

Term Indexing for the Beagle Theorem Prover

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- Beagle is a First-Order-Logic resolution theorem prover with equality, built to show off the capabilities of the Hierarchic Superposition with Weak Abstraction Calculus.

The Beagle Theorem Prover

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- Beagle is a First-Order-Logic resolution theorem prover with equality, built to show off the capabilities of the Hierarchic Superposition with Weak Abstraction Calculus.
- This calculus is capable of *hierarchic reasoning* by incorporating a *background prover*.
- Background provers act as a black box which can instantly prove known facts. For example integer arithmetic.

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- Beagle is a First-Order-Logic resolution theorem prover with equality, built to show off the capabilities of the Hierarchic Superposition with Weak Abstraction Calculus.
- This calculus is capable of *hierarchic reasoning* by incorporating a *background prover*.
- Background provers act as a black box which can instantly prove known facts. For example integer arithmetic.
- The calculus is carefully constructed with a process known as *weak abstraction* in order to ensure consistency and completeness.

Extending Beagle

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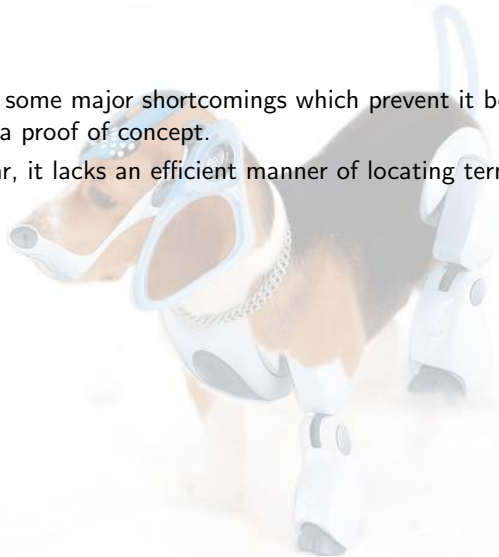
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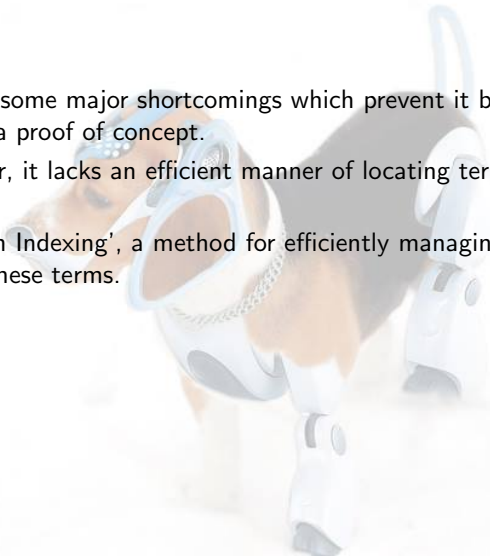
- Beagle has some major shortcomings which prevent it being more than a proof of concept.
- In particular, it lacks an efficient manner of locating terms for inference.



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- Beagle has some major shortcomings which prevent it being more than a proof of concept.
- In particular, it lacks an efficient manner of locating terms for inference.
- Enter 'Term Indexing', a method for efficiently managing and collecting these terms.



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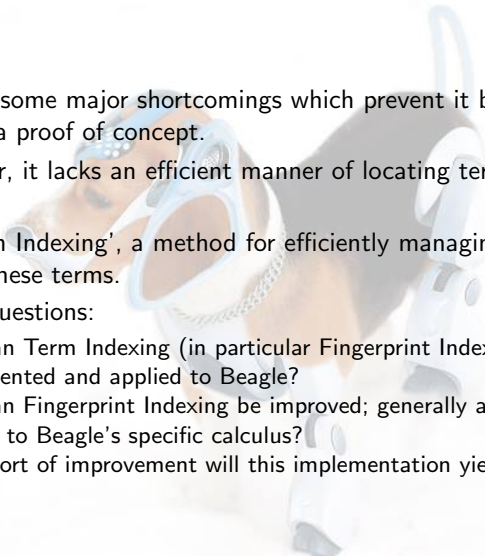
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- Beagle has some major shortcomings which prevent it being more than a proof of concept.
- In particular, it lacks an efficient manner of locating terms for inference.
- Enter 'Term Indexing', a method for efficiently managing and collecting these terms.
- Research Questions:
 - How can Term Indexing (in particular Fingerprint Indexing) be implemented and applied to Beagle?
 - How can Fingerprint Indexing be improved; generally and with respect to Beagle's specific calculus?
 - What sort of improvement will this implementation yield in the prover?



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- First Order Logic

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- First Order Logic
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- Substitutions:
 - s is '*unifiable*' with $t : \sigma s = \sigma t$
 - s '*subsumes*' $t : \sigma s = t$

The Superposition Calculus

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- Normal Superposition rule

Positive Superposition

$$\frac{l \approx r \vee C \quad s[u] \approx t \vee D}{(s[r] \approx t \vee C \vee D)\sigma}$$

Where (i) $\sigma = \text{simple mgu}(l, u)$,
and (ii) u is not a variable.

The Hierarchic Superposition with Weak Abstraction Calculus

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- Extension of the Superposition Calculus to accommodate hierarchic reasoning.

Positive Superposition

$$\frac{I \approx r \vee C \quad s[u] \approx t \vee D}{\text{abstr}((s[r] \approx t \vee C \vee D)\sigma)}$$

Where (i) $\sigma = \text{simple mgu}(I, u)$,

(ii) u is not a variable,

(iii) $r\sigma \not\approx I\sigma$,

(iv) $t\sigma \not\approx s\sigma$,

(v) I and u are not pure background terms,

(vi) $(I \approx r)\sigma$ is strictly maximal in $(I \approx r \vee C)\sigma$,

and (vii) $(s \approx t)\sigma$ is strictly maximal in $(s \approx t \vee D)\sigma$.

Term Indexing Techniques

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- Term indexers aim to collect all FOL terms which potentially match a 'query' term.

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- Term indexers aim to collect all FOL terms which potentially match a 'query' term.
- Top-Symbol Hashing.
- Discrimination Trees.
- Path Indexing.

Fingerprint Indexing

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- Maintain a collection of *fingerprints* for terms.

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- Maintain a collection of *fingerprints* for terms.
- A term fingerprint is an array over $F \cup \{\mathbf{A}, \mathbf{B}, \mathbf{N}\}$, the *Fingerprint Features*.

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- Maintain a collection of *fingerprints* for terms.
- A term fingerprint is an array over $F \cup \{\mathbf{A}, \mathbf{B}, \mathbf{N}\}$, the *Fingerprint Features*.

Table: Fingerprint Feature comparison tables for *unification* (left) and *subsumption* (right)

	f_1	f_2	A	B	N
f_1	Y	N	Y	Y	N
f_2	N	Y	Y	Y	N
A	Y	Y	Y	Y	N
B	Y	Y	Y	Y	Y
N	N	N	N	Y	Y

	f_1	f_2	A	B	N
f_1	Y	N	N	N	N
f_2	N	Y	N	N	N
A	Y	Y	Y	N	N
B	Y	Y	Y	Y	Y
N	N	N	N	N	Y

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	f_1	f_2	A	B	N
f_1	Y	N	Y	Y	N
f_2	N	Y	Y	Y	N
A	Y	Y	Y	Y	N
B	Y	Y	Y	Y	Y
N	N	N	N	Y	Y

	f_1	f_2	A	B	N
f_1	Y	N	N	N	N
f_2	N	Y	N	N	N
A	Y	Y	Y	N	N
B	Y	Y	Y	Y	Y
N	N	N	N	N	Y

- Schulz, Stephan: Fingerprint Indexing for Paramodulation and Rewriting. In: Lecture Notes in Computer Science volume 7364 pp. 447–483 (2012).

Fingerprint Indexing – Example

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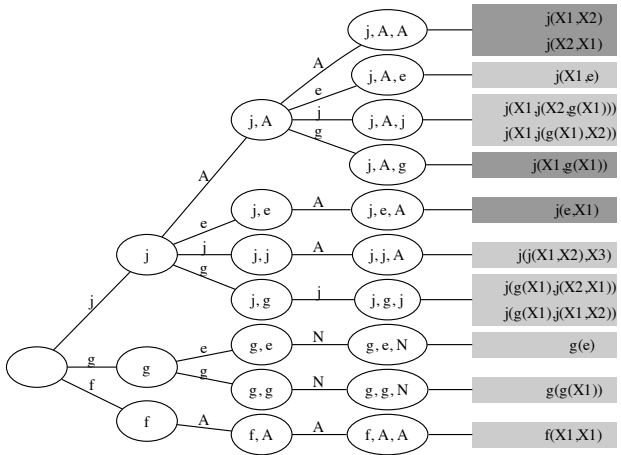
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Why Fingerprint Indexing?

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- New and not thoroughly tested technique.

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- New and not thoroughly tested technique.
- Currently showing very promising results.

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- New and not thoroughly tested technique.
- Currently showing very promising results.
- Highly customisable and configurable.

Creating the Fingerprint Index

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- Addition of terms.

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- Addition of terms.
- Requires an Fingerprint generation along with implementation and traversal of the Index tree structure.

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- Addition of terms.
- Requires an Fingerprint generation along with implementation and traversal of the Index tree structure.
- Retrieval of terms.

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- Addition of terms.
- Requires an Fingerprint generation along with implementation and traversal of the Index tree structure.
- Retrieval of terms.
- Requires implementation of the comparison tables and a more complex Index traversal algorithm.

Beagle's Main Procedure

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- Maintain two Clause Sets, *new* and *old*.
Remove Clauses from *new* one at a time, simplify them and then attempt inference rules.

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- Maintain two Clause Sets, *new* and *old*.
Remove Clauses from *new* one at a time, simplify them and then attempt inference rules.
- Two key areas of improvement ($O(n)$ operations):
 - Inferences via the Superposition rules.
 - Simplifying Clauses.

Indexing Superposition

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Positive Superposition

$$\frac{l \approx r \vee C \quad s[u] \approx t \vee D}{\text{abstr}((s[r] \approx t \vee C \vee D)\sigma)}$$

Where (i) $\sigma = \text{simple mgu}(l, u)$,

(ii) u is not a variable,

(iii) $r\sigma \not\approx l\sigma$,

(iv) $t\sigma \not\approx s\sigma$,

(v) l and u are not pure background terms,

(vi) $(l \approx r)\sigma$ is strictly maximal in $(l \approx r \vee C)\sigma$,

and (vii) $(s \approx t)\sigma$ is strictly maximal in $(s \approx t \vee D)\sigma$.

- Requires that we index all subterms. Furthermore we must implement two separate cases for *from* and *into*.

Indexing Simplification

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- Simplification rules exist to implement special cases of the rules in the Hierarchic Superposition with Weak Abstraction Calculus.
- These special cases allow redundant Clauses to be removed; preventing clutter in the inference process.

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- Simplification rules exist to implement special cases of the rules in the Hierarchic Superposition with Weak Abstraction Calculus.
- These special cases allow redundant Clauses to be removed; preventing clutter in the inference process.
- The two main simplification rules used by Beagle are *Negative Unit Simplification* and *Demodulation*

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- These special cases allow redundant Clauses to be removed; preventing clutter in the inference process.
- The two main simplification rules used by Beagle are *Negative Unit Simplification* and *Demodulation*
- These rules operate only on *unit Clauses*, so using our current index clogged with subterms is inefficient.
- The rules also require checking for *subsumption*, which requires implementing a new comparison table for Fingerprint Indexing.

Indexing Negative Unit Simplification

Negative Unit Simplification

$$\frac{l \not\approx r \quad s \approx t \vee C}{C}$$

Where (i) $\exists \sigma \text{ s.t. } (l \approx r)\sigma \equiv s \approx t$.

The clause $s \approx t \vee C$ may be removed.

Indexing Negative Unit Simplification

Negative Unit Simplification
$$\frac{l \not\approx r \quad s \approx t \vee C}{C}$$

Where (i) $\exists \sigma \text{ s.t. } (l \approx r)\sigma \equiv s \approx t$.

The clause $s \approx t \vee C$ may be removed.

- Searching for valid subsuming Literals is extremely time consuming.
- Requires an index capable of matching Equations rather than Terms.

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Demodulation
$$\frac{l \rightarrow r \quad s[u] \approx t \vee D}{s[r\sigma] \approx t \vee D}$$

Where $l\sigma = u$

The clause $s[u] \approx t \vee D$ may be removed.

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Where $l\sigma = u$

The clause $s[u] \approx t \vee D$ may be removed.

- For a simple example, with a Literal $X \rightarrow f(a)$ we may replace all occurrences of X with $f(a)$.

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Where $l\sigma = u$

The clause $s[u] \approx t \vee D$ may be removed.

- For a simple example, with a Literal $X \rightarrow f(a)$ we may replace all occurrences of X with $f(a)$.
- Like in Negative Unit Simplification, the most costly operation is searching for subsuming l Terms.
- We must perform this search for every possible subterm u of s .

Fingerprint Indexing for the Hierarchic Superposition with Weak Abstraction Calculus

- The Hierarchic Superposition with Weak Abstraction Calculus imposes many restrictions on what can be used for inference.

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- We may take advantage of some of these conditions to increase the effectiveness of Fingerprint Indexing.

Fingerprint Indexing for the Hierarchic Superposition with Weak Abstraction Calculus

- The Hierarchic Superposition with Weak Abstraction Calculus imposes many restrictions on what can be used for inference.
- We may take advantage of some of these conditions to increase the effectiveness of Fingerprint Indexing.

Table: Fingerprint comparison table for unification; extended by considering the term hierarchy.

	f_1	f_2	A	B	N	f_1+	f_2+	A+	B+
f_1	Y	N	Y	Y	N	N	N	N	N
f_2	N	Y	Y	Y	N	N	N	N	N
A	Y	Y	Y	Y	N	Y	Y	Y	Y
B	Y	Y	Y	Y	Y	Y	Y	Y	Y
N	N	N	N	Y	Y	N	N	N	Y
f_1+	N	N	Y	Y	N	Y	N	Y	Y
f_2+	N	N	Y	Y	N	N	Y	Y	Y
A+	N	N	Y	Y	N	Y	Y	Y	Y
B+	N	N	Y	Y	Y	Y	Y	Y	Y

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- Total run time - Need to be careful to consider all factors.

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- Total run time - Need to be careful to consider all factors.
- False Positives - Relevant, but can be misleading depending on number of positions being sampled.

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- Total run time - Need to be careful to consider all factors.
- False Positives - Relevant, but can be misleading depending on number of positions being sampled.
- Run time *per Inference* - Most accurate measure of performance. Must still take care when interpreting.

Comparing Varieties of Beagle

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Table: Totalled inference counts and indexing statistics for various versions of beagle.

Version	Inference Counts			Indexing Results		
	Sup	Demod	NegUnit	TotalFound	SupFP	SimpFP
Unmodified ¹	414216	29097	1826	0	0	0
Standard	162881	41414	2452	61884768	15525	39778148
Enhanced	146861	35326	1960	58119897	17641	39916687

Table: Totalled timing results for various versions of beagle.

Version	Time Spent (seconds)					
	Indexing	Retrieving	Sup	Demod	NegUnit	Total
Unmodified ¹	0	0	730.44	9.44	31.99	5623.21
Standard	28.4	38.73	254.17	41.66	3.18	381.36
Enhanced	18.74	17.58	168.79	30.56	2.12	259.02

¹This version failed to solve two out of the fifty problems within 8 hours.

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Table: Superposition time for the 6 most extreme problem examples.

Version	Superposition	Demodulation	NegUnit Simplification
Unmodified	1.7ms	0.3ms	17.5ms
Standard	1.5ms	1.0ms	1.3ms
Enhanced	1.1ms	0.8ms	1.0ms

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- Most typical application of Demodulation is a Literal like $X \rightarrow f(a)$. X will match anything, making fingerprint indexing a waste of time.

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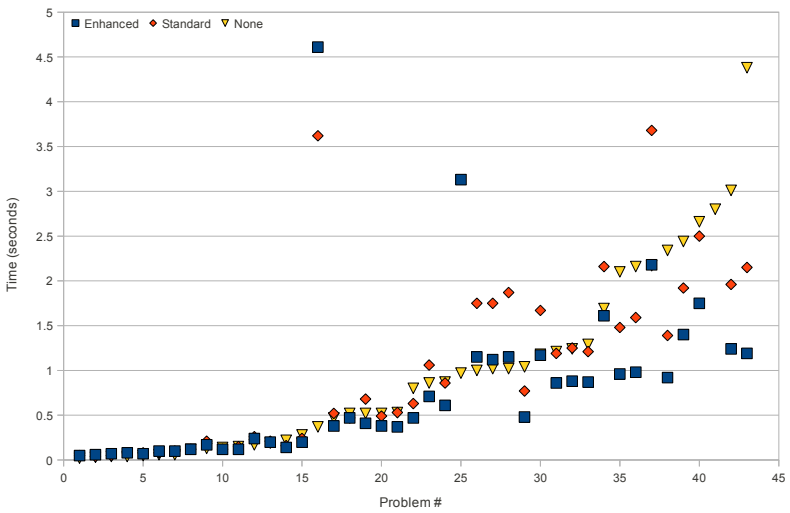
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- Most typical application of Demodulation is a Literal like $X \rightarrow f(a)$. X will match anything, making fingerprint indexing a waste of time.
- When excluding PUZ037-1.p we have 0.29, 0.39 and 0.31 milliseconds per Demodulation.

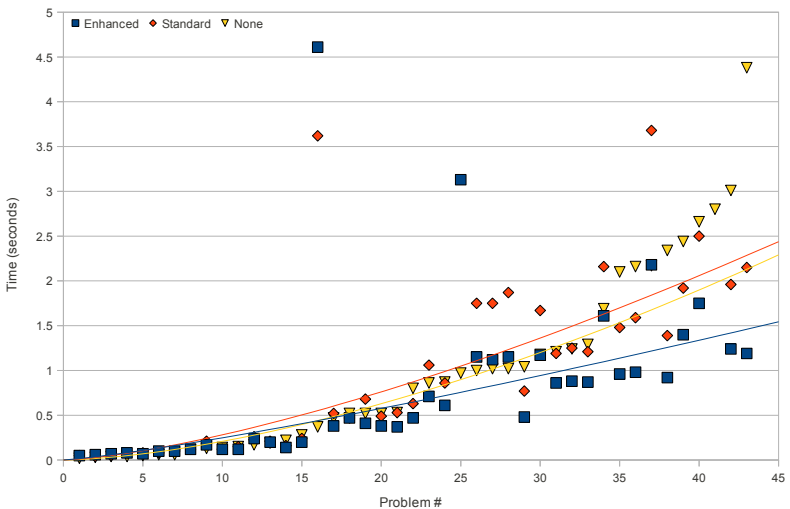
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Table: Superposition time for the 6 most extreme problem examples.

Problem	Enhanced	Standard	Unmodified
DAT050=1.p	17.53	31.54	48.62
DAT039=1.p	13.2	22.51	130.77
DAT040=1.p	14.49	21.29	190.71
DAT038=1.p	12.53	24.04	294.86
DAT043=1.p	18.67	26.08	N/A
DAT048=1.p	17.65	35.77	N/A

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DAT043=1.p	18.67	26.08	N/A
DAT048=1.p	17.65	35.77	N/A

- When taking number of inferences into account for DAT038=1.p we observe 1.2 milliseconds per superposition for the full implementation versus 2.2 milliseconds per superposition for unindexed beagle.

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- Reasoning. Cite shulz and FP/Speed balance

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- Reasoning. Cite shulz and FP/Speed balance
- Different position samples

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Table: Totalled inference counts and indexing statistics for various Fingerprint sampling sets.

Sample Set	Inference Counts			Indexing Results		
	Sup	Demod	NegUnit	TotalFound	SupFP	SimpFP
FP3W	162218	42402	2472	13913606	69429	1815992
FP4M	147798	35709	1963	13469779	26847	1851515
FP6M	144505	35326	1959	12601762	16406	1694731
FP7	159055	41005	2440	13011130	21281	1596575
FP8X2	159385	40876	2438	12819184	11229	1602033

Table: Totalled timing results for various Fingerprint sampling sets.

Sample Set	Time Spent (seconds)					
	Indexing	Retrieving	Sup	Demod	NegUnit	Total
FP3W	11.52	14.02	170.37	9.26	1.78	237.75
FP4M	13.09	14.12	164.95	9.51	1.82	230.68
FP6M	16.82	16.5	159.93	10.78	2.11	229.59
FP7	19.98	18.74	170.83	12.37	2.37	249.22
FP8X2	45.56	32.59	181.43	21.45	4.06	294.8

Note that for more relevant comparisons these results exclude PUZ037-1.p.

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- The Hierarchic Superposition with Weak Abstraction Calculus is a

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- The Hierarchic Superposition with Weak Abstraction Calculus is a