

1. (a)  $z = 1 + \left(\cos\left(\frac{\pi k}{8}\right) + i \sin\left(\frac{\pi k}{8}\right)\right)$  for  $k = 0, 1, 2, 3$ .  
 (b)  $\exp(3 \log 2 - \frac{\pi}{2} + i(\frac{3\pi}{2} + \log 2))$ .  
 (c) 0.
2. True; first use definition of uniform convergence, then with upper-bound considerations, use ratio test to see  $\sum \frac{\sqrt{n} \cdot 2^n}{n!}$  converges absolutely on  $\overline{D_2(0)}$ . By Cauchy Criterion for infinite series, the result follows.
3. (a) Not entire; write  $u(x, y) = x^2 + y^2$  and  $v(x, y) = 0$  and look at the Cauchy-Riemann equations.  
 (b) Not entire; Cauchy-Riemann equations are not satisfied.
4. (a) (DRAWINGS).  
 (b)  $S$  is compact;  $S$  is bounded and closed, so by Heine-Borel,  $S$  is compact.  
 (c) Consider  $f_M(z) = z + 3$ , where  $M = \begin{pmatrix} 1 & 3 \\ 0 & 1 \end{pmatrix}$  and  $\det M = 1 \neq 0$ .
5.  $\frac{2\pi \cdot 16}{5}$ .
6. Seek to use Louisville's theorem, but not sure on how to show that  $|f|$  is bounded.
7. this follows from maximum modulus principle.
8. Use Rouche's theorem (try to use maximum modulus principle to show  $|f(z)| < 1$  on the unit circle?).
9. Gamma function ( $\Gamma$ )?
10.  $-\frac{\pi}{5}$  (hopefully my arithmetic is correct).