

O que George Boole tem a ver com Ciência de Dados?

Pesquisando relações entre lógica e ciência de dados

Cássia Sampaio

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Já ouviu falar em **booleano**?

Tipo de variável

```
>>> bool(1)
True
>>> bool(0)
False
>>> bool([])
False
>>> bool( (1,) )
True
```

PEP 285

Operadores lógicos

```
1 A = True
2 B = False
3 print ("Valor de A and B: ", A and B)
4
```

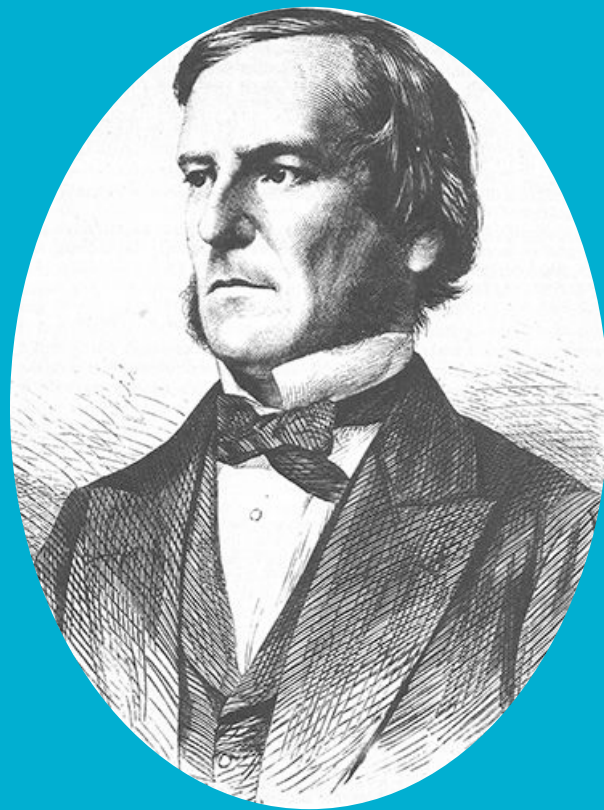
```
['Valor de A and B: ', False]
```

Expressões

```
1 a = 3
2 b = 4
3 c = a < b    # c recebe o valor da comparação a < b
4 d = a > b    # d recebe o valor da comparação a > b
5 e = a == b   # e recebe o valor da comparação a == b
6
7 print("Valor de c: ", c)
8 print("Valor de d: ", d)
9 print("Valor de e: ", e)
```

```
['Valor de c: ', True]
['Valor de d: ', False]
['Valor de e: ', False]
```

Georginho



Georginho e Data Science? Será?

Me propus a entender.



Tem ligação?

—

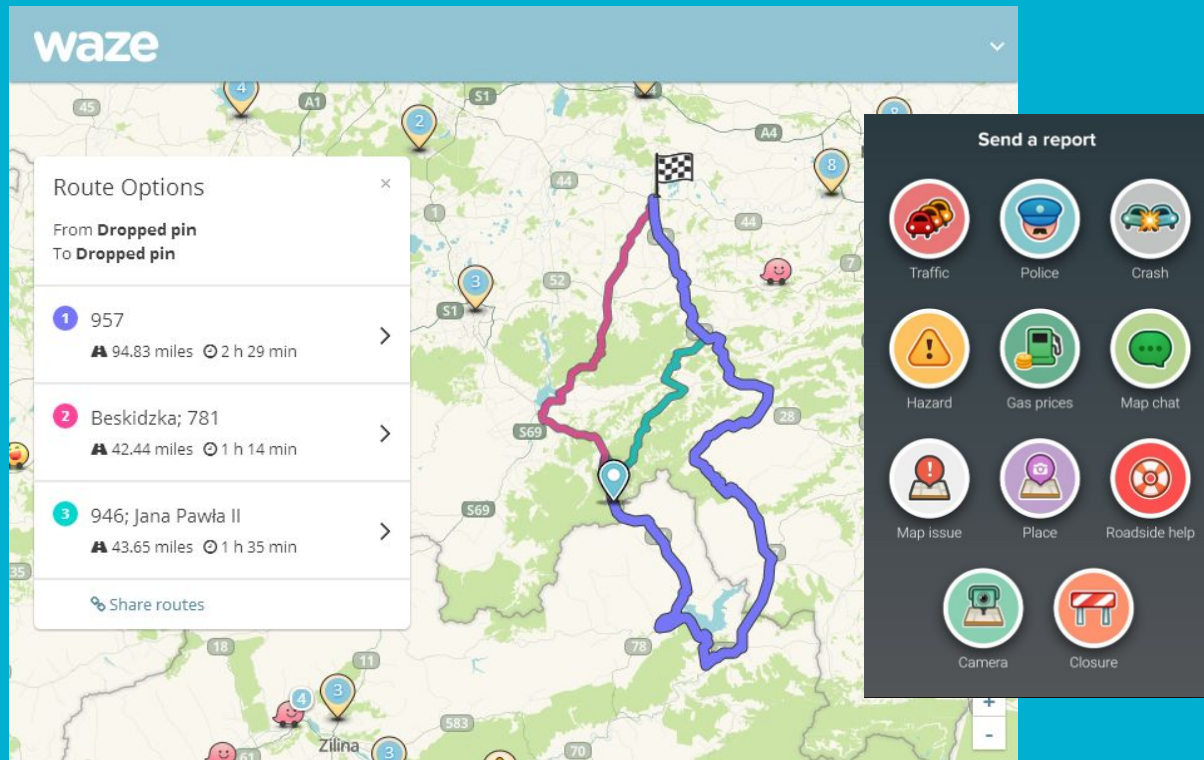
Não tem ligação?

—

Pensa no Waze



Estimativa por crowdsourcing



Estimativa por crowdsourcing



Estimativa por crowdsourcing

$$\begin{array}{c} \text{Car crash} \\ \text{Car crash} \end{array} + \begin{array}{c} \text{Traffic jam} \end{array} = 80\%$$

$$\begin{array}{c} \text{Car crash} \end{array} + \begin{array}{c} \text{Traffic jam} \\ \text{Traffic jam} \end{array} = 70\%$$

$$\begin{array}{c} \text{Traffic jam} \end{array} = 30\%$$

Estimativa por crowdsourcing

$$\text{Car Crash} + \text{Car Crash} \leq 80\%$$

$$\text{Car Crash} + \text{Car Crash} \leq 70\%$$

$$\text{Car Crash} \leq 30\%$$

Estimativa por crowdsourcing

$$2a + 1t \leq 80\%$$

$$1a + 2t \leq 70\%$$

$$1t \leq 30\%$$

Estimativa por crowdsourcing

2 + 1t <= 80%

1 + 2t <= 70%

1t <= 30%

Estimativa por crowdsourcing

2 + 1 \leq 80%

1 + 2 \leq 70%

1 \leq 30%

Estimativa por crowdsourcing

$$2 + 1 \leq 0.8$$

$$1 + 2 \leq 0.7$$

$$1 \leq 0.3$$

Estimativa por crowdsourcing

$$\begin{bmatrix} 2 & 1 \\ 1 & 2 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.7 \\ 0.3 \end{bmatrix}$$

Estimativa por crowdsourcing



Estimativa por crowdsourcing

$$1a + 1t = ?$$

Estimativa por crowdsourcing

$$\begin{bmatrix} 1 & 1 \end{bmatrix} = ?$$

Função objetiva

$$\begin{bmatrix} 1 & 1 \end{bmatrix} = ?$$

Scipy linprog


```
from scipy.optimize import linprog
```


Scipy linprog

```
from scipy.optimize import linprog  
coeficientes_da_funcao_objetiva = [-1, -1]
```

Scipy linprog

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Scipy linprog

```
from scipy.optimize import linprog  
  
coeficientes_da_funcao_objetiva = [-1, -1]  
  
coeficientes_das_inequacoes = [[2, 1],  
                                [1, 2],  
                                [0, 1]]
```

Scipy linprog

```
from scipy.optimize import linprog
```

```
coeficientes_da_funcao_objetiva = [-1, -1]
```

```
coeficientes_das_inequacoes = [[2, 1],  
                                [1, 2],  
                                [0, 1]]
```

```
valores_maximos = [0.8,  
                   0.7,  
                   0.3]
```

Scipy linprog

```
res = linprog(coeficientes_da_funcao_objetiva,  
              coeficientes_das_inequacoes,  
              valores_maximos,  
              bounds=(valor_min_e_max_de_a, valor_min_e_max_de_t),  
              method='simplex')  
print(res)
```

Scipy linprog

```
from scipy.optimize import linprog

coeficientes_da_funcao_objetiva = [-1, -1]

coeficientes_das_inequacoes = [[2, 1],
                                [1, 2],
                                [0, 1]]

valores_maximos = [0.8,
                   0.7,
                   0.3]

valor_min_e_max_de_a = (0, None)
valor_min_e_max_de_t = (0, None)

res = linprog(coeficientes_da_funcao_objetiva,
               coeficientes_das_inequacoes,
               valores_maximos,
               bounds=(valor_min_e_max_de_a, valor_min_e_max_de_t),
               method='simplex')

print(res)
```

Scipy linprog

```
(lp) cassia@galadriel:~/lp$ python simplex.py
con: array([], dtype=float64)
fun: -0.5
message: 'Optimization terminated successfully.'
nit: 3
slack: array([0. , 0. , 0.1])
status: 0
success: True
x: array([0.3, 0.2])
```

$$a = 0.3 \quad t = 0.2$$

Scipy linprog

$$a = 0.3 \quad t = 0.2$$

$$\text{🚗💥🚗} + \text{🚗🚗🚗} = 50\%$$

Matrizes

```
import numpy as np

coeficientes_das_inequacoes = np.matrix('0 2 1 ; 0 1 2 ; 0.1 0 1')

resultados = np.matrix('1; 0.3; 0.2')

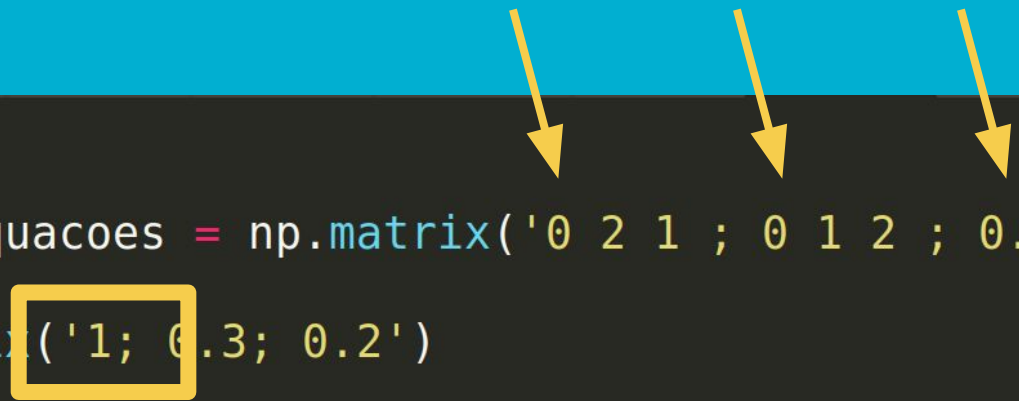
print(coeficientes_das_inequacoes*resultados)
```

Matrices

```
(lp) cassia@galadriel:~/lp$ python matrix.py  
[[0.8]  
 [0.7]  
 [0.3]]
```

Matrizes

```
import numpy as np
coeficientes_das_inequacoes = np.matrix('0 2 1 ; 0 1 2 ; 0.1 0 1')
resultados = np.matrix('1; 0.3; 0.2')
print(coeficientes_das_inequacoes*resultados)
```



Scipy linprog

```
(lp) cassia@galadriel:~/lp$ python simplex.py
  con: array([], dtype=float64)
  fun: -0.5
message: 'Optimization terminated successfully.'
  nit: 3
  slack: array([0. , 0. , 0.1])
status: 0
success: True
   x: array([0.3, 0.2])
```

Scipy linprog

```
res = linprog(coeficientes_da_funcao_objetiva,  
              coeficientes_das_inequacoes,  
              valores_maximos,  
              bounds=(valor_min_e_max_de_a, valor_min_e_max_de_t),  
              method='simplex')  
print(res)
```

Estimativa por crowdsourcing

$$\begin{bmatrix} 2 & 1 \\ 1 & 2 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.7 \\ 0.3 \end{bmatrix}$$

Estimativa por crowdsourcing

$$\begin{bmatrix} 0 \\ 0 \\ 0.1 \end{bmatrix} + \begin{bmatrix} 2 & 1 \\ 1 & 2 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.7 \\ 0.3 \end{bmatrix}$$

Estimativa por crowdsourcing

$$\begin{bmatrix} 0 & 2 & 1 \\ 0 & 1 & 2 \\ 0.1 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.7 \\ 0.3 \end{bmatrix}$$

Estimativa por crowdsourcing

$$\begin{bmatrix} 0 & 2 & 1 \\ 0 & 1 & 2 \\ 0.1 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 \\ 0.3 \\ 0.2 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.7 \\ 0.3 \end{bmatrix}$$

Estimativa por crowdsourcing

slack

a

t

$$\begin{bmatrix} 0 & 2 & 1 \\ 0 & 1 & 2 \\ 0.1 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 \\ 0.3 \\ 0.2 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.7 \\ 0.3 \end{bmatrix}$$

Estimativa por crowdsourcing

$$\begin{array}{c} \text{slack} \\ \begin{bmatrix} 0 & 2 & 1 \\ 0 & 1 & 2 \\ 0.1 & 0 & 1 \end{bmatrix} \end{array} \begin{array}{c} \text{a} \\ \text{t} \end{array} \begin{array}{c} * \\ \end{array} \begin{bmatrix} 1 \\ 0.3 \\ 0.2 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.7 \\ 0.3 \end{bmatrix}$$

Estimativa por crowdsourcing

slack

a

t

$$\begin{bmatrix} 0 & 1+1 & 1 \\ 0 & 1 & 2 \\ 0.1 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 \\ 0.3 \\ 0.2 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.7 \\ 0.3 \end{bmatrix}$$

Estimativa por crowdsourcing

slack

a

t

$$\begin{bmatrix} 0 & 1 & 1 \\ 0 & 1 & 2 \\ 0.1 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 \\ 0.3 \\ 0.2 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.7 \\ 0.3 \end{bmatrix}$$

Estimativa por crowdsourcing

slack

a

t

$$\begin{bmatrix} 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0.1 & 0 & 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 \\ 0.3 \\ 0.2 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.7 \\ 0.3 \end{bmatrix}$$

Estimativa por crowdsourcing

slack $P(a)$ $P(t)$

$$\begin{bmatrix} 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0.1 & 0 & 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 \\ 0.3 \\ 0.2 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.7 \\ 0.3 \end{bmatrix}$$

Probabilidades

$P(a)$		$P(t)$	
1	1	0	1
1	0	1	1
0	0	0	1

Álgebra

$P(a)$		$P(t)$	
1	1	0	1
1	0	1	1
0	0	0	1

Álgebra

$P(a)$ $P(t)$

1	1
---	---

0 1

1 0

1 1

0 0

0 1



P_{11}

Álgebra

$P(a) \quad P(t)$

1 1 | 0 1

1 0 | 1 1

0 0 | 0 1



P_{11}



Álgebra

P(a) P(t)

1 1 | 0 1

1 0 | 1 1

0 0 | 0 1



P_{11}

P_{01}

P_{10}

P_{11}

P_{00}

P_{01}


Álgebra

Tabela verdade

P_{11}	P_{01}	a	t
		0	0
P_{10}	P_{11}	1	1
		0	1
P_{00}	P_{01}	1	0

Álgebra

P_{11}	P_{01}	
P_{10}	P_{11}	
P_{00}	P_{01}	



a	t	
0	0	
1	1	P_{11}
0	1	
1	0	

Álgebra

$$\begin{array}{c|c} P_{11} & P_{01} \\ P_{10} & P_{11} \\ P_{00} & P_{01} \end{array}$$



a	t	
0	0	P_{00}
1	1	P_{11}
0	1	P_{01}
1	0	P_{10}

Álgebra

a	t	
0	0	P_{00}
1	1	P_{11}
0	1	P_{01}
1	0	P_{10}

Acidente e trânsito **ou** só acidente

Trânsito e acidente **ou** só trânsito

Trânsito

Acidente e trânsito = ?

Álgebra

a	t	
0	0	P_{00}
1	1	P_{11}
0	1	P_{01}
1	0	P_{10}

A e t ou a

T e a ou t

T

A e t = ?

Álgebra

A e t o u a

T e a o u t

T

A e t = ?

Álgebra

$A \wedge t$ ou a

$T \wedge a$ ou t

T

$A \wedge t = ?$

Álgebra

$$A \wedge t \vee a$$

$$T \wedge a \vee t$$

$$T$$

$$A \wedge t = ?$$

Álgebra

$$(A \wedge t) \vee a$$

$$(T \wedge a) \vee t$$

$$T$$

$$A \wedge t = ?$$

Álgebra

$$(a \wedge t) \vee a$$

$$(b \wedge a) \vee t$$

$$t$$

$$a \wedge t = ?$$

Álgebra

$((a \wedge t) \vee a)$

$((b \wedge a) \vee t)$

(t)

$(a \wedge t) = ?$

Lógica booleana probabilística

$$P((a \wedge t) \vee a)$$

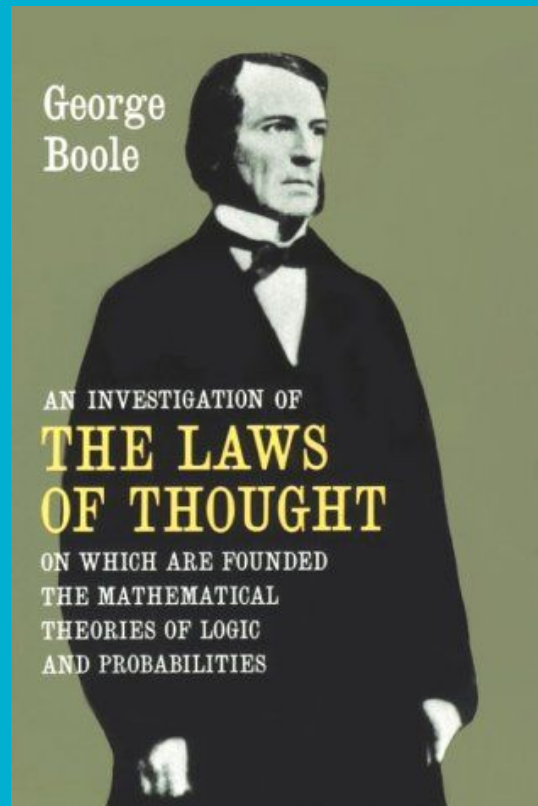
$$P((b \wedge a) \vee t)$$

$$P(t)$$

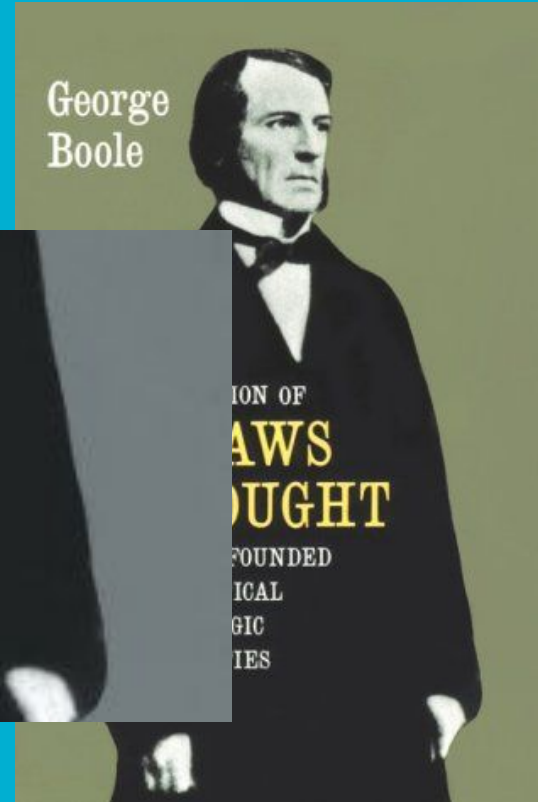
$$P(a \wedge t) = ?$$

Georginho

Leis do Pensamento
[Boole 1854]



Georginho

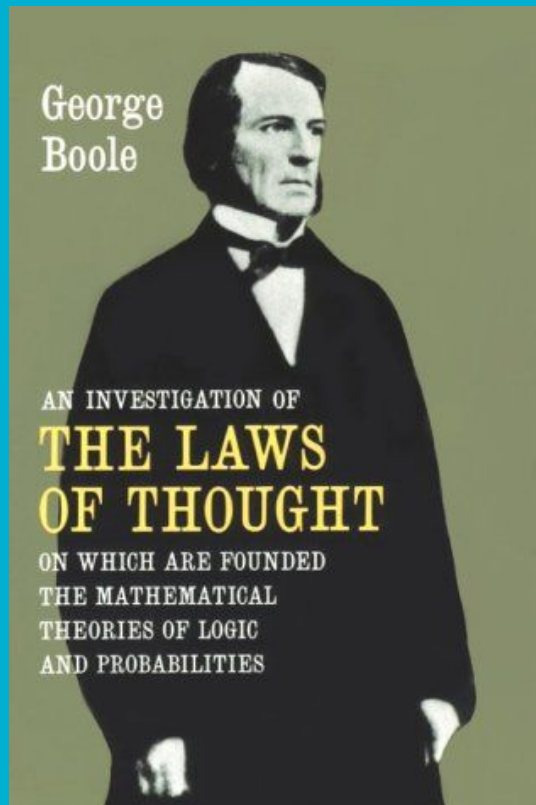


THE LAWS
OF THOUGHT
ON WHICH ARE FOUNDED
THE MATHEMATICAL
THEORIES OF LOGIC
AND PROBABILITIES

Georginho

**Satisfatibilidade
probabilística (PSAT)**

**foi proposta em
Leis do Pensamento
[Boole 1854]**



Pesquisa

slack

$$\begin{bmatrix} 0 \\ 0 \\ 0.1 \end{bmatrix} \begin{matrix} a \\ 2 \\ 1 \\ 0 \end{matrix} \begin{matrix} t \\ 1 \\ 2 \\ 1 \end{matrix} * \begin{bmatrix} 1 \\ 0.3 \\ 0.2 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.7 \\ 0.3 \end{bmatrix}$$

Pesquisa

slack

a

t

0

2

1

0

1

2

*

1

0.3

=

0.8

0.7

0.1

0

1

0.2

0.3

Contato

twitter: @cassiasamp

linkedin: /in/cassiasamp/

Fontes

<https://panda.ime.usp.br/aulasPython/static/aulasPython/aula05.html>

<https://public.tepper.cmu.edu/jnh/booleBicentenary.pdf>

<https://docs.python.org/2.3/whatsnew/section-bool.html>

<https://www.ime.usp.br/~mfinger/home/psat/Hansen+-Models+AlgoProb+BayesLogic-IJCAI1995.pdf>

<https://www.youtube.com/watch?v=Q1qPHIGWJDg>

Imagens

<http://i.imgur.com/B6XlewH.png>

<http://pluspng.com/img-png/waze-png-waze-icon-png-50-px-1600.png>

<https://tech4gamers.com/wp-content/uploads/2015/11/boole.jpg>

<https://i.pinimg.com/736x/a2/99/cc/a299cc484dfc6c3c9c6b891f977e4b3b--family-trips-nerdy.jpg>