$$f(x_{i+1}(t_{coll_k})) = \epsilon$$
 submanifold
$$x_{i+1}(t_{coll_k}) = 0$$
 linearization
$$x_i$$

$$f(x_i(t_{coll_k})) = 0$$