

2A - L1 images as functions

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- Sum
 - one image is a function
 - manipulation of the image through the matrix
 - add, multiply, subtract, blend, crop
 - display the image
 - imshow, plot
 - Octave/matlab functions
 - imread, imshow, hist,
 - noise
 - Gaussian noise
 - sigma
- [2. Images as Functions](#) – mathematical view
 - One image can be regarded as a function. $I(x, y)$, the value of the light intensity
 - can be shown in matlab
 - function – grey scaled
 - mapping: $R \times R \rightarrow R$
 - $f: [a, b] \times [c, d] \rightarrow [\min, \max]$
 - each (x, y) corresponding to a value i

Images as functions

We think of an image as a *function*, f or I , from R^2 to R :

$f(x, y)$ gives the intensity or value at position (x, y)

Practically define the image over a rectangle, with a finite range:

$$f: [a, b] \times [c, d] \rightarrow [\min, \max]$$

- function – colored
 - mapping: $R \times R \rightarrow R \times R \times R$
 - $f: [a, b] \times [c, d] \rightarrow [\min, \max] \times [\min, \max] \times [\min, \max]$
 - each (x, y) corresponding to a vector (r, g, b)
 - each channel can be taken out alone as a r/g/b plane to be processed

A color image is just three functions “stacked” together. We can write this as a “vector-valued” function:

$$f(x, y) = \begin{bmatrix} r(x, y) \\ g(x, y) \\ b(x, y) \end{bmatrix}$$

- #we do in grey scale images, it’s easier cuz it only has one channel

■

- [8. Digital Images](#)

- It’s the discrete-valued image. so we require two discretions: Sample and Quantize

- **ATT: when computing, regard the value as floating point**

- **# pixel : an image element**

In computer vision we typically operate on digital (discrete) images:

Sample the 2D space on a regular grid

Quantize each sample (round to “nearest integer”)

- Image thus represented as a **matrix** of integer values.

- matlab typically with interger values

- index

- x, y used in math, x is along the column, y is along the row

- i, j used in computation, i is along the row, j is along the column

- 1 D signals are just represented as vectors

- [9. Quiz: Compute Image Size Quiz](#)

- image size = #row x #column x #channel #value size

- [10. Matlab Images are Matrices](#)

- Matlab Images are Matrices, (r, c, rgb), so that you can manipulate them as matrices.

- [12. Load and Display an Image](#)

- imread('xx.xxx')

- [14. Quiz: Image Size and Data Type Quiz](#)

- size

- size()

- class type
 - e.g. uint8
 - u: unsigned means only non-negative value
 - int: integer
 - 8: 8 bits, 1 byte
 -
- [15. Inspect Image Values](#)
 - as to access matrix
 - but to show a row/column, better to use `plot(img(1,:))`
- [18. Crop an Image](#)
 - to take a big part of the image
 - for index, both the start and end row/column are included
- [21. Color Planes](#)
 - in images, bright area represents higher values, while dark area represents lower values.
- [23. Add 2 Images Demo](#)
 - `img [0, 255]`, when the value exceeds, round to 255;
 - Octave rounds the value to the nearest integer for uint8, $1.5 \Rightarrow 2$
 - add
 - average: $/2 \Rightarrow +$; not $+ \Rightarrow /2$
- [25. Multiply by a Scalar Demo](#)
- [26. Quiz: Blend 2 Images](#)
 - Rule: keep the sum of the weights equal to 1; the bigger the weight, the more the effect of this image.
- [27. Common Types of Noise](#)
 - $\eta(x, y)$
 - salt and pepper noise: random occurrences of black and white pixels
 - Impulse noise: random occurrences of white pixels
 - Gaussian noise -- most common
 - variations in intensity drawn from a Gaussian normal distribution
 - `rand(size(img)) .* sigma`
 - zero mean, sigma standard deviation
 - `imgnew = img + noise`
- [28. Image Difference Demo](#)
 - directly subtract may lose some values, since uint8 is `[0,255]`;
 - so use `imabsdiff(a,b)` - order doesn't matter

- [30. Generate Gaussian Noise](#)

- e. g.

- `noise = randn(1,10000);`
 - `noise2 = noise .* 2;`
 - `std(noise)`
 - % noise2 has doubled standard deviation of noise
 - because the GD represents the distribution the number of values in certain bin rather than the values themselves.

- when add the noise to certain signal, what should be the concern is the noise magnitude compared to image magnitude. that's the effect of the sigma

- [35. Displaying Images in Matlab](#)

- determine how to show the image

- `imshow(im)`

- original range

- `imshow(im, [low, high])`

- rescaled, low represents the darkest black, high represents the whitest white

- `imshow(im, [])`

- rescaled, low is the min, high is the max in the original image

- ATT

- only the display may require rescale, never the computation