

# CS409

# Software Testing

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Slides adapted from CS4218 in NUS

# Administrative Info

- Project Proposal posted. Due on 4 December 2020
- No bugs posted in GitHub discussion so far
- Submit bug reports for bonus early!
  - If the bug is fixed or is old bug, then you couldn't get the bonus points

# Mutation testing in Google

- Use as a code review tool in Google
  - If an automated diff analyzer finding (e.g. a living mutant) is not useful, developers can report that with a single click on the finding. If any other author is not at the diff shown in Figure 1.

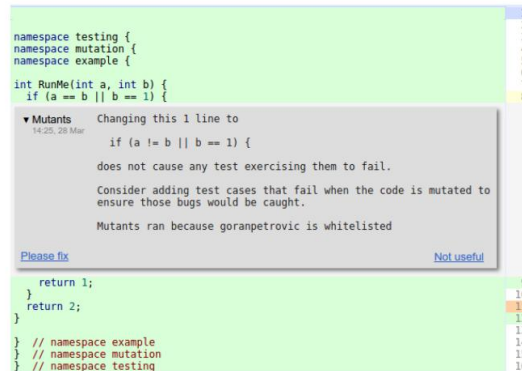


Figure 1: Mutant finding shown in the Critique - Google code review tool

# Recap: Syntax-Based Coverage Criteria

**Mutation Coverage (MC) : For each  $m \in M$ , TR contains exactly one requirement, to kill  $m$ .**

- The RPR model from chapter 2:
  - *Reachability* : The test causes the **faulty statement** to be reached (in mutation – the **mutated** statement)
  - *Infection* : The test causes the faulty statement to result in an **incorrect state**
  - *Propagation* : The incorrect state **propagates** to incorrect output
  - *Revealability* : The tester must **observe** part of the incorrect output
- The RPR model leads to **two variants** of mutation coverage ...

# Strong Versus Weak Mutation

```
1  boolean isEven (int X)
2  {
3      if (X < 0)
4          X = 0 - X;
5      if (double) (X/2) == ((double) X) / 2.0
6          return (true);
7      else
8          return (false);
9  }
```

Δ 4

X = 0;

Reachability :  $X < 0$

Infection :  $X \neq 0$

(X = -6) will kill mutant  
4 under weak mutation

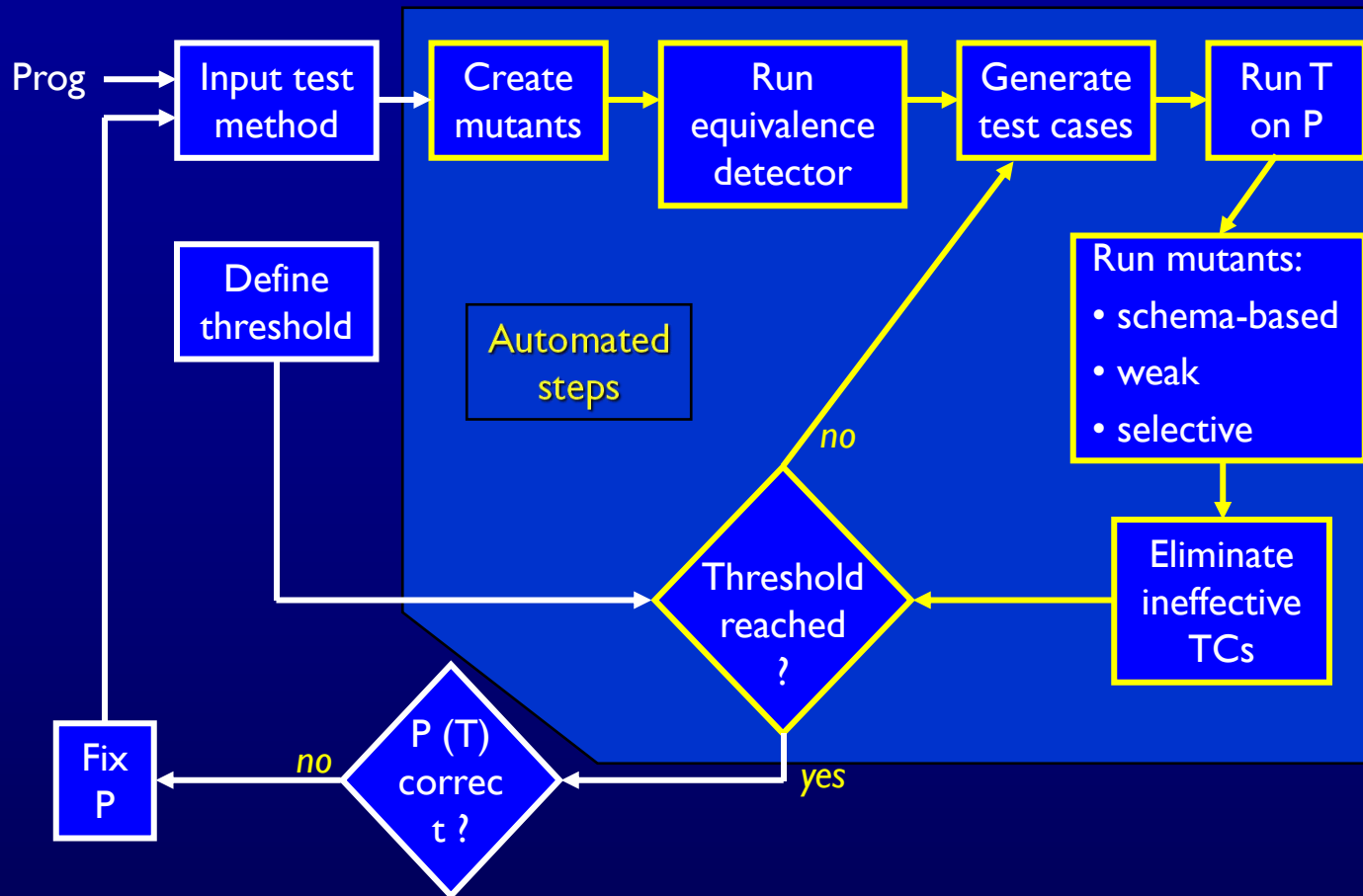
Propagation :

$((\text{double}) ((0-X)/2) == ((\text{double}) 0-X) / 2.0)$   
 $\neq ((\text{double}) (0/2) == ((\text{double}) 0) / 2.0)$

That is, X is not even ...

Thus (X = -6) does not kill the mutant under  
strong mutation

# Testing Programs with Mutation



# Why Mutation Works

## Fundamental Premise of Mutation Testing

**If the software contains a fault, there will usually be a set of mutants that can only be killed by a test case that also detects that fault**

- This is not an absolute !
- The mutants guide the tester to an effective set of tests
- A very challenging problem :
  - Find a **fault** and a set of **mutation-adequate tests** that do **not** find the fault
- Of course, this depends on the mutation operators ...

# Designing Mutation Operators

- At the **method level**, mutation operators for different programming languages are similar
- Mutation operators do one of **two things** :
  - Mimic typical programmer **mistakes** ( incorrect variable name )
  - Encourage common test **heuristics** ( cause expressions to be 0 )
- Researchers design lots of operators, then experimentally **select** the most useful

## Effective Mutation Operators

**If tests that are created specifically to kill mutants created by a collection of mutation operators  $O = \{o_1, o_2, \dots\}$  also kill mutants created by all remaining mutation operators with very high probability, then  $O$  defines an effective set of mutation operators**



# Mutation Operators for Java

1. **ABS** — Absolute Value Insertion
2. **AOR** — Arithmetic Operator Replacement
3. **ROR** — Relational Operator Replacement
4. **COR** — Conditional Operator Replacement
5. **SOR** — Shift Operator Replacement
6. **LOR** — Logical Operator Replacement
7. **ASR** — Assignment Operator Replacement
8. **UOI** — Unary Operator Insertion
9. **UOD** — Unary Operator Deletion
10. **SVR** — Scalar Variable Replacement
11. **BSR** — Bomb Statement Replacement

Full  
definitions ...

# Mutation Operators for Java

## 1. ABS — Absolute Value Insertion:

Each arithmetic expression (and subexpression) is modified by the functions *abs()*, *negAbs()*, and *failOnZero()*.

Examples:

```
a = m * (o + p);  
Δ1 a = abs (m * (o + p));  
Δ2 a = m * abs ((o + p));  
Δ3 a = failOnZero (m * (o + p));
```

## 2. AOR — Arithmetic Operator Replacement:

Each occurrence of one of the arithmetic operators *+*, *−*, *\**, */*, and *%* is replaced by each of the other operators. In addition, each is replaced by the special mutation operators *leftOp*, and *rightOp*.

Examples:

```
a = m * (o + p);  
Δ1 a = m + (o + p);  
Δ2 a = m * (o * p);  
Δ3 a = m leftOp (o + p);
```

# Mutation Operators for Java (2)

## 3. ROR — Relational Operator Replacement:

Each occurrence of one of the relational operators ( $<$ ,  $\leq$ ,  $>$ ,  $\geq$ ,  $=$ ,  $\neq$ ) is replaced by each of the other operators and by *falseOp* and *trueOp*.

Examples:

if ( $X \leq Y$ )

$\Delta 1$  if ( $X > Y$ )

$\Delta 2$  if ( $X < Y$ )

$\Delta 3$  if ( $X$  *falseOp*  $Y$ ) // always returns false

## 4. COR — Conditional Operator Replacement:

Each occurrence of one of the logical operators (and -  $\&\&$ , or -  $\|\|$ , and with no conditional evaluation -  $\&$ , or with no conditional evaluation -  $|$ , not equivalent -  $\wedge$ ) is replaced by each of the other operators; in addition, each is replaced by *falseOp*, *trueOp*, *leftOp*, and *rightOp*.

Examples:

if ( $X \leq Y \&\& a > 0$ )

$\Delta 1$  if ( $X \leq Y \|\| a > 0$ )

$\Delta 2$  if ( $X \leq Y$  *leftOp*  $a > 0$ ) // returns result of left clause

# Mutation Operators for Java (4)

## 5. SOR — Shift Operator Replacement:

Each occurrence of one of the shift operators <<, >>, and >>> is replaced by each of the other operators. In addition, each is replaced by the special mutation operator *leftOp*.

Examples:

```
byte b = (byte) 16;
```

```
b = b >> 2;
```

Δ1 `b = b << 2;`

Δ2 `b = b leftOp 2; // result is b`

## 6. LOR — Logical Operator Replacement:

Each occurrence of one of the logical operators (bitwise and - &, bitwise or - |, exclusive or - ^) is replaced by each of the other operators; in addition, each is replaced by *leftOp* and *rightOp*.

Examples:

```
int a = 60; int b = 13;
```

```
int c = a & b;
```

Δ1 `int c = a | b;`

Δ2 `int c = a rightOp b; // result is b`

# Mutation Operators for Java (5)

## 7. ASR — Assignment Operator Replacement:

Each occurrence of one of the assignment operators (=, +=, -=, \*=, /=, %=, &=, |=, ^=, <=>, >>=, >>>=) is replaced by each of the other operators.

Examples:

`a = m * (o + p);`

$\Delta 1$  `a += m * (o + p);`

$\Delta 2$  `a *= m * (o + p);`

## 8. UOI — Unary Operator Insertion:

Each unary operator (arithmetic +, arithmetic -, conditional !, logical ~) is inserted in front of each expression of the correct type.

Examples:

`a = m * (o + p);`

$\Delta 1$  `a = m * -(o + p);`

$\Delta 2$  `a = -(m * (o + p));`

# Mutation Operators for Java (6)

## 9. UOD — Unary Operator Deletion:

Each unary operator (arithmetic +, arithmetic -, conditional !, logical~) is deleted.

Examples:

if !(X <= Y && !Z)

Δ1 if (X > Y && !Z)

Δ2 if !(X < Y && Z)

## 10. SVR — Scalar Variable Replacement:

Each variable reference is replaced by every other variable of the appropriate type that is declared in the current scope.

Examples:

a = m \* (o + p);

Δ 1 a = o \* (o + p);

Δ 2 a = m \* (m + p);

Δ 3 a = m \* (o + o);

Δ 4 p = m \* (o + p);

# Mutation Operators for Java (7)

## *// BSR — Bomb Statement Replacement:*

Each statement is replaced by a special Bomb() function.

Example:

```
a = m * (o + p);
```

*Δ1 Bomb() // Raises exception when reached*

Form a team with 1-2 students

## **IN CLASS EXERCISE**



```

public static int cal (int month1, int day1, int month2, int day2, int year){
    int numDays;
    Δ1 if (month2!=month1)
        if (month2 == month1)
            numDays = day2 - day1;
        else{
            // Skip month 0.
            int daysIn[] = {0, 31, 0, 31, 30, 31, 30, 31, 31, 30, 31, 30, 31};
            // Are we in a leap year?
            int m4 = year % 4;
            int m100 = year % 100;
            int m400 = year % 400;
            if ((m4 != 0) || ((m100 == 0) && (m400 != 0)))
                daysIn[2] = 28;
            else
                daysIn[2] = 29;

            // start with days in the two months
            numDays = day2 + (daysIn[month1] - day1);

            // add the days in the intervening months
            for (int i = month1 + 1; i <= month2-1; i++)
                numDays = daysIn[i] + numDays;
        }
    return (numDays);}

```

What is the mutation operator in mutation Δ1 ?

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```

1. Find a test that **weakly kills** the mutant, but not strongly
2. Generalize :What **must be true** to weakly kill the mutant, but not strongly?
3. Try to write down the **conditions** needed to (i) **reach** the mutated statement, (ii) **infect** the program state, and (iii) **propagate** to output

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# Summary : Subsuming Other Criteria

- Mutation is widely considered the **strongest** test criterion
  - And most **expensive** !
  - By far the most test requirements (each mutant)
  - Usually the most tests
- Mutation **subsumes** other criteria by including specific mutation operators
- Subsumption can only be defined for **weak mutation** – other criteria only impose local requirements
  - Node coverage, Edge coverage, Clause coverage
  - General active clause coverage: **Yes–Requirement on single tests**
  - Correlated active clause coverage: **No–Requirement on test pairs**
  - All-defs data flow coverage

# Mutation testing in Google

- Use as a code review tool in Google
  - If an automated diff analyzer finding (e.g. a living mutant) is not useful, developers can report that with a single click on the finding. If any of the reviewers consider a finding to be important, they can indicate that to the diff author with a single click, as shown in Figure 1.

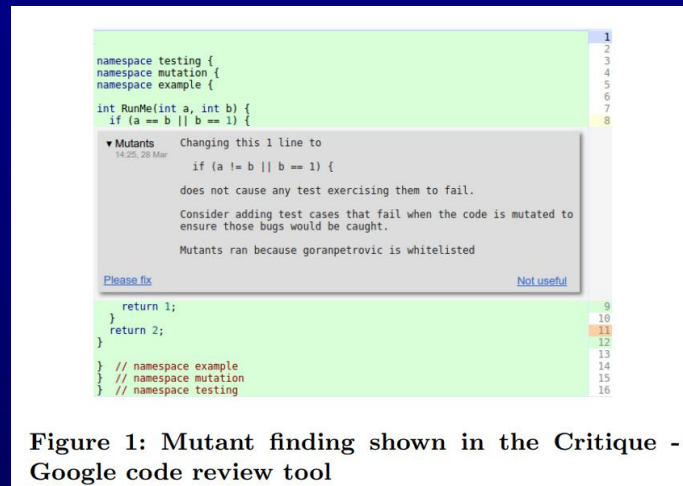


Figure 1: Mutant finding shown in the Critique - Google code review tool

# Automated Debugging

# Automated Debugging

Debugging techniques that use program executions in different ways:

- Statistical Fault Localization
- Dynamic Slicing
- Delta Debugging

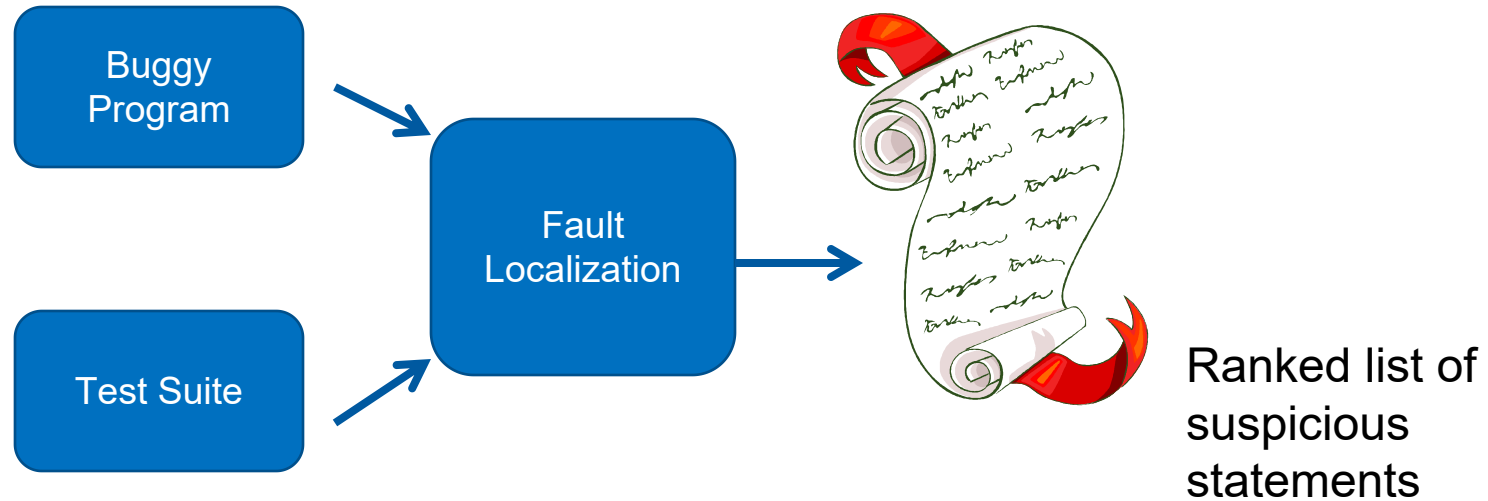


# Automated Debugging

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## Statistical Fault Localization

# Statistical Fault localization



Assign scores to program statements based on their occurrence in passing / failing tests. ***Correlation equals causation!***

$$\text{Score}(s) = \frac{\frac{\text{fail}(s)}{\text{allfail}}}{\frac{\text{fail}(s)}{\text{allfail}} + \frac{\text{pass}(s)}{\text{allpass}}}$$

An example of scoring scheme [Tarantula]

# Producing Ranked Bug report

- We use the Tarantula toolkit.
- Given a test-suite T

$$\text{Score}(s) = \frac{\frac{\text{fail}(s)}{\text{allfail}}}{\frac{\text{fail}(s)}{\text{allfail}} + \frac{\text{pass}(s)}{\text{allpass}}}$$

- $\text{fail}(s) \equiv \#$  of failing executions in which s occurs
- $\text{pass}(s) \equiv \#$  of passing executions in which s occurs
- $\text{allfail} \equiv$  Total # of failing executions
- $\text{allpass} \equiv$  Total # of passing executions
  - $\text{allfail} + \text{allpass} = |T|$
- Can also use other metric like Ochiai.

Name	Formula	Name	Formula
Jaccard	$\frac{a_{ef}}{a_{ef}+a_{nf}+a_{ep}}$	Anderberg	$\frac{a_{ef}}{a_{ef}+2(a_{nf}+a_{ep})}$
Sørensen-Dice	$\frac{2a_{ef}}{2a_{ef}+a_{nf}+a_{ep}}$	Dice	$\frac{2a_{ef}}{a_{ef}+a_{nf}+a_{ep}}$
Kulczynski1	$\frac{a_{ef}}{a_{nf}+a_{ep}}$	Kulczynski2	$\frac{1}{2} \left( \frac{a_{ef}}{a_{ef}+a_{nf}} + \frac{a_{ef}}{a_{ef}+a_{ep}} \right)$
Russell and Rao	$\frac{a_{ef}}{a_{ef}+a_{nf}+a_{ep}+a_{np}}$	Hamann	$\frac{a_{ef}+a_{np}-a_{nf}-a_{ep}}{a_{ef}+a_{nf}+a_{ep}+a_{np}}$
Simple Matching	$\frac{a_{ef}+a_{np}}{a_{ef}+a_{nf}+a_{ep}+a_{np}}$	Sokal	$\frac{2(a_{ef}+a_{np})}{2(a_{ef}+a_{np})+a_{nf}+a_{ep}}$
M1	$\frac{a_{ef}+a_{np}}{a_{nf}+a_{ep}}$	M2	$\frac{a_{ef}}{a_{ef}+a_{np}+2(a_{nf}+a_{ep})}$
Rogers-Tanimoto	$\frac{a_{ef}+a_{np}}{a_{ef}+a_{np}+2(a_{nf}+a_{ep})}$	Goodman	$\frac{2a_{ef}-a_{nf}-a_{ep}}{2a_{ef}+a_{nf}+a_{ep}}$
Hamming etc.	$a_{ef} + a_{np}$	Euclid	$\sqrt{a_{ef} + a_{np}}$
Ochiai	$\frac{a_{ef}}{\sqrt{(a_{ef}+a_{nf})(a_{ef}+a_{ep})}}$	Overlap	$\frac{a_{ef}}{\min(a_{ef}, a_{nf}, a_{ep})}$
Tarantula	$\frac{\frac{a_{ef}}{a_{ef}+a_{nf}}}{\frac{a_{ef}}{a_{ef}+a_{nf}} + \frac{a_{ep}}{a_{ep}+a_{np}}}$	Zoltar	$\frac{a_{ef}}{a_{ef}+a_{nf}+a_{ep} + \frac{10000a_{nf}a_{ep}}{a_{ef}}}$
Ample	$\left  \frac{a_{ef}}{a_{ef}+a_{nf}} - \frac{a_{ep}}{a_{ep}+a_{np}} \right $	Wong1	$a_{ef}$
Wong2	$a_{ef} - a_{ep}$		
Wong3	$a_{ef} - h$ , where $h = \begin{cases} a_{ep} & \text{if } a_{ep} \leq 2 \\ 2 + 0.1(a_{ep} - 2) & \text{if } 2 < a_{ep} \leq 10 \\ 2.8 + 0.001(a_{ep} - 10) & \text{if } a_{ep} > 10 \end{cases}$		
Ochiai2	$\frac{a_{ef}a_{np}}{\sqrt{(a_{ef}+a_{ep})(a_{np}+a_{nf})(a_{ef}+a_{nf})(a_{ep}+a_{np})}}$		
Geometric Mean	$\frac{a_{ef}a_{ep}-a_{nf}a_{np}}{\sqrt{(a_{ef}+a_{ep})(a_{np}+a_{nf})(a_{ef}+a_{nf})(a_{ep}+a_{np})}}$		
Harmonic Mean	$\frac{(a_{ef}a_{np}-a_{nf}a_{ep})((a_{ef}+a_{ep})(a_{np}+a_{nf})+(a_{ef}+a_{nf})(a_{ep}+a_{np}))}{(a_{ef}+a_{ep})(a_{np}+a_{nf})(a_{ef}+a_{nf})(a_{ep}+a_{np})}$		
Arithmetic Mean	$\frac{2a_{ef}a_{np}-2a_{nf}a_{ep}}{(a_{ef}+a_{ep})(a_{np}+a_{nf})+(a_{ef}+a_{nf})(a_{ep}+a_{np})}$		
Cohen	$\frac{2a_{ef}a_{np}-2a_{nf}a_{ep}}{(a_{ef}+a_{ep})(a_{np}+a_{ep})+(a_{ef}+a_{nf})(a_{nf}+a_{np})}$		
Scott	$\frac{4a_{ef}a_{np}-4a_{nf}a_{ep}-(a_{nf}-a_{ep})^2}{(2a_{ef}+a_{nf}+a_{ep})(2a_{np}+a_{nf}+a_{ep})}$		
Fleiss	$\frac{4a_{ef}a_{np}-4a_{nf}a_{ep}-(a_{nf}-a_{ep})^2}{(2a_{ef}+a_{nf}+a_{ep})+(2a_{np}+a_{nf}+a_{ep})}$		
Rogot1	$\frac{1}{2} \left( \frac{a_{ef}}{2a_{ef}+a_{nf}+a_{ep}} + \frac{a_{np}}{2a_{np}+a_{nf}+a_{ep}} \right)$		
Rogot2	$\frac{1}{4} \left( \frac{a_{ef}}{a_{ef}+a_{ep}} + \frac{a_{ef}}{a_{ef}+a_{nf}} + \frac{a_{np}}{a_{np}+a_{ep}} + \frac{a_{np}}{a_{np}+a_{nf}} \right)$		

Can use several other available metrics for ranking statements, e.g. Ochiai metric

$$\text{Score}(s) = \frac{\text{fail}(s)}{\sqrt{\text{allfail} * (\text{fail}(s) + \text{pass}(s))}}$$

A model for spectra-based software diagnosis, Naish et. al., TOSEM 20(3), 2011.

# Example 1

$$\text{Score}(s) = \frac{\frac{\text{fail}(s)}{\text{allfail}}}{\frac{\text{fail}(s)}{\text{allfail}} + \frac{\text{pass}(s)}{\text{allpass}}}$$

mid() { int x,y,z,m;	3,3,5	1,2,3	3,2,1	5,5,5	5,3,4	2,1,3	suspiciousness	rank
1: read("Enter 3 numbers:",x,y,z);	●	●	●	●	●	●	0.5	7
2: m = z;	●	●	●	●	●	●	0.5	7
3: if (y<z)	●	●	●	●	●	●	0.5	7
4:   if (x<y)	●	●			●	●	0.63	3
5:       m = y;		●					0.0	13
6:   else if (x<z)	●				●	●	0.71	2
7:       m = y;   // *** bug ***	●					●	0.83	1
8: else			●	●			0.0	13
9:   if (x>y)			●	●			0.0	13
10:       m = y;			●				0.0	13
11:   else if (x>z)				●			0.0	13
12:       m = x;							0.0	13
13: print("Middle number is:",m);	●	●	●	●	●	●	0.5	7
}								
Pass/Fail Status	P	P	P	P	P	F		

Executed mostly by failing test

- High suspiciousness score

# Example 2

Test Cases

		T15	T16	T17	T18
1	<pre>int count; int n; Ele *proc; List *src_queue, *dest_queue; if (prio &gt;= MAXPRIO) /*maxprio=3*/</pre>	●	●	●	●
2	<pre>{return;}</pre>		●	●	●
3	<pre>src_queue = prio_queue[prio]; dest_queue = prio_queue[prio+1]; count = src_queue-&gt;mem_count; if (count &gt; 1) /* Bug!/* supposed : count&gt;0*/ {</pre>	●	●	●	●
4	<pre>n = (int) (count*ratio + 1); proc = find_nth(src_queue, n); if (proc) {</pre>		●	●	
5	<pre>src_queue = del_ele(src_queue, proc); proc-&gt;priority = prio; dest_queue = append_ele(dest_queue, proc); }</pre>		●	●	
Pass/Fail of Test Case Execution :		Pass	Pass	Pass	Fail

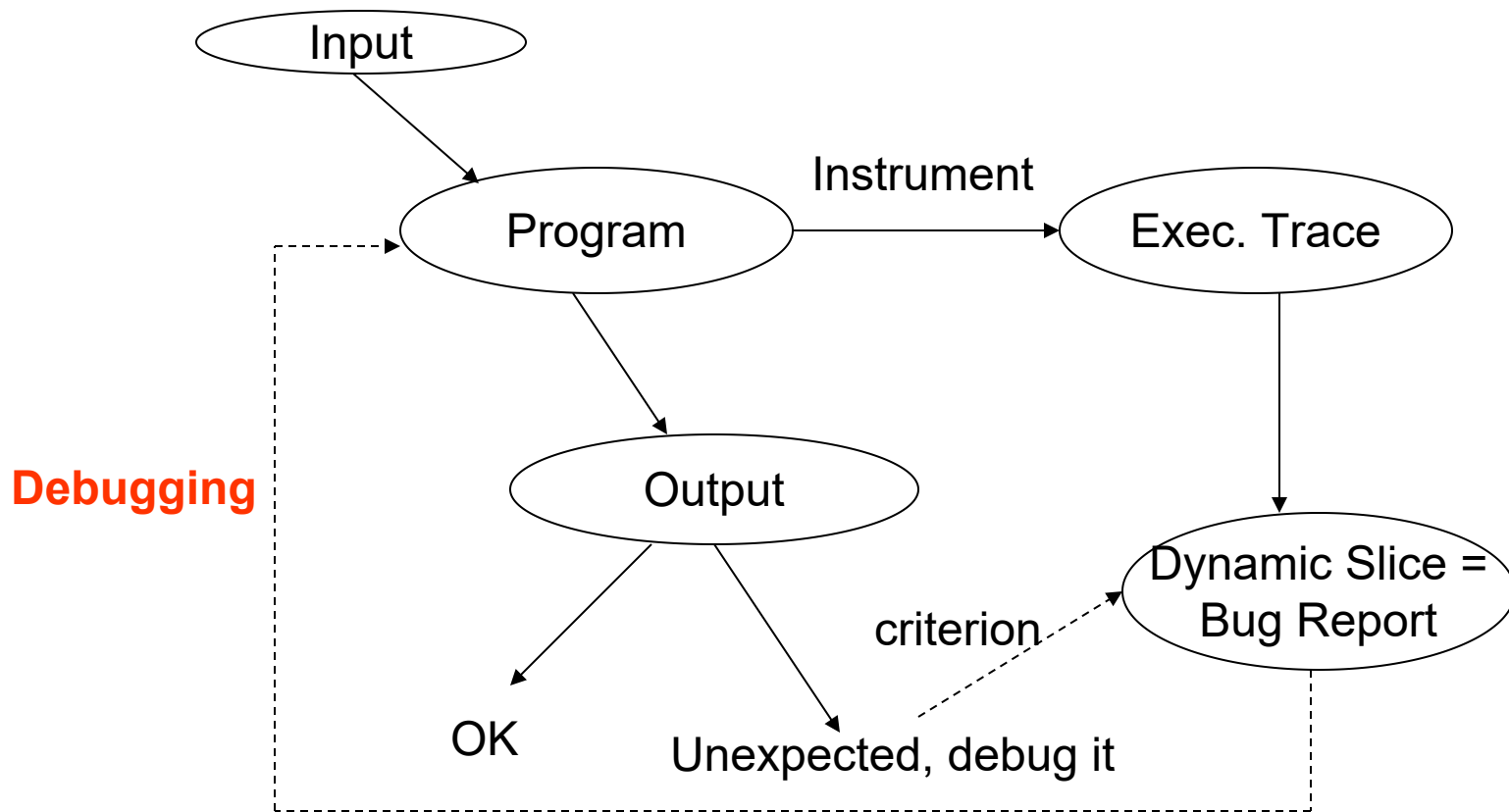
Which basic block is the most suspicious?

# Automated Debugging

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## Dynamic Slicing

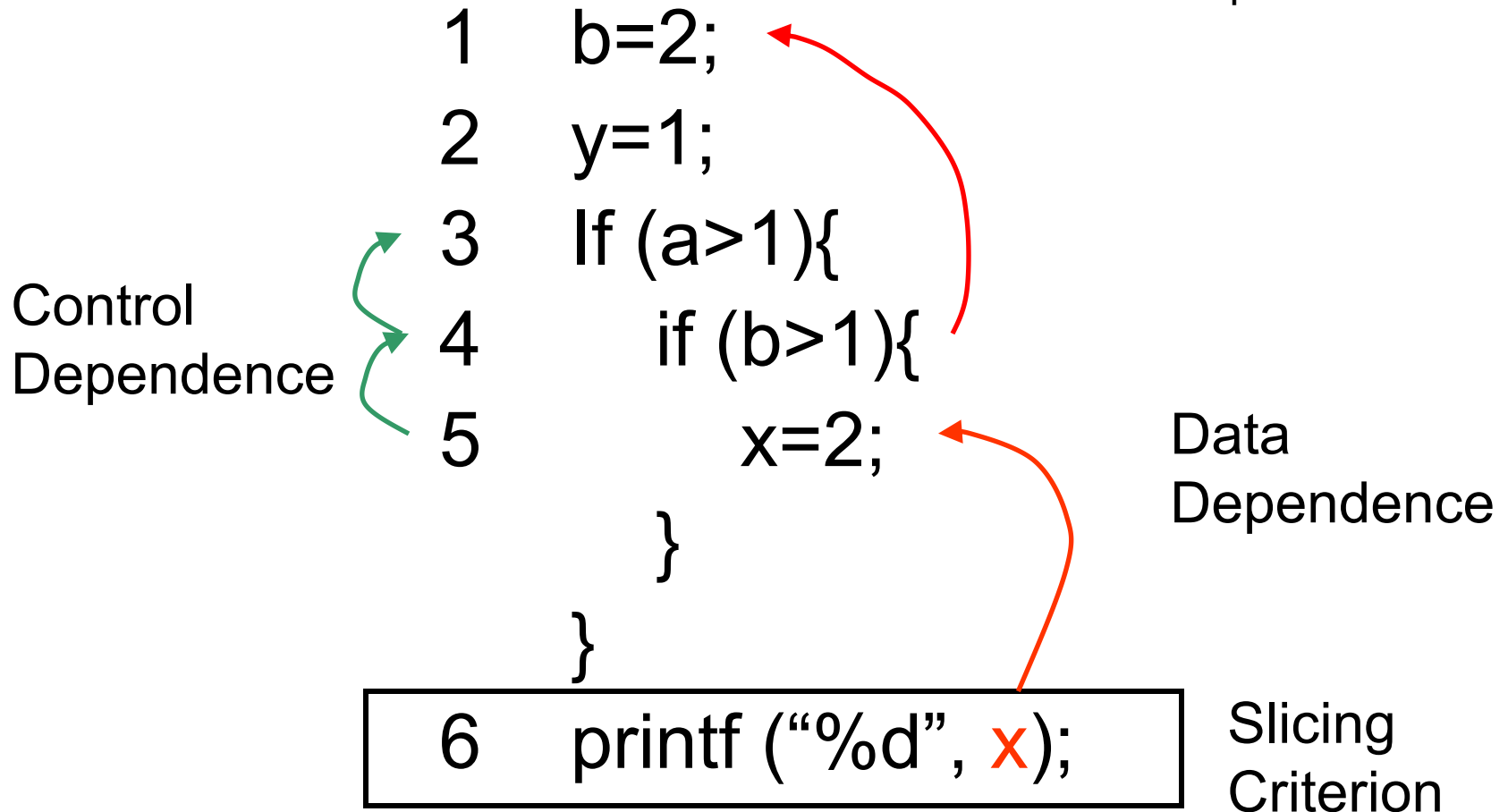
# Dynamic Slicing for Debugging



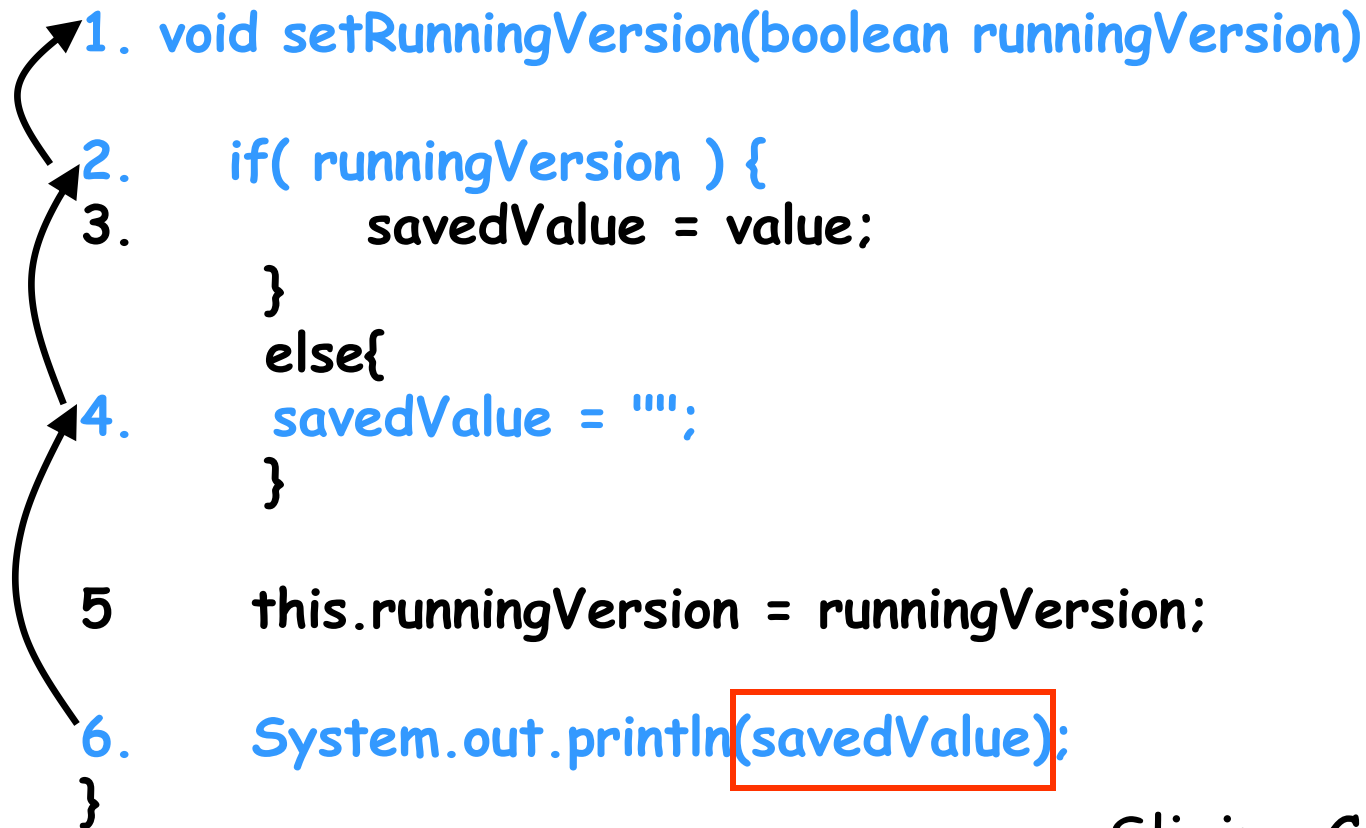


# Dynamic Slicing

Consider input `a == 2`



# Dynamic Slice



```
1. void setRunningVersion(boolean runningVersion)
2.     if( runningVersion ) {
3.         savedValue = value;
4.     } else{
5.         savedValue = "";
6.     }
7.     this.runningVersion = runningVersion;
8.     System.out.println(savedValue);
9. }
```

Slicing Criterion

# Dynamic slicing for debugging?

- Scalability
  - Large traces to analyze (and store?)
    - Optimizations exist – online compression.
  - Slice is too huge – slice comprehension
    - Tools such as WHYLINE have made it more user friendly
- Slicing still does not tell us what is actually wrong
  - Where did we veer off from the intended behavior? (我们从什么地方开始驶离原来的路径? )
  - What *is* the intended behavior? Often not documented! Lack of specifications is a problem.

# Automated Debugging

---

## Delta Debugging



udacity — ssh — 115x31

[regehr@dyson r48]\$

# Simplification

---

Once we have reproduced a program failure, we must find out what's relevant:

- Does failure really depend on 10,000 lines of code?
- Does failure really require this exact schedule of events?
- Does failure really need this sequence of function calls?

# Why Simplify?

---

- Ease of communication: a simplified test case is easier to communicate
- Easier debugging: smaller test cases result in smaller states and shorter executions
- Identify duplicates: simplified test cases subsume several duplicates

# Real-World Scenario

---

In July 1999, Bugzilla listed more than 370 open bug reports for Mozilla's web browser

- These were not even simplified
- Mozilla engineers were overwhelmed with the work
- They created the Mozilla BugAthon: a call for volunteers to simplify bug reports

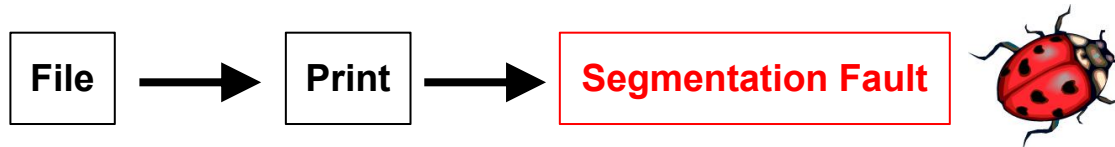
*When you've cut away as much HTML, CSS, and JavaScript as you can, and cutting away any more causes the bug to disappear, you're done.*

— Mozilla BugAthon call



# How do we go from this ...

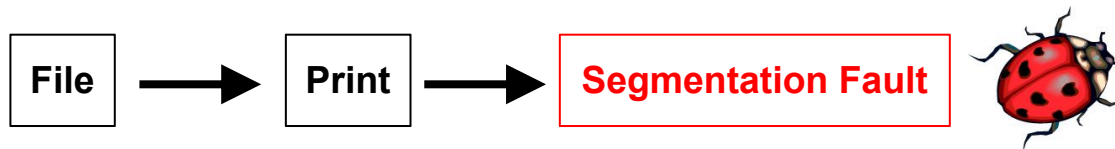
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<td align=left valign=top>
<SELECT NAME="op sys" MULTIPLE SIZE=7>
<OPTION VALUE="All">All<OPTION VALUE="Windows 3.1">Windows 3.1<OPTION VALUE="Windows 95">Windows 95<OPTION VALUE="Windows 98">Windows 98<OPTION
VALUE="Windows ME">Windows ME<OPTION VALUE="Windows 2000">Windows 2000<OPTION VALUE="Windows NT">Windows NT<OPTION VALUE="Mac System 7">Mac
System 7<OPTION VALUE="Mac System 7.5">Mac System 7.5<OPTION VALUE="Mac System 7.6.1">Mac System 7.6.1<OPTION VALUE="Mac System 8.0">Mac System
8.0<OPTION VALUE="Mac System 8.5">Mac System 8.5<OPTION VALUE="Mac System 8.6">Mac System 8.6<OPTION VALUE="Mac System 9.x">Mac System
9.x<OPTION VALUE="MacOS X">MacOS X<OPTION VALUE="Linux">Linux<OPTION VALUE="BSDI">BSDI<OPTION VALUE="FreeBSD">FreeBSD<OPTION
VALUE="NetBSD">NetBSD<OPTION VALUE="OpenBSD">OpenBSD<OPTION VALUE="AIX">AIX<OPTION VALUE="BeOS">BeOS<OPTION VALUE="HP-UX">HP-UX<OPTION
VALUE="IRIX">IRIX<OPTION VALUE="Neutrino">Neutrino<OPTION VALUE="OpenVMS">OpenVMS<OPTION VALUE="OS/2">OS/2<OPTION VALUE="OSF/1">OSF/1<OPTION
VALUE="Solaris">Solaris<OPTION VALUE="SunOS">SunOS<OPTION VALUE="other">other</SELECT>
</td>
<td align=left valign=top>
<SELECT NAME="priority" MULTIPLE SIZE=7>
<OPTION VALUE="--">--<OPTION VALUE="P1">P1<OPTION VALUE="P2">P2<OPTION VALUE="P3">P3<OPTION VALUE="P4">P4<OPTION VALUE="P5">P5</SELECT>
</td>
<td align=left valign=top>
<SELECT NAME="bug severity" MULTIPLE SIZE=7>
<OPTION VALUE="blocker">blocker<OPTION VALUE="critical">critical<OPTION VALUE="major">major<OPTION VALUE="normal">normal<OPTION
VALUE="minor">minor<OPTION VALUE="trivial">trivial<OPTION VALUE="enhancement">enhancement</SELECT>
</tr>
</table>
```



# ... to this?

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<SELECT>



# Your Solution

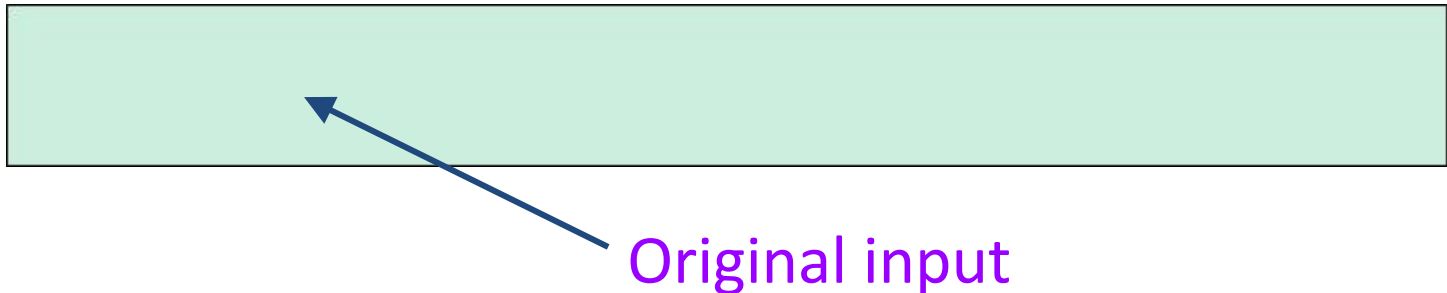
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- How do you solve these problems?
- Binary Search
  - Cut the test-case in half
  - Iterate
- Brilliant idea: why not automate this?

# Binary Search

---

- Proceed by binary search. Throw away half the input and see if the output is still wrong.
- If not, go back to the previous state and discard the other half of the input.



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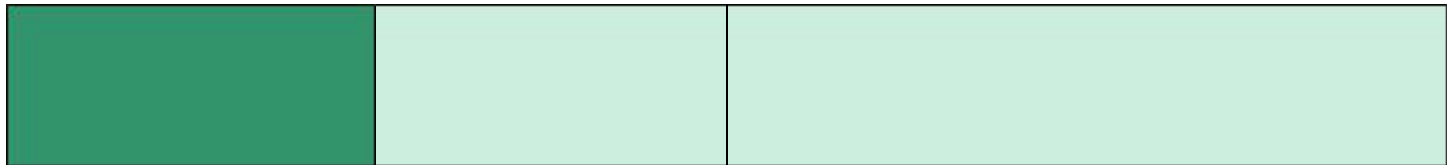
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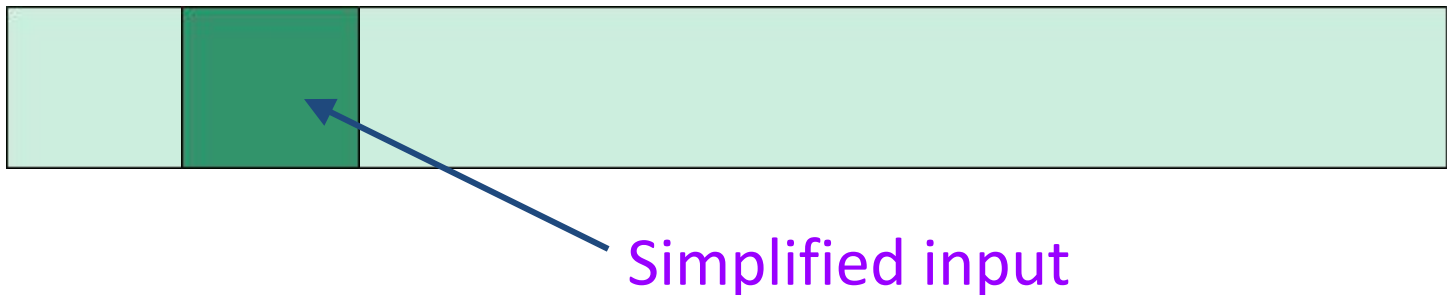
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# Complex Input

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