
                                               L31
## parki 3.247584 11.476314
                              -41.326877 -29.850563
## perch 21.052273 53.381119 -110.414404 -57.033286
## pike 21.652958 -7.118363
                              -4.070489 -11.188852
## roach 40.080837 -97.879755
                               48.046917 -49.832838
## smelt 18.368009 -49.871001
                               10.217040 -39.653961
## white 26.549555 49.233978 -52.220852 -2.986874
## Residual Deviance: 2.009681e-11
## AIC: 84
table(newfish$Species,predict(newfish.logd,newfish))
##
##
          bream parki perch pike roach smelt white
    bream 33 0 0 0 0 0 0
```

```
##
     parki
                0
                     10
                             0
                                  0
                                         0
                                               0
                                                      0
                      0
                                                      0
##
     perch
                0
                            54
                                  0
                                         0
                                               0
                0
                      0
                                               0
                                                      0
##
     pike
                             0
                                 16
                                         0
##
     roach
                0
                      0
                             0
                                  0
                                        18
                                               0
                                                      0
     smelt
                0
                      0
                             0
                                  0
                                         0
                                              12
                                                      0
##
##
     white
                      0
                             0
                                  0
                                         0
                                               0
                                                      5
                0
library(glmnet)
## Loading required package: Matrix
## Loading required package: foreach
## Loaded glmnet 2.0-16
x <- as.matrix(newfish[,-1])</pre>
y <- newfish$Species</pre>
cvfit <- cv.glmnet(x, y, family="multinomial", type.measure="class", nf</pre>
olds=148)
predict.value <- predict(cvfit, x, s = "lambda.min", type = "class")</pre>
table(predict.value,newfish$Species)
##
## predict.value bream parki perch pike roach smelt white
                                                      0
           bream
                     33
                             0
                                   0
                                         0
                                               0
                                                            0
##
                      0
                            10
                                   0
                                               0
                                                      0
                                                            0
           parki
                                         0
##
            perch
                      0
                             0
                                   54
                                         0
                                               0
                                                      0
                                                            0
                      0
                                   0
                                               0
                                                      0
                                                            0
##
           pike
                                        16
                                                            0
##
            roach
                      0
                             0
                                   0
                                         0
                                              18
                                                      0
##
            smelt
                      0
                             0
                                   0
                                         0
                                               0
                                                     12
                                                            0
           white
                      0
                             0
                                   0
                                         0
                                               0
                                                      0
                                                            5
##
predict(newfish.logd,newfish.test)
    [1] bream bream perch perch pike smelt smelt parki roach roach whi
##
## Levels: bream parki perch pike roach smelt white
```