

Please send the pdf file to my email: zhaoruitong1986@163.com.

Deadline 2016-11-16 before class.

1. The trace of a matrix is the sum of the eigenvalues of this matrix. If  $\sigma_x = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$ , validate it.
2.  $X = \int dx |x\rangle\langle x|$ ,  $Y = \int dy |y\rangle\langle y|$ ,  $Z = \int dz |z\rangle\langle z|$ . Prove  $[X, Y] = [Y, Z] = [X, Z] = 0$ .
3. Prove: (1) Translation operator  $T_a$  is unitary.  
(2)  $[T_a, T_b] = 0$ ;  $T_a + T_b = T_{a+b}$ .