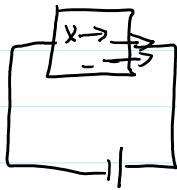


## Electric Current

- Electric current in meaning of phenomena:
  - Directional motion of charges
- Electric current in meaning of  $I$ 
  - the rate of flow of charge



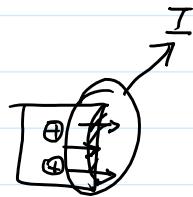
## Electric Variables

Definition

Current ( $I$ ) **in**

$$I = \frac{Q}{t}$$

rate of flow of charge.



$$I = \frac{V}{R} \text{ is only a statement} \quad \text{Unit} \Rightarrow [A] \quad 1A = \frac{1C}{1s}$$

Definition

Voltage ( $V$ ) **across**

$$V = \frac{E}{Q}$$

energy/work done per Unit charge

$$V = IR \text{ is only a statement} \quad \text{Unit} \Rightarrow [V] \quad 1V = \frac{1J}{1C}$$

\* It's not p.d. (p.d. 'will be'), voltage 'is'



$$[V/m] = [(J/C)/m] = [Nm/Cm] = [N/C] = [kgm^2/s^2]$$

## Resistance ( $R$ )

$$R = \frac{V}{I} \text{ is a statement, but should be considered as definition: Voltage per current}$$

Units  $\Rightarrow [\Omega]$

$$\text{Power (P)} \quad P = \frac{E}{t}$$

$$P = \frac{E}{t} = \frac{VQ}{t} = VI \Rightarrow \text{statement only use in electricity}$$

$$P = I^2R \quad \frac{V^2}{R} \text{ are only statement}$$

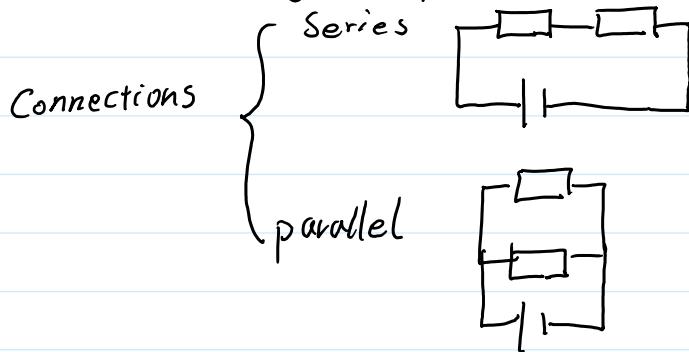
$$\text{Energy (E)} \quad E = Pt$$

$$E = Pt = IVt = I^2 R t = V^2 R t$$

# 11/29 Series and Parallel

Wednesday, November 29, 2017 10:00 AM

component - any part put into circuit



$$\begin{cases} V = V_1 = V_2 \\ I = I_1 = I_2 \end{cases} \quad R = R_1 + R_2$$

$$\begin{cases} V = V_1 = V_2 \\ I = I_1 + I_2 \end{cases} \quad \frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} = \frac{R_1 + R_2}{R_1 R_2}$$

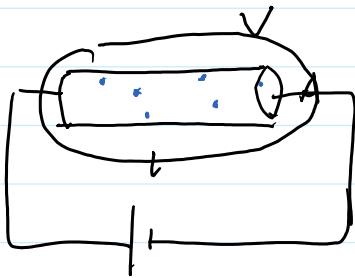
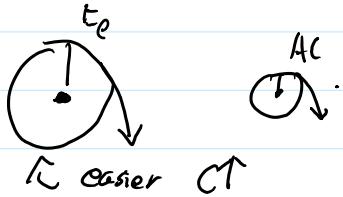
Home: parallel  $\Rightarrow$  robustness and voltage

## Drift Velocity

Speed of electrons in circuit / ions in electrolyte (cm/s)



$$C = \frac{n}{V} \text{ is different}$$



$$I = \frac{Q}{t}$$

$$Q = Ne$$

$N$  - numbers of  $e^-$  in wire [no unit]

$$N = nV$$

$n$  - concentration of  $e^-$  [ $m^{-3}$ ]  
number density

$$V = AL$$

$A$  - cross section area,  $L$  - length

$$I = \frac{nA\langle v \rangle e}{\text{drift velocity}}$$

$$= nAVe / nAVq$$

$$V = \frac{I}{nAq} \Rightarrow v \propto I \quad \& \quad V \propto \frac{1}{A} \quad \& \quad V \propto \frac{1}{n}$$

- electrons charge is quantized quantum  $\rightarrow$  a certain amount

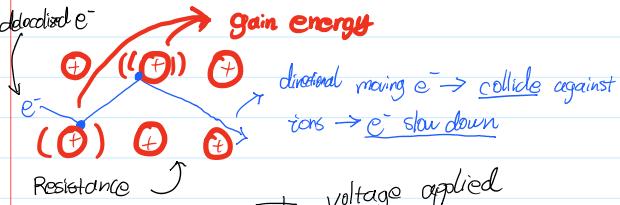
$e = +1.6 \times 10^{-19} C \rightarrow$  smallest charge

$2e = +3.2 \times 10^{-19} C \rightarrow$  second smallest charge

therefore  $\frac{1C}{e} = \frac{Q}{e} =$  whole number always!

any other charge is the multiple of whole number

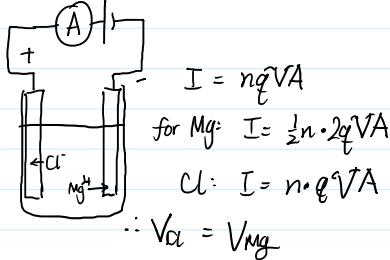
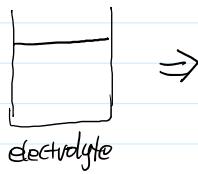
de-localized  $e^-$



Resistance  $\downarrow$  + voltage applied

Drift  $\bar{V} = \frac{V}{t}$   $\leftarrow$  average velocity, not instantaneous.  
 not in a straight line

$MgCl_2 \rightarrow$



Resistance ( $R$ )  $[\Omega]$

factors affecting resistance

- length ( $l$ )

$$R \propto l \Rightarrow$$
 more  $e^-$  collide on ions  $\Rightarrow R \uparrow$

- Area ( $A$ )

$$R \propto \frac{1}{A}$$

$e^-$  easier to maneuver

$e^-$  harder to maneuver

harder for  $e^-$  to squeeze through  $\Rightarrow$  collide more

- Temperature ( $T$ )

~~$R \propto T$~~   $\Rightarrow$  no direct relationship

parallel   
 $R = \frac{R_1 R_2}{R_1 + R_2}$   $A \uparrow$

series   
 $R = R_1 + R_2$   $l \uparrow$

$R \uparrow$  if temperature rises, resistance rises.

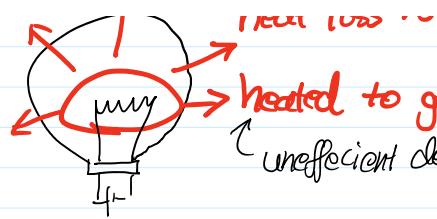
ions vibration increase

- Type of metal / conductor

$\downarrow$  small  $\Rightarrow$  usual application

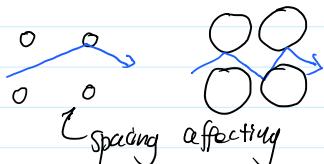
heated to above  $\therefore$   $\propto 1: 1 + \alpha \Delta T$

small  $\Rightarrow$  usual application  
large  $\Rightarrow$  iron/cooker/bulb

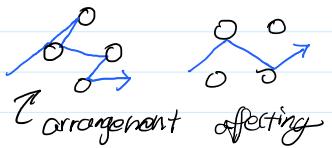


25% is highest efficiency

because of ions arrangement & spacing



silver & gold has smallest resistance  
(copper is also good)  
tungsten has highest resistance



$$R \propto l \quad \text{resistivities}$$

Therefore  $\Rightarrow R = \rho \frac{l}{A}$  this is actually the definition of resistance, but

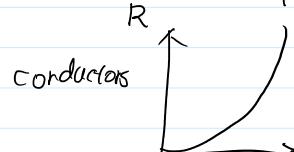
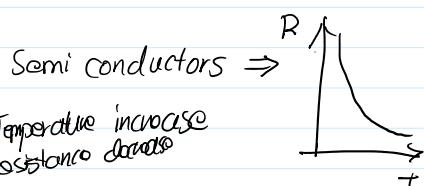
$$R = \frac{V}{I}$$
  
CIE's definition,

$$R = \frac{V}{I} \Rightarrow |R| = |V| = |I|$$
  
Show the resistance of  $1m^3$  cubic of material between opposite faces

$\Rightarrow \rho$  is the numerical value of resistance between opposite faces of unit volume cubic

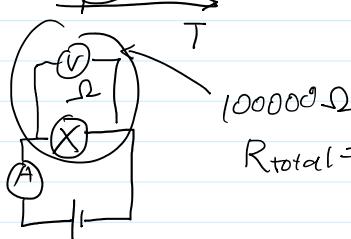
Substances	Conductor	$\rho \leftarrow$ small value	$\times 10^{-8}$
	Semiconductor	$\rho \leftarrow$ intermediate	$\times 10^3$
	Insulator	$\rho \leftarrow$ a very big value	$\times 10^8$

$$\rho = \frac{RA}{l} = \left[ \frac{\Omega m^2}{m} \right] = \left[ \frac{\Omega m^2}{m} \right] \frac{1}{\rho} \Rightarrow \frac{1}{4\rho} = \frac{A \times 2}{l/2} \Rightarrow \rho \propto A$$



Resistance of ammeters and voltmeters.

$R_A$  should be as small as possible.



$$R_{\text{total}} = \frac{R_1 R_2}{R_1 + R_2} \approx 1\Omega \text{ (doesn't change)}$$

$R_V$  should be as large as possible

Registers

Resistors just increase the resistance  $\Rightarrow$  control the voltage & current

Resistors

Resistors just increase the resistance  $\Rightarrow$  control the voltage & current



fixed value resistors



Variable Resistor (potentiometer)



fuses

(melts when too high)

## 12/6 Ohm's Law

Wednesday, December 6, 2017 10:00 AM

Ohm's law  $\left\{ \begin{array}{l} \text{Ohm's law (for the external part of circuit)} \Rightarrow \text{IGCSE} \\ \text{Ohm's law for the full circuit} \end{array} \right.$

$$I = \frac{Q}{t} \quad V = \frac{E}{Q}$$

move faster  $\downarrow$  push stronger more energy  $\downarrow$

$R \mapsto$  collision  $R = \rho \frac{l}{A}$  definition

$\Rightarrow I \propto V$  current related to voltage, but

however:  $V \propto I$  is wrong! Voltage is independent to current, it is relate with batteries.

$R \uparrow \Rightarrow$  more collision  $\Rightarrow$  slow down  $e^- \Rightarrow I \downarrow \Rightarrow I \propto \frac{1}{R}$

Combining

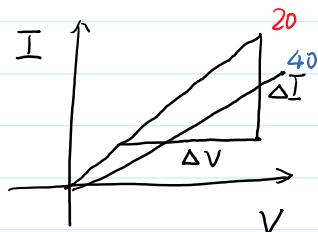
again:  $R \propto \frac{1}{I}$  is wrong!  $\Rightarrow$  Resistance is properties of conductor

$$I = \frac{V}{R}$$

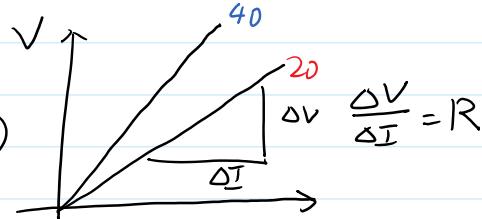
Ohm's law (temperature remains the same)

Ohm's law state that for a conductor at constant temperature, the current in the conductor is proportional to the potential difference across it [U]

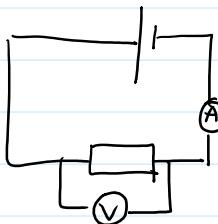
So,  $R = \frac{V}{I}$  should be write as the definition of resistance.



$$\frac{\Delta I}{\Delta V} = \frac{1}{R} \text{ (reciprocal)}$$



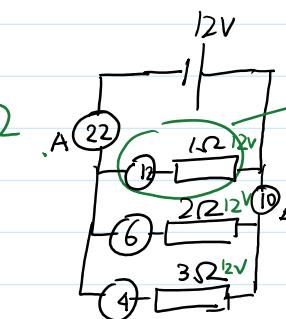
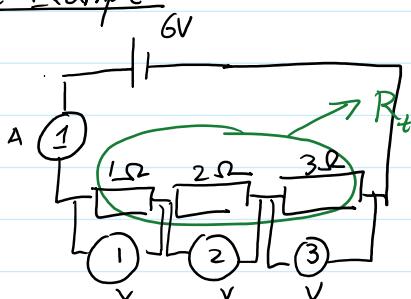
(physically this is wrong, it's only mathematically correct)



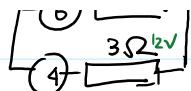
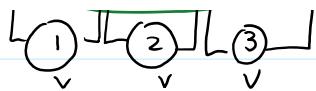
← circuit used for measuring resistance

$$I = \frac{V}{R}$$

### Worked Example

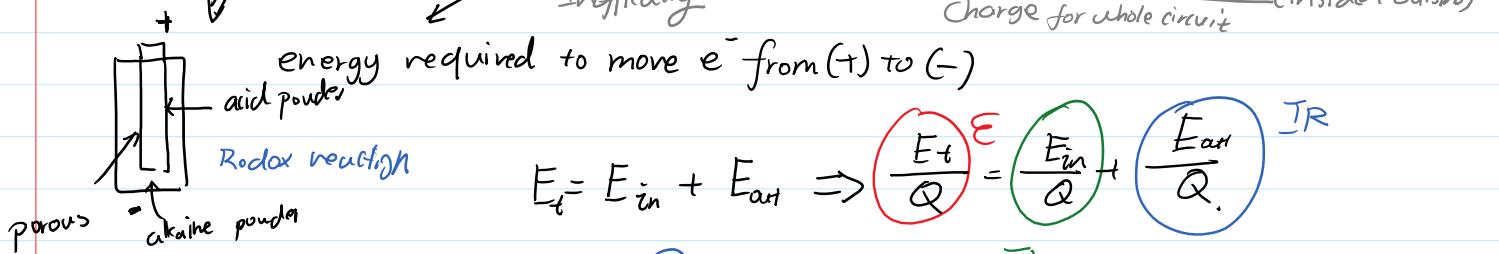
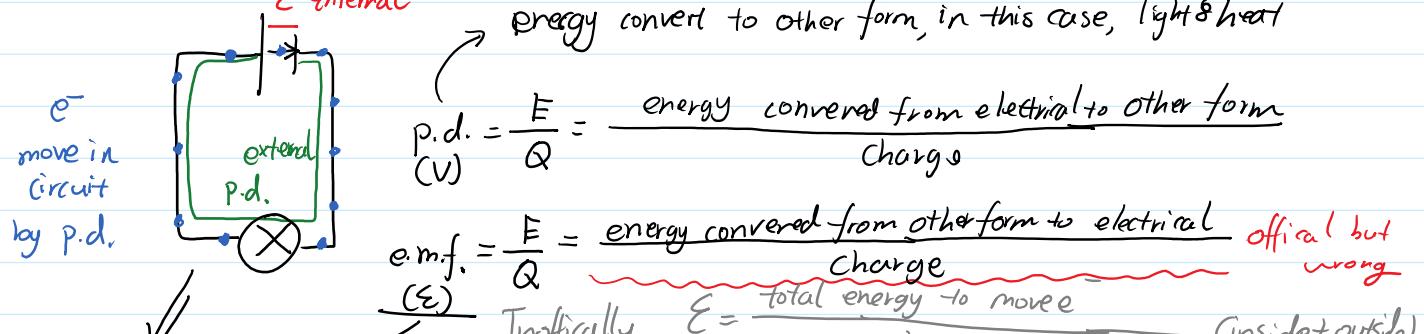


Use  $I = \frac{V}{R}$  individually



Ohm's law for the full circuit

$E$  - more by e.m.f. in batteries



$$E_t = E_{in} + E_{out} \Rightarrow \frac{E_t}{Q} = \frac{E_{in}}{Q} + \frac{E_{out}}{Q}$$

$$E = I_r + IR \quad \leftarrow I_r$$

e.m.f. *terminal p.d.* loss volts *internal resistance  $\Rightarrow$  resistance of power pack*

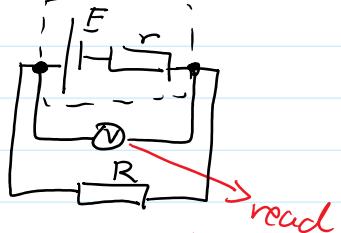
$$E = \underline{IR} + \underline{I_r} = V + I_r \quad \text{if internal resistance neglected} \Rightarrow V = IR$$

Ohm's law for the full circuit

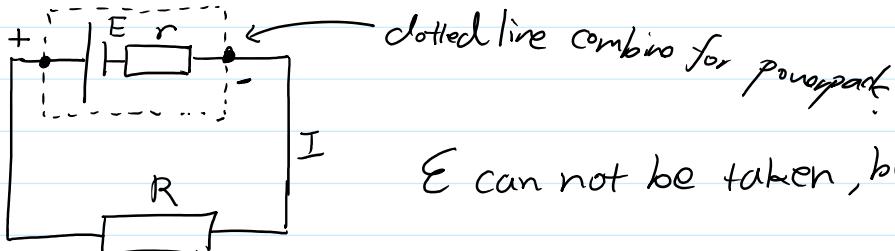


notice:  $E = E$  in CIE

better to write e.m.f.



but if not, then  $E = I_r + IR$ , and

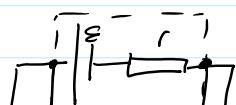
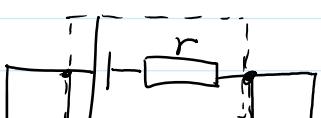


$E$  can not be taken, but need calculated *terminal p.d.*

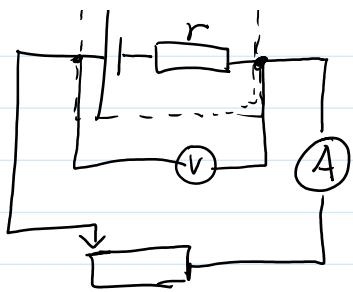
$$V < E \Rightarrow V = E - I_r \quad \text{some energy used in power pack}$$

terminal p.d. = e.m.f. - loss volts

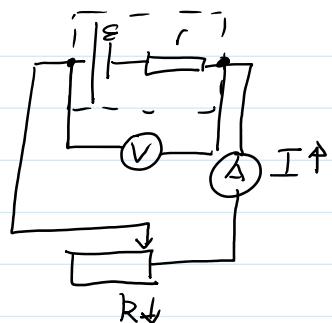
Experiment to find  $E$  and internal resistance  $r$



$$E = V - I_r$$

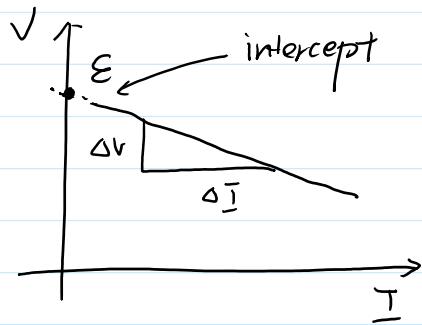


$\Rightarrow$



$$\mathcal{E} = V - Ir$$

$Ir \uparrow \mathcal{E}$  constant  
 $V \downarrow$

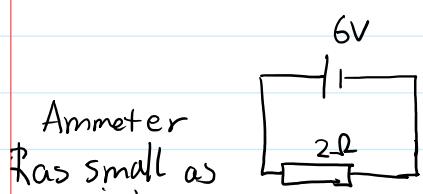


$$V = -Ir + \mathcal{E}$$

$$r = \frac{\Delta V}{\Delta I} = \text{gradient}$$

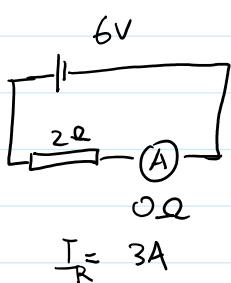
## 12/11 Internal Resistance

Monday, December 11, 2017 3:44 PM

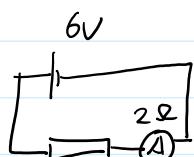


Ammeter  
has small as  
possible

$$I = \frac{V}{R} = \frac{6V}{2\Omega} = 3A$$



$$I = \frac{V}{R} = \frac{6V}{2\Omega} = 3A$$



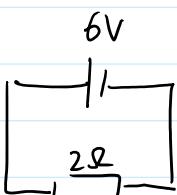
$$\frac{I}{R} = \frac{1.5A}{2\Omega} = 0.75A$$

(I read is smaller before connecting)

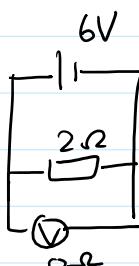
- ammeter connect in series

- $R_{\text{total}}$  in circuit grows, current will be smaller than before connecting

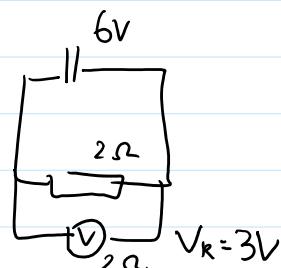
Voltmeter  
R as large  
as possible



$$V = 6V$$



$$V_R = 6V$$

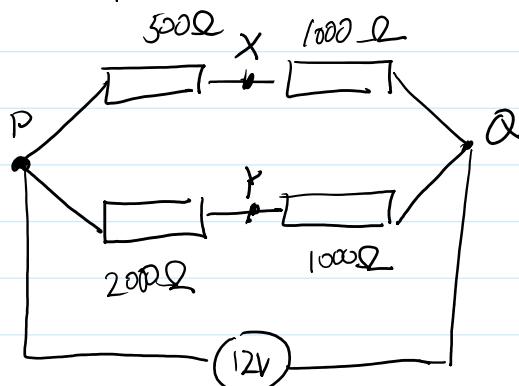


$$V_R = 3V$$

- voltmeter connect in parallel

- $R_{\text{total}}$  decrease, voltage will be smaller than before connecting

Example 1



$$R_{\text{total}} = R_1 + R_2 = 500\Omega + 1000\Omega = 1500\Omega \quad I_1 = \frac{V}{R_{\text{total}}} = \frac{12V}{1500\Omega} = 0.008A$$

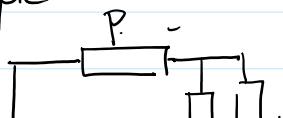
$$R_{\text{total}} = R_3 + R_4 = 200\Omega + 1000\Omega = 1200\Omega \quad I_2 = \frac{V}{R_{\text{total}}} = \frac{12V}{1200\Omega} = 0.01A$$

$$V_1 = 0.008 \times 500 = 4V \quad V_2 = 0.008 \times 1000 = 8V$$

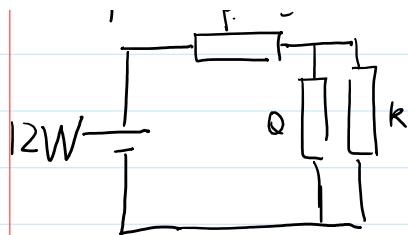
$$V_3 = 0.01 \times 200 = 8V \quad V_4 = 0.01 \times 1000 = 10V$$

$$X - Y = V_1 - V_3 = -4V$$

Example 2



$$R_p = R + r = R$$



$$R_P = R_Q = R_R = R$$

find  $P_P$ ,  $P_Q$ ,  $P_R$

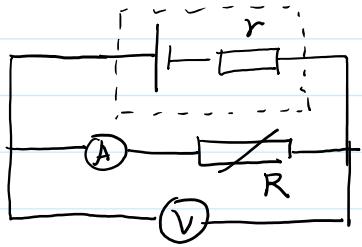
$$P_P = I^2 R \quad P_Q = \left(\frac{1}{2}I\right)^2 R = \frac{1}{4}I^2 R = P_R$$

$$I^2 R + \frac{1}{4}I^2 R + \frac{1}{4}I^2 R = 12W$$

$$\frac{3}{2}I^2 R = 12W$$

$$I^2 R = 8W \quad \therefore P_P = 8W, P_Q = P_R = 2W$$

### Example 3

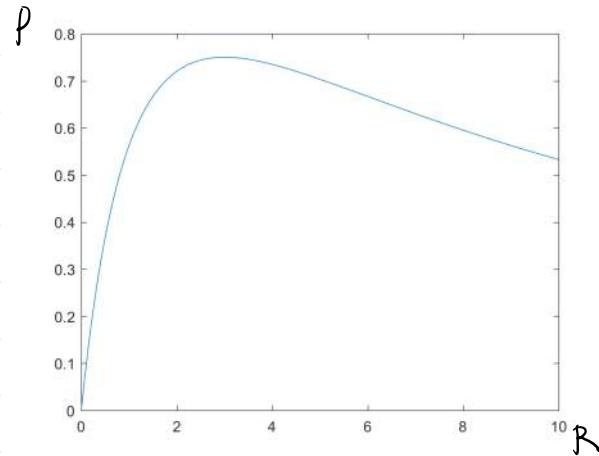
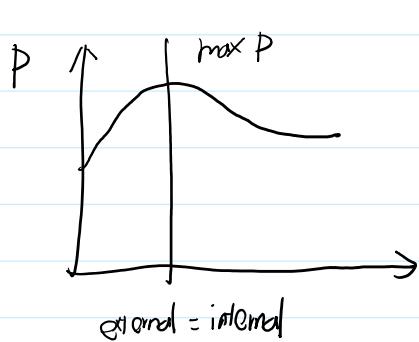


$$r = 3\Omega, E = 3.0A$$

calculate  $P$  on  $R$  if

- $R = 2\Omega$
- $R = 3\Omega$
- $R = 4\Omega$

$$P = I^2 R \quad I = \frac{E}{R+r}$$



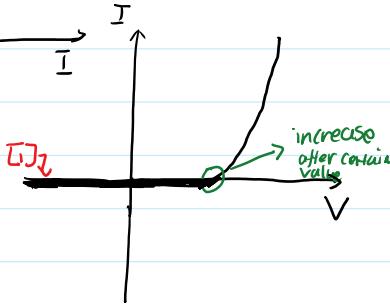
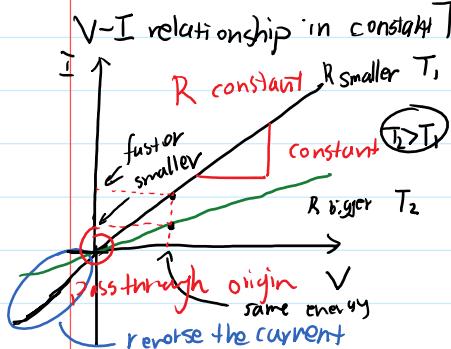
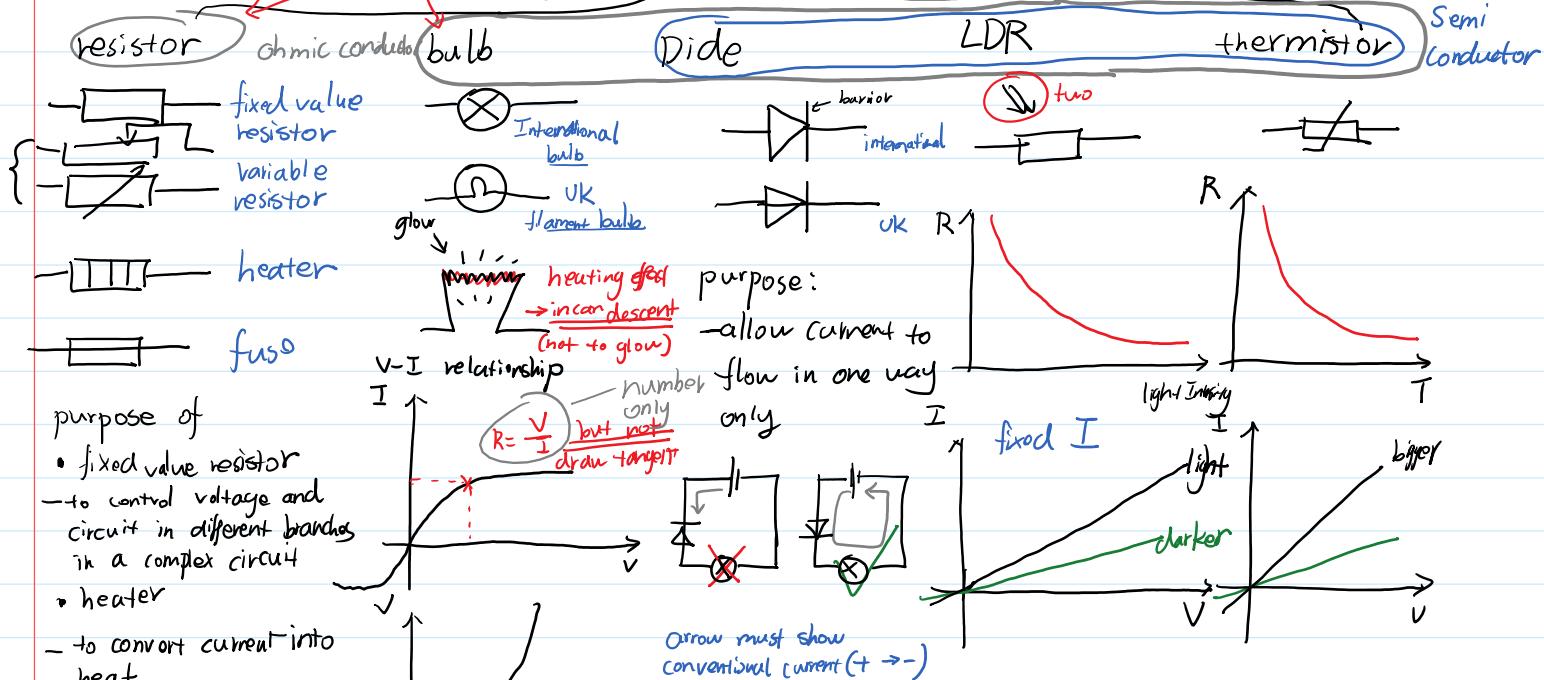
# 12/13 Circuit Component

Wednesday, December 13, 2017 10:19 AM

Component: anything we connect to the circuit  
 Ohm's law apply for all of them, but non-ohmic conductor  
 (not a linear relationship)

non-ohmic conductor

Semi-conductor



# 12/15 Kirchhoff's Law

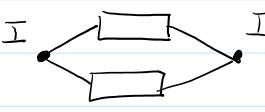
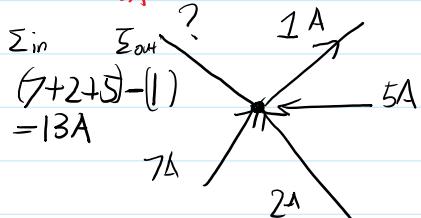
Friday, December 15, 2017 8:56 AM

## Kirchhoff's law



$$V = V_1 + V_2$$

BA

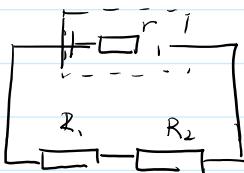


$$I = I_1 + I_2$$

1<sup>st</sup> Kirchhoff's law:

$$\sum I_{\text{enter}} = \sum I_{\text{leave}} \quad \boxed{\text{definition}}$$

conservation of charge  
no  $e^-$  create at junction.



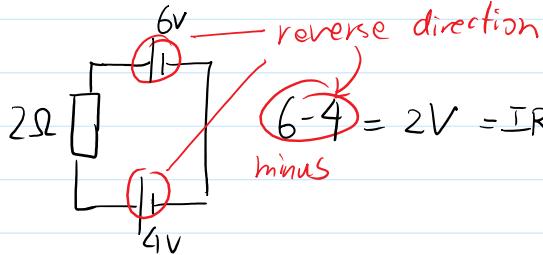
$$E = IR_1 + Ir$$

2<sup>nd</sup> Kirchhoff's law:

$$\sum E = \sum IR + I\epsilon \quad \boxed{\text{definition}}$$

conservation of energy

internal resistance



Step to solve:

① draw current (if not done already)  $\Rightarrow$  Use conventional current

$$I_1 + I_3 = I_2$$

should be in and out

② write 1<sup>st</sup> Kirchhoff's law for the junction

} solve equation should be the same direction of loop

③ choose a loop and write 2<sup>nd</sup> Kirchhoff's law

$$6 + 3 = -I_3 * 3 + I_1 * 2$$

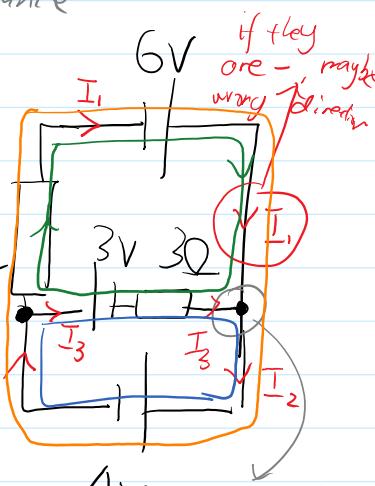
use letter to show correct loop

$$\begin{cases} I_1 + I_3 = I_2 \\ 6 + 3 = -I_3 * 3 + I_1 * 2 \\ 6 - 4 = I_1 * 2 \end{cases}$$

$$\begin{cases} I_1 = 1A \\ I_2 = -1.5A \\ I_3 = -2.5A \end{cases}$$

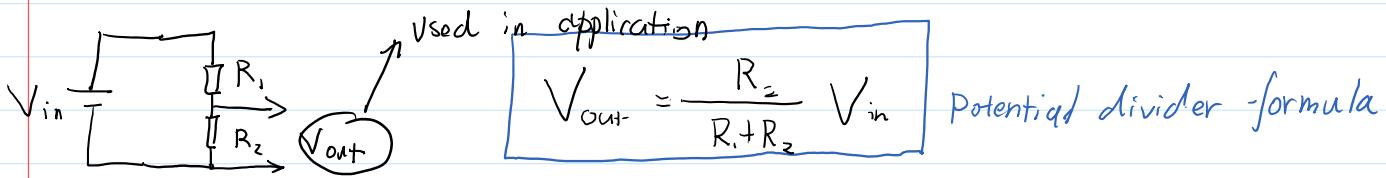
$$6 - 4 = I_1 * 2$$

$\Rightarrow$  these two direction will be actually reverse



# 1/5 Potential Divider

Friday, January 5, 2018 8:26 AM



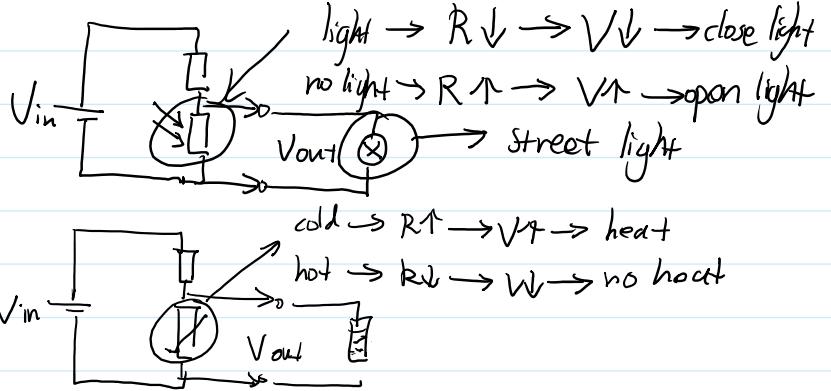
$$I = \frac{V_{in}}{R_1 + R_2} \Rightarrow V_{out} = IR_2$$

$$V_{out} = \frac{V_{in}}{R_1 + R_2} \cdot R_2 \Rightarrow V_{out} = \frac{R_2}{R_1 + R_2} V_{in}$$

Where to use?

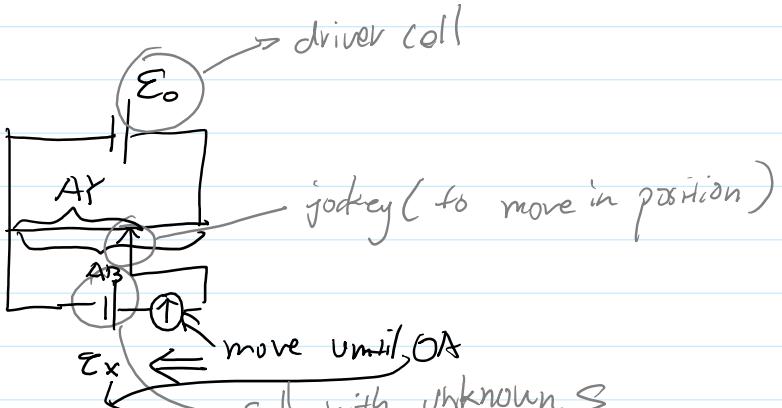
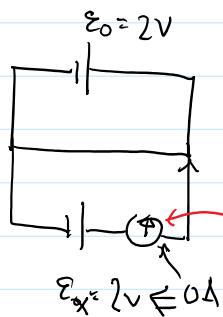
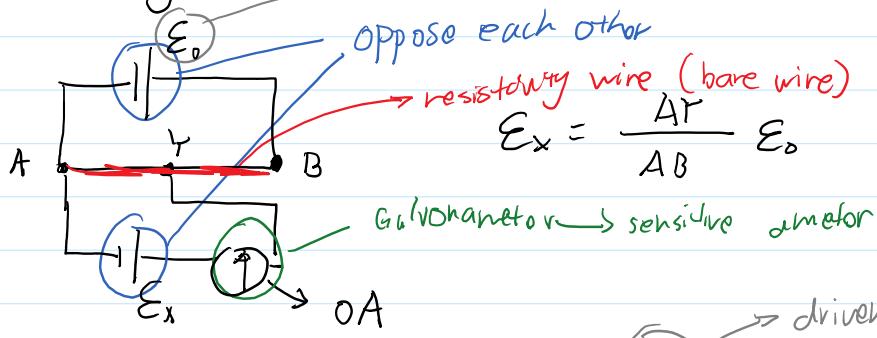
Direct Sensing

Robots  
street light  
temperature  
etc...



Potentiometer circuit

a simpler way to check the  $\mathcal{E}$   $\rightarrow$  standard cell known  $\mathcal{E}$



$\mathcal{E}_x$  unknown

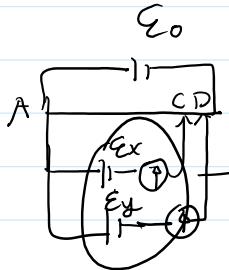
$$\mathcal{E}_x = \frac{R_x}{R_x + R_k} \mathcal{E}_0 = \frac{R_x}{R_x + R_k} \mathcal{E} = \frac{l_x}{l_x + l_k} \mathcal{E}_0$$

$$\mathcal{E}_x = \frac{R_x}{R_0} \mathcal{E}_0 = \frac{R_{\frac{r_x}{A_x}}}{R_0} \mathcal{E}_0 = \frac{\frac{r_x}{A_x}}{R_0} \mathcal{E}_0 = \frac{r_x}{R_0} \mathcal{E}_0$$

~~$\cancel{R}$~~   ~~$\cancel{A_x}$~~

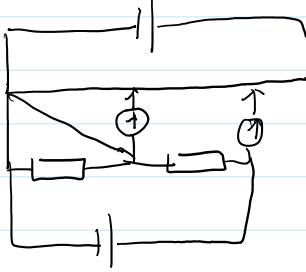
$R_0 = r_x$

Assumption: internal resistance identical  $\Rightarrow$  if not  $\rightarrow$  no accuracy



now only these two need to be the same  $r_x = r_y$

$$\frac{\mathcal{E}_x}{\mathcal{E}_y} = \frac{AC}{AD} \Rightarrow \text{if knowing } \mathcal{E}_x / \mathcal{E}_y, \text{ we can find another}$$



← compare  $R_x$  &  $R_y$

# 1/15 Subatomic Particles

Wednesday, January 10, 2018

9:36 AM

Subatomic particles	charge / elementary charge	mass / amu	charge / C	mass / kg
e <sup>-</sup>	-1	$\approx 0.0001$	$-1.6 \times 10^{-19}$	$9.11 \times 10^{-31}$
p <sup>+</sup> (nucleons)	+1	1 (1.006)	$+1.6 \times 10^{-19}$	$1.67 \times 10^{-27}$
n	0	1	0	$1.67 \times 10^{-27}$

atomic mass unit / universal atomic mass unit  $1.66 \times 10^{-27}$  kg  
notice the different !

make up nucleus  
amu  $\rightarrow \frac{1}{12}$  of  $^{12}_6$  C mass  
nucleus  $\rightarrow$  mass concentrated

e<sup>-</sup> doesn't contribute mass of atom significantly

$A$  (2)  $\rightarrow$  mass / nucleon number  $\rightarrow \sum p^+ + n$   
 $N$  (13)  $\rightarrow$  element symbol  
proton / atomic number  $\rightarrow \sum p^+ / \sum e^-$   
number of e<sup>-</sup>  $\rightarrow$  atoms are neutral

⚠ particles are required to be called in correct name

atom - (used to be) smallest neutral particle of a substance

molecule - 2 or more atom bonded together to form neutral

ion - former atom which gain / lost electrons

isotope - type of atom which has the same number of p<sup>+</sup>, but different n

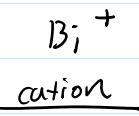
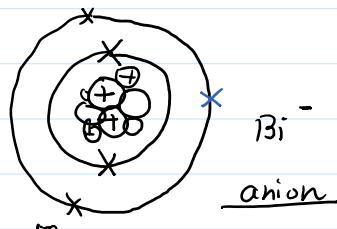
minimum 3 of isotope

$^{26.98}_{13} \text{Al}$   $\rightarrow$  isotope  $\Rightarrow$  average isotopic mass

cross effect -



different mass  
define isotope



# 1/17 Structure of Atoms

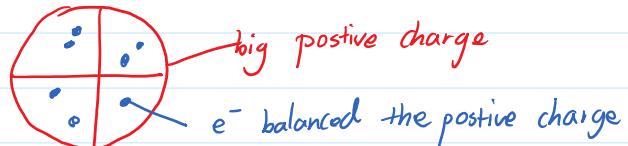
Wednesday, January 17, 2018 9:31 AM

## Thomson's Model

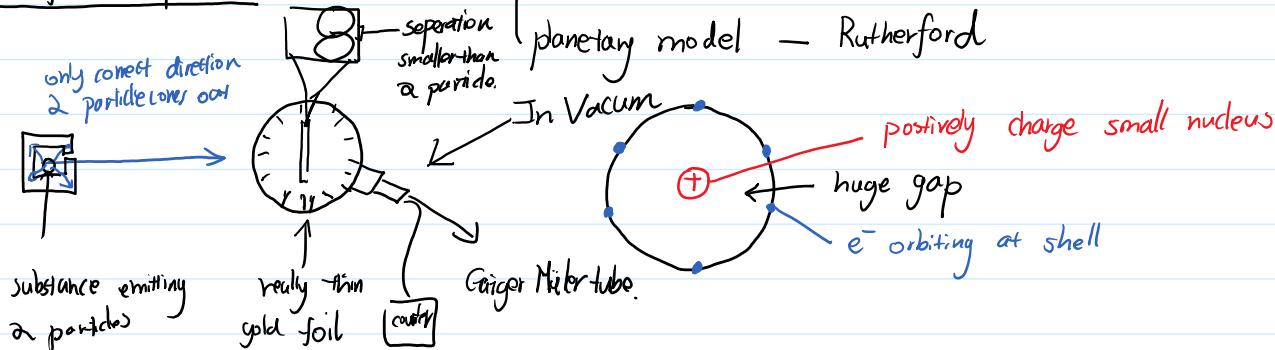
originally they think that atom is undivisible

$\frac{m}{Q}$   
In 1897 Thomson discovered  $e^-$  and find charge/mass

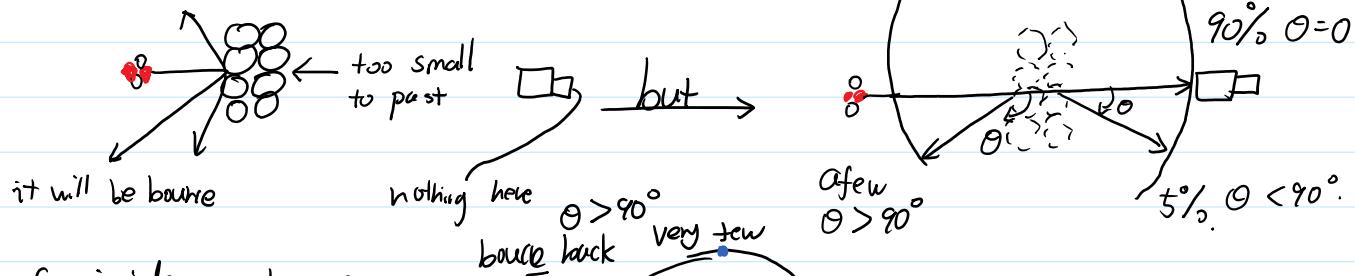
plump pudding model — J.J. Thomson



## Rutherford Experiment

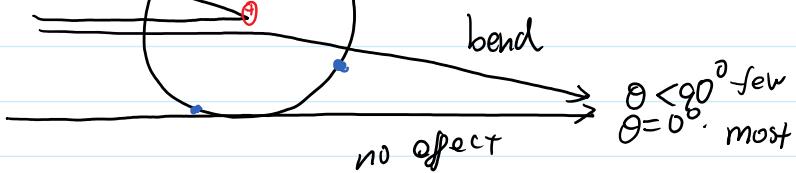


If the plum pudding is correct then.



proof: inside emptiness →

↳ planetary model



Ob	Con
most α particles went straight through the foil	atoms are mostly spaced
a few are deflected at angle less than 90°	Nucleus is very small and is very dense and it's all positive charge
very few are deflected at angle greater than 90°	

## Radioactive Decay

D-dimension shear

r-12

all the element heavier than Pb are naturally unstable and beta-radioactive  
 $\approx 14 \rightarrow$  wants to loss 2 n

Radiation  
heat  
radioactive

$C-12$   
 $6p^+/6n$

natively unstable and ~~unstable~~ -

$C-14$   
 $6p^+/8n$

wants to loss 2 n  
to get stabl.

before Pb only heavy isotope  
are unstable

only 3 things can come out



$\alpha - 2p^+ 2n$

$\beta - e^- \bar{e}$

$\gamma$ -photon m, (loose weight slightly)

Radioactive Decay - Some isotopes and heavy chemical elements are unstable - their nuclei split (Decay) emitting radiation - i.e.  $\alpha, \beta, \gamma$

depends

Types of radiation	Description	speed	Penetration	E/M field	Ranger	Ionizing Ability
$\alpha$ (alpha)	$2p^+ + 2n$ stuck together / helium nucleus / double ionized Helium	$\approx 0.5C$	(ouost paper far cm of air)	Yes	In most out: least	highest Chargin/8)
$\beta$ (beta)	fast moving $e^-$	range $0.6C - 0.9C$	medium Al foil (mm)	Yes	In Medium out	middle/low
$\gamma$ (gamma)	highest f and highest E em. wave	$3.0 \times 10^8 \text{ m/s}$	highest few cm of Pb few m of concrete can relate to safe	No	In: least out: most	low/middle

ionizing radiation → knock out ions  
why? → radiation from nucleus (Not from Orbit!) →

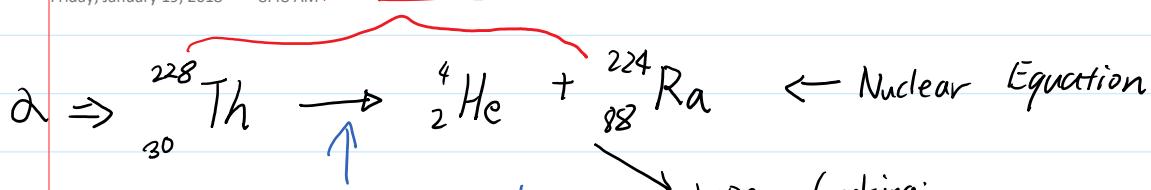
$e^-$  moves different ways  
up to 5  $e^-$  emittes

in the cell → burst / lack of cytoplasm → also DNA will have mutation  
mitosis → tumor  
apoptosis → kill itself

# 1/19 Nuclear Decay

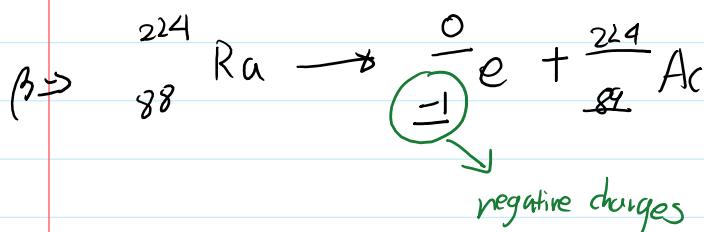
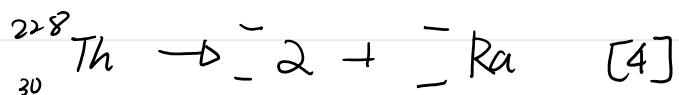
Friday, January 19, 2018

8:48 AM mass number is conserved

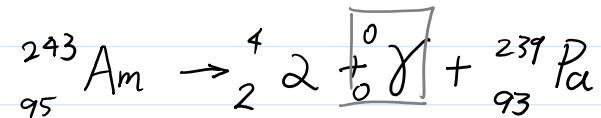


mass is not conserved!  
energy released

type of asking:



negative charges



$\gamma$  is  ${}^0$  but must write here

## Conservation Laws during nuclear processes

### Conserved

- momentum
- mass-energy  $E=mc^2$

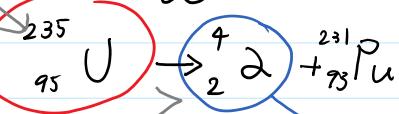
Mass-Energy selection

Artificially  
due to rounding

- nucleon/mass number  $^{16}_8 O$
- charge

### Not Conserved

- mass NOT conserved
- energy NOT conserved

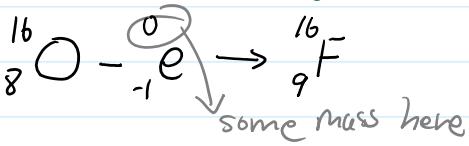


a reverse example:  
Big Bang

mass bigger

mass convert to energy

K.E. appear.



## Alternative units for energy

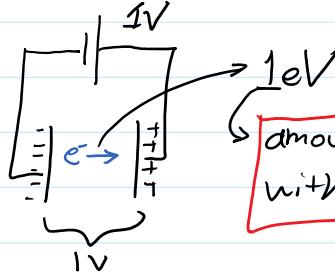
eV (electron-volt)

$$V = \frac{E}{Q} \Rightarrow \begin{cases} E = VQ \\ [Q = V \times C] \end{cases}$$

$$1 \text{ eV} = \frac{1 \times 1.6 \times 10^{-19} \text{ C}}{e} \times 1 \text{ V} \Rightarrow 1.6 \times 10^{-19} \text{ J}$$

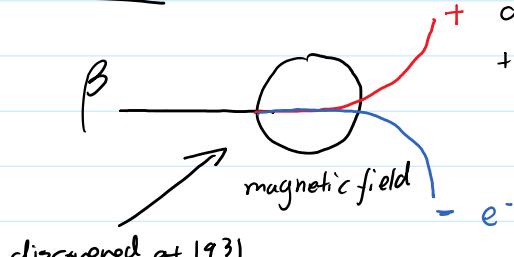
$$1 \text{ MeV} = 1 \times 10^6 \text{ eV} = 1.6 \times 10^{-13} \text{ J}$$

more frequent unit



amount of energy given to  $e^-$  in a field with 1V p.d. / accelerate by field of 1V

## Positrons



a particle that's the antiparticle of the electron  $\Rightarrow$  same mass / opposite charge

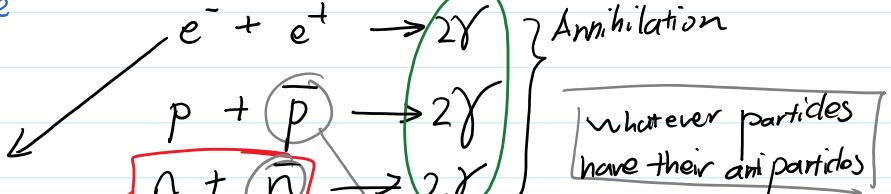
positron.

	charge	mass
$e^-$	-1	$\frac{1}{1860}$
$e^+$	+1	$\frac{1}{1860}$

discovered at 1931  
by Carl Anderson

$$E = mc^2 = 2 \times 9.1 \times 10^{-31} \text{ kg} \times (9 \times 10^8)^2$$

1.02  $\text{eV}$  can't distinguish by 1 meV



disappear releasing pure energy

Annihilation

whatever particles have their anti-particles

If they touch and disappear

they don't distinguish by charge  
so we only know that when they touch

antiproton  
antineutron

if they touch and disappear,  
then they are antiparticles

Every particles has its own antiparticles (represented by dash above except  $e^+$ )

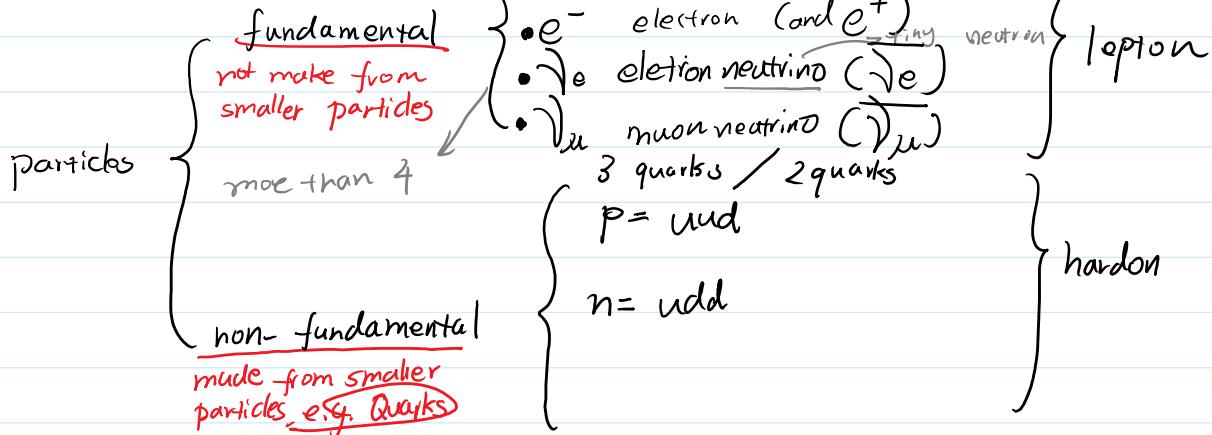
particles + antiparticles  $\rightarrow$  Annihilation (pure energy release in  $\gamma$ )

must totally convert into energy

pair production

note this could also happen by reverse:  $2\gamma \rightarrow e^+ + e^- / p + \bar{p} / n + \bar{n}$

### classifying Particles



Quarks	flavour	symbol	charge/e
6-type	up	u	+2/3
	down	d	-1/3
	strange	s	-1/3
	charm	c	+2/3
	top	t	+2/3
	bottom	b	-1/3

why the charge is still quantised  
even the quarks are fraction of elementary charge

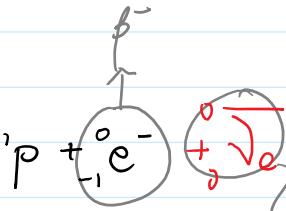
Quarks are not in there own  
they are all in the way to make a charge  
that makes elementary charge

### closer look to $\beta^-$ decay

directly means

$\beta^-$  decay  $\Rightarrow \beta^-$  decay

${}^1_n \rightarrow {}^1_p + {}^0_{-1} \bar{e}$



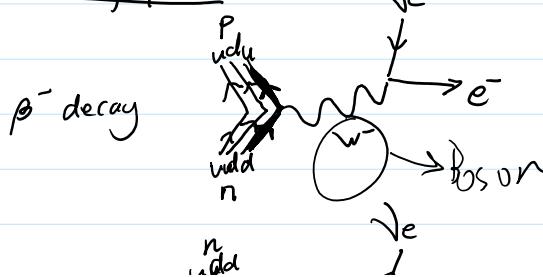
This is the complete reaction  
high penetration

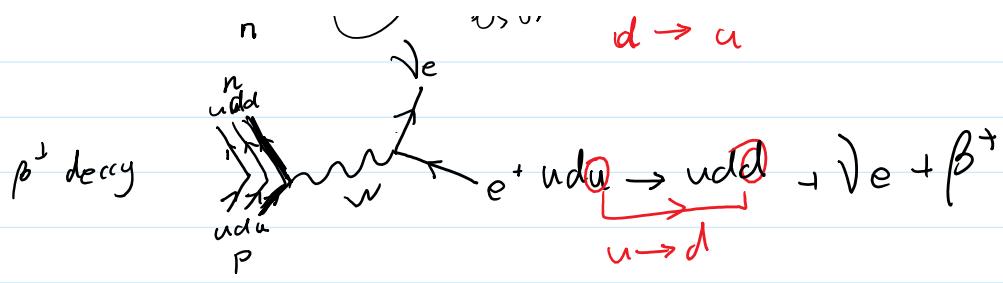
not easy to detect (a Nobel prize)

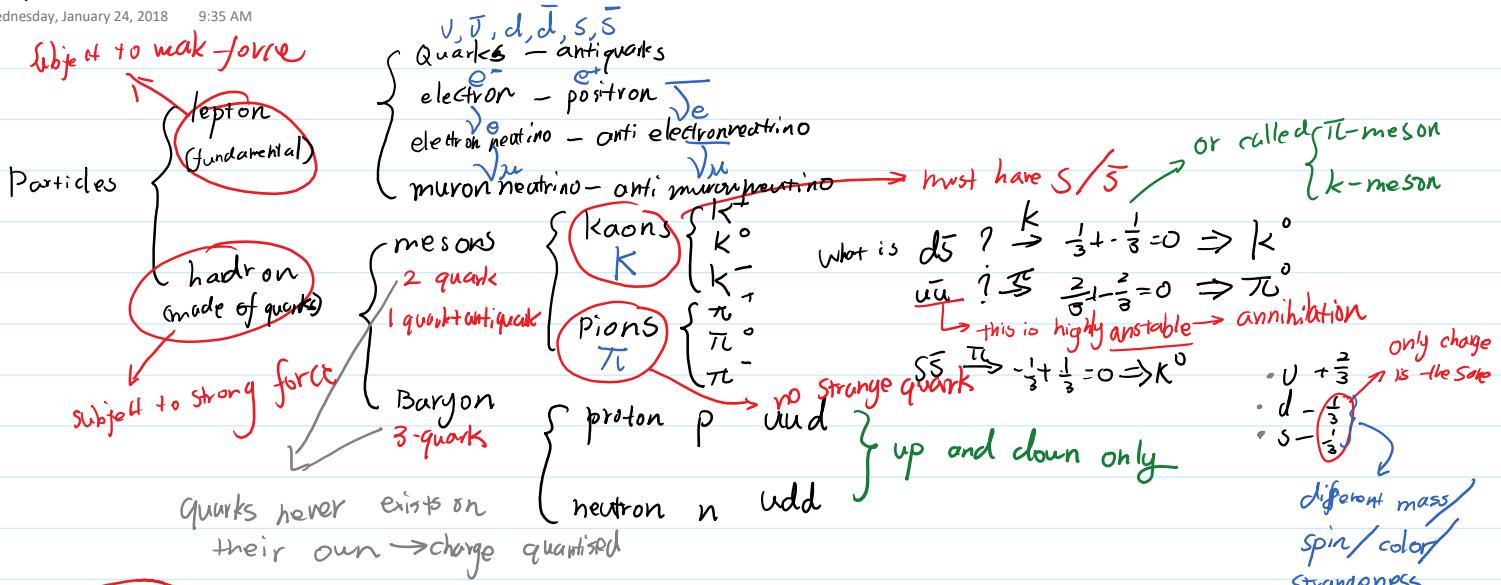
$e^- \rightarrow e^-$  to know

- fundamental particles
- disappear when stop
- move at C
- no charge
- can not stop
- very small but not negligible mass

### In terms of quark





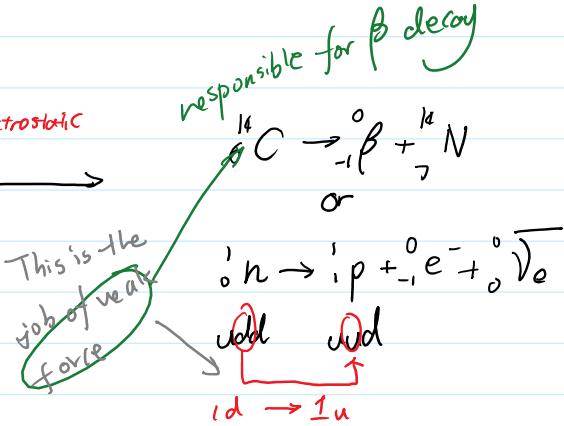
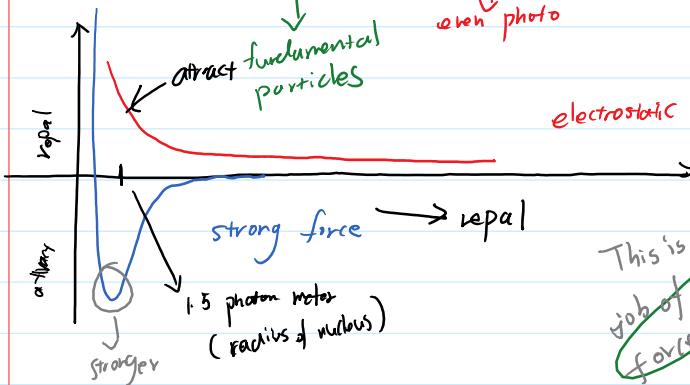


## Fundamental Forces

Force we can not explain their origin (we can describe it)

	subject
strong force	hold nucleons, quarks together
weak force	responsible for $\beta/\gamma$ decay acts on leptons
electromagnetic force	anything which has charge
gravitational force	anything which has mass

	weak	electromagnetic	strong
quarks	✓	✓	✓
charged lepton	✓	✓	✗
uncharged lepto	✓	✗	✗



## GCA

- energy skate park MCQ

WaveDefinition

Wave is the pattern of disturbances which transport energy and does NOT transport matter

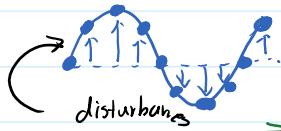
main properties of waves

• no disturbances

• Seismic wave → Right-angle vibration

• transverse → particles (or fields) vibrate at right angle to the wave's propagation

• all e.m. wave



energy transported

only goes up and down

• sound longitudinal → particles vibrate along the direction of the wave's propagation

• shiny spring → particles vibrate along the direction of the wave's propagation

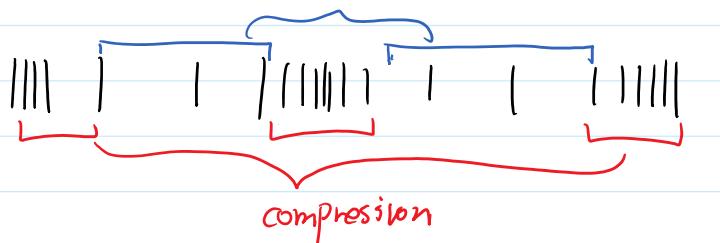
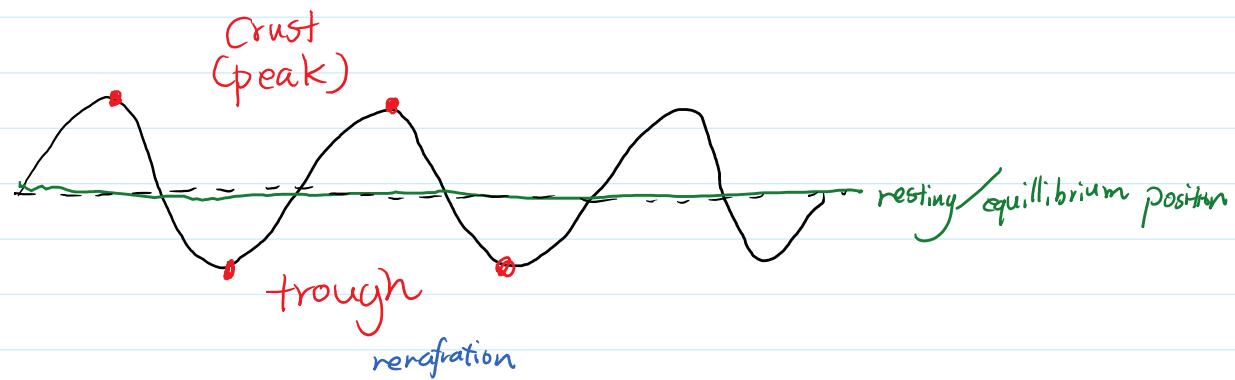
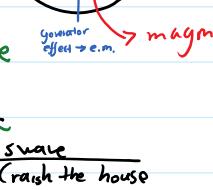
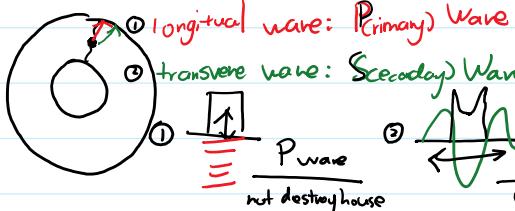
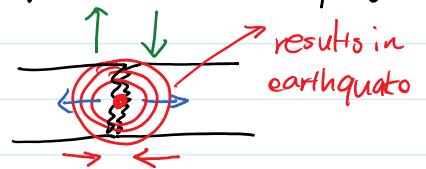
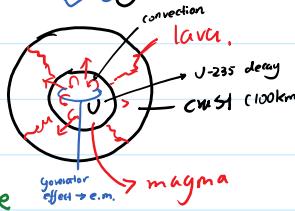
• Seismic wave → Earthquakes wave

direction where energy is transported to

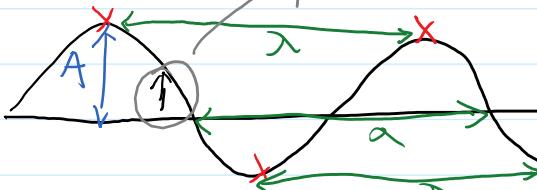
No fields

particles (or fields) vibrate at right angle to the wave's propagation

particles vibrate along the direction of the wave's propagation

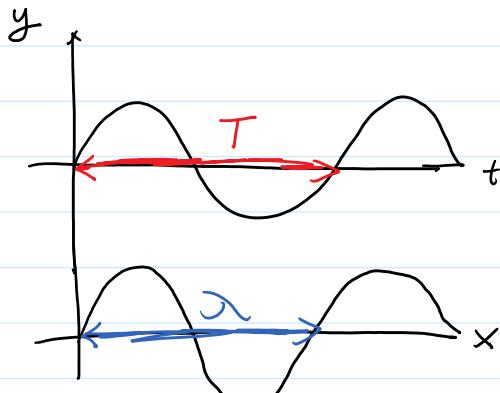
Variables describing waves

- amplitude ( $A$ ) [m] — maximum disturbance / maximum displacement / distance from crest to crest
- wave length ( $\lambda$ ) [m] — distance between two consecutive disturbances / adjacent crest

- wave length ( $\lambda$ ) [m] — distance between two consecutive <sup>(nearest)</sup> disturbances / adjacent crest
- 
- displacement
- $\lambda$

- frequency — number of waves made ( $f$ ) [Hz] in one second  $[s^{-1}]$   $T = \frac{1}{f} \Leftrightarrow f = \frac{1}{T}$

- Period — time taken to make one wave  $(T)$  [s]



- Velocity (ULM)

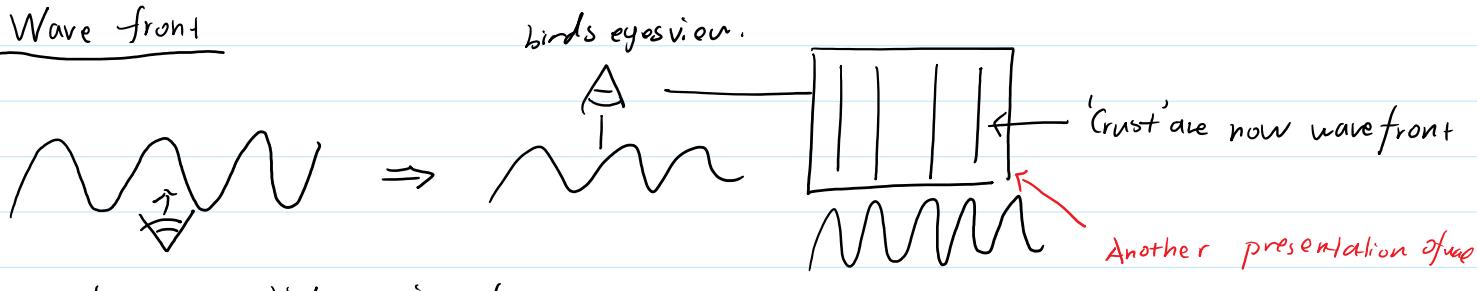
$$V = \frac{S}{t} = \frac{\lambda}{T} = f\lambda$$

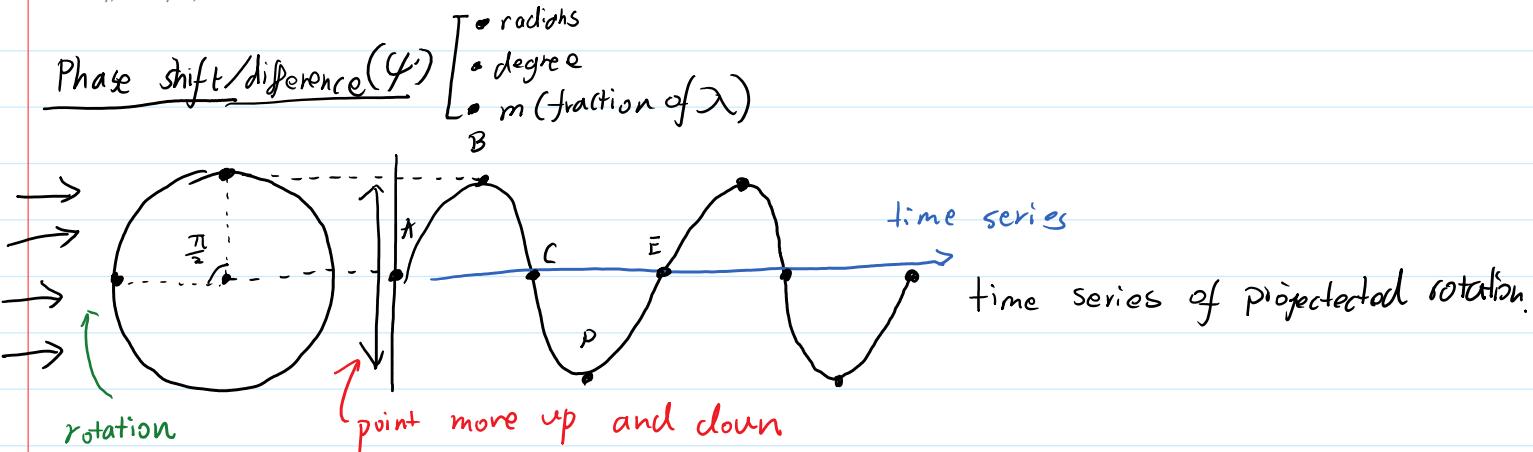
$[m/s]$

wave equation

e.m. wave  $\Rightarrow C = \lambda f$  <sup>inverse proportion</sup>

### Wave front





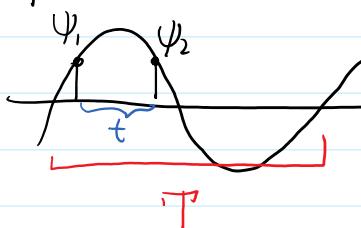
$$\Rightarrow \psi_{AB} = \frac{\pi}{2} \text{ rad} = 90^\circ = \frac{1}{4}\lambda$$

$$\psi_{AE} = \pi \text{ rad} = 180^\circ = \frac{1}{2}\lambda$$

Unit must be added

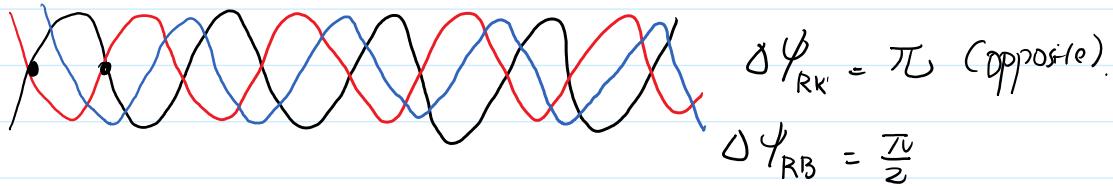
} apply to these also by using correct t respond to T

- point



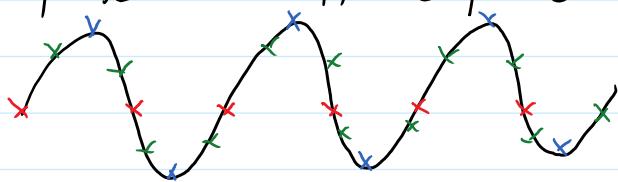
$$\Delta\psi = \frac{2\pi}{T} \cdot t$$

- wave



Inphase  $\rightarrow$  moving identically in the same phase

Antiphase  $\rightarrow$  in opposite phase

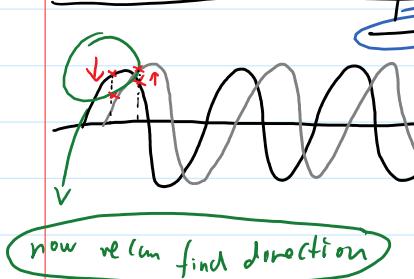


Red Red  $\Rightarrow \Delta\psi = 2k\pi \rightarrow$  inphase

Red blue  $\Rightarrow \Delta\psi = (2k+1)\pi \rightarrow$  antiphase

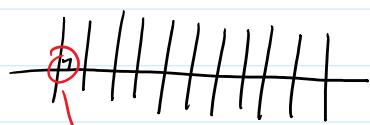
Red green  $\Rightarrow \Delta\psi = \text{any other} \rightarrow$  out of phase

which direction the particle oscillate?



direction required

Ray:



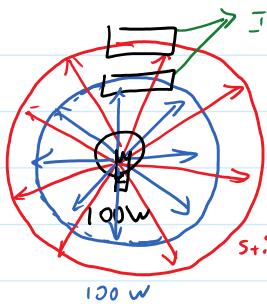
perpendicular to the direction

another way in  $(t+1)$

Notice: for crest and trough are not moving at  $t$  (i.e. they are stationary point)

### Intensity of the wave

$$I = \frac{E}{A} = \frac{P}{A} \quad (\text{Energy per Unit time per Unit Area}) \quad \left[ \frac{W}{m^2} \right]$$

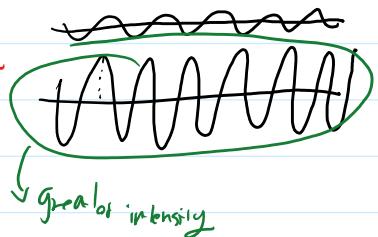


$$\text{Intensity not the same.}$$

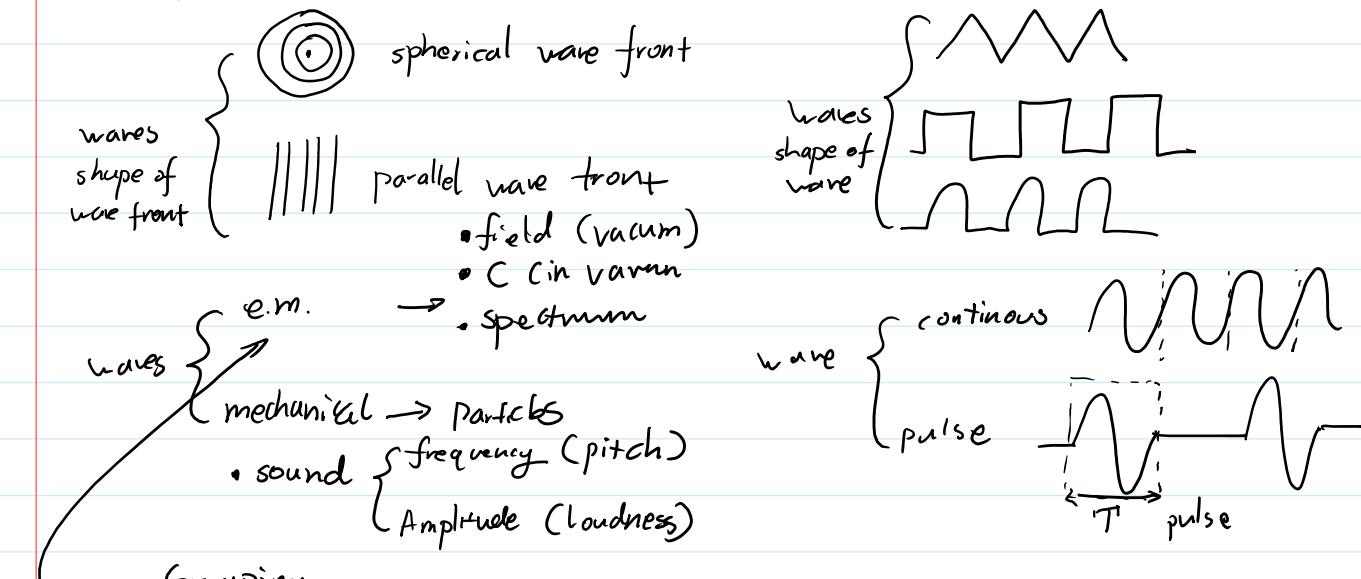
$$\text{① } I = \frac{1}{d^2} \quad \text{Inverse Square.}$$

$$\text{② } I \propto A^2 \quad \text{amplitude} \quad \text{Direct Square}$$

$$\frac{I}{A^2} = \text{constant}$$

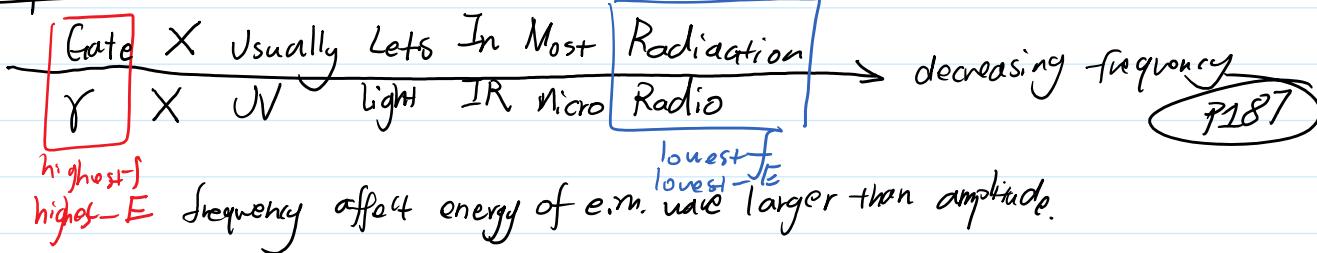


### Classifying waves

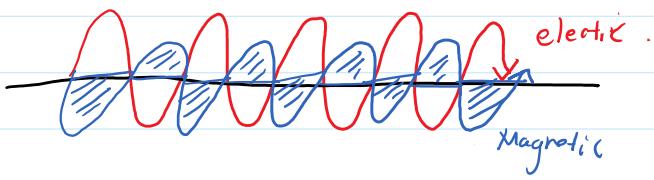


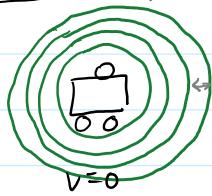
### Grouping

#### e.m. spectrum



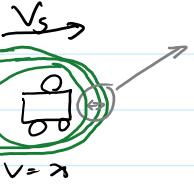
Make E.M. wave.



Doppler Effect

$\lambda \uparrow$   
 $f \downarrow$   
 wavelength for observer

These effects are called Doppler effect



wave length for observer  
 $\lambda \downarrow$   
 $f \uparrow$



observer hears higher f when sound approaches, when goes away hear lower f

- apparent change in frequency for an observer, when the source of sound is moving

$$f_o = \frac{f_s V}{V \pm V_s}$$

O-observer

S-source

V-real speed of waves in the medium

$$f_o = \frac{f_s V}{V + V_s}$$

moving away (smaller f)

$$f_o = \frac{f_s V}{V - V_s}$$

moving toward (bigger f)

Derivation

- for 1s

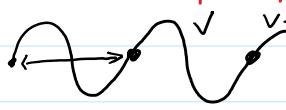
$$S = Vt = V \text{ (numerical value)}$$

$$\xrightarrow{V_s}$$

for a moving source away at  $V_s$

$$S_o = (V + V_s)t = V + V_s \text{ (numerical value)}$$

- 



$$S = 6 \text{ m (in 1s)}$$

$$N = 4 \Rightarrow \lambda = \frac{S}{N} = \frac{6}{4} = \frac{3}{2}$$

- case a:

$$V_s = 0$$

case b:

away at  $V_s$

$$\lambda_o = \frac{S}{N} \text{ (takes 1s)} \Rightarrow \lambda_o = \frac{S}{N} = \frac{V + V_s}{f_s}$$

$$= \frac{V}{f_s}$$

transform

$$f_o = \frac{V}{\lambda_o} = \frac{V}{\frac{V + V_s}{f_s}} = \frac{f_s V}{V + V_s}$$

Vice versa for moving towards you

another formula

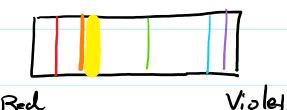
$$\frac{\Delta \lambda}{\lambda_s} = \frac{V_s}{V}$$

Doppler effects apply to all waves (e.m. waves)  
 but its name only apply to sound.

For light and e.m. wave  $\Rightarrow$  the name is red shift

$$f_o = \frac{f_s c}{V_s \pm c}$$

spectrum



Richard of York gave battle in vain

Red orange yellow green blue indigo Violet

lowest f  
 highest λ  
 smallest E

highest f  
 lowest λ  
 highest E

G X U I M R  
 V I R G Y O R

