### K-Means Clustering Mini-Project

# Carl Larson 2/2/2018

First we are asked to get the proper packages set up and load the data.

```
require(cluster)
## Loading required package: cluster
require(rattle.data)
## Loading required package: rattle.data
require(NbClust)
## Loading required package: NbClust
data(wine, package="rattle.data")
head(wine)
     Type Alcohol Malic Ash Alcalinity Magnesium Phenols Flavanoids
## 1
            14.23 1.71 2.43
                                    15.6
                                               127
                                                       2.80
                                                                  3.06
## 2
            13.20 1.78 2.14
                                    11.2
                                               100
                                                       2.65
                                                                  2.76
        1
## 3
        1
            13.16 2.36 2.67
                                    18.6
                                               101
                                                       2.80
                                                                  3.24
## 4
            14.37
                  1.95 2.50
        1
                                    16.8
                                               113
                                                       3.85
                                                                  3.49
## 5
        1
            13.24 2.59 2.87
                                    21.0
                                               118
                                                       2.80
                                                                  2.69
## 6
            14.20 1.76 2.45
                                    15.2
                                               112
                                                       3.27
                                                                  3.39
##
     Nonflavanoids Proanthocyanins Color Hue Dilution Proline
## 1
              0.28
                               2.29 5.64 1.04
                                                   3.92
                                                            1065
## 2
              0.26
                               1.28 4.38 1.05
                                                   3.40
                                                            1050
## 3
              0.30
                               2.81
                                     5.68 1.03
                                                   3.17
                                                            1185
## 4
              0.24
                               2.18 7.80 0.86
                                                   3.45
                                                            1480
## 5
              0.39
                               1.82
                                     4.32 1.04
                                                   2.93
                                                             735
## 6
              0.34
                               1.97
                                     6.75 1.05
                                                   2.85
                                                            1450
```

# Exercise 1 – Remove the first column from the data and scale it using the scale() function.

```
df <- scale(wine[,-1])</pre>
scale(df)
##
              Alcohol
                            Malic
                                           Ash
                                                              Magnesium
                                                 Alcalinity
##
     [1,]
           1.51434077 -0.56066822 0.23139979 -1.166303174
                                                             1.90852151
##
     [2,]
           0.24559683 -0.49800856 -0.82566722 -2.483840525
                                                             0.01809398
##
     [3,]
           0.19632522  0.02117152  1.10621386  -0.267982252
                                                             0.08810981
##
     [4,]
           1.68679140 -0.34583508 0.48655389 -0.806974805
                                                             0.92829983
##
     [5,]
           0.29486844 0.22705328 1.83522559 0.450674485
                                                             1.27837900
##
     [6,]
           1.47738706 -0.51591132 0.30430096 -1.286079296
                                                             0.85828399
##
     [7,]
           1.71142720 -0.41744613 0.30430096 -1.465743481 -0.26196936
##
           1.30493643 -0.16680747 0.88751034 -0.567422559
     [8,]
                                                             1.48842650
##
     [9,]
           2.25341491 -0.62332789 -0.71631546 -1.645407665 -0.19195352
    [10,] 1.05857838 -0.88291793 -0.35180959 -1.046527051 -0.12193769
```

```
1.35420804 -0.15785609 -0.24245783 -0.447646437 0.36817315
          1.37884384 -0.76654998 -0.16955666 -0.806974805 -0.33198519
##
    [12.]
    [13,]
          0.92308146 -0.54276546 0.15849862 -1.046527051 -0.75208020
    [14,]
          2.15487169 -0.54276546 0.08559744 -2.423952463 -0.61204853
##
    [15,]
          1.69910930 -0.41744613 0.04914686 -2.244288279
                                                          0.15812565
##
          0.77526663 -0.47115441 1.21556562 -0.687198682 0.85828399
    [16,]
    [17.]
          1.60056608 -0.37268923 1.28846679 0.151234178
                                                          1.41841067
##
    [18,]
          1.02162467 -0.68598755 0.92396093 0.151234178
                                                         1.06833150
##
    Г19.7
          1.46506916 -0.66808479 0.41365272 -0.896806897
                                                          0.57822065
##
    [20,]
          1.13834733
    [21,]
          1.30493643 -0.63227927 -0.31535901 -1.046527051 1.83850567
    [22,] -0.08698653 1.31017034 1.03331269 -0.267982252
##
                                                          0.15812565
    [23,] 0.87380985 -0.42639751 -0.02375431 -0.866862867
                                                          0.08810981
    [24,] -0.18552975 -0.65913341 0.55945507 -0.507534498 -0.33198519
##
##
          0.61513390 -0.47115441 0.88751034 0.151234178 -0.26196936
    [25,]
##
    [26,]
          0.06082829 -0.25632128 3.11099611 1.648435713 1.69847400
##
          0.47963697 - 0.50695994 \ 0.92396093 - 1.016583020 - 0.47201686
    [27,]
    [28,]
          0.36877585 -0.55171684 -0.82566722 -0.747086744 -0.40200103
          1.07089628 -0.39059199 1.58007149 -0.028430007 0.50820482
##
   [29,]
##
    [30,]
          1.25566482 -0.58752236 -0.57051311 -1.046527051 -0.26196936
##
    [31,]
          0.89844565 -0.74864721 1.21556562 0.899834945 0.08810981
          0.71367712 -0.60542512 -0.02375431 -0.118262099
                                                          0.43818899
          0.83685614 \ -0.45325165 \ -0.02375431 \ -0.687198682 \ \ 0.29815732
##
    [33,]
          0.93539936 -0.72179307 1.21556562 0.001514024
##
    [34.]
                                                          2.25860068
##
    [35,]
          0.62745180 -0.48010579 1.03331269 -0.148206130 0.71825232
    [36,]
          0.59049809 -0.47115441 0.15849862 0.300954331 0.01809398
##
    [37,]
          0.34414005 -0.62332789
                                 1.72587383 -1.196247204
                                                          0.71825232
    [38,]
          0.06082829 - 0.61437650 \quad 0.66880683 - 0.447646437 - 0.12193769
##
    [39,]
          0.08546410 - 0.74864721 - 0.97146956 - 1.196247204 - 0.12193769
    [40,]
          1.50202286 1.48024658 0.52300448 -1.884959911 1.97853734
          0.68904131 -0.56066822 -0.20600725 -0.986638989
##
    [41,]
                                                          1.20836316
##
    [42,]
          0.50427278 1.34597587 -0.89856839 -0.208094191 -0.68206436
##
   [43,]
          0.29486844 1.47129519 -0.27890842 -0.597366590 0.22814148
##
   [44,]
##
    [45,]
          0.06082829 -0.50695994 -0.97146956 -0.747086744
                                                          0.50820482
##
          1.48970496 1.52500348 0.26785038 -0.178150160
    [46,]
                                                         0.78826816
##
    [47,]
          1.69910930 1.12219135 -0.31535901 -1.046527051 0.15812565
##
   [48,]
          1.10784999 -0.58752236 -0.89856839 -1.046527051 0.08810981
    [49,]
          1.35420804 -0.28317542 0.12204803 -0.208094191
                                                          0.22814148
##
##
          1.15712160 -0.54276546 -0.35180959 -0.627310621
    [50,]
                                                          0.57822065
          0.06082829 -0.54276546 -1.19017308 -2.124512156 -0.54203270
    [51,]
##
    [52,]
          1.02162467 -0.61437650 0.85105976 -0.687198682 -0.40200103
##
    [53.]
          1.00930677 -0.52486270 0.19494920 -1.645407665
                                                          0.78826816
##
          0.94771726 - 0.39059199 1.14266445 - 0.717142713
    [54,]
                                                          1.06833150
          0.91076355 - 0.59647374 - 0.42471076 - 0.926750928
                                                          1.27837900
          0.68904131 -0.54276546 0.34075155 0.300954331
    [56,]
##
                                                          1.13834733
##
    [57,]
          1.50202286 -0.56961960 -0.24245783 -0.956694959
                                                          1.27837900
##
    [58,]
          0.35645795 -0.32793232 1.14266445 -0.806974805
                                                          0.15812565
                                                         0.57822065
    [59,]
          0.88612775 -0.81130688 0.48655389 -0.836918836
##
    [60,] -0.77678907 -1.24992453 -3.66881295 -2.663504709 -0.82209603
##
    [61,] -0.82606067 -1.10670244 -0.31535901 -1.046527051 0.08810981
##
    [62,] -0.44420570 -0.87396654 -1.26307425 -0.806974805 0.01809398
##
    [63,] 0.82453824 -0.97243173 -1.62758012 -0.447646437 -0.40200103
    [64,] -0.77678907 -1.07984830 -0.75276604 -0.148206130 -0.89211187
```

```
[65,] -1.02314711 -0.79340412 0.59590565 -0.148206130 0.29815732
   [66,] -0.77678907 -1.00823725 0.70525741 -0.417702406 -0.12193769
##
   [67,] 0.13473571 -1.18726487 -2.42949302 -1.345967358 -1.52225438
   [68,] -0.77678907 -1.04404278 -1.62758012 0.031458055 -1.52225438
##
##
   [69,] 0.41804746 -1.24992453 -0.02375431 -0.747086744 0.71825232
   [70,] -0.97387550 -1.02614002 -2.24724008 -0.806974805 3.58890153
##
   [71,] -0.87533228 -0.65018203 -0.57051311 0.271010300 0.22814148
   [72,] 1.05857838 -0.73969583 1.10621386 1.648435713 -0.96212770
##
   [73,] 0.60281600 -0.60542512 -0.46116135 1.348995406 -0.89211187
##
##
   [74,] -0.01307912 -0.59647374 0.85105976 3.145637249 2.74871152
   [75,] -1.28182306 -1.11565382 -0.24245783 0.450674485 0.08810981
   [76,] -1.65136013 -0.40849475 -1.62758012 -1.046527051 -0.19195352
##
   [77,] 0.03619249 -1.28573006 -2.39304243 -1.046527051 -0.96212770
   [78,] -1.42963789  0.49559470 -0.49761194 -0.447646437  0.85828399
##
##
   [79,] -0.82606067 -1.20516763 -1.51822836 -1.405855419 2.53866402
   [80,] -0.37029829 1.37283001 0.12204803 1.049555099 0.08810981
##
   [81,] -1.23255145 -1.26782729 -1.33597542 -0.148206130 -0.96212770
##
   [82,] -0.34566248 -0.47115441 -0.60696370 -0.208094191 -0.96212770
   [83,] -1.13400823 -1.07984830 0.52300448 1.348995406 -1.52225438
   [84,] 0.06082829 1.36387863 -0.16955666 0.899834945 -1.03214354
##
##
   [85,] -1.42963789 -1.29468144 0.77815859 -0.447646437 -0.40200103
   [86,] -0.40725200 -1.21411901 -0.46116135 -0.447646437 -0.05192185
   [87,] -1.03546501 -0.65018203 -0.20600725 0.989667037 -0.68206436
##
   [88,] -1.66367803 -0.59647374 0.92396093 1.947876020 -0.82209603
##
   [89,] -1.67599593 -0.24736990 0.34075155 0.630338669 -1.10215937
   [90,] -1.13400823 -0.90082069 -0.24245783 1.229219283 -2.08238105
   [91,] -1.13400823 -0.45325165 -0.16955666 -0.297926283 -1.31220687
##
   [92,] -1.23255145 -0.73969583 0.19494920 0.750114792 -0.96212770
   [93,] -0.38261619 -0.72179307 -0.38826018 0.360842393 -1.38222271
   [94,] -0.87533228  0.44188642 -0.53406252 -0.447646437 -0.82209603
##
   [95,] -1.70063174 -0.31002956 -0.31535901 -0.447646437 -0.12193769
   [96,] -0.65361004 -0.73074445 -0.60696370 -0.148206130 4.35907571
   [97,] -1.46659160 -0.19366161 1.36136797 0.600394638 2.39863235
   [98,] -0.87533228 -0.82920964 -1.40887660 -1.046527051 -1.03214354
   [99,] -0.77678907 -1.13355658 -0.97146956 -0.297926283 -0.82209603
## [101,] -1.13400823 -0.22946714 -2.42949302 -0.597366590 -0.19195352
## [102,] -0.49347731 -0.89186931 -1.70048129 -0.297926283 -0.82209603
## [104,] -1.45427369 -0.55171684 -1.77338246 0.001514024 -0.96212770
## [105,] -0.60433843 -0.54276546 -1.40887660 0.300954331 -1.03214354
## [107,] -0.92460389 -0.54276546 -0.89856839 -0.148206130 -1.38222271
## [108,] -0.34566248 -0.52486270 -0.31535901 0.899834945 -1.10215937
## [109,] -0.96155760 -0.93662621 -1.55467894 -0.148206130 -0.54203270
## [110,] -1.71294964 -0.88291793 1.21556562 0.151234178 -0.40200103
## [113,] -1.52818111 0.30761571 2.01747852 0.151234178 0.22814148
## [114,] -1.95930769 -1.42895215 0.48655389
                                          0.450674485 -0.82209603
## [115,] -1.13400823 -0.84711240 0.48655389
                                         0.899834945 -1.10215937
## [116,] -2.42738798 -0.73969583 -0.60696370 0.600394638 -1.03214354
## [117,] -1.45427369 -0.77550136 -1.37242601 0.390786423 -0.96212770
## [118,] -0.71519955 -0.65018203 -0.64341428 0.899834945 0.57822065
```

```
## [122,] -1.77453915 -0.25632128 3.14744670 2.696476788 1.34839483
## [124,] 0.06082829 3.10044648 -0.86211780 0.600394638 -0.96212770
## [126,] -1.14632613 -0.15785609 -0.71631546 0.450674485 -1.03214354
## [127,] -0.70288165 -0.72179307 -0.27890842 0.600394638 -0.96212770
## [128,] -1.49122740 -0.18471023 1.50717031 2.696476788 -0.54203270
## [129,] -0.77678907 -0.63227927 -0.24245783 1.498715559 -0.82209603
## [130,] -1.18327984 1.75773938 0.04914686 0.750114792 -1.38222271
## [131,] -0.17321185 -0.88291793 -0.16955666 -0.447646437 1.55844234
## [135,] -0.60433843 -0.98138311 -0.42471076 -0.597366590 -1.03214354
## [136,] -0.49347731 0.11068533 -0.60696370 -0.297926283 -0.40200103
## [137,] -0.92460389 2.13369737 0.63235624 0.450674485 -0.75208020
## [138,] -0.57970263 2.84085644 0.99686210 1.648435713 -0.26196936
## [139,] 0.60281600 1.12219135 -0.64341428 0.001514024 -0.82209603
## [142,] 0.44268327 0.20019914 -0.06020490 0.151234178 -0.75208020
## [143,] 0.63976970 0.74623336 1.28846679 1.199275252 -0.19195352
## [144,] 0.76294873 2.33957912 -0.06020490 0.151234178 -0.54203270
## [146,] 0.19632522 1.10428859 -0.78921663 0.450674485 0.15812565
## [147,] 1.08321419 2.42014155 -0.49761194 0.151234178 -1.38222271
## [148,] -0.16089395 2.03523218 0.41365272 0.600394638 -0.96212770
## [149,] 0.39341166 0.80889302 0.04914686 0.600394638 -0.54203270
## [150,] 0.09778200 1.39968415 -0.02375431 0.600394638 0.92829983
## [151,] 0.61513390 0.70147646 0.92396093 1.348995406 1.62845817
## [153,] 0.13473571 -0.39059199 1.39781855 1.798155867
                                     1.13834733
## [154,] 0.28255053 0.86260131 -0.31535901 -0.297926283 -0.12193769
## [155,] -0.51811312 -0.93662621 -0.97146956 0.151234178 0.22814148
## [156,] 0.20864312 2.55441226 -0.16955666 0.750114792 -0.47201686
## [157,] 1.03394258 1.59661452 0.04914686 0.001514024 -0.75208020
## [159,] 1.64983769 -0.58752236 1.21556562 1.648435713 -0.12193769
## [160,] 0.59049809 -0.59647374 0.99686210 0.899834945 -0.75208020
## [161,] -0.78910697 1.33702448 0.04914686 0.450674485 -0.82209603
## [162,] 0.84917404 0.82679579 0.63235624 0.151234178 0.50820482
## [165,] 0.96003516 0.37922675 -0.24245783 0.750114792 -0.68206436
## [166,] 0.89844565 1.81144766 -0.38826018 0.899834945 -0.82209603
## [167,] 0.55354439 1.22065654 0.85105976 1.049555099 0.78826816
## [169,] 0.71367712 0.21810190 1.17911504 1.498715559 0.36817315
## [170,] 0.49195487 2.02628080 1.79877500 1.648435713 0.85828399
```

```
## [173,]
           1.42811545 0.15544223 0.41365272 0.151234178 -0.61204853
   [174,]
           0.87380985
                        2.96617577
                                     0.30430096
                                                  0.300954331 -0.33198519
                                     0.41365272
   [175,]
           0.49195487
                        1.40863553
                                                  1.049555099
                                                                0.15812565
   [176,]
           0.33182214
                        1.73983662 -0.38826018
                                                  0.151234178
                                                                1.41841067
##
   [177,]
           0.20864312
                        0.22705328
                                     0.01269627
                                                  0.151234178
                                                                1.41841067
##
   [178,]
            1.39116174
                        1.57871176
                                    1.36136797
                                                  1.498715559 -0.26196936
##
                Phenols
                            Flavanoids Nonflavanoids Proanthocyanins
##
     [1,]
           0.806721729
                         1.0319080692
                                         -0.65770780
                                                            1.22143845
##
     [2,]
           0.567048088
                         0.7315652835
                                         -0.81841060
                                                           -0.54318872
##
     [3,]
           0.806721729
                         1.2121137407
                                         -0.49700500
                                                            2.12995937
##
     [4,]
           2.484437221
                         1.4623993954
                                          -0.97911340
                                                            1.02925134
##
     [5,]
           0.806721729
                         0.6614853002
                                          0.22615759
                                                            0.40027531
##
     [6,]
           1.557699140
                         1.3622851335
                                         -0.17559941
                                                            0.66234866
##
                                         -0.49700500
     [7,]
           0.327374446
                         0.4912910549
                                                            0.67982021
##
     [8,]
           0.487156874
                         0.4812796287
                                          -0.41665360
                                                           -0.59560339
##
     [9,]
           0.806721729
                         0.9518166597
                                          -0.57735640
                                                            0.67982021
##
    [10,]
           1.094330099
                         1.1220109049
                                                            0.45268998
                                          -1.13981619
##
    [11,]
           1.046395371
                         1.2922051502
                                          -1.13981619
                                                            1.37868246
##
    [12,] -0.151972837
                         0.4011882192
                                          -0.81841060
                                                           -0.03651359
##
    [13,]
           0.487156874
                         0.7315652835
                                          -0.57735640
                                                            0.38280376
##
    [14,]
           1.286069013
                         1.6626279192
                                          0.54756319
                                                            2.12995937
##
    [15,]
           1.605633868
                         1.6125707883
                                          -0.57735640
                                                            2.39203271
##
    [16,]
           0.886612943
                         0.8817366764
                                          -0.49700500
                                                           -0.22870071
    [17,]
##
           0.806721729
                         1.1119994787
                                          -0.25595080
                                                            0.66234866
##
    [18,]
           1.046395371
                         1.3722965597
                                          0.30650899
                                                            0.22555975
    [19,]
           1.605633868
                         1.9029021478
                                          -0.33630220
                                                            0.47016154
##
    [20,]
           0.646939302
                         1.0018737906
                                          -1.54157319
                                                            0.12073042
##
    [21,]
           1.126286585
                         1.1420337573
                                         -0.97911340
                                                            0.88947889
##
    [22,]
           0.183570261
                         0.3811653668
                                         -0.89876200
                                                            0.67982021
           0.503135117
##
    [23,]
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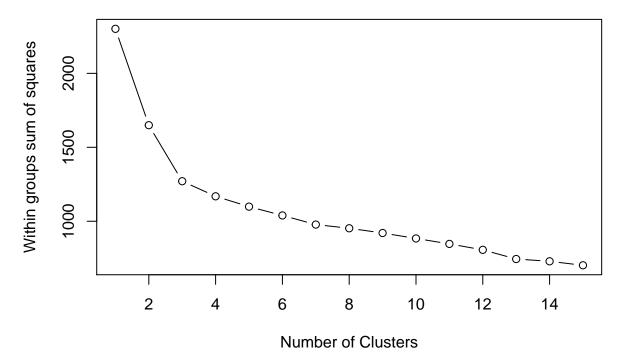
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##
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                                      Dilution
                                                     Proline
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##
    [26,] -0.637578782
                        0.75490825
                                    0.82862329
                                                 0.263908444
##
    [27,] -0.111327893 -0.16384119
                                    0.85679269
                                                 1.422979059
##
   [28,] -0.477978102 0.27365854
                                    0.22298133
                                                1.708777293
##
    [29,] -0.240733849 1.27990794
                                    1.11031723 0.533828998
    [30,] -0.154463212  0.36115849  1.37792647  0.914893310
```

```
[31,] 0.276889975 1.01740810 0.13847314 1.708777293
##
    [32,] 0.794513800 0.57990836
                                   0.37791299 2.439150558
    [33,] -0.525426953
                       1.19240799
                                   0.36382829
                                               0.771994193
                       1.27990794
                                   0.54692935
##
    [34,] 0.147484019
                                               1.550000497
##
    [35,] -0.370139806
                       0.62365833
                                   0.36382829
                                               1.105425466
                                   1.20891011
##
    [36,] 0.018078063
                       0.36115849
                                              0.549706678
##
    [37.] -0.197598531
                       0.57990836
                                  0.23706602
                                              0.422685241
##
    [38,] -0.348572146 0.71115828 -0.14322079
                                               1.137180826
##
    [39,] -0.585816399 0.97365812
                                   0.11030375
                                               0.867260271
##
    [40,] 0.018078063 -0.29509111
                                   1.29341829
                                               0.041620929
    [41,] 0.462371846 -0.03259127
                                   1.08214784
                                              0.152764686
                                   0.54692935
##
    [42,] -0.335631551 -0.20759117
                                              0.914893310
##
    [43,] 0.160424615 -0.33884109
                                   1.33567238
                                              1.105425466
    [44,] -0.301123296 -0.60134093
##
                                   0.54692935 -0.212421946
##
    [45,] -0.007803128 -0.33884109
                                   1.03989375
                                              0.438562920
##
    [46,]
         0.078467509 -0.38259106
                                   1.01172435
                                               1.057792427
    [47,] -0.068192574 0.36115849
##
                                   1.16665602
                                               1.010159388
##
    [48,]
          0.449431250 -0.20759117
                                   1.01172435
                                              0.756116514
##
    [49,]
          0.492566569 0.49240841
                                   0.19481193
                                              0.994281709
##
    [50,]
          1.657220175
                       0.71115828
                                   0.68777632
                                               1.629388895
##
    [51,]
          0.923919756
                       0.71115828
                                   0.42016708
                                              1.280079943
    [52,]
                                   1.06806314
##
          0.233754657
                       1.23615797
                                              1.645266575
    [53,]
##
          0.859216778
                       0.22990857
                                   0.91313147
                                               1.407101380
          0.535701888 0.75490825
                                   0.44833648
##
    [54.]
                                               1.994575527
                                              0.994281709
##
    [55,]
          0.341592953 -0.16384119
                                   0.82862329
    [56,]
          0.514134228 0.09865865
                                   0.58918345
                                               1.184813865
    [57,]
          0.570210143 -0.07634125
                                   0.98355496
##
                                               0.708483475
##
    [58,]
          0.406295932 0.49240841
                                   0.32157420
                                               1.661144254
##
    [59,] 0.751378481 -0.29509111 0.36382829
                                              1.708777293
##
    [60,] -1.340684477   0.40490846 -1.11506488 -0.720507695
##
    [61,] -0.771298270
                      1.27990794 -1.32633534 -0.212421946
##
    [62,] 0.298457635
                       0.09865865 -1.43901291 -0.942795210
##
    [63,] -0.542681081
                       1.19240799 -0.21364428 -0.371198742
                       1.14865802 0.36382829 -1.038061288
##
    [64,] -0.262301509
##
    [65,] -0.909331290
                       2.15490741 -0.53759231 -1.244471124
##
                       1.01740810 -0.43899943 -0.218773018
    [66,] -0.197598531
##
    [67,] 0.104348700
                       ##
    [68,] -0.163090276
                       0.71115828 1.22299481 -0.752263054
    [69,] -0.814433589
                       0.27365854 -0.96013322 0.009865569
##
##
    [70,] -0.952466609 1.41115786 0.64552223 -0.091751580
    [71,] -0.866195971 -0.22509116 -1.11506488 0.390929881
    [72,] -0.723849419
                      1.76115765 0.77228450 -1.069816648
##
##
    [73,] -0.568562272
                       ##
    [74,] -0.736790015
                       1.54240778 1.25116420 0.756116514
    [75,] -0.797179461
                       0.14240862 0.73003041 0.441738456
##
    [76,] -0.542681081
                       1.19240799 -0.66435458 -1.012657001
##
    [77,] -0.197598531
                       1.01740810 -0.18547489 -1.126976294
##
    [78,] -1.038737246
                       0.01115870 -0.12913610 -0.784018414
##
    [79,] -0.715222356
                       0.44865844 -0.42491473 0.009865569
##
    [80,] -1.073245501
                       1.01740810 0.73003041 -0.901513243
##
    [81,] -1.103440224
                       1.84865760 0.71594572 -1.488987391
##
    [82,] -0.499545762  0.88615818  0.74411511 -0.104453724
##
    [83,] -1.232846180 1.54240778 0.15255784 -0.371198742
    [84,] -0.111327893 -0.51384098 -0.84745564 -0.736385375
```

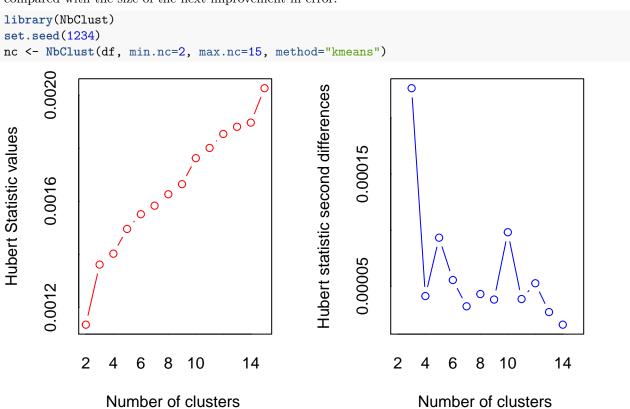
```
[85,] -0.866195971 -0.73259085 0.65960693 -0.720507695
##
   [86,] -1.051677842 1.19240799 0.77228450 -0.942795210
   [87,] -1.125007884 1.62990773 -0.49533822 -0.799896093
                    1.76115765 0.84270799 -0.587135186
   [88,] -1.060304905
##
   [89,] -0.974034268  0.18615860  0.19481193 -0.212421946
##
   [90,] -1.431268647
                     0.49240841 0.84270799 -0.387076422
   [91,] -1.146575543 0.53615839 -0.48125352 -0.847529132
##
   [92,] -0.628951718  0.40490846  0.05396496 -0.942795210
##
   ##
   [95,] -0.779925334
                     [96,] -1.060304905
   [97,] -1.103440224 -0.03259127 -0.49533822 -0.387076422
   [98,] -0.930898949
                    1.19240799 0.18072723 -1.012657001
   [99,] -0.240733849
                     0.36115849
                                0.22298133 -0.275932664
## [100,] -1.189710862
                     2.02365749
                                0.30748951 -1.082518791
  [101,] -0.758357674 1.36740789
                                0.49059057 -0.117155868
## [102,] -1.125007884 0.36115849
                                0.22298133 -0.587135186
## [103,] -0.974034268 -0.68884088
                               1.08214784 -0.980901641
## [104,] -1.293235627 -0.07634125 -0.24181367 -1.053938968
## [105,] -0.913644822 0.36115849
                               1.34975708 -0.237826233
## [106,] -1.017169587 -0.42634104 0.96947026 -1.371492561
## [107,] -0.715222356  0.18615860  0.78636920 -0.752263054
## [108,] -0.758357674 -0.33884109 -0.26998307 -0.822124845
## [109,] -1.017169587 -0.42634104 0.57509875 -1.381019169
## [110,] -1.038737246  0.01115870  0.91313147 -0.212421946
## [111,] -0.930898949 -0.90759075 0.27932011 -0.587135186
## [112,] -1.319116818 -0.25134114 0.23706602 -1.339737202
## [113,] -0.542681081 1.19240799 -0.15730549 -0.444236069
## [114,] -0.853255375   0.62365833 -0.42491473 -0.993603785
## [116,] -1.362252137 3.29240673 0.36382829 -1.079343255
## [117,] -1.340684477 -0.03259127
                                1.01172435 -0.799896093
## [118,] -1.293235627  0.44865844  0.49059057 -1.276226483
## [119,] -0.715222356 -1.12634062 -0.69252397 -1.190487013
## [120,] -1.629691113 -0.12009122 0.61735284 -0.580784114
## [121,] -0.779925334 -0.68884088
                               1.09623253 -0.387076422
## [122,] 0.406295932 -0.12009122 1.51877344 -0.895162171
## [123,] -1.284608563 -0.16384119
                                0.71594572 -1.212715765
## [124,] -1.060304905 -0.99509069 0.68777632 -1.165082726
## [125,] -0.974034268 -0.90759075
                               1.44834996 -1.165082726
## [126,] -0.991288395 -0.42634104 0.94130087 -1.171433797
## [127,] -0.482291634 -1.17009059 0.32157420 -1.253997732
## [129,] -1.267354435 -0.29509111 0.23706602 -1.285753091
## [130,] -1.060304905 -0.73259085 -0.05871261 -0.529975539
## [131,] -0.413275124 -0.86384077 -1.86155382 -0.371198742
## [132,] 0.147484019 -0.95134072 -1.67845276 -0.688752336
## [133,] 0.276889975 -1.30134051 -1.76296094 -0.593486258
## [134,] -0.025057256 -0.77634083 -1.86155382 -0.466464820
## [135,] 0.169051679 -0.90759075 -1.55169049 -0.307688024
## [136,] 0.880784438 -0.99509069 -1.45309761 -0.164788907
## [137,] -0.521113421 -0.90759075 -1.88972321 -0.085400508
## [138,] -0.025057256 -0.60134093 -1.29816594 -0.736385375
```

```
## [139,] 0.276889975 -0.64509090 -1.11506488 -0.529975539
## [140,] -0.059565511 -0.29509111 -0.65026988 -0.498220180
## [141,] -0.197598531 -0.82009080 -0.42491473 -0.466464820
## [142,] 0.233754657 -1.12634062 -0.19955958 0.105131647
## [143,] -0.305436828 -0.29509111 -0.77703216 -0.720507695
## [144,] -0.283869168 -0.20759117 -0.79111685 -0.625241617
## [145,] 1.359586476 -1.34509048 -0.86154034 0.343296842
## [146,] -0.456410443 -1.56384035 -1.31225064 0.263908444
## [147,] -0.068192574 -1.65134030 -1.80521503 -1.053938968
## [148,] 1.118028691 -1.82634020 -1.05872609 -0.387076422
## [149,]
          1.450170645 -1.78259022 -1.39675882 -0.307688024
## [150,]
          1.872896769 -1.69509027 -1.80521503 -0.625241617
## [151,]
          1.527814219 -1.60759033 -1.84746912 -0.784018414
## [152,]
          2.476791231 -2.08884004 -1.60802927 -0.847529132
## [153,]
          0.880784438 -1.52009038 -1.80521503 -1.022183609
## [154,]
          2.356012338 -1.73884025 -1.55169049 -0.228299625
## [155,]
          1.096461031 -1.65134030 -1.49535170 -0.339443383
## [156,]
          1.225866988 -1.56384035 -1.59394458 -0.069522829
          1.704669026 -1.69509027 -1.36858943 -0.847529132
## [157,]
## [158,]
          1.053325713 -1.25759054 -1.24182715 0.422685241
## [159,]
          3.425768243 -1.69509027 -0.91787912 -0.275932664
## [160,]
          2.886576759 -1.69509027 -1.17140367 -0.402954102
## [161,]
          1.118028691 -1.73884025 -1.45309761 -0.720507695
## [162.]
          ## [163,]
          0.225127593 -0.38259106 -0.70660867 -0.561730898
## [164,]
          0.095721637 -1.21384056 -1.21365776 -0.228299625
## [165,]
          1.950540342 -1.12634062 -1.31225064 -0.418831781
## [166,]
          0.673734908 -0.77634083 -1.21365776 -0.720507695
## [167,]
          2.425028848 -0.47009101 -1.48126700 -0.164788907
## [168,]
          2.243860510 -1.03884067 -1.21365776 -0.196544266
          1.553695410 -0.95134072 -1.14323428 0.009865569
## [169,]
## [170,]
          1.484678900 -1.25759054 -0.97421791 -0.371198742
## [171,]
          0.190619338 -1.30134051 -1.10098018 -0.752263054
## [172,]
          2.088572931 -1.69509027 -1.38267412 -0.879284492
## [173,]
          2.002302725 -1.47634041 -1.26999655 -0.275932664
## [174,]
          1.139596350 -1.38884046 -1.22774246 -0.021889790
## [175,]
          0.967055075 -1.12634062 -1.48126700 0.009865569
## [176,]
          2.217979318 -1.60759033 -1.48126700 0.279786124
          1.829761450 -1.56384035 -1.39675882 0.295663803
## [177,]
## [178,] 1.786626131 -1.52009038 -1.42492821 -0.593486258
  attr(, "scaled:center")
##
           Alcohol
                            Malic
                                              Ash
                                                       Alcalinity
##
     -8.594093e-16
                    -6.734236e-17
                                     8.046486e-16
                                                    -7.684922e-17
##
                                                    Nonflavanoids
        Magnesium
                          Phenols
                                       Flavanoids
     -4.095117e-17
                     -1.391677e-17
                                     6.950589e-17
                                                    -1.041614e-16
## Proanthocyanins
                            Color
                                              Hue
                                                         Dilution
##
     -1.223272e-16
                     3.676054e-17
                                     2.100087e-16
                                                     3.009648e-16
##
          Proline
##
     -1.037131e-16
##
   attr(, "scaled:scale")
##
          Alcohol
                            Malic
                                              Ash
                                                       Alcalinity
##
                                                1
##
        Magnesium
                          Phenols
                                       Flavanoids
                                                    Nonflavanoids
##
```

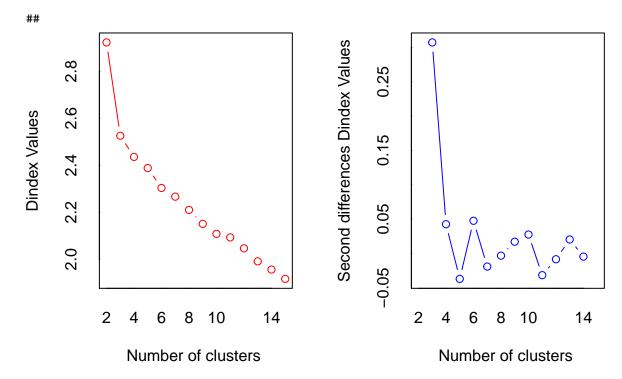
```
## Proanthocyanins
                             Color
                                               Hue
                                                          Dilution
##
                                                 1
                                 1
                                                                 1
##
           Proline
##
                 1
head(df)
##
          Alcohol
                        Malic
                                     Ash Alcalinity Magnesium
## [1,] 1.5143408 -0.56066822 0.2313998 -1.1663032 1.90852151 0.8067217
## [2,] 0.2455968 -0.49800856 -0.8256672 -2.4838405 0.01809398 0.5670481
## [3,] 0.1963252 0.02117152 1.1062139 -0.2679823 0.08810981 0.8067217
## [4,] 1.6867914 -0.34583508 0.4865539 -0.8069748 0.92829983 2.4844372
## [5,] 0.2948684 0.22705328 1.8352256 0.4506745 1.27837900 0.8067217
## [6,] 1.4773871 -0.51591132 0.3043010 -1.2860793 0.85828399 1.5576991
##
        Flavanoids Nonflavanoids Proanthocyanins
                                                      Color
                                                                   Hue
## [1,]
         1.0319081
                      -0.6577078
                                       1.2214385 0.2510088
                                                             0.3611585
## [2,]
        0.7315653
                      -0.8184106
                                      -0.5431887 -0.2924962
                                                             0.4049085
## [3,]
        1.2121137
                      -0.4970050
                                       2.1299594 0.2682629
                                                             0.3174085
## [4,]
        1.4623994
                      -0.9791134
                                       1.0292513 1.1827317 -0.4263410
## [5,]
        0.6614853
                       0.2261576
                                       0.4002753 -0.3183774
                                                             0.3611585
                                       0.6623487 0.7298108 0.4049085
## [6,]
        1.3622851
                      -0.1755994
##
         Dilution
                      Proline
## [1,] 1.8427215 1.01015939
## [2,] 1.1103172 0.96252635
## [3,] 0.7863692 1.39122370
## [4,] 1.1807407 2.32800680
## [5,] 0.4483365 -0.03776747
## [6,] 0.3356589 2.23274072
Next to use K Means clustering. First we are asking how many clusters to use?
wssplot <- function(data, nc=15, seed=1234){
  wss <- (nrow(data)-1)*sum(apply(data,2,var))
    for (i in 2:nc){
          set.seed(seed)
     wss[i] <- sum(kmeans(data, centers=i)$withinss)}</pre>
  plot(1:nc, wss, type="b", xlab="Number of Clusters",
       ylab="Within groups sum of squares")
}
str(wssplot)
## function (data, nc = 15, seed = 1234)
## - attr(*, "srcref")=Class 'srcref' atomic [1:8] 1 12 10 1 12 1 1 10
   ...- attr(*, "srcfile")=Classes 'srcfilecopy', 'srcfile' <environment: 0x7fc7f746c8d0>
wssplot(df)
```



This one seems to suggest using 3 clusters. 3 clusters represents the biggest improvement in previous error compared with the size of the next improvement in error.

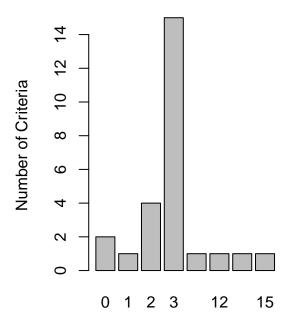


## \*\*\* : The Hubert index is a graphical method of determining the number of clusters.
## In the plot of Hubert index, we seek a significant knee that corresponds to a
## significant increase of the value of the measure i.e the significant peak in Hubert
index second differences plot.



```
## *** : The D index is a graphical method of determining the number of clusters.
##
                 In the plot of D index, we seek a significant knee (the significant peak in Dindex
##
                 second differences plot) that corresponds to a significant increase of the value of
##
                 the measure.
##
## * Among all indices:
\#\# * 4 proposed 2 as the best number of clusters
## * 15 proposed 3 as the best number of clusters
## * 1 proposed 10 as the best number of clusters
## * 1 proposed 12 as the best number of clusters
\#\# * 1 proposed 14 as the best number of clusters
## * 1 proposed 15 as the best number of clusters
##
##
                    **** Conclusion ****
##
## * According to the majority rule, the best number of clusters is 3
##
barplot(table(nc$Best.n[1,]),
             xlab="Numer of Clusters", ylab="Number of Criteria",
                  main="Number of Clusters Chosen by 26 Criteria")
```

#### lumber of Clusters Chosen by 26 Ci



#### Numer of Clusters

This one also seems to suggest we run 3 clusters. 0 has a high bar here for some reason, and 2 also has somewhat of a bar, but this strategy really suggests using 3 clusters.

```
fit.km <- kmeans(df, 3, nstart=25)
table(fit.km$cluster)
##
##
   1 2 3
## 51 65 62
table(wine$Type)
##
##
   1 2
         3
## 59 71 48
fit.km
## K-means clustering with 3 clusters of sizes 51, 65, 62
##
## Cluster means:
##
        Alcohol
                     Malic
                                  Ash Alcalinity
                                                   Magnesium
                                                                 Phenols
## 1 0.1644436 0.8690954 0.1863726
                                      0.5228924 -0.07526047 -0.97657548
## 2 -0.9234669 -0.3929331 -0.4931257 0.1701220 -0.49032869 -0.07576891
     0.8328826 -0.3029551 0.3636801 -0.6084749 0.57596208
                                                             0.88274724
## 3
##
      Flavanoids Nonflavanoids Proanthocyanins
                                                    Color
                                                                 Hue
## 1 -1.21182921
                    0.72402116
                                   -0.77751312 0.9388902 -1.1615122
     0.02075402
                   -0.03343924
                                    0.05810161 -0.8993770 0.4605046
##
     0.97506900
                   -0.56050853
                                    0.57865427 0.1705823 0.4726504
##
      Dilution
                   Proline
## 1 -1.2887761 -0.4059428
## 2 0.2700025 -0.7517257
```

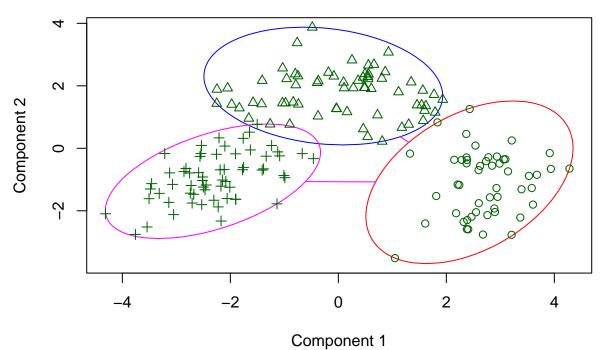
```
## 3 0.7770551 1.1220202
##
## Clustering vector:
##
  ##
 ##
## [176] 1 1 1
##
## Within cluster sum of squares by cluster:
## [1] 326.3537 558.6971 385.6983
 (between_SS / total_SS = 44.8 %)
##
## Available components:
##
## [1] "cluster"
          "centers"
                 "totss"
                        "withinss"
## [5] "tot.withinss" "betweenss"
                 "size"
                        "iter"
## [9] "ifault"
```

This is an interesting clustering, it seems to be based primarily off color. First and foremost, we see our three clusters have 3 distinct wine colors that act as the basis for the 3 clusters. We see a sum of squared errors at 44.8%, so this isn't terribly good or bad at predictions one way or another, it's decent but could likely use a larger sample size.

#### Exercise 6: Visualize these clusters

```
aggregate(wine[-1], by=list(cluster=fit.km$cluster), mean)
     cluster Alcohol
##
                         Malic
                                    Ash Alcalinity Magnesium Phenols
           1 13.13412 3.307255 2.417647
## 1
                                          21.24118 98.66667 1.683922
## 2
           2 12.25092 1.897385 2.231231
                                           20.06308
                                                    92.73846 2.247692
## 3
           3 13.67677 1.997903 2.466290
                                          17.46290 107.96774 2.847581
                                                              Hue Dilution
##
     Flavanoids Nonflavanoids Proanthocyanins
                                                  Color
## 1
     0.8188235
                    0.4519608
                                     1.145882 7.234706 0.6919608 1.696667
## 2
     2.0500000
                    0.3576923
                                     1.624154 2.973077 1.0627077 2.803385
## 3
     3.0032258
                    0.2920968
                                     1.922097 5.453548 1.0654839 3.163387
##
       Proline
## 1 619.0588
## 2 510.1692
## 3 1100.2258
#We are asked to use clusplot() to model this
clusplot(df, fit.km$cluster, color=TRUE)
```

## CLUSPLOT( df )



These two components explain 55.41 % of the point variability.

After getting this to graph, it does look like the most sensible way to cluster this data on a 2d frame.