

Numerical Analysis Assignment 4

亚历克上 M202161029 Ex: 1(a,b), 2 a, Sa.

1) a)

x	f(x)	1st diff	2nd diff	3rd diff	4th diff
0	8,1	16,9441	3,1041	0,06	-0,002083333
1	8,3	17,56492	3,1341	0,05875	
2	8,6	18,50515	3,1576		
3	8,7	18,82091			

$$P(x) = 16,9441 + 3,1041(x-8,1) + 0,06(x-8,1)(x-8,3) + (-0,002083333)(x-8,1)(x-8,3)(x-8,6)$$

$$f(8,4) = 17,87714$$

b)

x	f(x)	1st diff	2nd diff	3rd diff	4th diff
0	0,6	-0,1769446	1,9069687	0,959224	-1,78574125
1	0,7	0,01375227	2,0988135	0,2449295	
2	0,8	0,22363362	2,1722915		
3	1	0,65809197			

$$P(x) = (-0,1769446) + 1,9069687(x-0,6) + 0,959224(x-0,6)(x-0,7) + (-1,78574125)(x-0,6)(x-0,7)(x-0,8)$$

$$f(0,9) = 0,441985$$

2 a)

x	$f(x)$	1 st diff	2 nd diff	3 rd diff	4 th diff
0	-0,75	-0,0718125	0,18825	2,501	1
1	-0,5	-0,02475	1,43875	3,251	
2	-0,25	0,3349375	3,6425		
3	0	1,101			

$$P(x) = -0,0718125 + 0,18825(x - (-0,75)) + 2,501(x - (-0,75))(x - (-0,5)) + 1(x - (-0,75))(x - (-0,5))(x - (-0,25))$$

$$\underline{\underline{f(-0,33333) = 0,174574}}$$

5 a)

x	$f(x)$	1 st diff	2 nd	3 rd	4 th diff
0	0	1	1,107	0,61275	0,061479
1	0,2	1,2214	1,3521	0,7485	0,22625
2	0,4	1,49182	1,6515	0,914	0,2758333
3	0,6	1,82212	2,0171		
4	0,8	2,22554			

$$P(x) = 1 + 1,107(x-0) + 0,612575(x-0)(x-0,2) + 0,22625(x-0)(x-0,2)(x-0,4) + 0,061479(x-0)(x-0,2)(x-0,4)(x-0,6)$$

$$f(x) = f(0,05)$$

$$\underline{\underline{f(0,05) = 1,051259}}$$

5th diff
0,061479