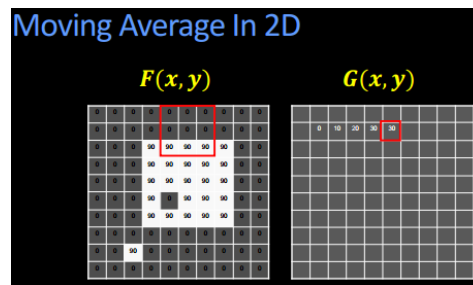


2A-L2-Filtering

2017/11/03 20:23

- Sum
 - remove noise in an image - [Correlation Filtering](#)
 - average filter
 - average assumptions
 - Gaussian filter
- [Remove the Noise](#)
 - intro
 - if we know the noise, we can certainly subtract it but we don't know. Here are some ways to realize it.
 - Alternative 1
 - Replace each pixel with an average of all the values in its neighborhood - a moving average:
 - [3. Averaging Assumptions](#)
 - 1. The “true” value of pixels are similar to the true value of pixels nearby.
 - 2. The noise added to each pixel is done independently
 - so the sum is 0;
 - Alternative 2: [5. Weighted Moving Average](#)
 - generate a smoother result than alternative 1
 - The basic idea is that nearby pixels have similar true underlying values. the closer a pixel is to some reference pixel, the more similar it would be. So the more it should contribute to an average.
 - the To do the moving average computation the number of weights should be Odd and symmetric - makes it easier to have a middle pixel
 - the sum of the weight should be 1
- [8. Moving Average In 2D](#)
 - use a squared region to calculate the average



- Questions
 - how to deal with the edge?
- this is called [9. Correlation Filtering](#)
 - uniform weights

Say the averaging window size is $2k+1 \times 2k+1$:

$$G[i, j] = \frac{1}{(2k+1)^2} \sum_{u=-k}^k \sum_{v=-k}^k F[i+u, j+v]$$

*Uniform
weight for
each pixel*

*Loop over all pixels in
neighborhood around
image pixel $F[i, j]$*

- non-uniform weights

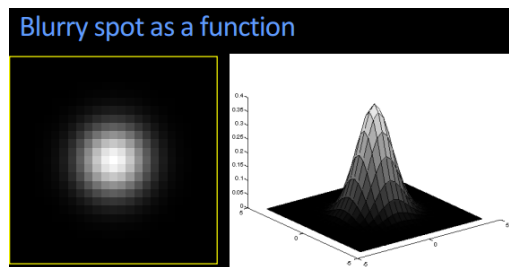
Now generalize to allow **different weights** depending on neighboring pixel's relative position:

$$G[i, j] = \sum_{u=-k}^k \sum_{v=-k}^k H[u, v] F[i+u, j+v]$$

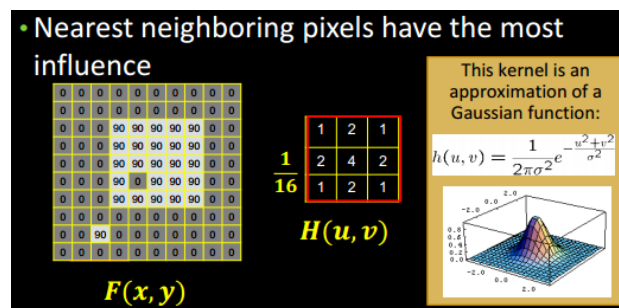
Non-uniform weights

This is called **cross-correlation**, denoted $G = H \otimes F$

- The filter “kernel” or “mask” $H[u, v]$ is the matrix of weights in the linear combination.
 - this kernel is different from the one in ML
- what makes a good kernel?
 - Alternative 1: Averaging Filter – uniform one
 - the result is really bad
 - what’s the problem
 - squares aren’ t smooth
 - And filtering an image with a filter that is not “smooth” seems wrong if we’ re trying to “blur” the image.
 - analogy
 - think about what a single spot of light viewed by an out of focus camera would look like.



- so To blur a single pixel into a “blurry” spot, we would need to need to filter the spot with Something that looks like a blurry spot - higher values in the middle, falling off to the edges
- Alternative 2 - Gaussian Filter
 - we get sth so much better - no clear edges in the image



- Key
 - nearest neighboring pixels have the most influence
- called: circularly symmetric Gaussian function or isotropic
- formula

$$h(u,v) = \frac{1}{2\pi\sigma^2} \exp\left(-\frac{x^2 + y^2}{2\sigma^2}\right)$$

- The amount of smoothing is define by the Variance or Standard Deviation (sigma), the only parameter in the isotropic funciton
- another influential parameter, the size of the kernel/square
 - the bigger one with the same sigma has better performance

- the kernel has to be big enough, it's a default parameter. So often a "big kernel" means a "big sigma" actually

■

- [15. Matlab](#) code

```
sigmav = [3, 13, 23, 33];
for sigma = sigmav
    hsize = 31;
    h = fspecial('gaussian', hsize, sigma);
    out = imfilter(nmona, h);
    figure(sigma);imshow(out);
end
```

- [16. Quiz: Remove Noise](#)

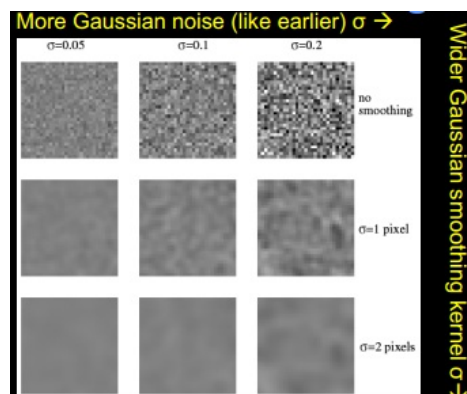
- the Gaussian filter can smooth/blur the image but it affect the original image, too. so you don't get back exactly the same as the original one.
- even through the smoothed image doesn't look good virtually, but it benefits the image process a lot.

- [17. Quiz: Gaussian Filter Quiz](#)

- When filtering with a Gaussian, which is true:
 - The sigma is most important - it defines the blur kernel's scale with respect to the image
 - Altering the normalization coefficient does not effect the blur, only the brightness.

- [18. Keeping the Two Gaussians Straight](#)

- when talking about Gaussian filter, sigma defines a width of a the Gaussian filter.
- when talking about Gaussian noise, sigma defines the variance of a noise function or the value of the noise. The bigger the noise sigma was the more likely that large values of noise can be created.



- [19. End](#)