# **Multiclass Support Vector Machine exercise**

Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. For more details see the <u>assignments page</u> (http://vision.stanford.edu/teaching/cs231n/assignments.html) on the course website.

In this exercise you will:

- implement a fully-vectorized loss function for the SVM
- implement the fully-vectorized expression for its analytic gradient
- check your implementation using numerical gradient
- use a validation set to tune the learning rate and regularization strength
- optimize the loss function with SGD
- **visualize** the final learned weights

```
In [1]:
        1 # Run some setup code for this notebook.
         3 from __future__ import print_function
         4 import random
         5 import numpy as np
         7 from cs231n.data utils import load CIFAR10
         8 import matplotlib.pyplot as plt
        10
        11 # This is a bit of magic to make matplotlib figures appear inline in the
        12 # notebook rather than in a new window.
        13 %matplotlib inline
        14 plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        15 plt.rcParams['image.interpolation'] = 'nearest'
        16 plt.rcParams['image.cmap'] = 'gray'
        17
        18 # Some more magic so that the notebook will reload external python modules;
        19 # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
        20 %load ext autoreload
        21 %autoreload 2
```

## **CIFAR-10 Data Loading and Preprocessing**

```
1 # Load the raw CIFAR-10 data.
In [2]:
         2 cifar10 dir = 'cs231n/datasets/cifar-10-batches-py'
         4 # Cleaning up variables to prevent loading data multiple times (which may cause memory issue)
         5 try:
         6
              del X train, y train
              del X_test, y_test
         7
         8
              print('Clear previously loaded data.')
         9 except:
        10
              pass
        11
        12 | X train, y train, X test, y test = load CIFAR10(cifar10 dir)
        13
        14 # As a sanity check, we print out the size of the training and test data.
        15 print('Training data shape: ', X train.shape)
        16 print('Training labels shape: ', y_train.shape)
        17 print('Test data shape: ', X test.shape)
        18 print('Test labels shape: ', y_test.shape)
         Training data shape: (50000, 32, 32, 3)
         Training labels shape: (50000,)
         Test data shape: (10000, 32, 32, 3)
         Test labels shape: (10000,)
In [3]: 1 # Visualize some examples from the dataset.
         2 # We show a few examples of training images from each class.
         3 classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', 'ship', 'truck'] #类别列表
         4 num classes = len(classes) #类别数目
         5 samples per class = 7 # 每个类别采样个数
         6 for y, cls in enumerate(classes): ## 对列表的元素位置和元素进行循环, y表示元素位置[0,num class), cls元素本身'plane'等
               idxs = np.flatnonzero(y train == y) #找出标签中y类的位置
         8
               idxs = np.random.choice(idxs, samples per class, replace=False) #从中选出我们所需的7个样本
               for i, idx in enumerate(idxs): #对所选的样本的位置和样本所对应的图片在训练集中的位置进行循环
         9
        10
                   plt idx = i * num classes + y + 1 # 在子图中所占位置的计算
        11
                   plt.subplot(samples per class, num classes, plt idx) # 说明要画的子图的编号
        12
                   plt.imshow(X train[idx].astype('uint8')) # 画图
        13
                   plt.axis('off')
        14
                   if i == 0:
                       plt.title(cls) # 写上标题, 也就是类别名
        15
        16 plt.show() # 显示
```



```
In [4]: 1 # Split the data into train, val, and test sets. In addition we will
         2  # create a small development set as a subset of the training data;
         3 # we can use this for development so our code runs faster.
         4 num training = 49000
         5 num validation = 1000
         6 num test = 1000
         7 | \text{num dev} = 500 
         9 # Our validation set will be num validation points from the original
        10 # training set.
        11 | mask = range(num training, num training + num validation) ##[49000,50000)
        12 X val = X train[mask]
        13 y_val = y_train[mask]
        14
        15 # Our training set will be the first num_train points from the original
        16 # training set.
        17 mask = range(num training) ####[0,49000)
        18 X_train = X_train[mask]
        19 y_train = y_train[mask]
        20
        21 # We will also make a development set, which is a small subset of
        22 # the training set.
        23 mask = np.random.choice(num training, num dev, replace=False) #shape500
        24 X dev = X train[mask]
        25 y dev = y train[mask]
        26
        27 # We use the first num test points of the original test set as our
        28 # test set.
        29 mask = range(num test)
        30 X test = X test[mask]
        31 y test = y test[mask]
        33 print('Train data shape: ', X_train.shape)
        34 print('Train labels shape: ', y_train.shape)
        35 print('Validation data shape: ', X_val.shape)
        36 print('Validation labels shape: ', y val.shape)
        37 print('Test data shape: ', X test.shape)
        38 print('Test labels shape: ', y test.shape)
          Train data shape: (49000, 32, 32, 3)
          Train labels shape: (49000,)
```

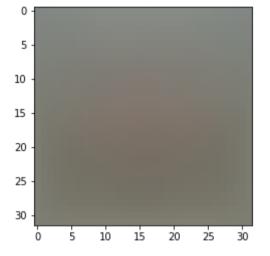
Validation data shape: (1000, 32, 32, 3)

Validation labels shape: (1000,)
Test data shape: (1000, 32, 32, 3)

Test labels shape: (1000,)

## 

[130.64189796 135.98173469 132.47391837 130.05569388 135.34804082 131.75402041 130.96055102 136.14328571 132.47636735 131.48467347]



### **SVM Classifier**

Your code for this section will all be written inside cs231n/classifiers/linear\_svm.py.

As you can see, we have prefilled the function compute\_loss\_naive which uses for loops to evaluate the multiclass SVM loss function.

```
In [9]:

# Evaluate the naive implementation of the loss we provided for you:
from cs23ln.classifiers.linear_svm import svm_loss_naive
import time

# generate a random SVM weight matrix of small numbers
# generate a random.randn(3073, 10) * 0.0001 ## 3073是数据集的特征数目3072再加上1,w中多出来的这一列对应的就是偏差值b

# Www.shape == (D,C) == (3073, 10) * **_dev.shape == (N,D) == (500,3073) **_y_dev.shape == (N,D) == (500,0)
loss, grad = svm_loss_naive(W, X_dev, y_dev, 0.000005)
print('loss: %f' % (loss, ))
```

loss: 8.943680

The grad returned from the function above is right now all zero. Derive and implement the gradient for the SVM cost function and implement it inline inside the function svm\_loss\_naive. You will find it helpful to interleave your new code inside the existing function.

To check that you have correctly implemented the gradient correctly, you can numerically estimate the gradient of the loss function and compare the numeric estimate to the gradient that you computed. We have provided code that does this for you:

```
1 # Once you've implemented the gradient, recompute it with the code below
In [10]:
          2 # and gradient check it with the function we provided for you
          4 # Compute the loss and its gradient at W.
          5 loss, grad = svm loss naive(W, X dev, y dev, 0.0)
          7 # Numerically compute the gradient along several randomly chosen dimensions, and
          8 # compare them with your analytically computed gradient. The numbers should match
          9 # almost exactly along all dimensions.
         10 from cs231n.gradient check import grad check sparse
         11 f = lambda w: svm loss naive(w, X dev, y dev, 0.0)[0]
         12 grad numerical = grad check sparse(f, W, grad)
         13
         14 # do the gradient check once again with regularization turned on
         15 # you didn't forget the regularization gradient did you?
         16 loss, grad = svm loss naive(W, X dev, y dev, 5e1)
         17 f = lambda w: svm loss naive(w, X dev, y dev, 5e1)[0]
         18 grad numerical = grad check sparse(f, W, grad)
```

```
numerical: 35.769934 analytic: 35.769934, relative error: 7.428433e-12
numerical: 10.757289 analytic: 10.757289, relative error: 3.039814e-11
numerical: 23.510778 analytic: 23.510778, relative error: 1.080096e-11
numerical: -0.769543 analytic: -0.769543, relative error: 8.175079e-11
numerical: 1.380252 analytic: 1.380252, relative error: 1.623525e-12
numerical: 2.838039 analytic: 2.838039, relative error: 2.467822e-11
numerical: 21.331356 analytic: 21.331356, relative error: 5.570144e-12
numerical: 6.749857 analytic: 6.749857, relative error: 9.462458e-12
numerical: 0.072874 analytic: 0.072874, relative error: 1.672515e-09
numerical: -14.212107 analytic: -14.212107, relative error: 4.358741e-12
numerical: -27.798089 analytic: -27.796582, relative error: 2.711249e-05
numerical: -36.294893 analytic: -36.298383, relative error: 4.807381e-05
numerical: 5.247237 analytic: 5.247207, relative error: 2.789185e-06
numerical: -8.238703 analytic: -8.239616, relative error: 5.542042e-05
numerical: -10.086545 analytic: -10.084483, relative error: 1.022036e-04
numerical: 16.459586 analytic: 16.459600, relative error: 4.199611e-07
numerical: -32.731761 analytic: -32.723241, relative error: 1.301718e-04
numerical: 0.874677 analytic: 0.880805, relative error: 3.490755e-03
numerical: 25.547095 analytic: 25.541069, relative error: 1.179465e-04
numerical: -51.988328 analytic: -51.988321, relative error: 6.908752e-08
```

#### **Inline Question 1:**

It is possible that once in a while a dimension in the gradcheck will not match exactly. What could such a discrepancy be caused by? Is it a reason for concern? What is a simple example in one dimension where a gradient check could fail? How would change the margin affect of the frequency of this happening? Hint: the SVM loss function is not strictly speaking differentiable

Your Answer: fill this in.

```
In [11]: 1 # Next implement the function sym loss vectorized; for now only compute the loss;
          2 # we will implement the gradient in a moment.
          3 tic = time.time()
          4 loss naive, grad naive = svm loss naive(W, X dev, y dev, 0.000005)
          5 toc = time.time()
          6 print('Naive loss: %e computed in %fs' % (loss naive, toc - tic))
          8 from cs231n.classifiers.linear svm import svm loss vectorized
          9 tic = time.time()
         10 loss vectorized, = svm loss vectorized(W, X dev, y dev, 0.000005)
         11 toc = time.time()
         12 print('Vectorized loss: %e computed in %fs' % (loss vectorized, toc - tic))
         13
         14 # The losses should match but your vectorized implementation should be much faster.
         15 print('difference: %f' % (loss naive - loss vectorized))
          Naive loss: 8.943680e+00 computed in 0.275538s
          Vectorized loss: 8.943680e+00 computed in 0.017083s
          difference: 0.000000
         1 # Complete the implementation of svm loss vectorized, and compute the gradient
          2 # of the loss function in a vectorized way.
          4 # The naive implementation and the vectorized implementation should match, but
          5 # the vectorized version should still be much faster.
          6 tic = time.time()
          7 , grad naive = svm loss naive(W, X dev, y dev, 0.000005)
          8 toc = time.time()
          9 print('Naive loss and gradient: computed in %fs' % (toc - tic))
         11 tic = time.time()
         12 , grad vectorized = svm loss vectorized(W, X dev, y dev, 0.000005)
         13 toc = time.time()
         14 print('Vectorized loss and gradient: computed in %fs' % (toc - tic))
         16 # The loss is a single number, so it is easy to compare the values computed
         17 # by the two implementations. The gradient on the other hand is a matrix, so
```

Naive loss and gradient: computed in 0.454984s Vectorized loss and gradient: computed in 0.006603s difference: 0.000000

19 difference = np.linalg.norm(grad naive - grad vectorized, ord='fro')

18 # we use the Frobenius norm to compare them.

20 print('difference: %f' % difference)

#### **Stochastic Gradient Descent**

We now have vectorized and efficient expressions for the loss, the gradient and our gradient matches the numerical gradient. We are therefore ready to do SGD to minimize the loss.

```
1 # In the file linear classifier.py, implement SGD in the function
In [13]:
                          2 # LinearClassifier.train() and then run it with the code below.
                          3 from cs231n.classifiers import LinearSVM
                          4 svm = LinearSVM()
                          5 tic = time.time()
                          6 loss hist = svm.train(X train, y train, learning rate=1e-7, reg=2.5e4,
                                                                                    num iters=1500, verbose=True)
                          8 toc = time.time()
                          9 print('That took %fs' % (toc - tic))
                         iteration 0 / 1500: loss 401.179673
                         iteration 100 / 1500: loss 236.957475
                         iteration 200 / 1500: loss 145.353562
                         iteration 300 / 1500: loss 89.138484
                         iteration 400 / 1500: loss 55.495465
                         iteration 500 / 1500: loss 35.054152
                         iteration 600 / 1500: loss 24.282576
                         iteration 700 / 1500: loss 16.155006
                         iteration 800 / 1500: loss 11.949770
                         iteration 900 / 1500: loss 9.582905
                         iteration 1000 / 1500: loss 7.003221
                         iteration 1100 / 1500: loss 6.624018
                         iteration 1200 / 1500: loss 6.332740
                         iteration 1300 / 1500: loss 5.313708
                         iteration 1400 / 1500: loss 5.623894
                         That took 9.446967s
In [14]:
                        1 # A useful debugging strategy is to plot the loss as a function of
                          2 # iteration number:
                          3 plt.plot(loss hist)
                          4 plt.xlabel('Iteration number')
                          5 plt.ylabel('Loss value')
                          6 plt.show()
                               400
                                350
                               300
                           250 Poss value 200 Po
                              150
                               100
                                 50
                                                               400
                                                                           600
                                                                                      800
                                                                                                1000
                                                                                                            1200
                                                    200
                                                                          Iteration number
In [15]: | 1 | # Write the LinearSVM.predict function and evaluate the performance on both the
                          2 # training and validation set
                          3 y train pred = svm.predict(X train)
                          4 print('training accuracy: %f' % (np.mean(y_train == y_train_pred), ))
                          5 y val pred = svm.predict(X val)
```

6 | print('validation accuracy: %f' % (np.mean(y\_val == y\_val\_pred), ))

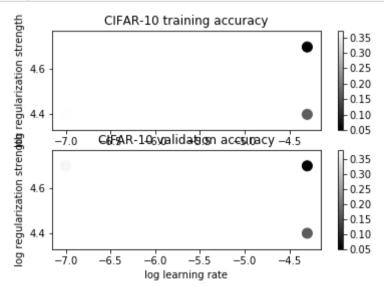
training accuracy: 0.377327 validation accuracy: 0.378000

```
In [16]:
        1 # Use the validation set to tune hyperparameters (regularization strength and
         2 # learning rate). You should experiment with different ranges for the learning
         3 | # rates and regularization strengths; if you are careful you should be able to
         4 # get a classification accuracy of about 0.4 on the validation set.
         5 learning rates = [1e-7, 5e-5]
         6 regularization strengths = [2.5e4, 5e4]
         8 # results is dictionary mapping tuples of the form
         9 # (learning rate, regularization strength) to tuples of the form
        10 # (training accuracy, validation accuracy). The accuracy is simply the fraction
        11 # of data points that are correctly classified.
        12 results = {}
        13 best val = -1 # The highest validation accuracy that we have seen so far.
        14 best svm = None # The LinearSVM object that achieved the highest validation rate.
        17 # TODO:
        18 # Write code that chooses the best hyperparameters by tuning on the validation #
        19 # set. For each combination of hyperparameters, train a linear SVM on the
        20 # training set, compute its accuracy on the training and validation sets, and #
        21 # store these numbers in the results dictionary. In addition, store the best
        22 # validation accuracy in best val and the LinearSVM object that achieves this
        23 # accuracy in best svm.
        24 #
        25 # Hint: You should use a small value for num iters as you develop your
        26 # validation code so that the SVMs don't take much time to train; once you are #
        27 # confident that your validation code works, you should rerun the validation
        28 # code with a larger value for num iters.
        30 # Your code
        31 num iters = 800 # test the para
        32 for lr in learning rates:
               for rs in regularization strengths:
        33
        34
                  svm = LinearSVM()
        35
                  svm.train(X_train, y_train, learning_rate=lr, reg=rs, num_iters=num_iters)
        36
        37
                  y train pred = svm.predict(X train)
                  train acc = np.mean(y_train == y_train_pred)
        38
        39
                  y val pred = svm.predict(X val)
        40
                  vali_acc = np.mean(y_val == y_val_pred)
        41
        42
                  results[(lr, rs)] = (train acc, vali acc)
        43
                  if best val < vali acc:</pre>
        44
        45
                      best val = vali acc
        46
                      best svm = svm
        47
            48
        49
                                       END OF YOUR CODE
           52 # Print out results.
        53 for lr, reg in sorted(results):
               train accuracy, val accuracy = results[(lr, reg)]
        55
               print('lr %e reg %e train accuracy: %f val accuracy: %f' % (
        56
                         lr, reg, train accuracy, val accuracy))
        57
        58 print('best validation accuracy achieved during cross-validation: %f' % best val)
```

lr 1.000000e-07 reg 2.500000e+04 train accuracy: 0.368061 val accuracy: 0.380000
lr 1.000000e-07 reg 5.000000e+04 train accuracy: 0.369980 val accuracy: 0.368000

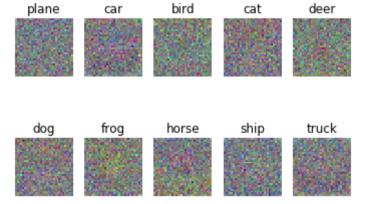
lr 5.000000e-05 reg 2.500000e+04 train accuracy: 0.167918 val accuracy: 0.167000 lr 5.000000e-05 reg 5.000000e+04 train accuracy: 0.049531 val accuracy: 0.049000 best validation accuracy achieved during cross-validation: 0.380000

```
In [17]: | 1 # Visualize the cross-validation results
          2 | import math
          3 x scatter = [math.log10(x[0]) for x in results]
          4 y scatter = [math.log10(x[1]) for x in results]
          6 # plot training accuracy
          7 marker size = 100
          8 colors = [results[x][0] for x in results]
          9 plt.subplot(2, 1, 1)
         10 plt.scatter(x scatter, y scatter, marker size, c=colors)
         11 plt.colorbar()
         12 plt.xlabel('log learning rate')
         13 plt.ylabel('log regularization strength')
         14 plt.title('CIFAR-10 training accuracy')
         15
         16 # plot validation accuracy
         17 colors = [results[x][1] for x in results] # default size of markers is 20
         18 plt.subplot(2, 1, 2)
         19 plt.scatter(x scatter, y scatter, marker size, c=colors)
         20 plt.colorbar()
         21 plt.xlabel('log learning rate')
         22 plt.ylabel('log regularization strength')
         23 plt.title('CIFAR-10 validation accuracy')
         24 plt.show()
```



linear SVM on raw pixels final test set accuracy: 0.362000

```
▶ In [19]: 1 # Visualize the learned weights for each class.
            2 # Depending on your choice of learning rate and regularization strength, these may
            3 # or may not be nice to look at.
            4 w = best svm.W[:-1,:] # strip out the bias
            5 \text{ w = w.reshape(32, 32, 3, 10)}
            6 w_min, w_max = np.min(w), np.max(w)
            7 classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', 'ship', 'truck']
            8 for i in range(10):
            9
                  plt.subplot(2, 5, i + 1)
           10
                  # Rescale the weights to be between 0 and 255
           11
           12
                  wimg = 255.0 * (w[:, :, i].squeeze() - w_min) / (w_max - w_min)
           13
                  plt.imshow(wimg.astype('uint8'))
           14
                  plt.axis('off')
           15
                  plt.title(classes[i])
```



### Inline question 2:

Describe what your visualized SVM weights look like, and offer a brief explanation for why they look they way that they do.

Your answer: fill this in