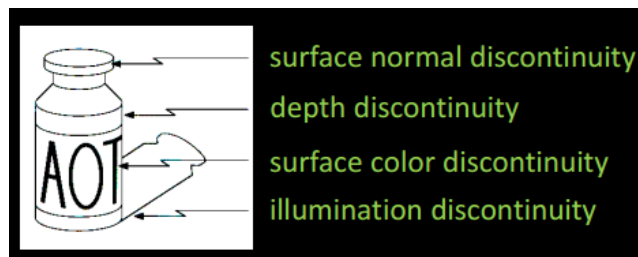
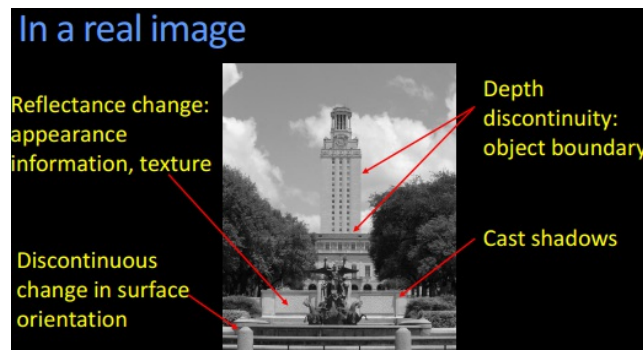


2A-L5 Edge detection - Gradients

2017/11/11 00:41

1. Sum
 - a. to find/recognize the obj, the obj boundary helps.
 - b. edge: where discontinuity happens: color, surface, depth, lumination
 - c. finit difference
 - d. gradient filter: sobel
 - e. use gradient to help find the edge
 - i. smooth
 - ii. gradient
 1. derivative of the filter first to save the computation
 - iii. 2nd gradient to find the max
 - f.
2. [1. Intro](#)
 - a. working on the problem, to find the obj on generic images which is not suitable through a template
3. [2. Reduced Images](#)
 - a. Edges are important and they give a lot of info. sometimes
4. [3. Edges](#)
 - a. origin
 - i. surface normal discontinuity
 - ii. depth discontinuity
 - iii. color discontinuity
 - iv. illumination discontinuity





5. 4. Quiz: Change Boundaries Quiz

Edges seem to occur “change boundaries” that are related to shape or illumination. Which is not such a boundary?

- a) An occlusion between two people
- b) A cast shadow on the sidewalk
- c) A crease in paper
- d) A stripe on a sign

i. analysis

1. An occlusion occurs when a physical object (or part of one) is in front of another, with respect to the viewing angle. This is part of the geometry or overall shape of the scene.
2. A shadow is caused due to difference in illumination falling on a surface.
3. A crease alters the shape of the paper, which is observable from certain viewing angles.
4. A stripe is essentially a color discontinuity, which is not caused by shape or illumination.

1. 5. Edge Detection

a. how to define a edge, or how can we determine certain pixel is on the edge?

i. on an image, edges look like steep cliffs, pixels with a strong change in a neighborhood

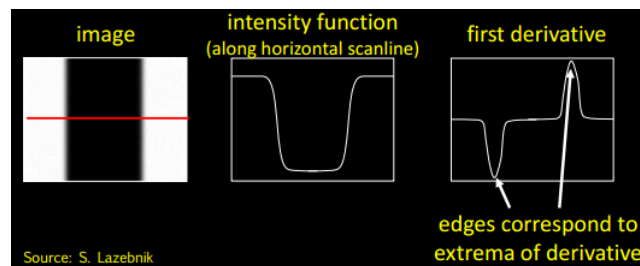
b. so the Basic idea: look for a neighborhood with strong signs of change.

i. Problems

1. neighborhood size
2. how to define a change is a strong change which can be regarded as boundary

2. 6. Derivatives and Edges

- a. when talking about changes in math, we rely on derivatives so
 - i. An edge is a place of rapid change in the image intensity function, and this rapid change corresponds to the maximum of the derivative, see e.g.



- ii. so the problem turns out to be find the peaks of the derivatives
- a. how to compute the derivative
 - i. differential operator, just like other filters
 - 1. Differential operators -when applied to the image returns some derivatives.
 - 2. • Model these “operators” as masks/kernels that compute the image gradient function.
 - 3. • Threshold the this gradient function to select the edge pixels.

1. 7. What is a Gradient

- a. The gradient points in the direction of most rapid increase in intensity

Image gradient

The gradient of an image: $\nabla f = \left[\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$

The gradient direction is given by: $\theta = \tan^{-1} \left(\frac{\frac{\partial f}{\partial y}}{\frac{\partial f}{\partial x}} \right)$

The *edge strength* is given by the gradient magnitude: $\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x} \right)^2 + \left(\frac{\partial f}{\partial y} \right)^2}$

9. 9. Finite Differences

For 2D function, $f(x,y)$, the partial derivative is:

$$\frac{\partial f(x,y)}{\partial x} = \lim_{\varepsilon \rightarrow 0} \frac{f(x + \varepsilon, y) - f(x, y)}{\varepsilon}$$

- a. finite difference

For discrete data, we can approximate using finite differences:

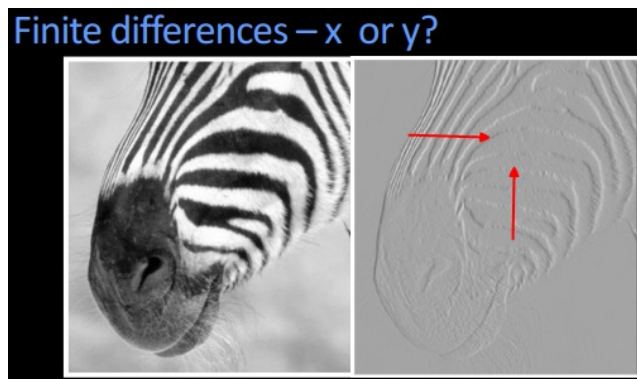
$$\frac{\partial f(x, y)}{\partial x} \approx \frac{f(x+1, y) - f(x, y)}{1}$$

$$\approx f(x+1, y) - f(x, y)$$

"right derivative" But is it???

i. this is also called right derivative

a. e.g.



1. it's a finite difference on x, since horizontally, the edges are stronger than the vertical ones

1. [10. Partial Derivatives of an Image](#)

a. filters along the x, is $[-1, 1]$; along the y depends on your origin, if on the top-left corner, positive downside[CS choice]; if on the bottom left corner, positive upside[math choice].



b. here correlation and convolution are different, be careful

c. how does this $[-1, 1]$ filter work?



i. it is an awful image for edge detection

1. 11. The Discrete Gradient Filter

a. what kind of filter should we use

0	0
-1	+1
0	0

Not symmetric around image point; which is "middle" pixel?

H

0	0	0
-1/2	0	+1/2
0	0	0

Average of "left" and "right" derivative. See?

H

$$\begin{array}{r} -1 \quad +1 \\ \hline -1 \quad 0 \quad +1 \\ \hline -\frac{1}{2} \quad 0 \quad +\frac{1}{2} \end{array}$$

i. the first is not suitable to find the middle pixel; so the left one, and the 1/2 is the average of the left and right derivatives

1. 12. Sobel Operator

$\frac{1}{8} * \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$
 S_x

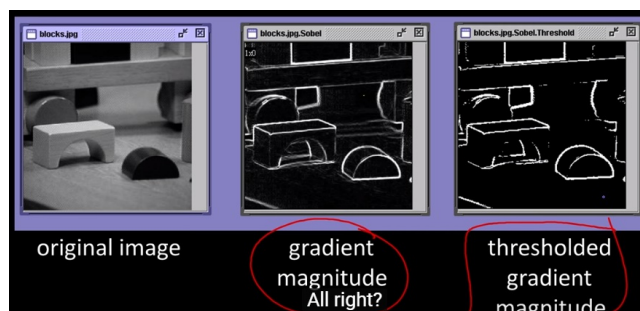
$\frac{1}{8} * \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$
 S_y

(here positive y is up)

(Sobel) Gradient is $\nabla I = [g_x \ g_y]^T$

$g = (g_x^2 + g_y^2)^{1/2}$ is the gradient magnitude.
 $\theta = \text{atan2}(g_y, g_x)$ is the gradient direction.

- a. the idea of adding the -1 & 1 is that we assume that images are sort of locally smooth so when compute the derivatives, it's better to look around the neighborhood and then normalize the filter.
- b. imgradient in matlab applies sobel operator by default but it doesn't normalize it by dividing 8
- c. how does it work



i. it's not a great edge detection, but also not an awful one.

So it's better than the previous one with $[-1, 1]$

1. [13. Well Known Gradients](#)

a. matlab code

- i. `filt = fspecial('sobel')`
- ii. `outim = imfilter(double(im), filt);`
- iii. `imagesc(outim);`
- iv. `colormap gray`

b. functions

i. `h = fspecial(type)` creates a two-dimensional filter `h` of the specified `type`.

- 1. `sobel, prewitt, roberts`

ii. `B = imfilter(A, h)` filters the multidimensional array `A` with the multidimensional filter `h`

- 1. The result `B` has the same size and class as `A`.
- 2. `B`, using double-precision floating point. so we need the conversion
- 3. by default, it uses correlation rather than convolution, but it can be changed.

iii. `imagesc(C)` displays the data in array `C` as an image that uses the full range of colors in the colormap. Each element of `C` specifies the color for 1 pixel of the image.

iv. `colormap maptype` sets the `colormap` for the current figure to one of the predefined `colormaps`.

- 1. `maptype: gray, spring, summer, ..., copper, colorcube, ...`

2. [15. Quiz: Gradient Direction Quiz](#)

a. to compute, it's better to use correlation since it's easy to know the left and right ???

b. matlab code

i. %% Load and convert image to double type, range $[0, 1]$ for convenience

- 1. `img = double(rgb2gray((imread('moon.jpg')))) / 255.;`

a. % assumes $[0, 1]$ range for

double images. since imshow img
range [0,1] or [min, max]
b. or imshow(img, [0, 255])
c. but if imshow(img), the range is
[min, max] may cause some problem,
just like imagesc()

2. imshow(img);

ii. %% Compute x, y gradients

1. [gx gy] = imgradientxy(img, 'sobel'); % Note:
gx, gy are not normalized

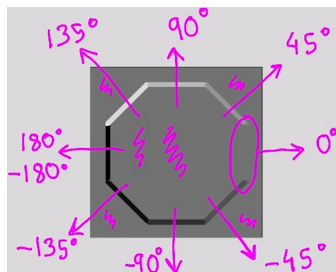
2. figure(5);imshow((gx + 4)/8);

iii. %% Obtain gradient magnitude and direction

1. [gmag gdir] = imgradient(gx, gy);

2. figure(2);imshow(gmag / (4 * sqrt(2))); % mag
= sqrt(gx^2 + gy^2), so [0, (4 * sqrt(2))]

3. figure(3);imshow((gdir + 180.0) / 360.0); %
angle in degrees [-180, 180]



4. %% Find pixels with desired gradient direction -
- set the desired pixels 1, the others 0

a. result = gmag > mag_min & gdir >
angle_low & gdir < angle_high;

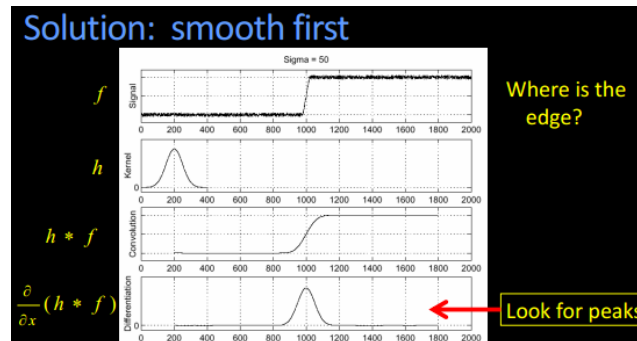
i. & is the element-wise
logic AND when applied with
matrix

ii. expr1 && expr2, && is

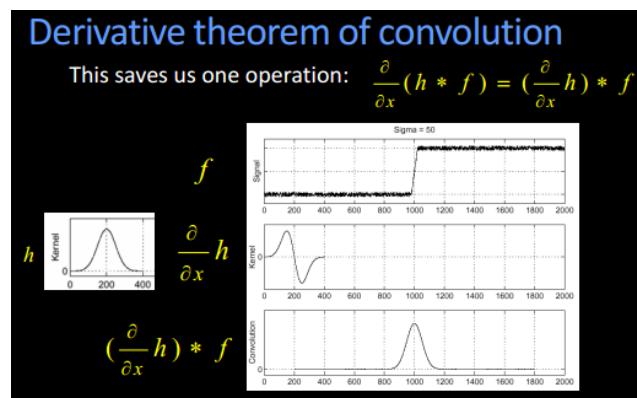
for expression

1. 16. But in the Real World

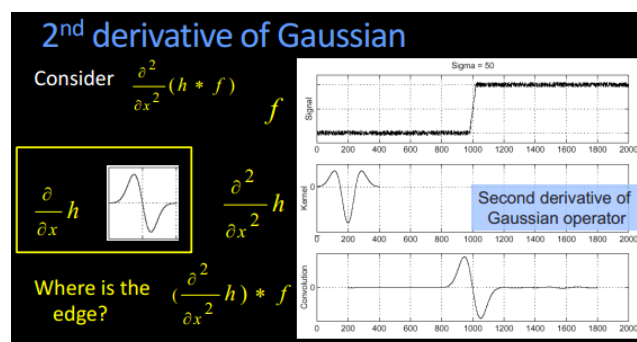
- Since in the real world, there're noise in the images, so we can't compute the gradient directly
- filter to smooth the images first and then gradient



- to save the computation, do the conv first



- edge is corresponds to the max of the gradient, so compute the second order derivative



16. 17. Quiz: Linearity Property Quiz

17. 18. End