

# Solutions to Pathria's Statistical Mechanics

## Chapter 7

SM-at-THU

April 24, 2016

### Problem 7.1

### Problem 7.4

We can deduce from 7.1.30 and 7.1.26a, when  $p$  is a const:

$$g_{\frac{5}{2}} \propto T^{-\frac{5}{2}}$$

So we have:

$$\left(\frac{\partial}{\partial T} g_{\frac{5}{2}}(z)\right)_p = -\frac{5}{2T} g_{\frac{5}{2}}(z)$$

According to the D.10 from appendix D:

$$z \frac{\partial}{\partial z} g_{\frac{5}{2}}(z) = g_{\frac{3}{2}}(z)$$

Combine the two equation:

$$\frac{1}{z} \left(\frac{\partial z}{\partial T}\right)_p = -\frac{5}{2T} \frac{g_{\frac{5}{2}}(z)}{g_{\frac{3}{2}}(z)}$$

If you compare with 7.1.36 you can get:

$$\gamma = \frac{5}{3} \frac{g_{\frac{5}{2}}(z) g_{\frac{1}{2}}(z)}{g_{\frac{3}{2}}(z)^2}$$

### Problem 7.14

From the definition of  $p$  and  $U$ :

$$p = \frac{kT}{\lambda^n} g_{\frac{5}{2}}(z)$$
$$U = \frac{nkTV}{s\lambda^n} g_{\frac{5}{2}}(z)$$

So we get:

$$p = \frac{sU}{nV}$$

And when  $T \rightarrow \infty$ , we could use the ideal gas equation.

$$pV = nRT$$

So

$$C_V = \frac{n}{s} Nk, C_p = \left(\frac{n}{s} + 1\right) Nk$$

## Problem 7.24

We can deduce from 7.3.12 and 7.3.19 and 7.3.23.

$$u = 4.16 * 10^{-14}$$

$$s = 2.03 * 10^{-14}$$

$$n = 4.09 * 10^8$$

## Problem 7.34

For the n-dimensional Debye system, we can get the function of state number:

$$g(\omega) \propto \begin{cases} 0 & (\omega > \omega_D) \\ \omega^{n-1} & (0 < \omega < \omega_D) \end{cases}$$

Then we consider the energy of the Debye system:

$$U_{ph} \propto \int_0^{\omega_D} \frac{\omega^n}{\exp(\beta \hbar \omega) - 1} d\omega \propto T^{n+1}$$

We can know the specific heat from thermodynamics:

$$C_V = \left( \frac{\partial U}{\partial T} \right)_V \propto T^n$$