



# CMP201 – Data Structures and Algorithms 1 Coursework

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# Comparison Between Lee and A\* Pathfinding Algorithms For Pathfinding With Seabed Bathymetry Data

# Problem

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# The Real-world Problem

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In the offshore tidal energy industry there is often a requirement to route subsea cables on the seabed. These routes need to factor in both the distance of a cable run and smoothness of the seabed for this run as the cables experience excess fatigue and movement on the seabed if they have any unsupported spans.

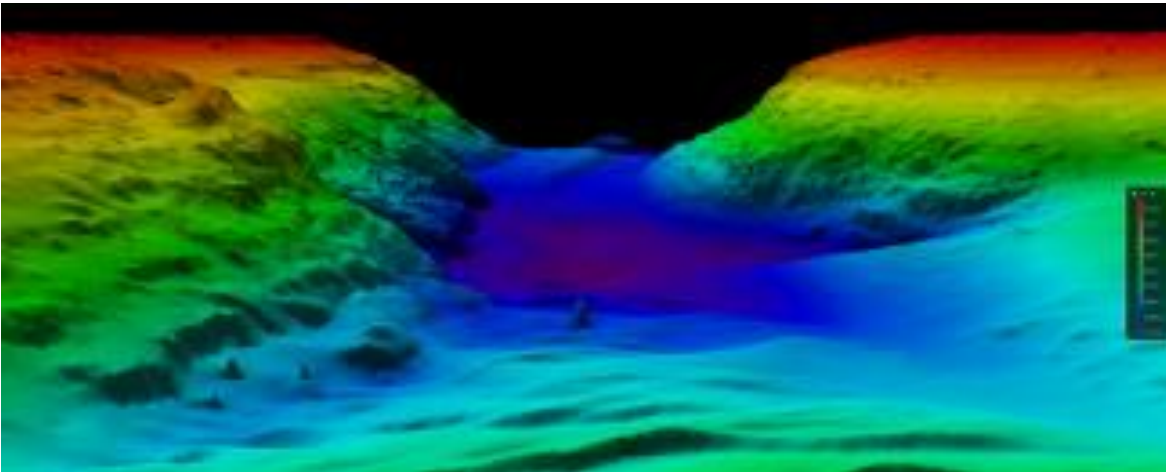
This project set out to implement a method to calculate these routes between a selected start point and endpoint.

# Bathymetry Data

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# Bathymetry Data

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National Centers for Environmental Information (2020). Available at [https://www.ncei.noaa.gov/sites/default/files/styles/max\\_325x325/public/sites/default/files/bathymetry-image-1200x480.png?itok=82loqMAs](https://www.ncei.noaa.gov/sites/default/files/styles/max_325x325/public/sites/default/files/bathymetry-image-1200x480.png?itok=82loqMAs)

Bathymetry Data is a 3D representation of the seabed gathered from a set of depth and position results. When interpolated and plotted as a contour or surface they give a 3D representation of the seabed.

# Bathymetry Data

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The data used for this project is a small sample of the bathymetry data for the North Connel River, UK Hydrographic Office Survey (2014 HI1441 Loch Etive 2m SDTP).

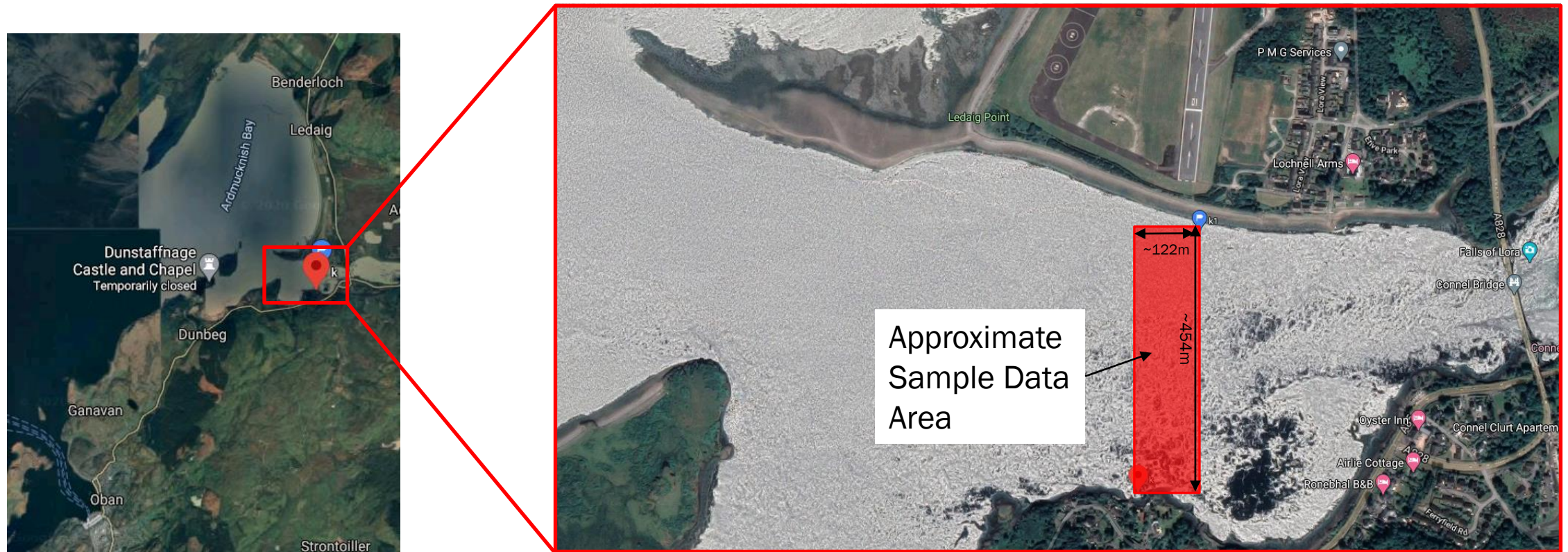
(Admiralty Marine Data Portal (2020). Available at:

[https://datahub.admiralty.co.uk/Bathy\\_Data/Prodbathy/Bathymetry/2014%20HI1441%20Loch%20Etive%202m%20SDTP.bag](https://datahub.admiralty.co.uk/Bathy_Data/Prodbathy/Bathymetry/2014%20HI1441%20Loch%20Etive%202m%20SDTP.bag))

Data converted from .bag to .csv using commercially available Global Mapper software



# Bathymetry Data



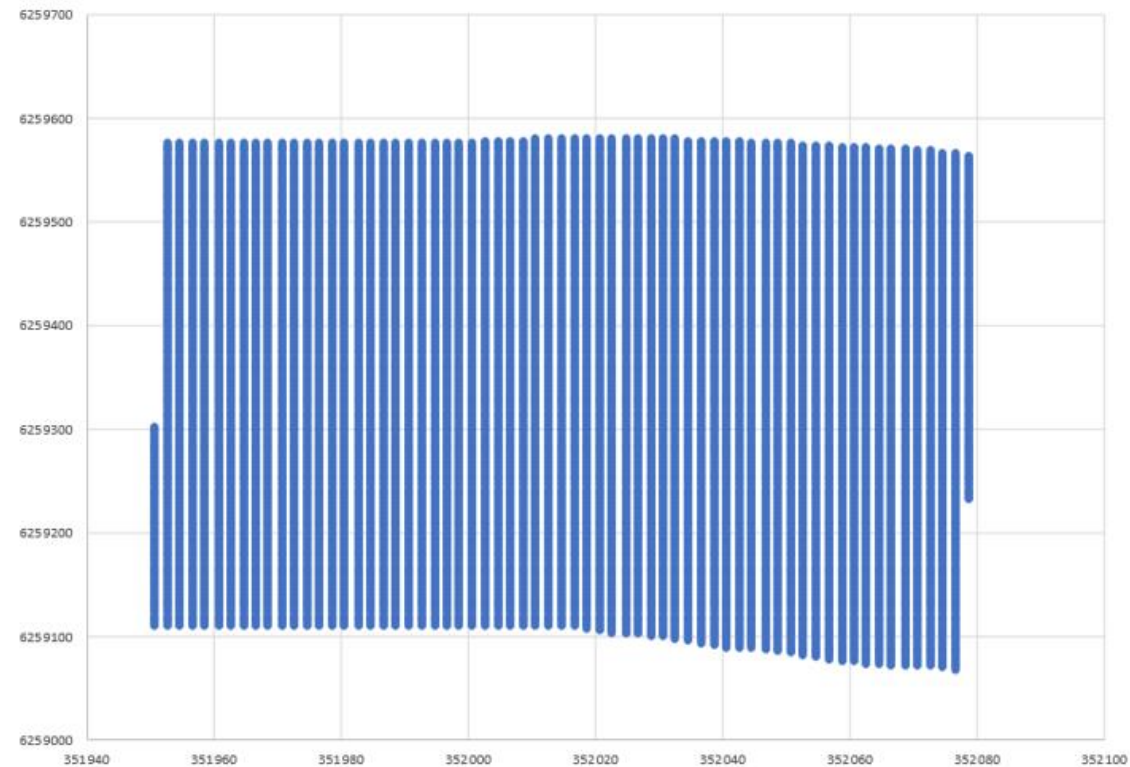
Google Maps(2020). Available at [https://www.google.com/maps?q=google+maps+connel&rlz=1C1CHBF\\_en-GBGB792GB792&um=1&ie=UTF-&sa=X&ved=2ahUKewjwgp3Bs4DuAhXlh1wKHSG-AGAQ\\_AUoAXoECAyQAw](https://www.google.com/maps?q=google+maps+connel&rlz=1C1CHBF_en-GBGB792GB792&um=1&ie=UTF-&sa=X&ved=2ahUKewjwgp3Bs4DuAhXlh1wKHSG-AGAQ_AUoAXoECAyQAw)



# Bathymetry Data

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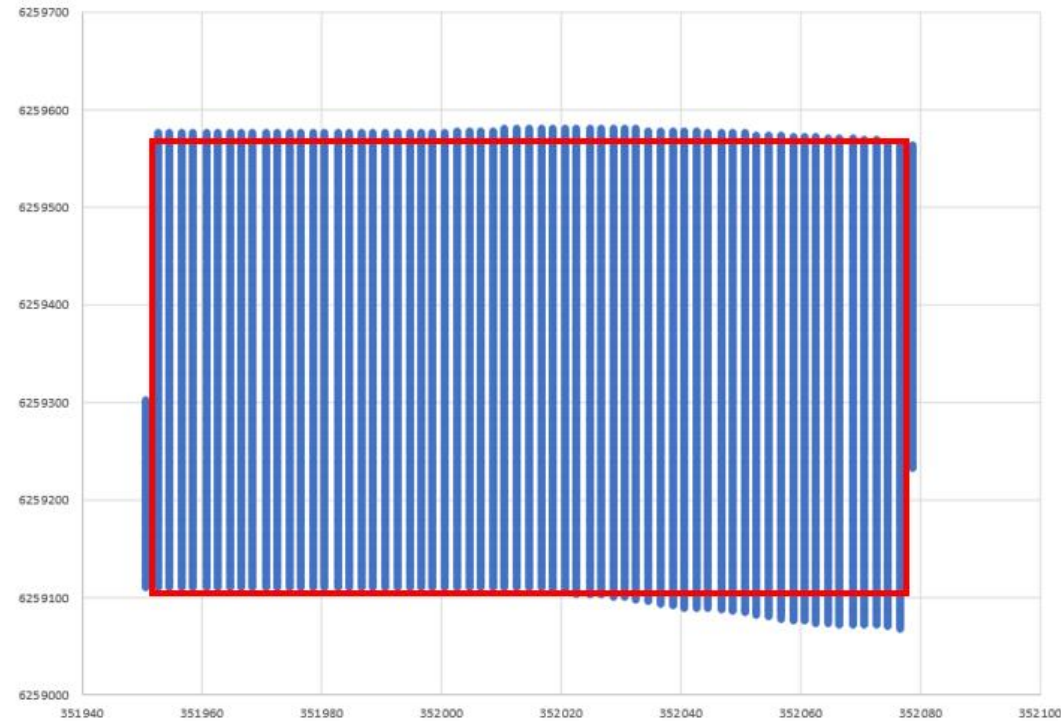
Data is a grid of discrete point in rows and columns as shown below:



# Bathymetry Data

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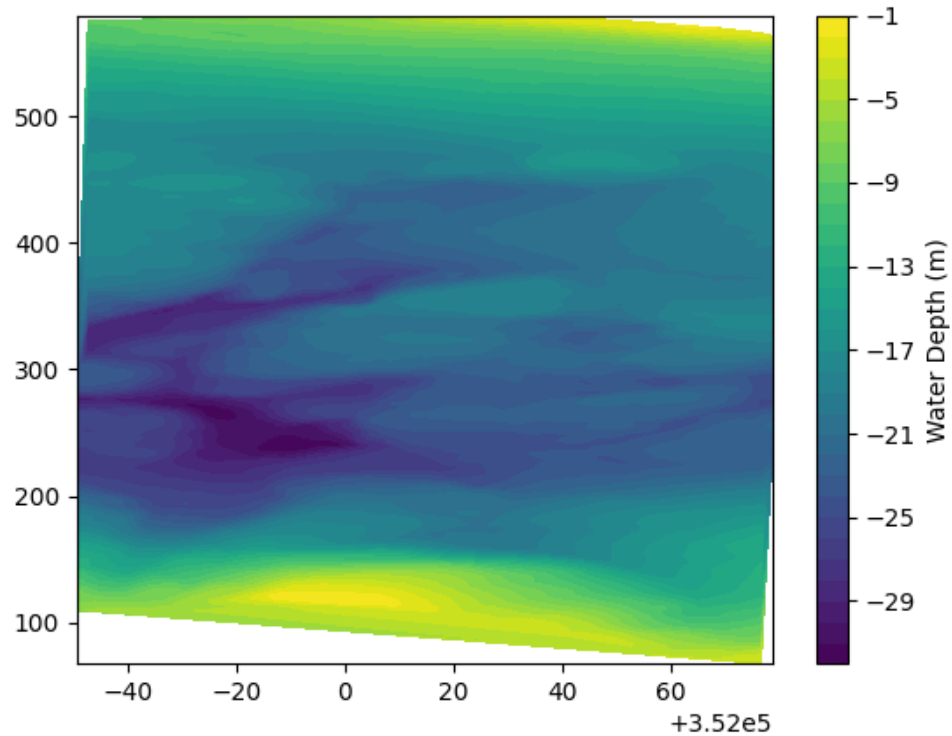
To make the data easier to process for this program the dataset has been trimmed:



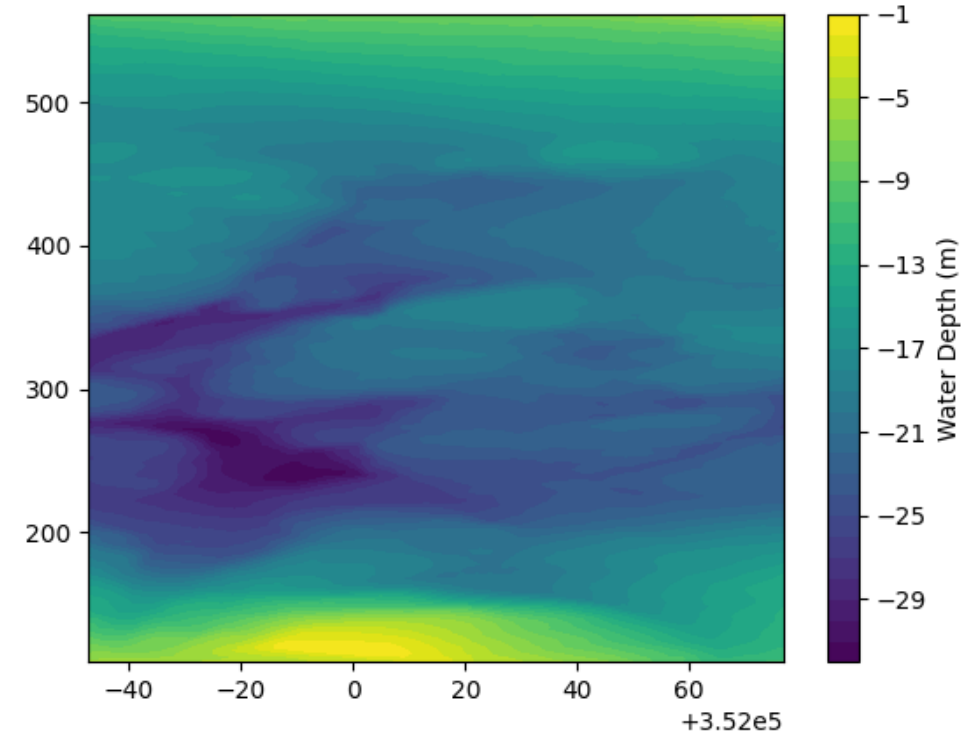
# Bathymetry Data

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Full Dataset



Trimmed Dataset

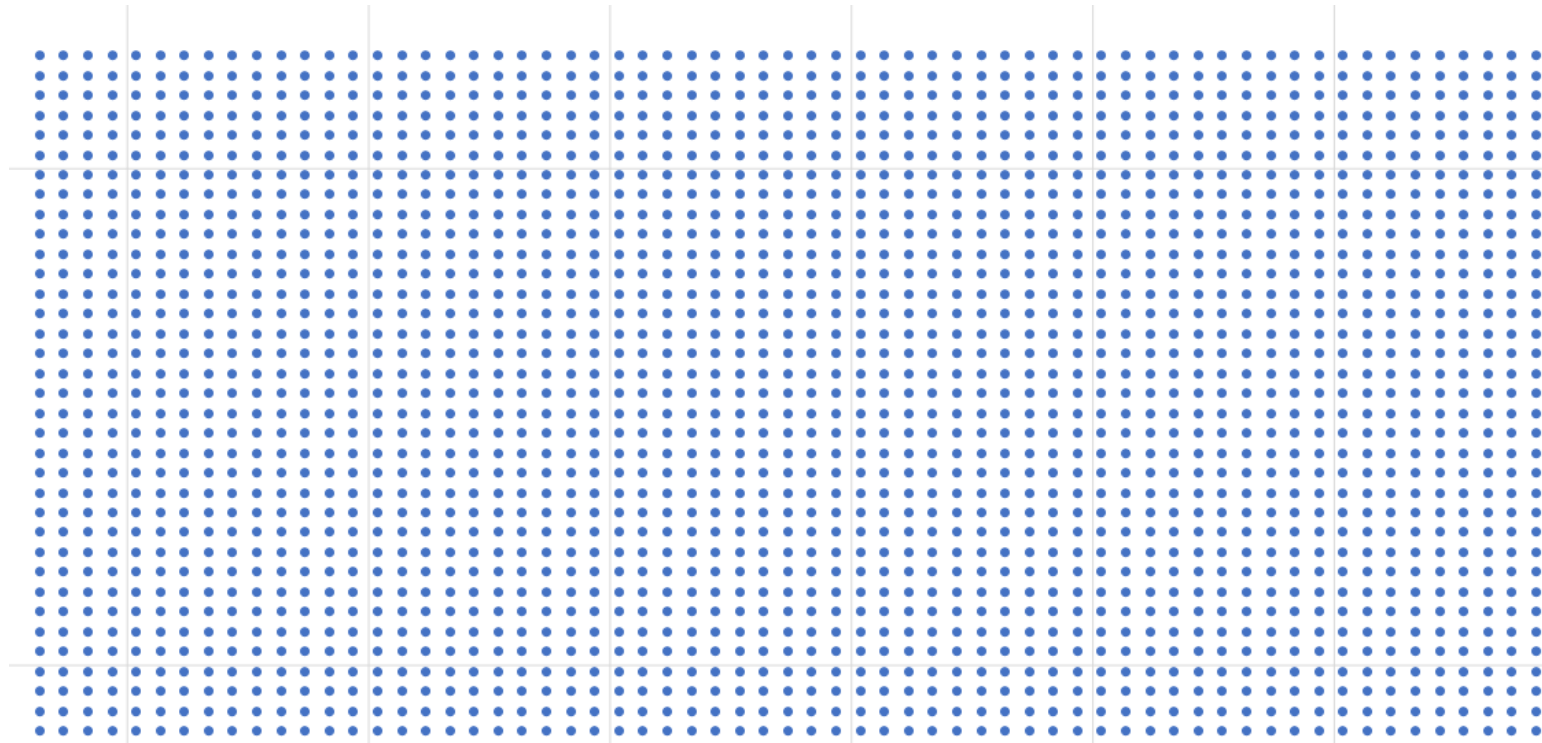


All Bathymetry plots except where referenced are plotted using the `PlotterV1.3.py` python script using Mathplotlib included in source code directory.

# Bathymetry Data

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Zoomed data showing the grid of point spaced by 2m



# Representation of Data

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As the bathymetry data itself is a grid of discrete points the choice was made to represent the data as a grid for the pathfinding algorithm. As the size of the data grid is not fixed the decision was made to use a **2D vector**. `std::vector<std::vector<node>>`, with the node being the relevant node type for each pathfinding algorithm.

The **population of this grid has a time complexity  $O(N^2)$**  however, this operation only needs to take place one at the start of the pathfinding function and no additional items need to be inserted into the 2D vector at a later stage.

One advantage of this approach is that to **access each element for pathfinding has a time complexity of  $O(1)$** .

# A\* Heuristic

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The heuristic selected for this A\* algorithm has was the Manhattan Distance because of this the route movement has been limited to **4 directions (up, down, left, right)**.

The Manhattan Distance is calculated:

**Manhattan Distance = minimum distance between nodes X (absolute  $\Delta x$  between this node and goal + absolute  $\Delta y$  between this node and goal)**



# A\* Open & Closed Lists

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## Open List

A custom implementation of a priority queue has been implemented for the A\* open list, **PriorityQueue**. This queue acts as a standard queue for **Push()** and **Pop()** but it will insert the Nodes in order of F-Cost of each node when the Push() is used. This means you have a worst-case insertion complexity of **O(N)** where N is the number of items in the queue and a **Pop()/Lowest()** complexity of **O(1)**. Push() resolves conflicts by adding the most recent at the end of the block of equal items, this is to maintain the FIFO characteristics of the Queue.

# A\* Open & Closed Lists

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## Closed List

An `std::unordered_set` has been used to store the closed list nodes, this has been selected because the order of this set is not important for the algorithm. The unordered set is based on hashtables so all operations on the unordered set are  **$O(1)$** .

# 'Smoothness' Weighting

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To account for adapting the route to find the shortest smoothest route each algorithm includes a weighting base on the difference in depth between the current node and the node being assessed.

For the Lee algorithm this is calculated as the difference in depth and added to the Distance value in the **LeeNode**, this summed value is saved in the **WeightedDistance**. It is this **WeightedDistance** that is used to find the shortest path in back track phase.

For the A\* algorithm this difference in depth is added to the **G\_Cost** for each **AStarNode**, so the **G\_Cost** of each node is calculated as:

**G\_Cost = Distance from this node to start point + abs(previous node depth – this node depth)**

# AStarNode

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Each AStarNode contains the below data:

- G\_Cost – Distance from this node to the start node
- H\_Cost – Estimated distance from this node to the goal
- F\_Cost – Total Node Cost ( $G\_Cost + H\_Cost$ )
- Depth – Depth of node based on bathymetry
- Distance – Distance between this node and the previous node
- Position – Relative position of node within the AStarGrid
- UtmPosition – Real-world UTM position of this node
- ParentNode – A pointer to the parent node of this node
- Visited – Set to true when a node has been visited and added to the closed set

# LeeNode

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Each LeeNode contains the below data:

- Position - Relative position of node within the LeeGrid
- UtmPosition - Real-world UTM position of this node
- Distance – Distance from this node to the start node
- WeightedDistance – Distance adjusted for depth bias (Depth + Difference in depth between nodes).
- Depth - Depth of node based on bathymetry

# Optimizations

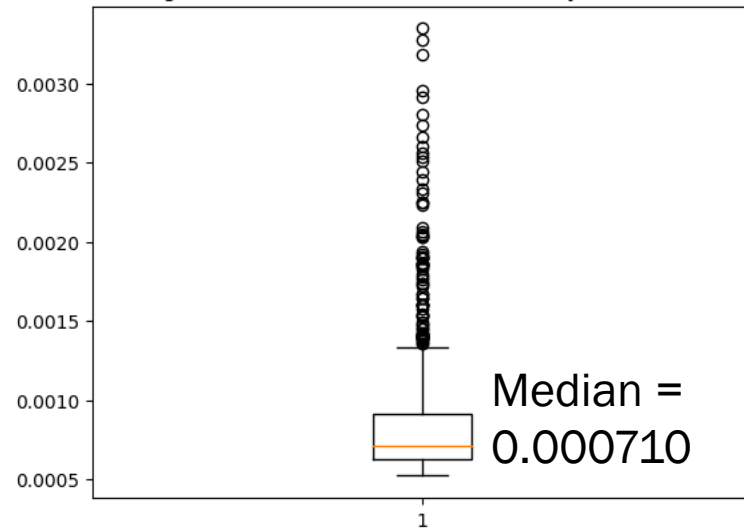
## Top Functions

Function Name	Total CPU [unit, %]	Self CPU [unit, %] 🔥
[External Code]	1993 (99.75%)	917 (45.90%)
Lee::initializeGrid	460 (23.02%)	215 (10.76%)
AStar::AStarPath	611 (30.58%)	181 (9.06%)
Lee::flood	144 (7.21%)	124 (6.21%)
AStar::createAStarGrid	233 (11.66%)	113 (5.66%)

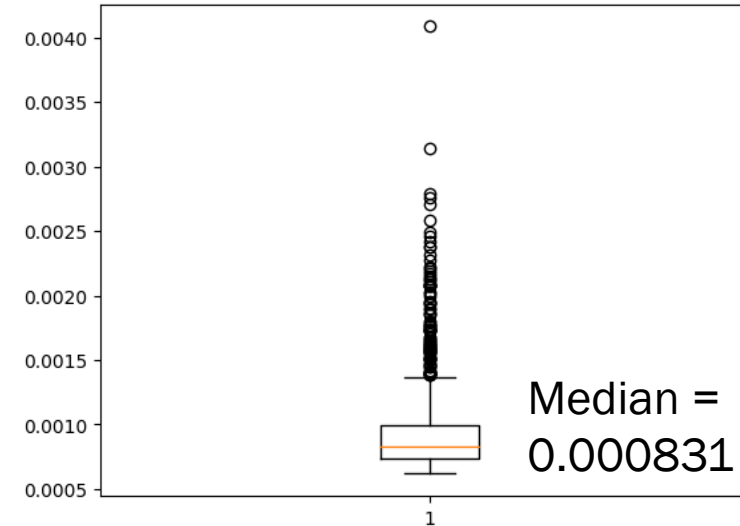
## Top Functions

Function Name	Total CPU [unit, %]	Self CPU [unit, %] 🔥
[External Code]	2214 (99.95%)	953 (43.02%)
AStar::createAStarGrid	375 (16.93%)	257 (11.60%)
Lee::initializeGrid	469 (21.17%)	224 (10.11%)
AStar::AStarPath	721 (32.55%)	172 (7.77%)
Lee::flood	165 (7.45%)	144 (6.50%)

A\* Algorithm Box Plot - Grid Generation By Col Then Row



A\* Algorithm Box Plot - Grid Generation By Row Then Col



All Boxplots are plotted using the BoxPlotter.py python script using Matplotlib included in source code



# Results

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# Results

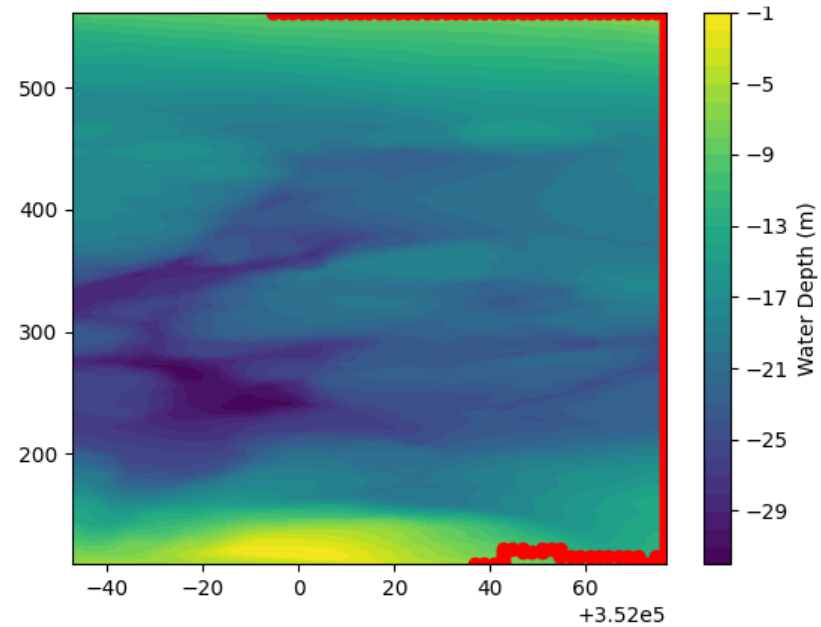
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- All results have been collected over 1000 executions of the code and the median value used to account for an non-normal data distribution.
- All other programs were closed during performance tests
- Start point, end point and dataset were kept the same for each comparison run direct comparison
- All debug code was removed from pathfinding functions before performance tests and release compile used
- Only the pathfinding algorithm time is measured all .csv writing is done after timer is stopped.
- The Steady\_clock was used to use monotonic time. This was used as intervals are constant and not affected by changes in the system clock, reducing errors introduced by changing system load.

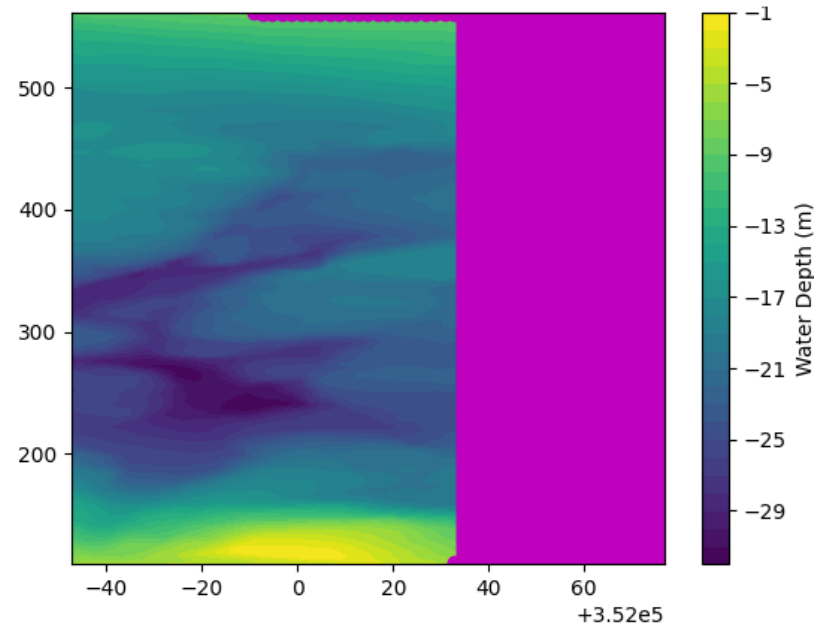
# Plot 1 - Lee

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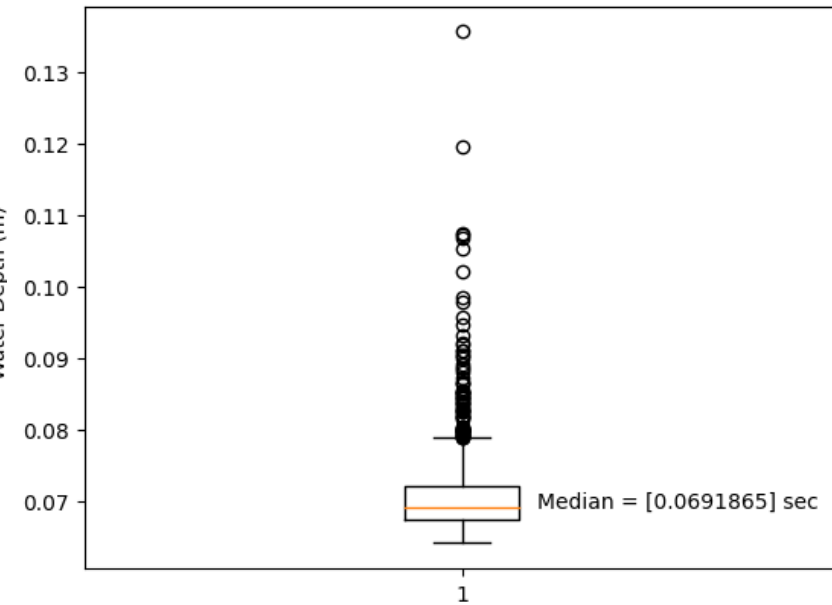
Full Data - Lee Path Plot 1



Full Data - Lee Visited Plot 1



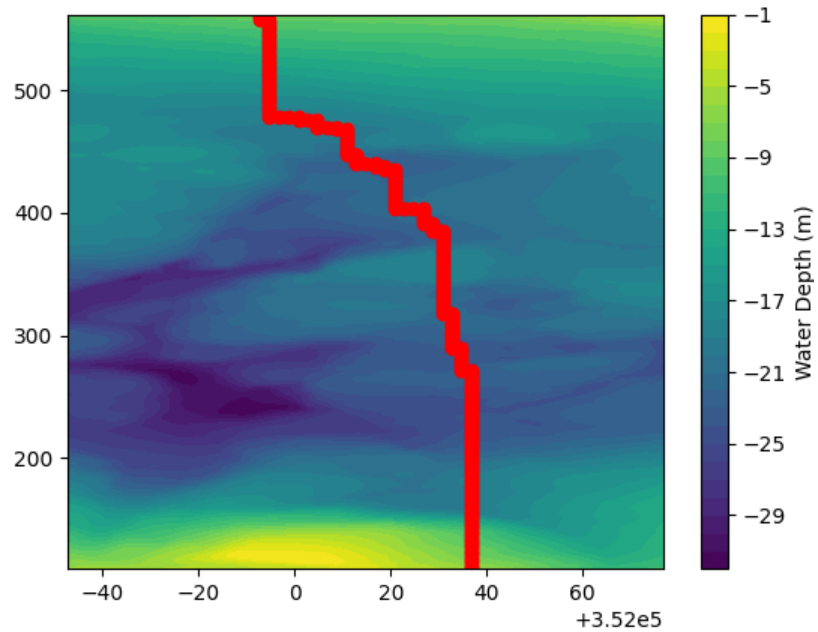
Full Data - Lee Performance Plot 1



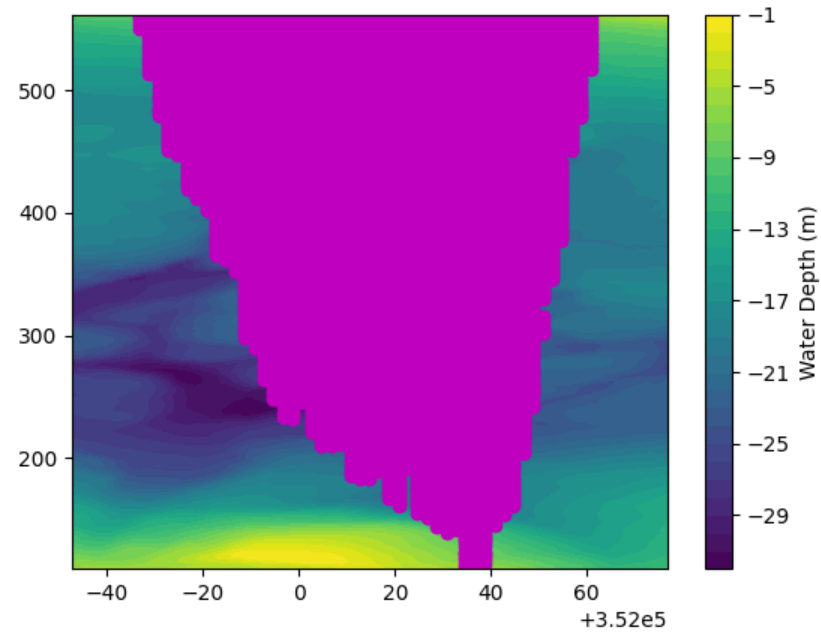
# Plot 1 – A\*

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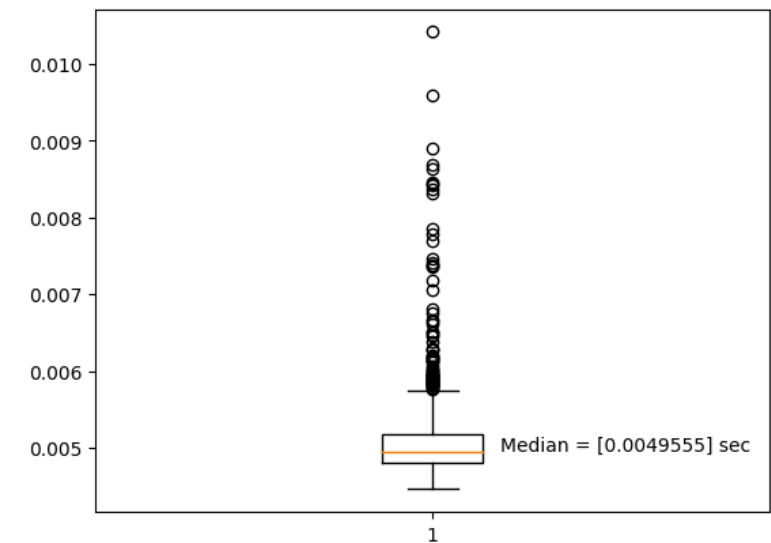
Full Data – A\* Path Plot 1



Full Data – A\* Visited Plot 1



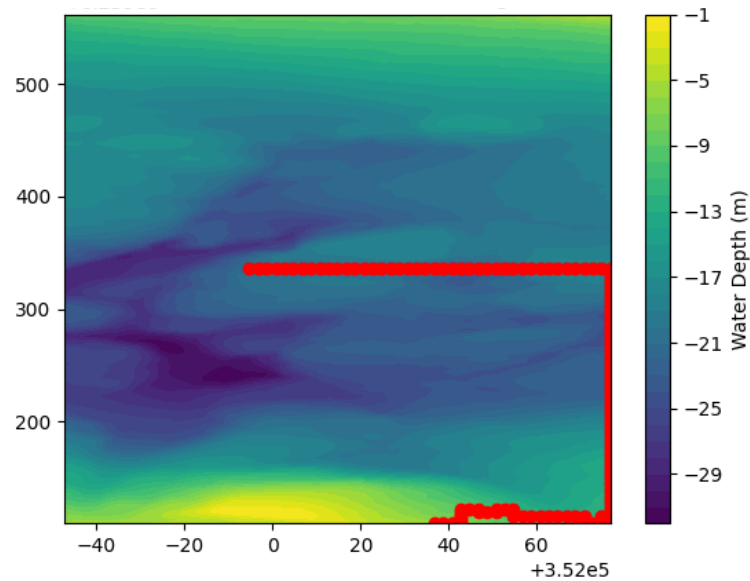
Full Data – A\* Performance Plot 1



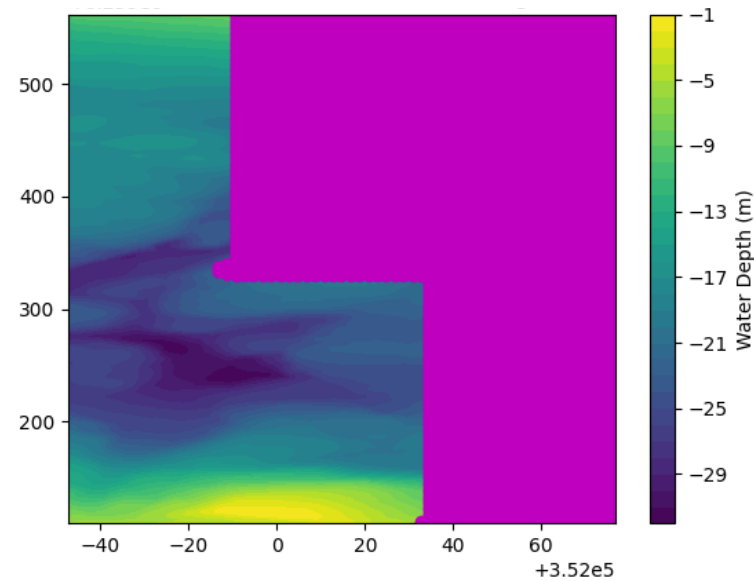
# Plot 2 – Lee

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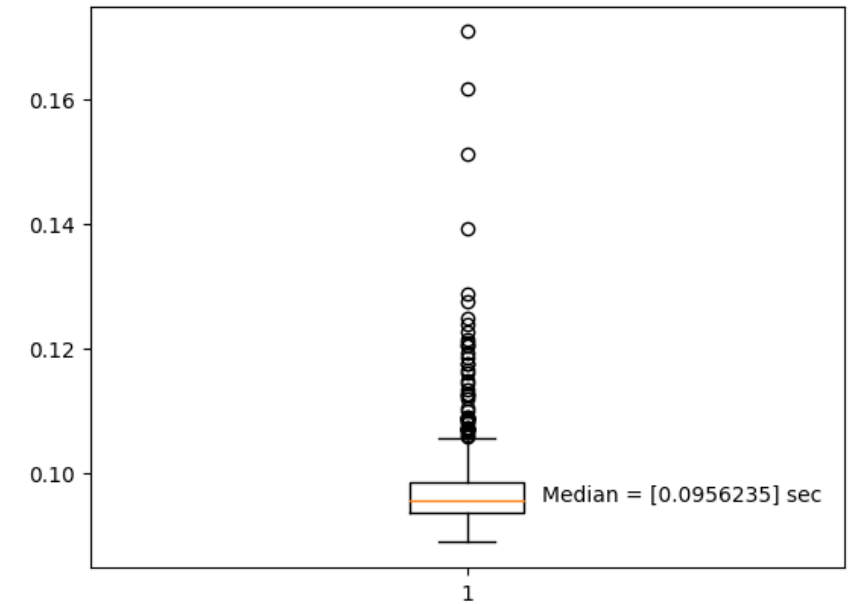
Full Data – Lee Path Plot 2



Full Data – Lee Visited Plot 2



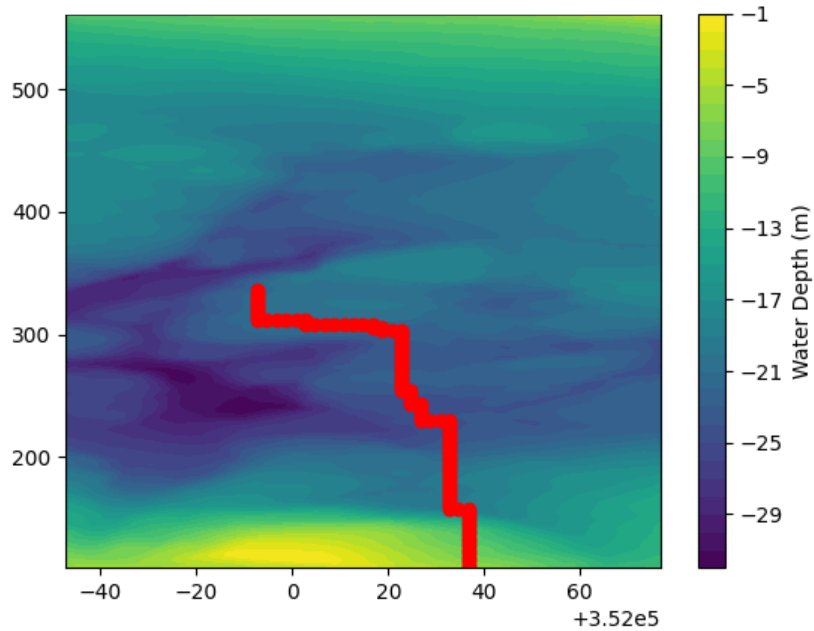
Full Data – Lee Performance Plot 2



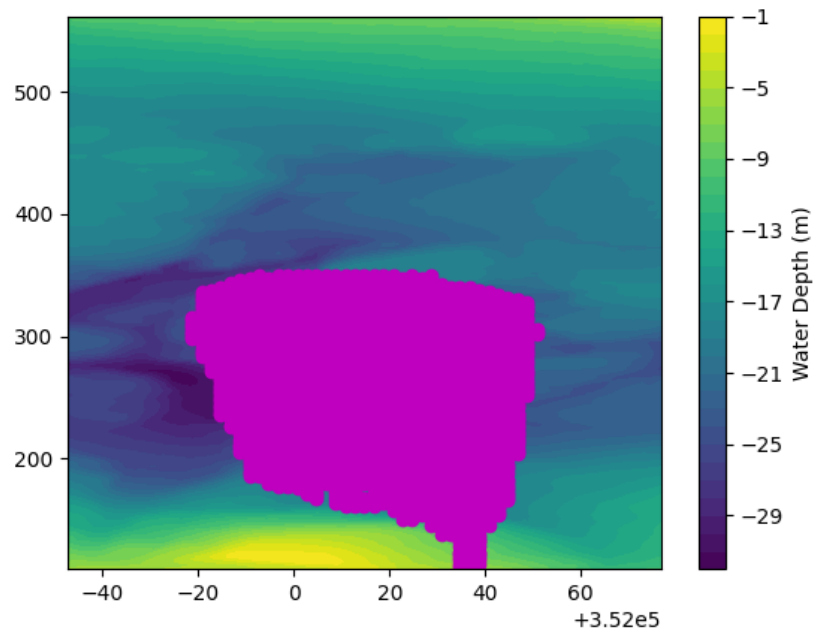
# Plot 2 – A\*

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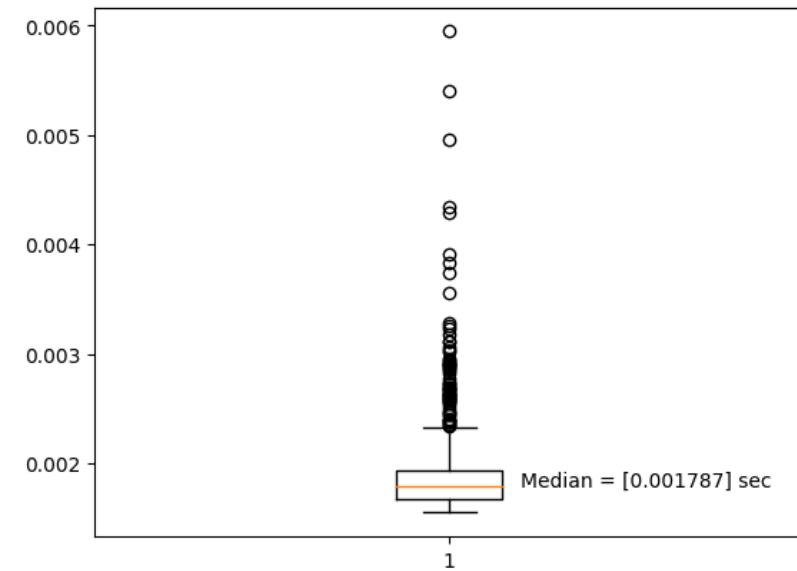
Full Data – A\* Path Plot 2



Full Data – A\* Visited Plot 2



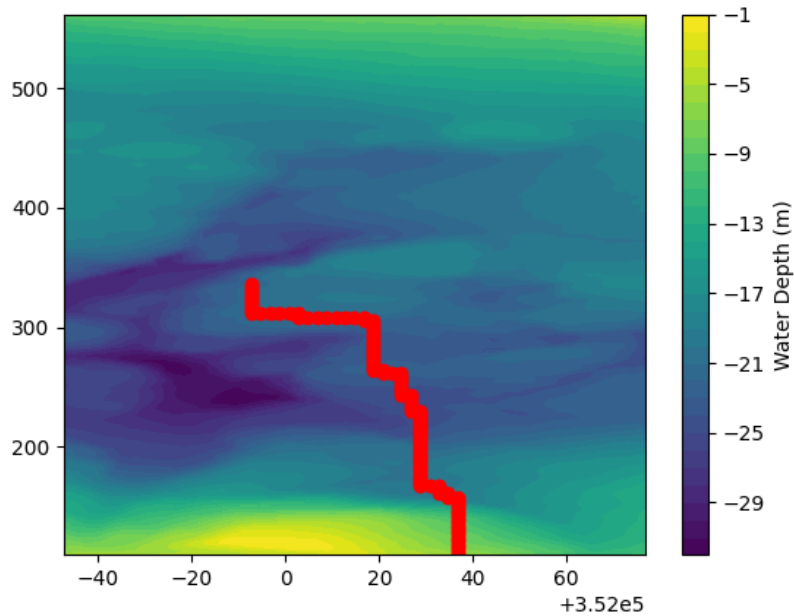
Full Data – A\* Performance Plot 2



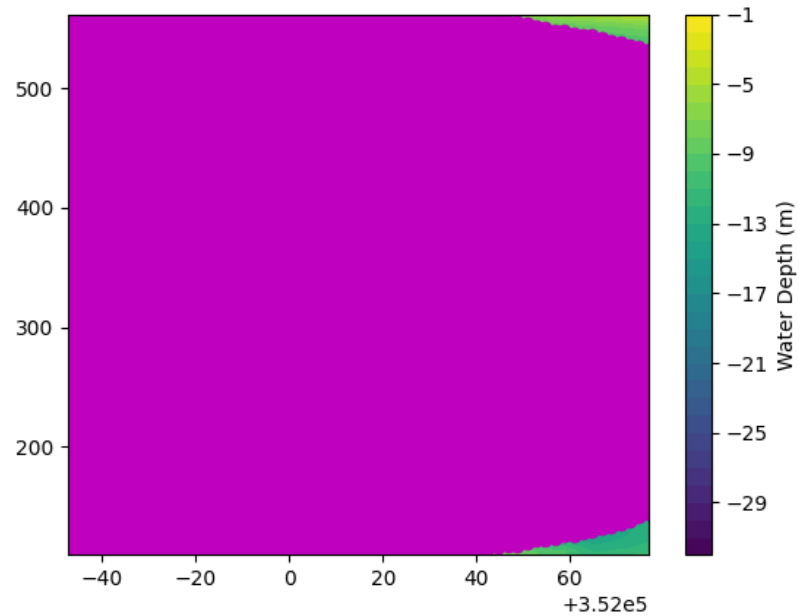


# Plot 2 – Dijkstra

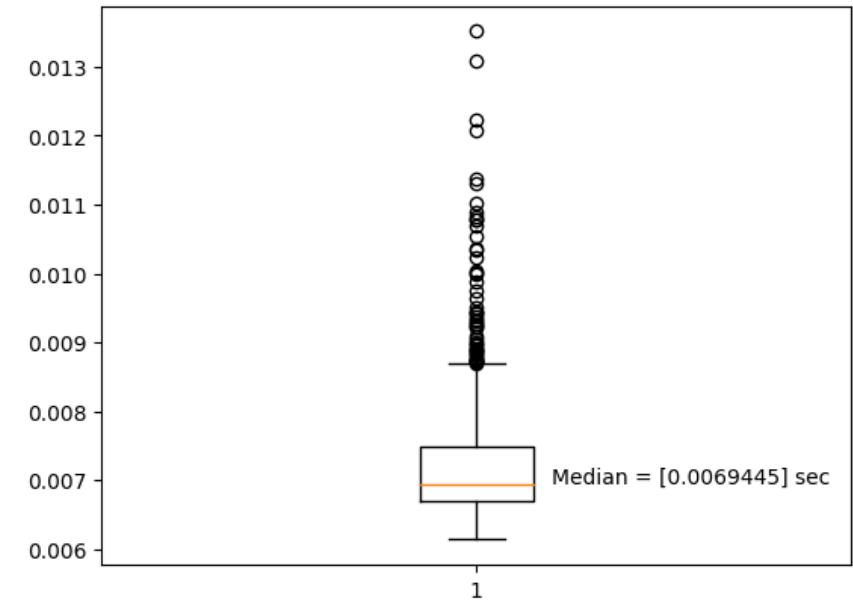
Full Data – Dijkstra Path Plot 2



Full Data – Dijkstra Visited Plot 2



Full Data – Dijkstra Performance Plot 2



This route is to confirm that the A\* heuristic is finding the same route. There are some very minor differences but this does mainly match the A\* path.

# Summary

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Algorithm	Plot 1 – Median Time (Seconds)	Plot 1 – Percentage Execution Time Increase Over A*	Plot 2 – Median Time (Seconds)	Plot 2 – Percentage Execution Time Increase Over A*
Lee	0.0691865	1296.16%	0.0956235	5251.06%
A*	0.0049555		0.0017870	
Dijkstra			0.0069445	288.612%

For both Plot 1 & Plot 2 the A\* algorithm was the fastest. The A\* algorithm was faster than the Lee algorithm by 0.064231 sec (1296.16% increase over A\*) for plot 1 and 0.0938365 sec (5251.06% increase over A\*) for Plot 2.

For comparison for Plot 2 the Dijkstra algorithm was included, this was 0.0051575 sec (288.612% increase over A\*).

# A\* Varying Data Size

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Predicted Best Case:

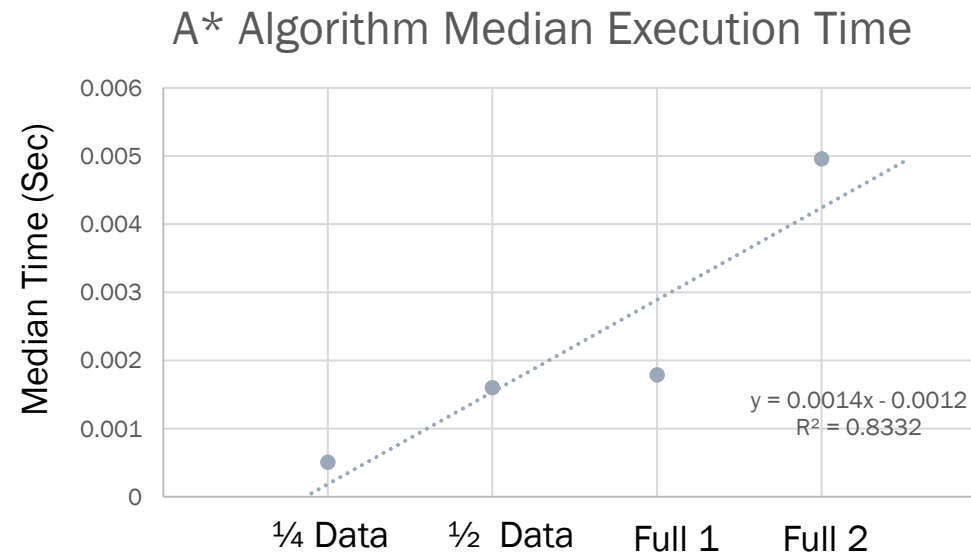
$O(N)$

**Where N is path**

Worst Case:

$O(NM)$  (NM are grid width

**And height)**



This Implementation is between the 2 cases and is closer to the best case

# Lee\* Varying Data Size

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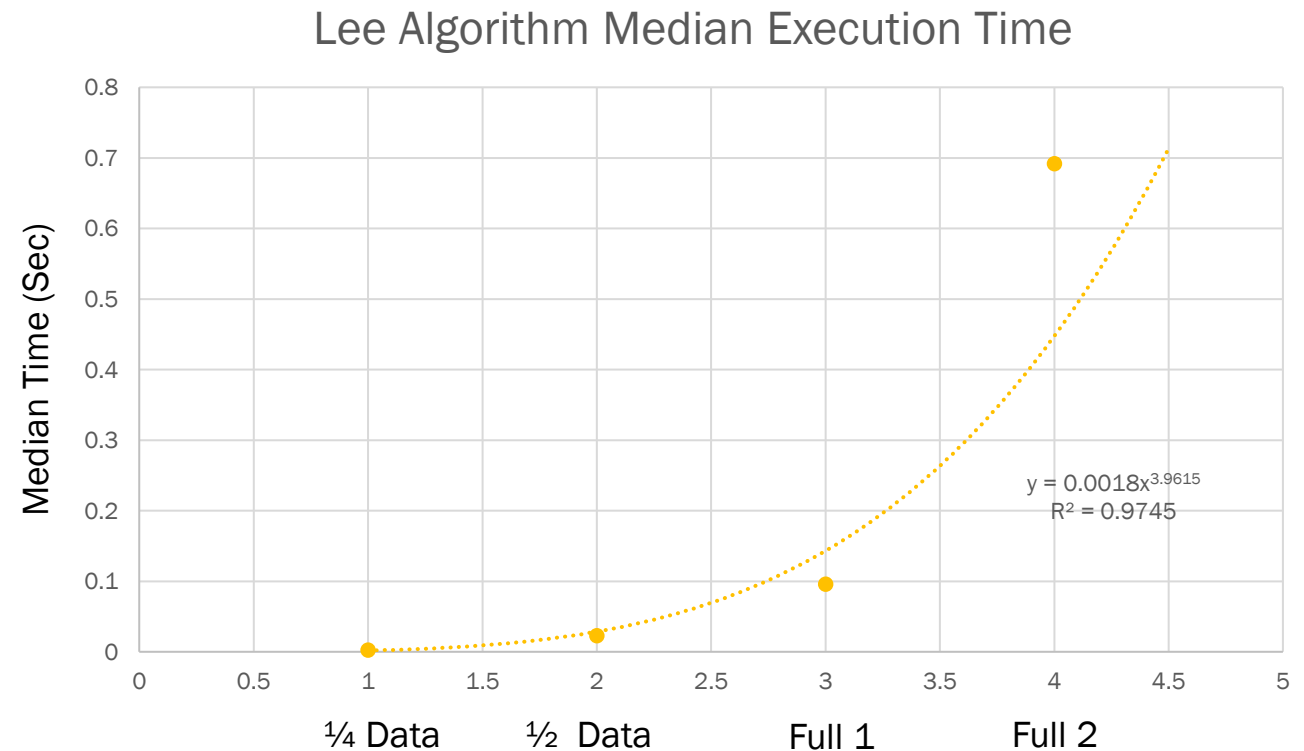
Predicted Performance:

$O(NM)$

(NM are grid width

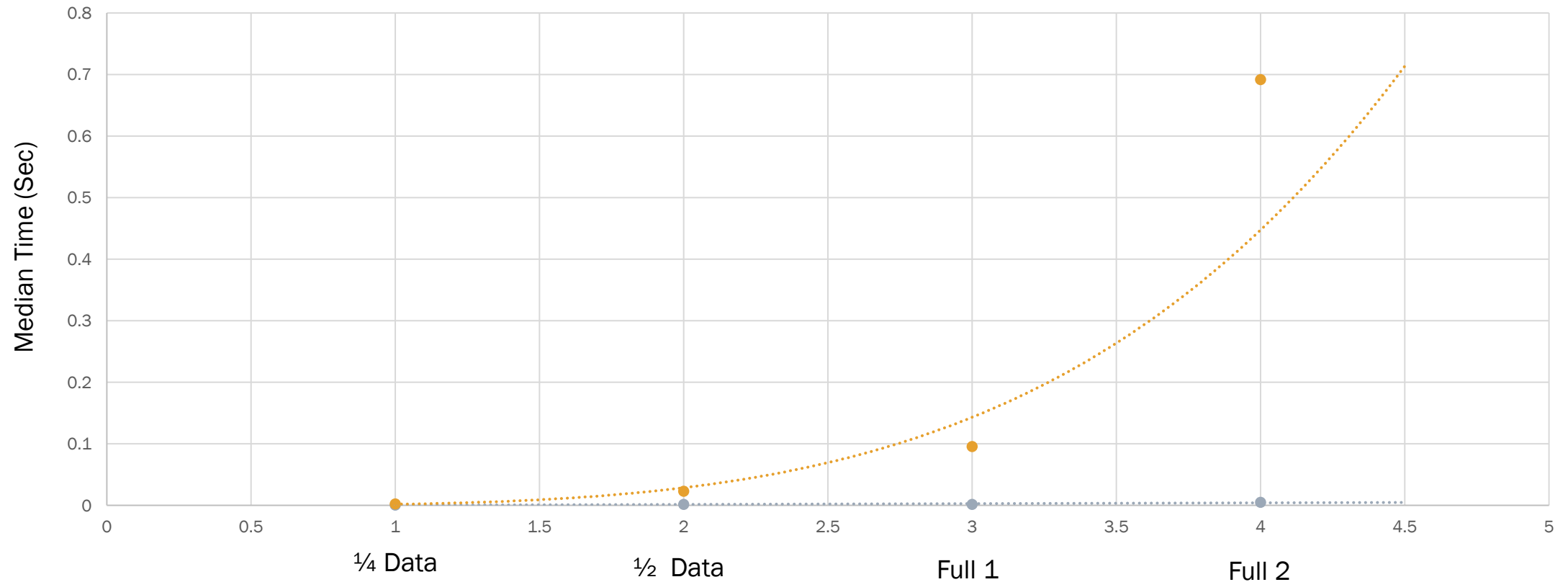
And height)

This Implementation slightly worse then the  
predicted  $O(NM)$  especially for Plot 2



# Combined Performance

Comparison Of Median Execution Time A\* and Lee Pathfinding Algorithms



# Conclusion

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# Conclusion

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The A\* algorithm is the most efficient method of finding a path on the bathymetry. This implementation of the algorithm is close to the best case of  $O(N)$  when compared to Dijkstra's algorithm there is very small difference in the path found, this suggests that some further adjustments might be needed to the A\* Heuristic to ensure it guarantees the shortest, smoothest path.

For certain cases to when start and end points are inline or at the dataset boundaries the Lee algorithm can be fairly efficient (e.g. Plot 1). However, as soon as the end point is at the centre of the grid (e.g. Plot 2) the algorithm runtime increases beyond the predicted  $O(NM)$ .

# Reflection Points

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- Having the Lee algorithm terminate its search when it finds the end node was a choice to reduce the total number of nodes searched. However, this means that the guaranteed shortest path is not found.
- For data set where a path along the boundary is not wanted a weighting should be applied as part of the H-Cost calculation to check the distance from the dataset boundary.

# Questions

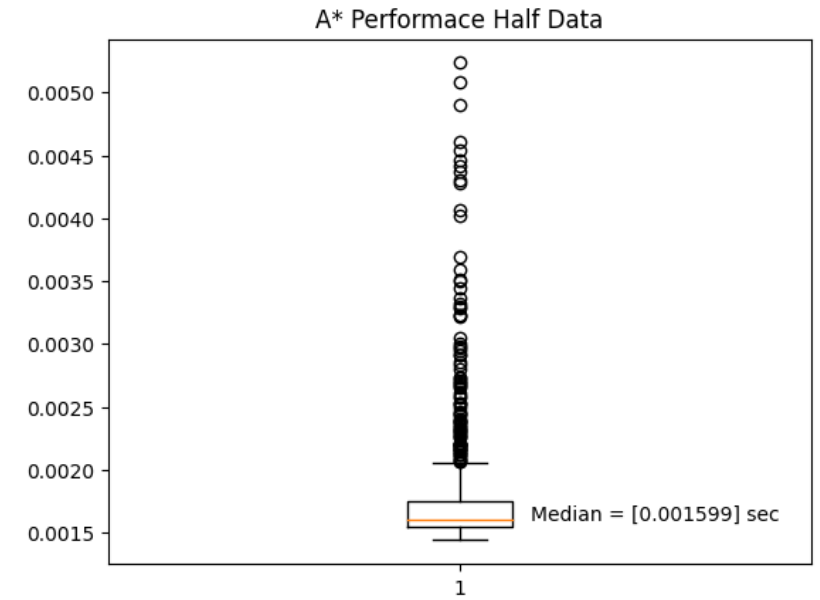
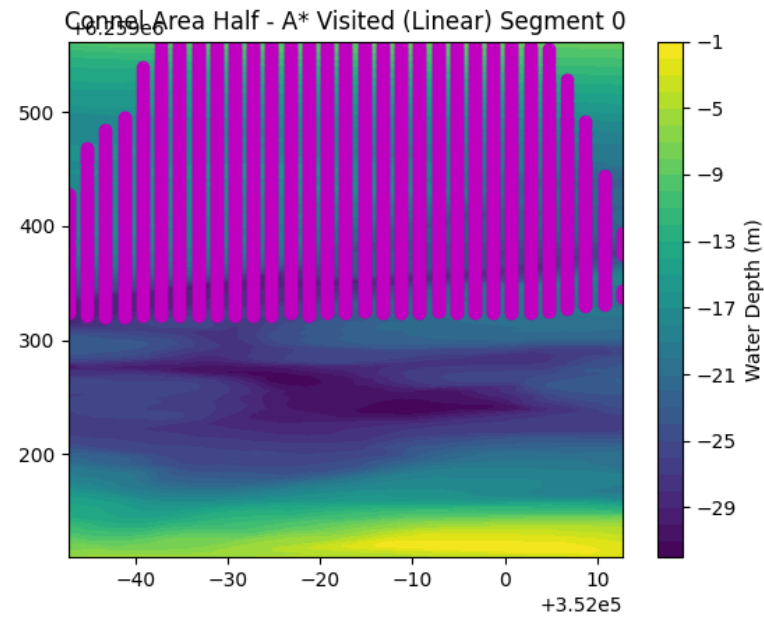
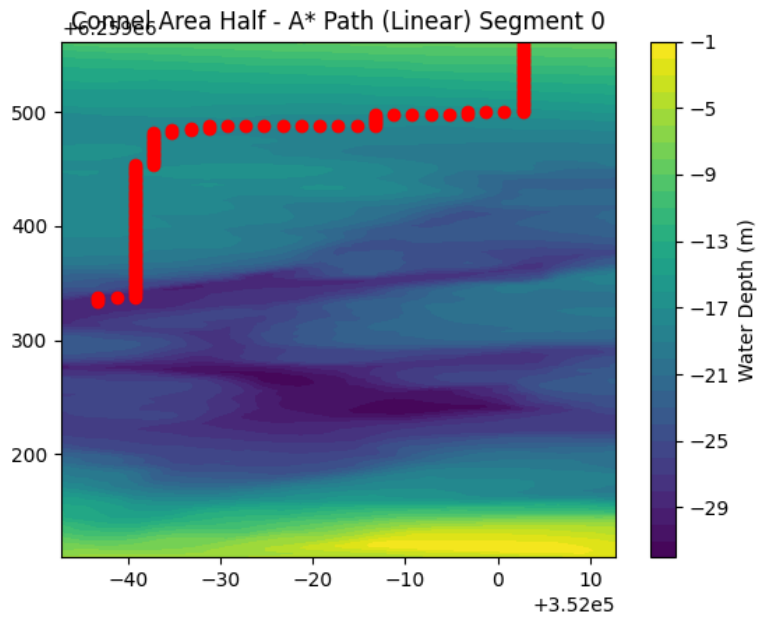
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# Appendices

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# Half Dataset – A\*

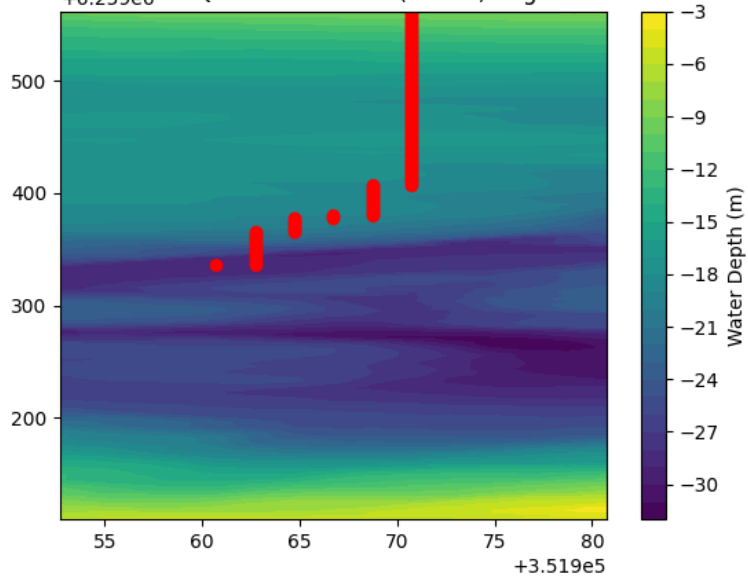
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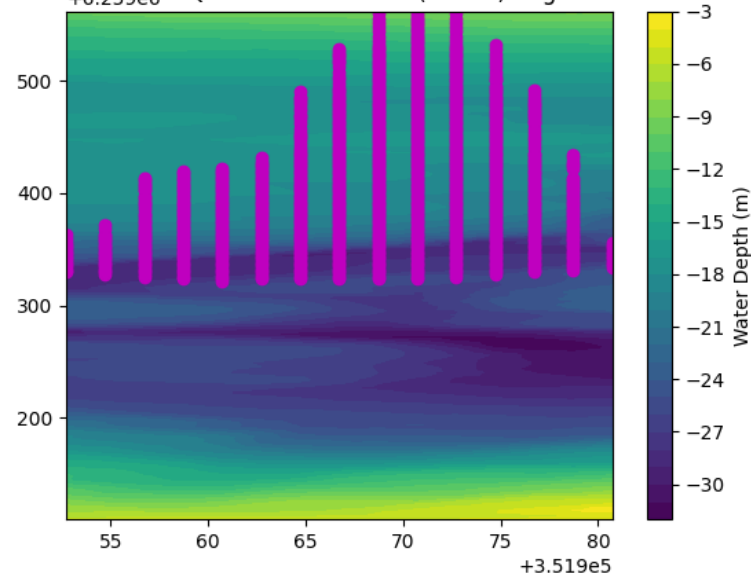
# Quarter Dataset – A\*

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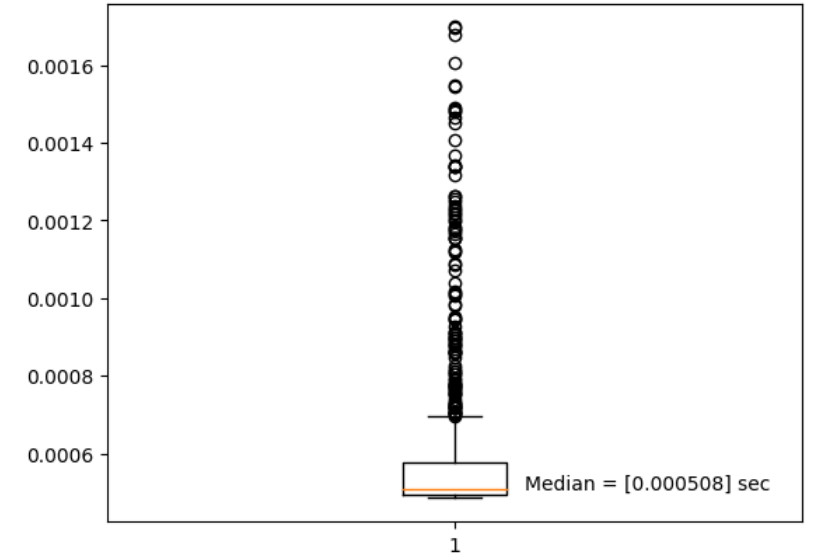
Connel Area Quarter - A\* Path (Linear) Segment 0



Connel Area Quarter - A\* Visited (Linear) Segment 0

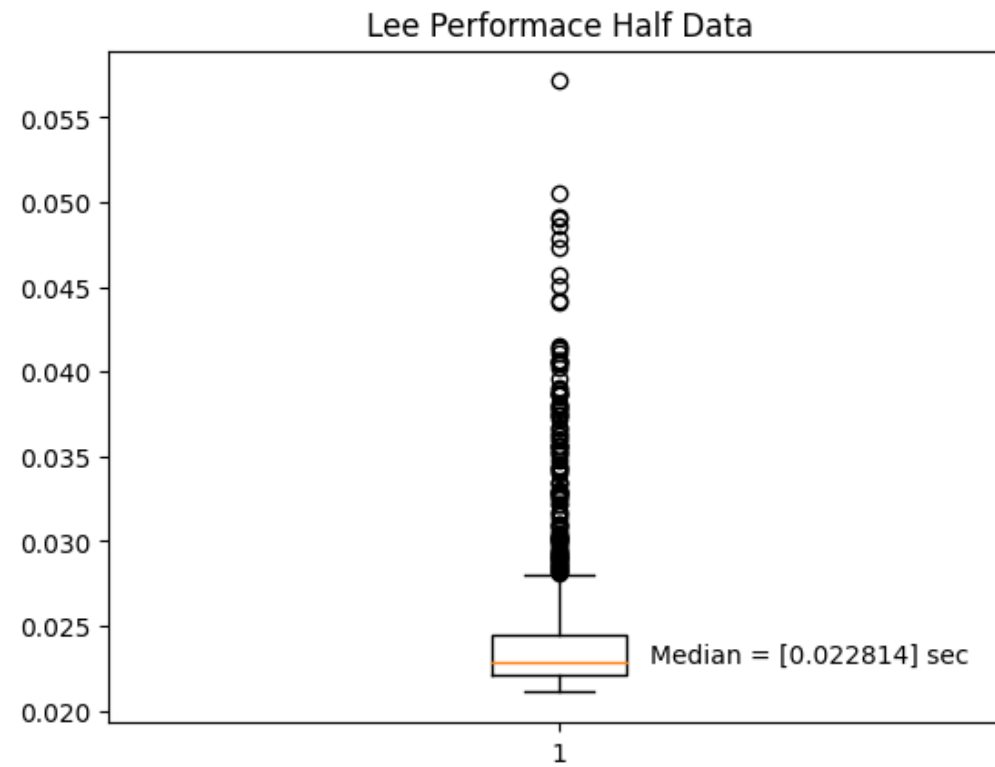


A\* Performace Quarter Data



# Half Dataset – Lee

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# Quarter Dataset – Lee

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