

Class Note

Friday, September 22, 2017

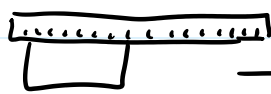
10:16 AM

Uncertainty

certain means 100% sure

uncertain means not 100% sure

Using a ruler to measure something



$$L = 11.2 \text{ cm}$$

$$L = 11.2 \pm 0.1 \text{ cm} \quad (\text{relative uncertainty})$$

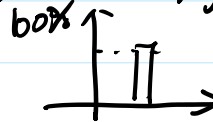
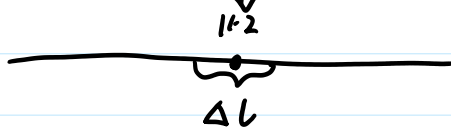
Uncertainty
(2 type)

ΔL (range)

$\frac{\Delta L}{L}$ (quality)

percentage uncertainty

The true value lies between the relative uncertainty gap



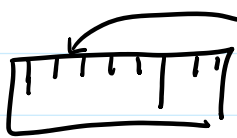
quality of data

$\frac{\Delta L}{L}$ percentage uncertainty → the ratio of the uncertainty over total

ΔL relative uncertainty

measurement:

(for 99% of measurement)

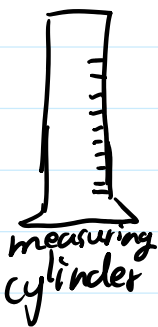


1 mm gap → uncertainty is $\frac{1}{2}$ of smallest gap

Δ (start point + end point) = 1 smallest gap.

Δ uncertainty = smallest division

however there is some few exception



measuring cylinder

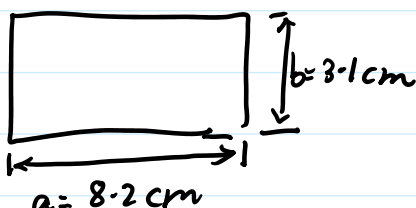


thermometer

← the zero is already dealt with by the design

Δ uncertainty = $\frac{1}{2}$ smallest gap (division)

Calculation:



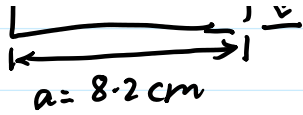
no multiplication

find $P = 2(a+b) = a+a+b+b$

$$P = 2(a+b) = 22.6 \text{ cm} \quad \Delta P = 0.1 + 0.1 + 0.1 + 0.1 = 0.4$$

$$P = 22.6 \pm 0.4 \text{ cm}$$

contain multiplication



$$p = 22.6 \pm 0.4 \text{ cm}$$

contain multiplication

$$A = ab$$

2-3 s.f (have something)

$$a = 8.2 \pm 0.1 \text{ cm} \quad b = 3.1 \pm 0.1 \text{ cm}$$

$$A = ab = 8.2 \times 3.1 = 25.4 \text{ cm}^2$$

$\left\{ \begin{array}{l} + / - : \text{ add relative uncertainty} \\ * / \div : \text{ add percentage uncertainty} \end{array} \right.$

$$A = 25.4 \pm \Delta A$$

not need percentage for further calculation

$$\frac{\Delta A}{A} = \frac{\Delta a}{a} + \frac{\Delta b}{b} = \frac{0.1}{8.2} + \frac{0.1}{3.1} = 0.044$$

decimal point need to be identical $\rightarrow \Delta A = A \cdot \frac{\Delta A}{A} = 25.4 \cdot 0.044 = 1.1$

however, if

$$A = \frac{C^3 \cdot V^2}{\sqrt{t}}$$

← find each individual and then combine together

$$\frac{\Delta A}{A} \approx \frac{\Delta C}{C} + 2 \frac{\Delta V}{V} + \frac{1}{2}$$

Do the example at home on the ppt in a separate sheet

Run the uncertainty ppt

Assignment book p16-18

Bring AS Lab book

★ If we are having multiple Δ for calculation, the Δ is the smallest possible number of decimal point in all of the number

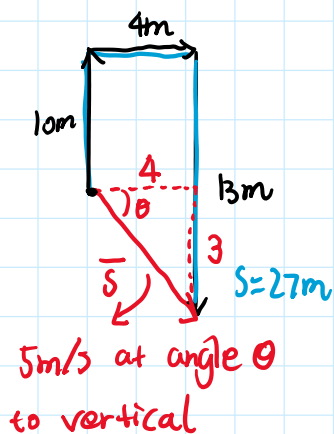
Vectors

Quantities

vector : quantity has both direction and magnitude size / number / numerical value

Scalar : has magnitude only

frequently asked question: Is this a vector / scalar



Vectors	Scalar
<ul style="list-style-type: none"> • velocity (\vec{v}) • displacement (\vec{s}) • Force (\vec{F}) (weight/tension/friction) • acceleration (\vec{a}) • momentum (\vec{mv}) 	<ul style="list-style-type: none"> • speed (v) • distance (s) • mass (m) • temperature (t) • moment • electric field strength (in AS level)

velocity is written as \vec{v} / v

distinguish between speed and velocity

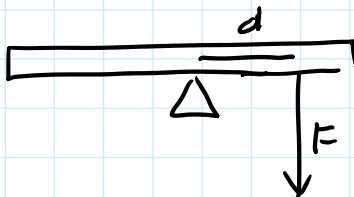
! \vec{v} means vector, not average!

The other are just scalar

if it's not vector.

The total 5 Vector you need to know in AS

Strange Vector in consideration:

Vector . scalar usually is Vector (99%) $V \cdot s$ 

$F \cdot d$ is a scalar (strictly a vector, but...)

① exception: moment

$E = \frac{F}{Q} \rightarrow \frac{\text{Vector}}{\text{Scalar}}$ should be Vector, but we make it scalar.

② exception: electric field strength

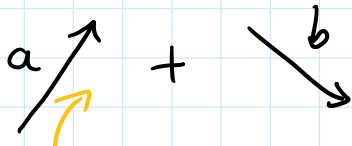
$W = \vec{F} \cdot \vec{s} \rightarrow \text{Vector} \cdot \text{Vector}$ results in a scalar

Operation with Vector

① Adding

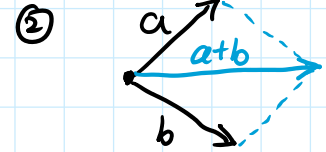
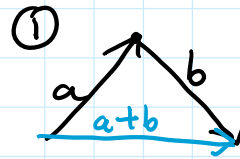
2 rules

① Adding



$$\vec{a} + \vec{b}$$

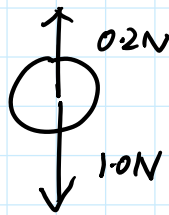
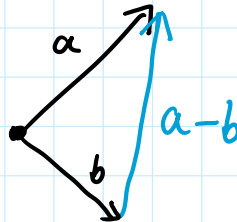
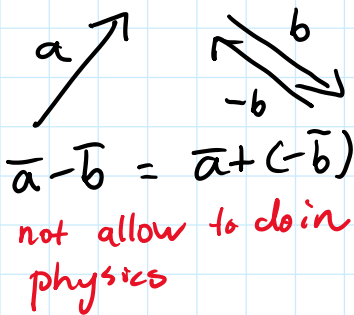
2 rules



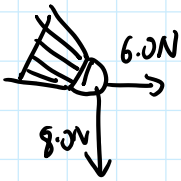
These are called coplanar vector (on the same plane)
collinear vector (belong to the same line)

② subtracting

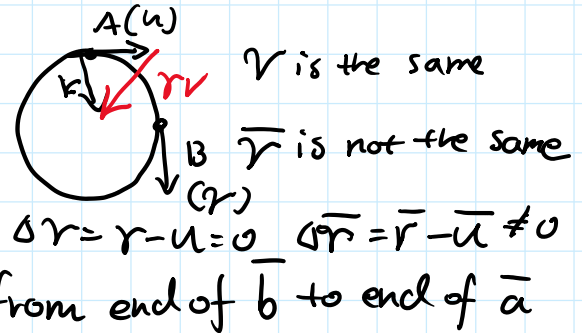
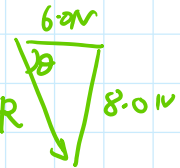
$\vec{a} - \vec{b}$ (from b to a) rules:



$$\vec{R} = 0.8 \text{ N downwards}$$

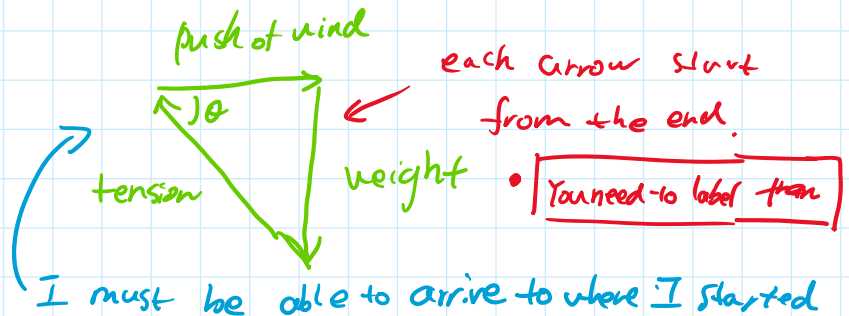
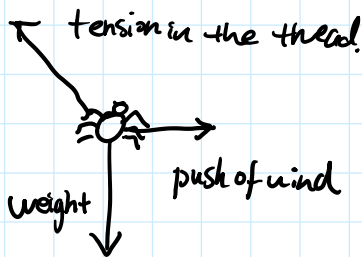


$$\vec{R} = 10.0 \text{ N}, 53^\circ \text{ downwards from vertical}$$



③ Vector triangle

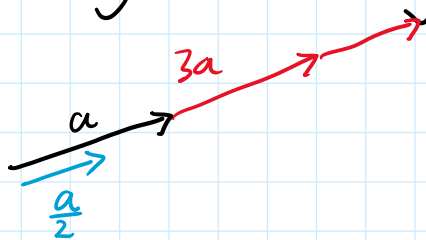
if the net force is 0, then it's equilibrium, and force will create the vector triangle



the drawing of vector triangle might be different, but they are all vector triangle.

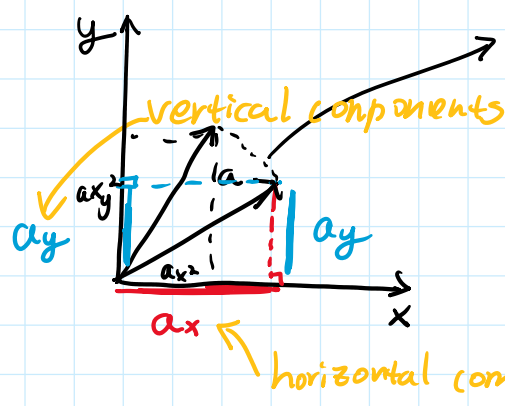
④ Timing and dividing

④ Timing and dividing



all of these primitive operation is used to describe complex things.

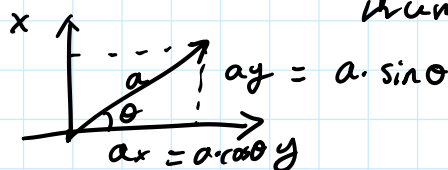
Resolving vectors \rightarrow change it to scalars



totally describe the direction

$$a = \sqrt{a_x^2 + a_y^2}$$

only operates with number



use sine rule and cosine rule

⑤ Projecting Vectors

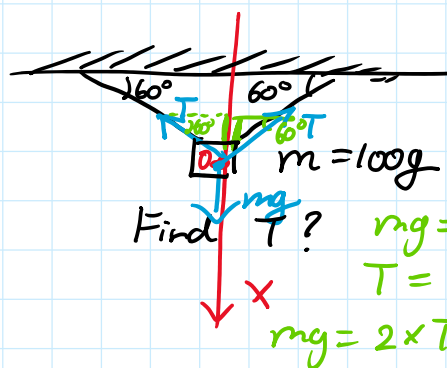
\hookrightarrow do on any axis (not the x-y axis on resolving)

worked example

1) draw free body diagram

2) chose axes

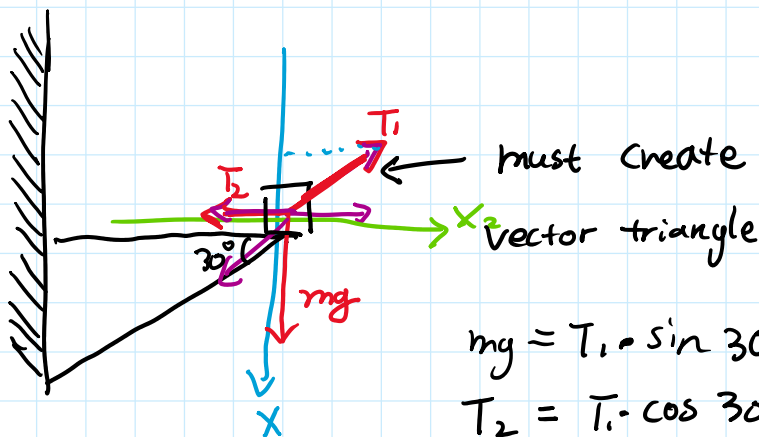
3) put perpendicular line



$$mg = mg$$

$$T = T \sin 60^\circ$$

$$mg = 2 \times T \sin 60^\circ$$



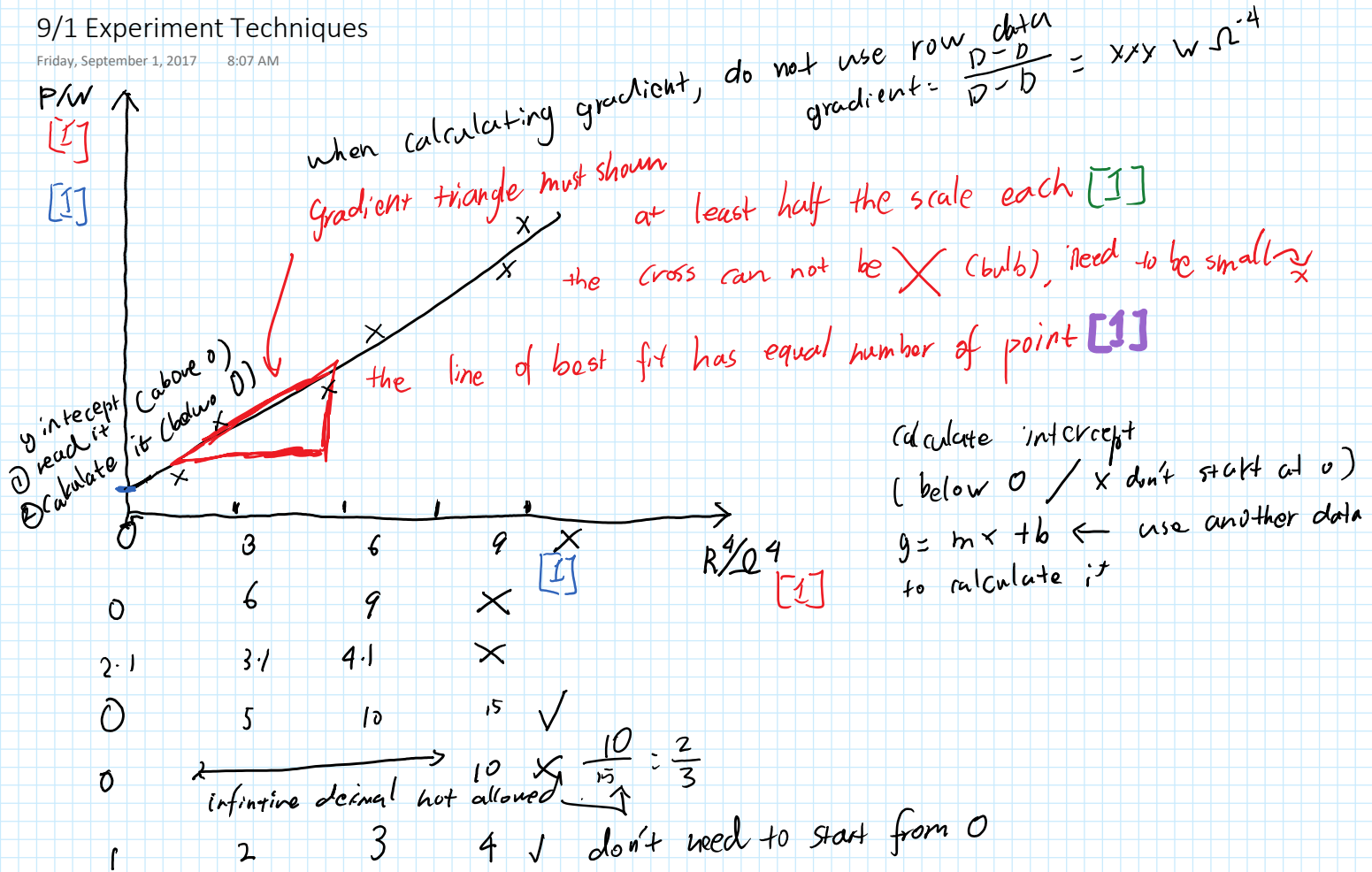
$$mg = T_1 \sin 30^\circ$$

$$T_2 = T_1 \cos 30^\circ$$

combine and get the result.

9/1 Experiment Techniques

Friday, September 1, 2017 8:07 AM



9/6: Inertia

Wednesday, September 6, 2017 10:32 AM

Inertia

Inertia is reluctance of objects to change the speed

- It takes time for an object to change the speed
- Mass is the measure of inertia
 - The longer the mass, the longer the time require to change the speed

Kinematics
(motion)

ULM
uniform linear motion
(steady speed motion)

definition:

means object covers = distances during equal times

formula:

$$V = \frac{s}{t} \quad V \text{ is rate of change of } s$$

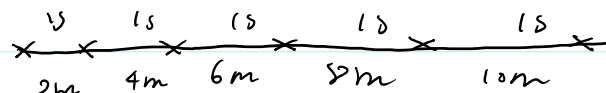
m/s or km/h

plasticine
modeling clay
blue tel

→ constant change of velocity

uniform acceleration motion
(constant acceleration)

UAM



change in speed = 2m/s

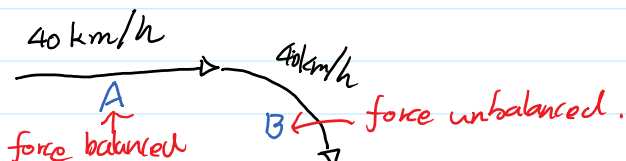
$$a = 2\text{m/s}^2$$

Δ (delta → change)

$$\vec{a} = \frac{\Delta v}{t}$$

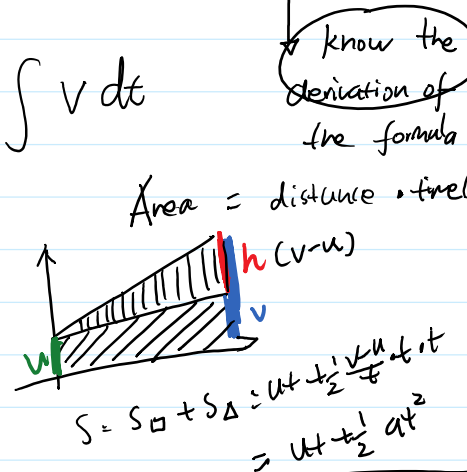
acceleration is the rate of change of velocity

20 min = ~~$\frac{1}{3}$~~ no fraction as the final answer! (allow in intermediate)



no h/min/km for acceleration!
only m/s^2 !

$$S = \int v dt$$



$V = u + at$ (from definition $a = \frac{v-u}{t}$)
 $a = \frac{\Delta v}{t} = \frac{v-u}{t} \quad at = v-u$

$S = \frac{1}{2} (v+u) t$ (distance is the area of velocity v.s. time)

$S = \frac{1}{2} (v+u) \cdot t$

$S = vt - \frac{1}{2} at^2$

$S = u + \frac{1}{2} at^2$

$v^2 - u^2 = 2as$ (by multiplying from v and u)

$S = \frac{u(v-u)}{a} + \frac{1}{2} a \frac{(v-u)^2}{a^2} = \frac{2u(v-u) + (v-u)^2}{2a}$

$$\downarrow$$

$$2as = 2u(v-u) + (v-u)^2 = \cancel{2u^2} - 2u^2 + v^2 - \cancel{2v^2} + 2u^2 = v^2 - u^2$$

the first five seconds of motion initial speed = 0

$$V_{\text{average}} = \text{average speed} = \frac{\text{total distance traveled}}{\text{total time taken}}$$

UAM
ULM

$$\text{average velocity} = \frac{\text{total displacement travelled}}{\text{total time taken.}}$$

work example $\xrightarrow[60\text{km/h}]{40\text{km/h}}$ $t_1 \neq t_2$

$V_{\text{average}} = ?$

[3]

$$V_{\text{average}} = \frac{S_{\text{total}}}{t_{\text{total}}} = \frac{2S}{t_1 + t_2} = \frac{2S}{\frac{S}{V_1} + \frac{S}{V_2}} = \frac{2}{\frac{1}{V_1} + \frac{1}{V_2}} = \frac{2V_1V_2}{V_1 + V_2}$$

Falling Under Gravity: ($g = 9.81 \text{ m/s}^2$).