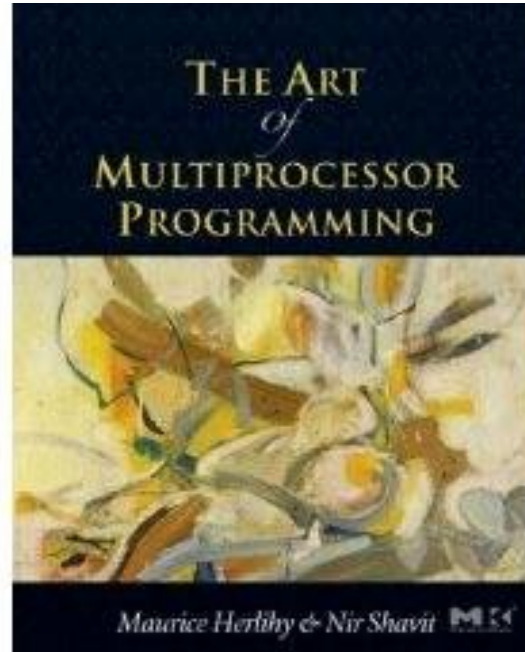


# COS 226

## Chapter 10

## Concurrent Queues and the ABA Problem

# Acknowledgement



- Some of the slides are taken from the companion slides for “The Art of Multiprocessor Programming” by Maurice Herlihy & Nir Shavit



# Pools

- Similar to Set class of Chapter 9 except:
  - Pool object does not necessarily have a `contains()` method
  - Same item can appear more than once



# Bounded vs Unbounded

- Bounded

- ☐ Fixed capacity
- ☐ Good when resources an issue

- Unbounded

- ☐ Holds any number of objects



# Total, partial or synchronous

## ■ Total:

- A method is total if calls do not wait for conditions to become true
- For example:
  - An attempt to dequeue from an empty queue throws an exception or failure code



# Total, partial or synchronous

- Partial:

- A method may wait for conditions to hold

- For example:

- Thread that tries to dequeue from an empty queue blocks (suspends) until item becomes available



# Total, partial or synchronous

## ■ Synchronous:

- A method is synchronous if it waits for another method to overlap its call interval
- For example:
  - A method call that adds an item to the pool is blocked until that item is removed by another method call
  - Used by CSP and Ada for threads to rendezvous and exchange values



# Blocking vs Non-Blocking

- Problem cases:
  - Removing from empty pool
  - Adding to full (bounded) pool
- Blocking
  - Caller waits until state changes
- Non-Blocking
  - Method throws exception





# Bounded Queues

- How much concurrency can we expect a bounded queue implementation with multiple concurrent enqueueers and dequeuers to have?

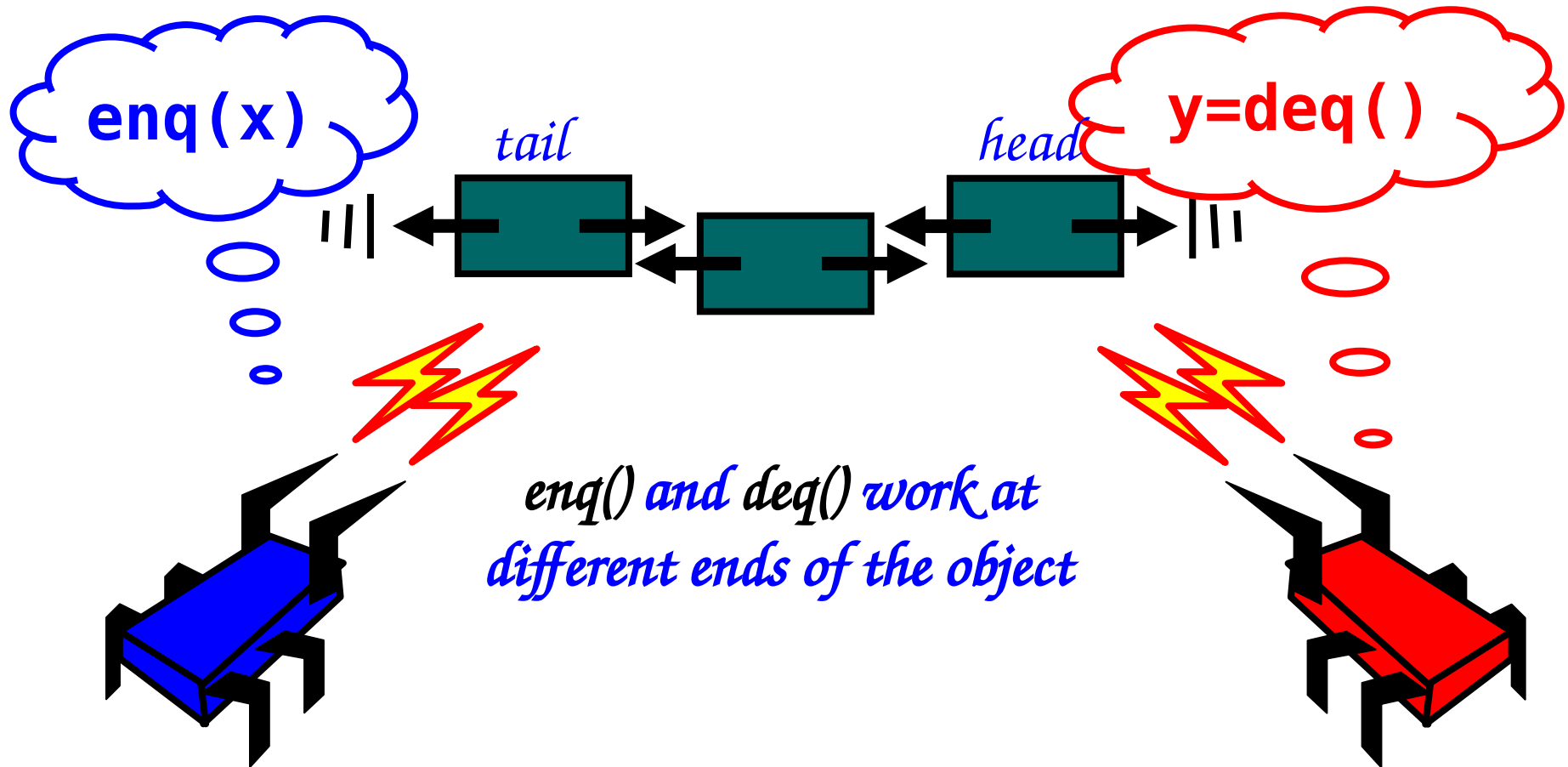


# Bounded Queues

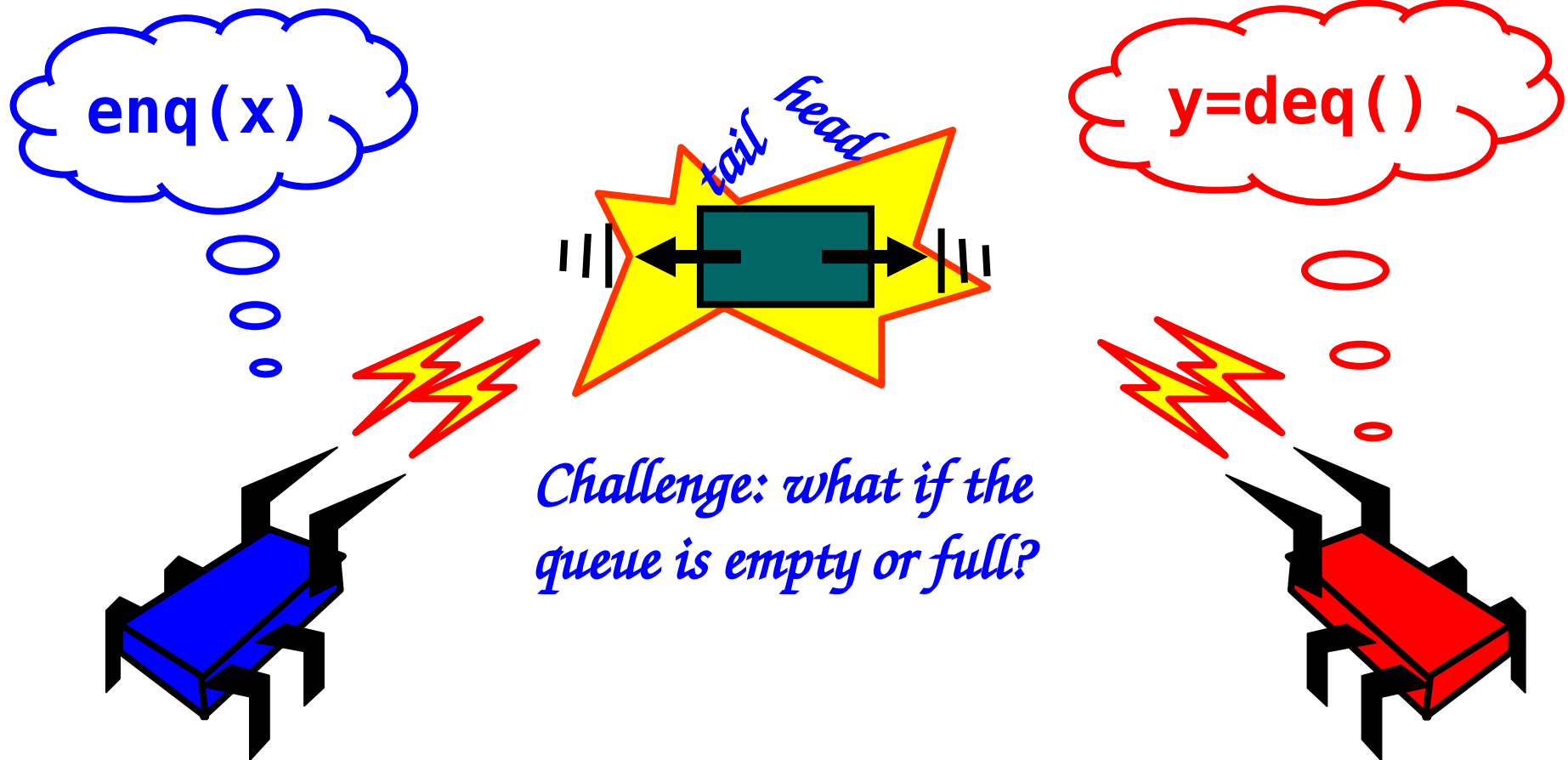
- Informally:

- ☐ enq() and deq() methods operate on opposite ends of the queue
- ☐ So an enq() call and a deq() call should be able to proceed concurrently without interference
- ☐ Concurrent deq() calls and concurrent enq() calls will however interfere

# Queue: Concurrency



# Concurrency

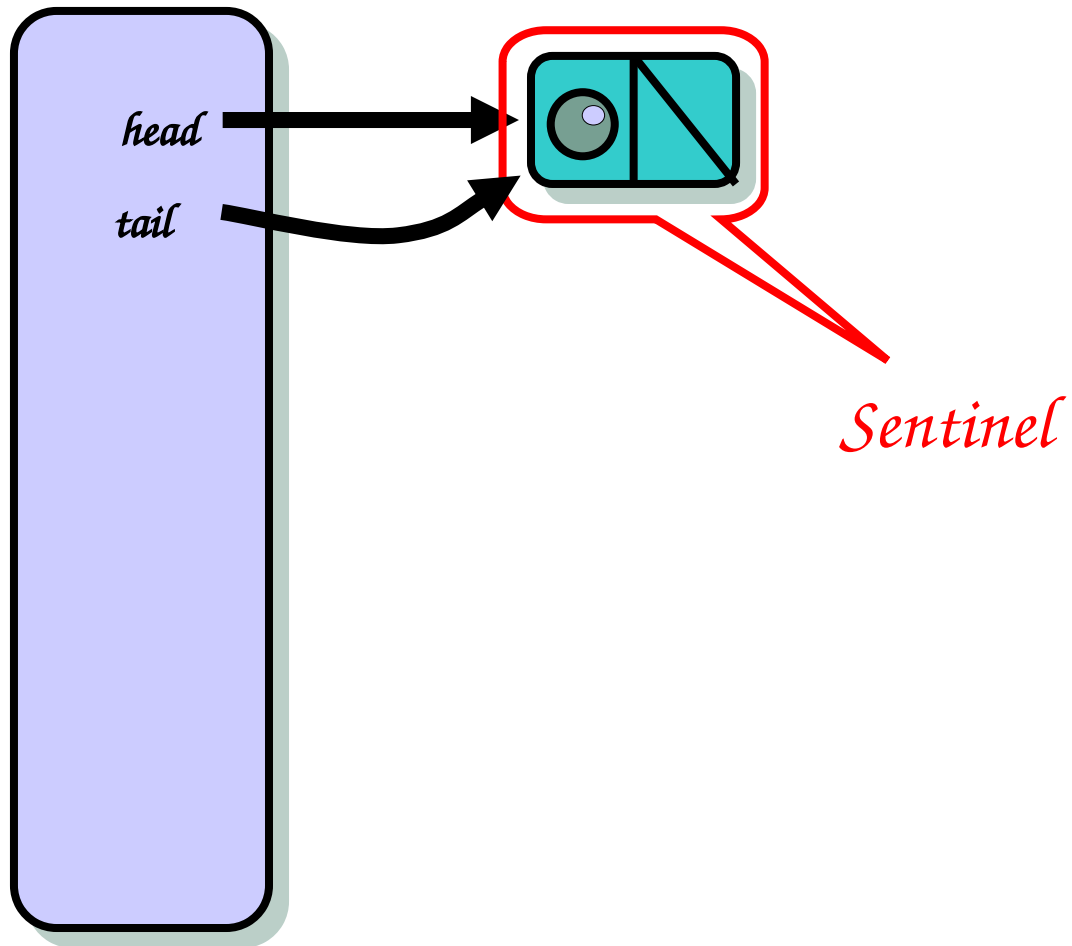




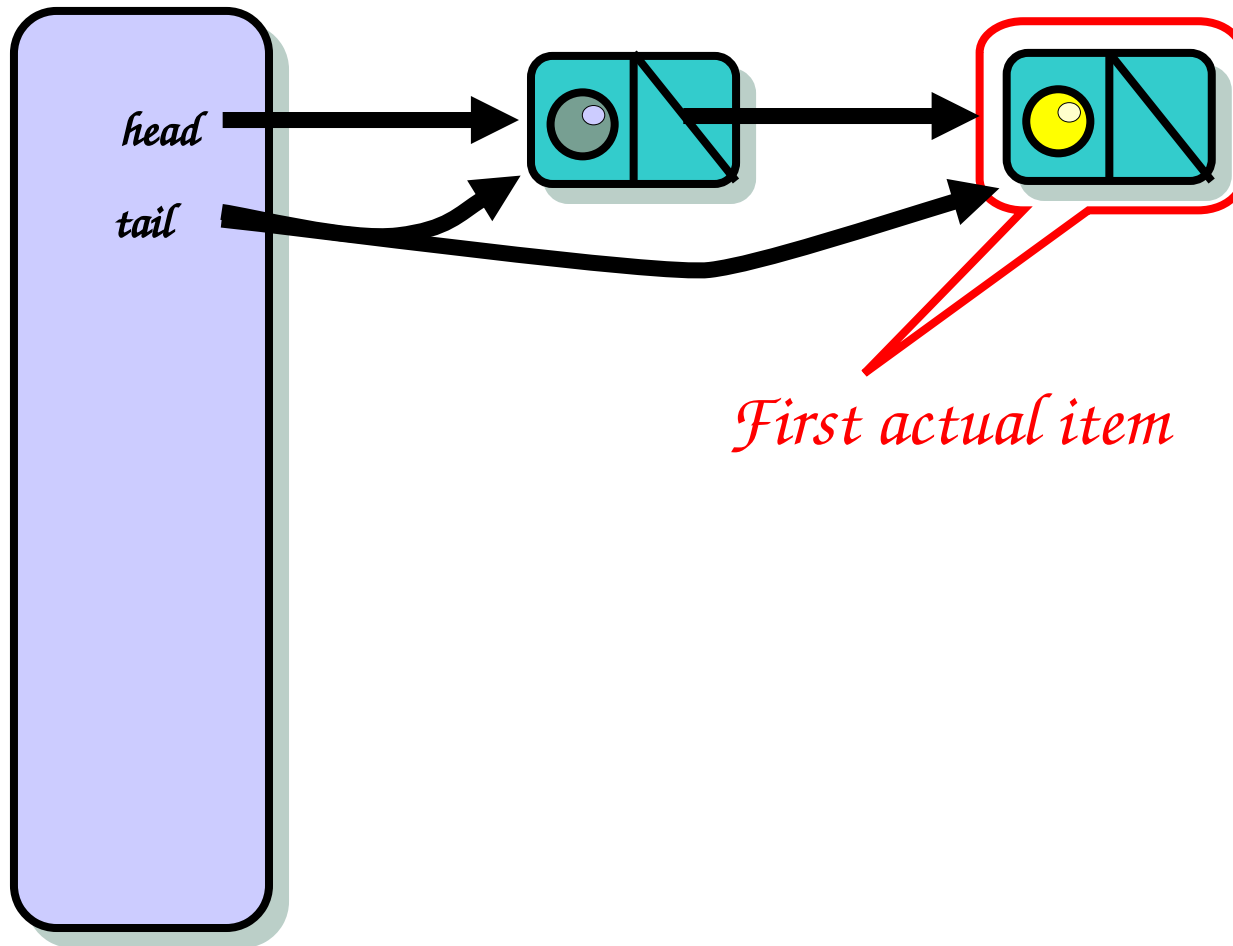
# Bounded lock-based queue

- Implement queue as linked list
- Queue has head and tail fields that refer to first and last nodes in list
- The queue contains a sentinel node – a place-holder

# Bounded Queue



# Bounded Queue





# Bounded Queue

- Two distinct locks are used:
  - **deqlock** – to lock the front of the queue to ensure that there is not more than one dequeuer at a time
  - **enqlock** – to lock the end of the queue to ensure that there is not more than one enqueueer at a time

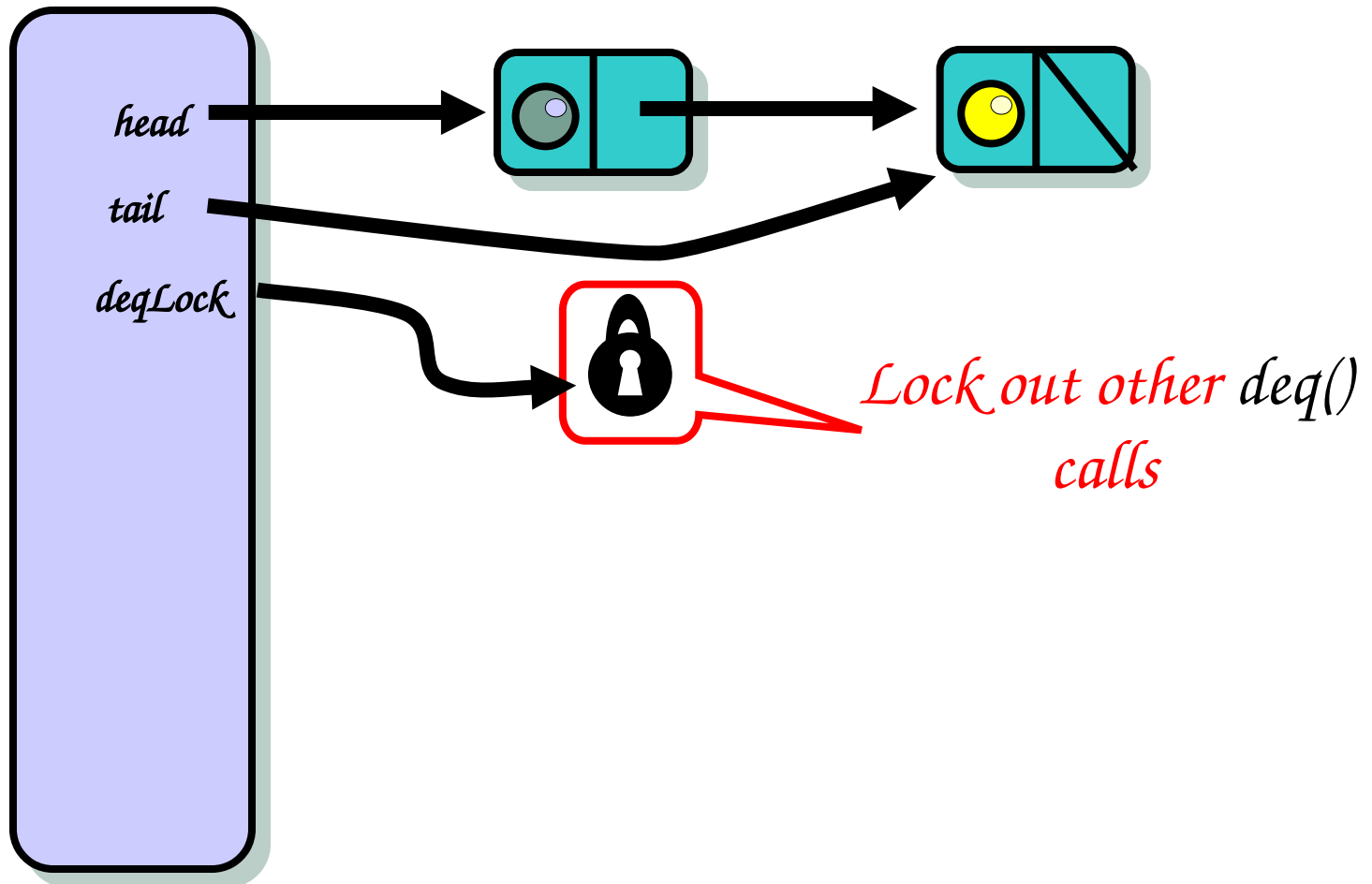




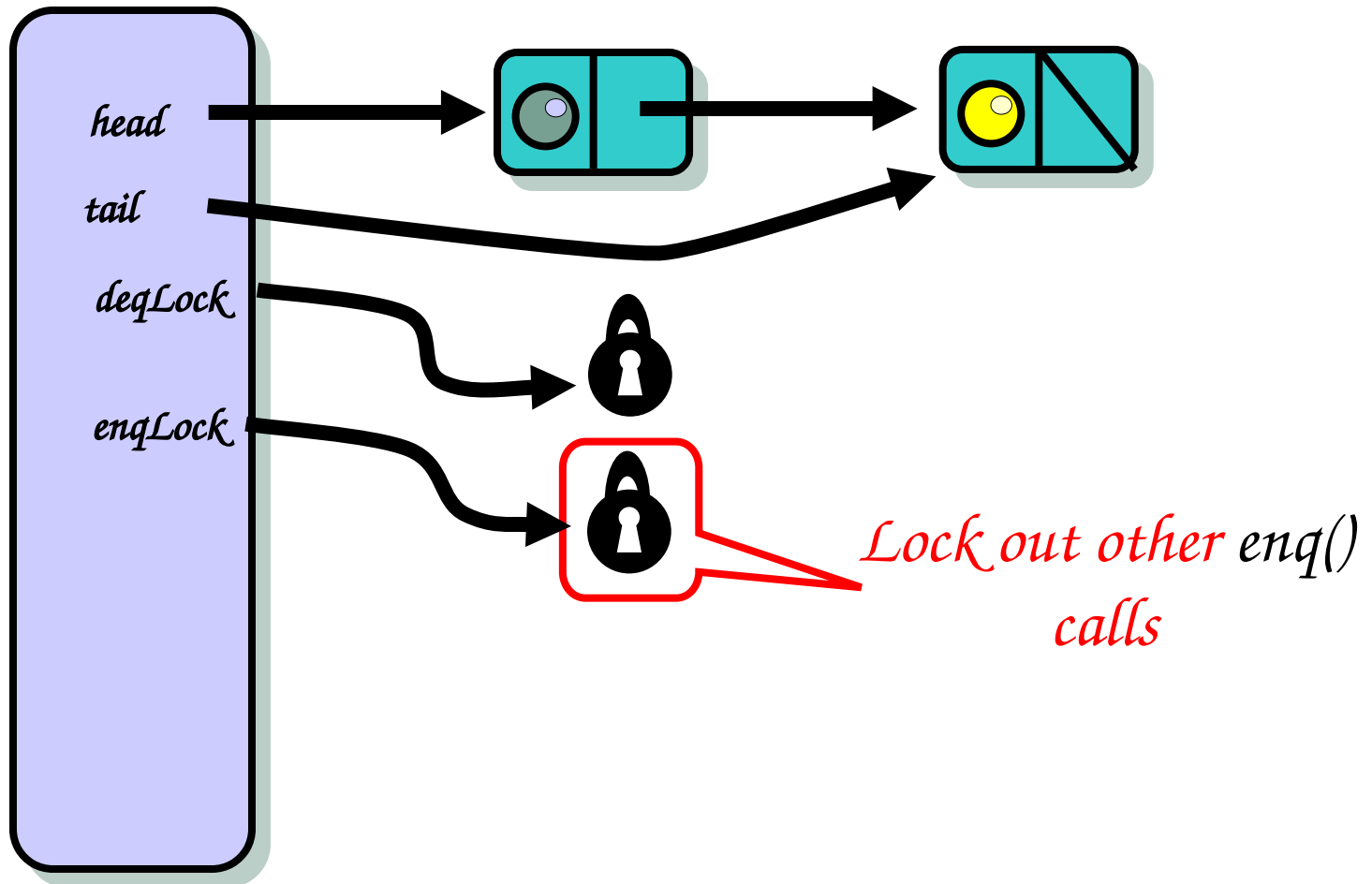
# Bounded Queue

- Using two locks instead of one means that enqueueers and dequeuers can operate independently and does not lock one another out unnecessarily

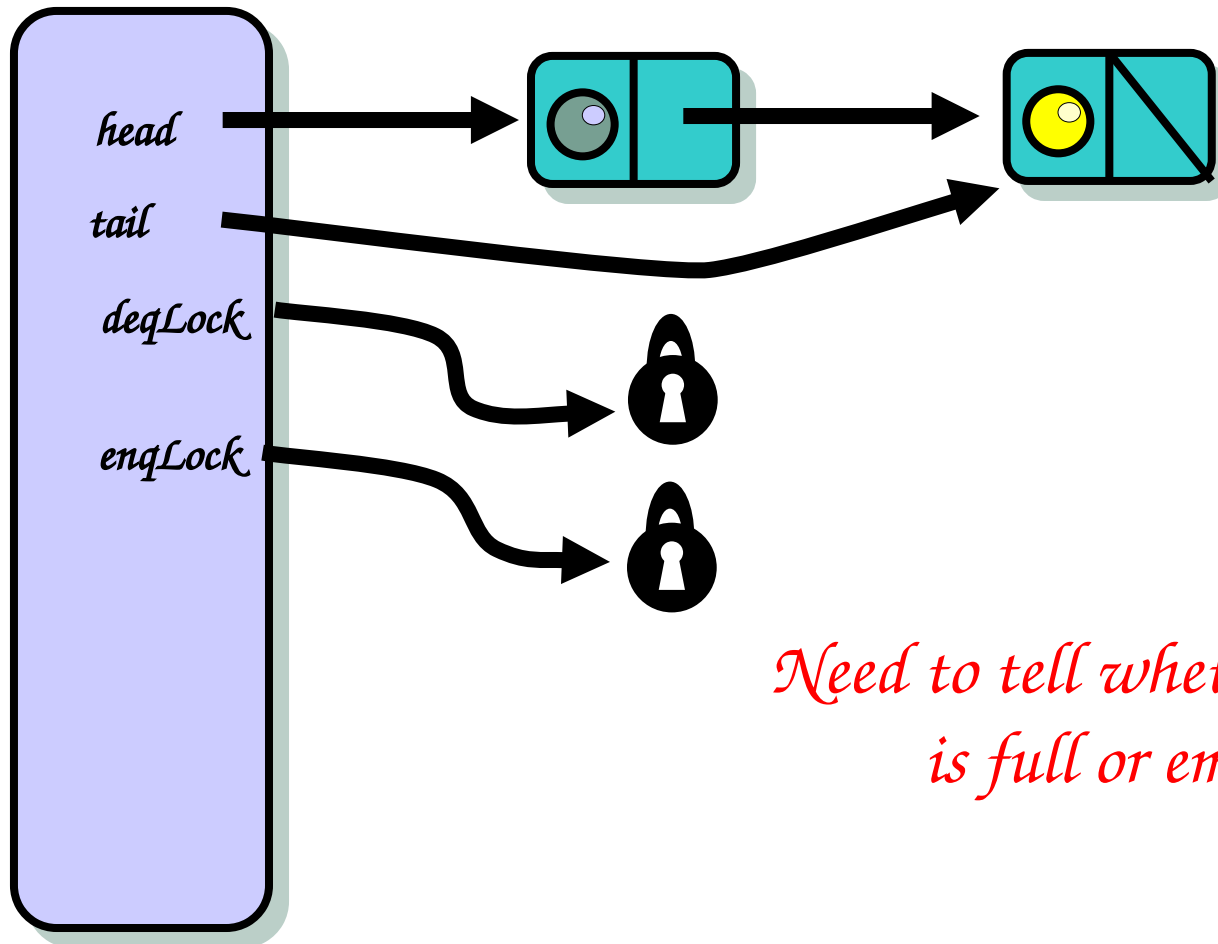
# Bounded Queue



# Bounded Queue



# Not Done Yet



*Need to tell whether queue  
is full or empty*



# Bounded Queues

- enq() calls cannot continue while list is full
- deq() calls cannot continue while list is empty



# Bounded Queue

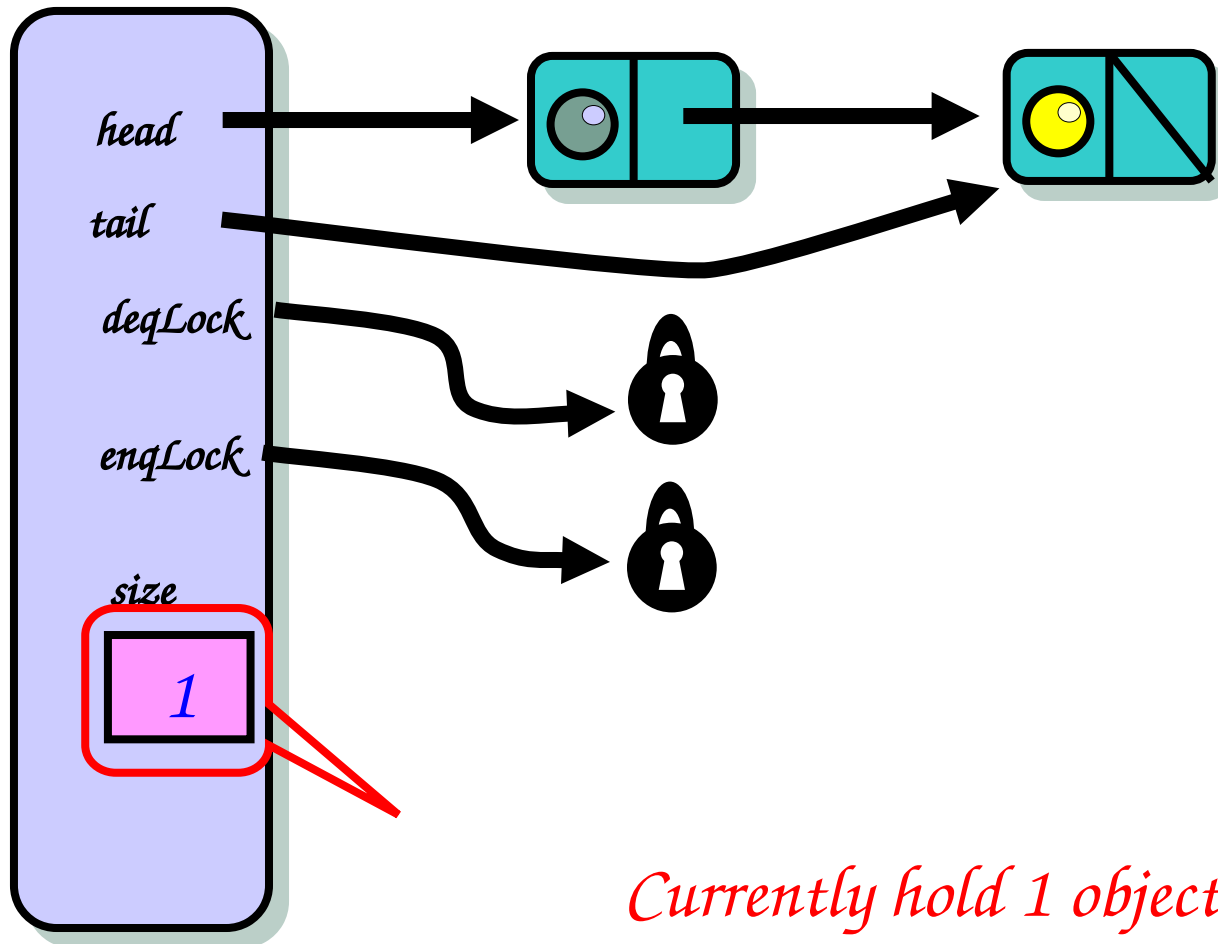
- Each lock has an associated condition field:
  - enqlock is associated with the notFullCondition
    - Notifies enqueueers when list is not full anymore
  - deqlock is associated with the notEmptyCondition
    - Notifies dequeuers when list is not empty anymore



# Bounded Queue

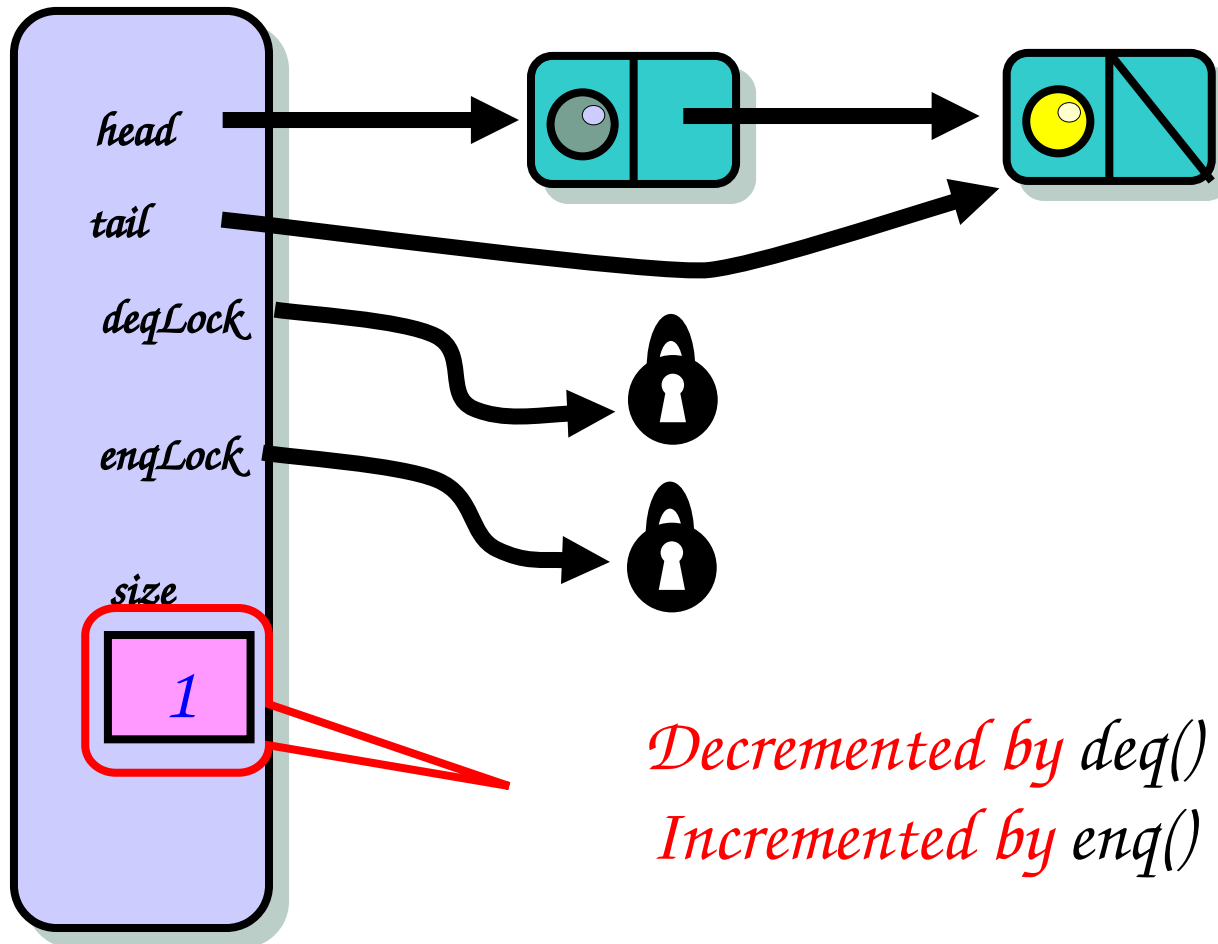
- Since the queue is bounded we must also keep track of the number of empty/available slots
- The size field keeps track of the number of objects currently in the queue
- The size field is an AtomicInteger

# Not Done Yet

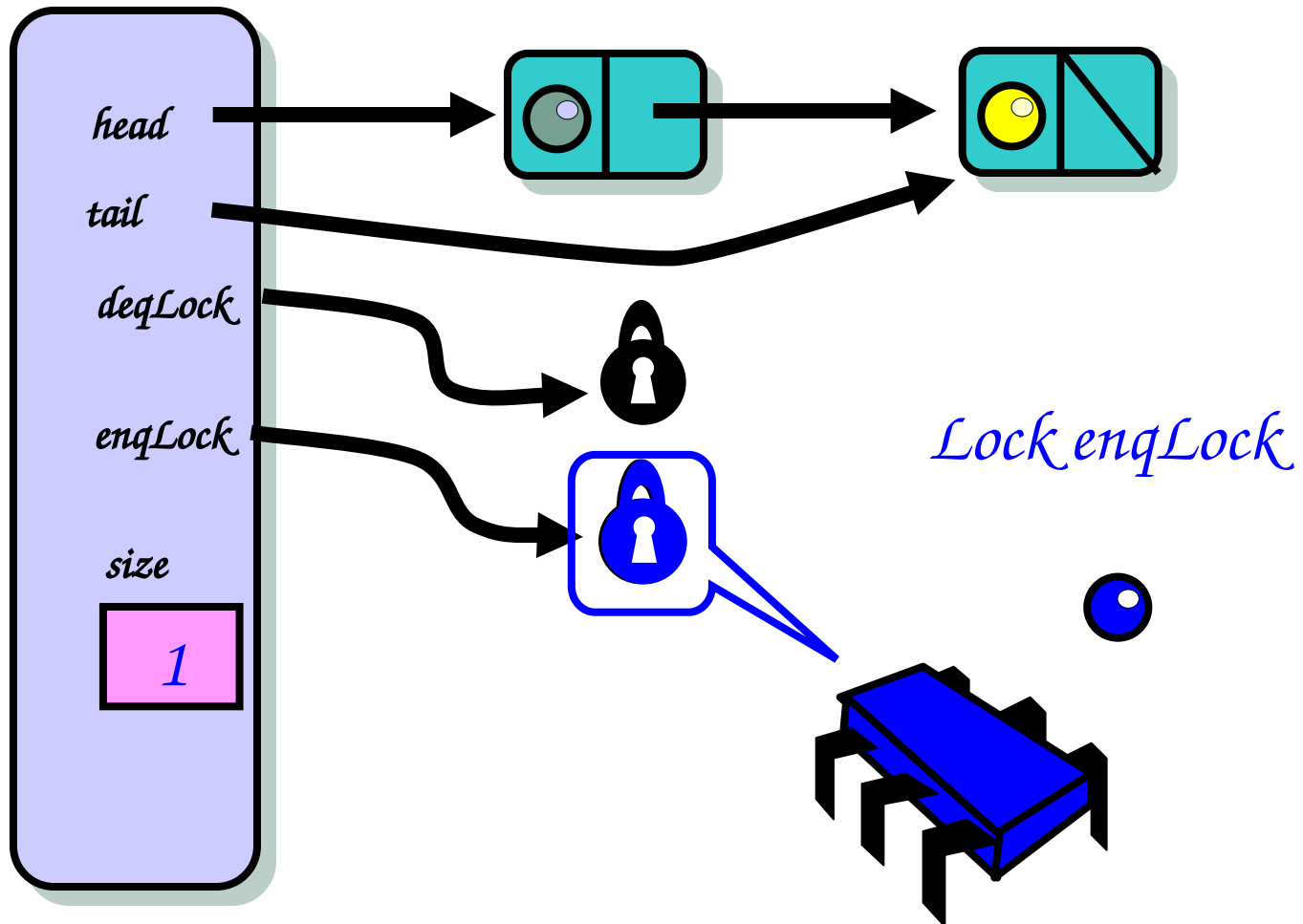




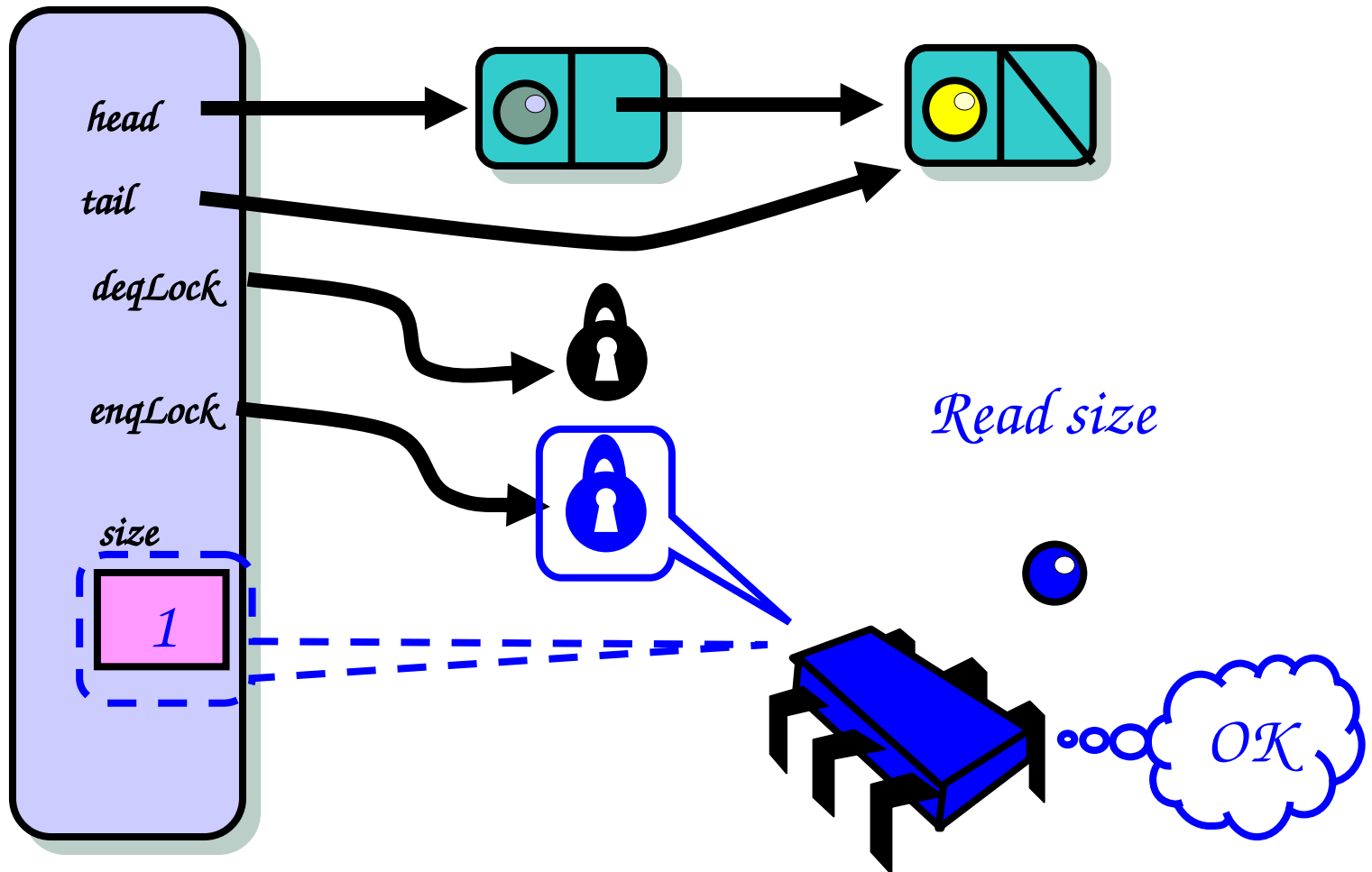
# Not Done Yet



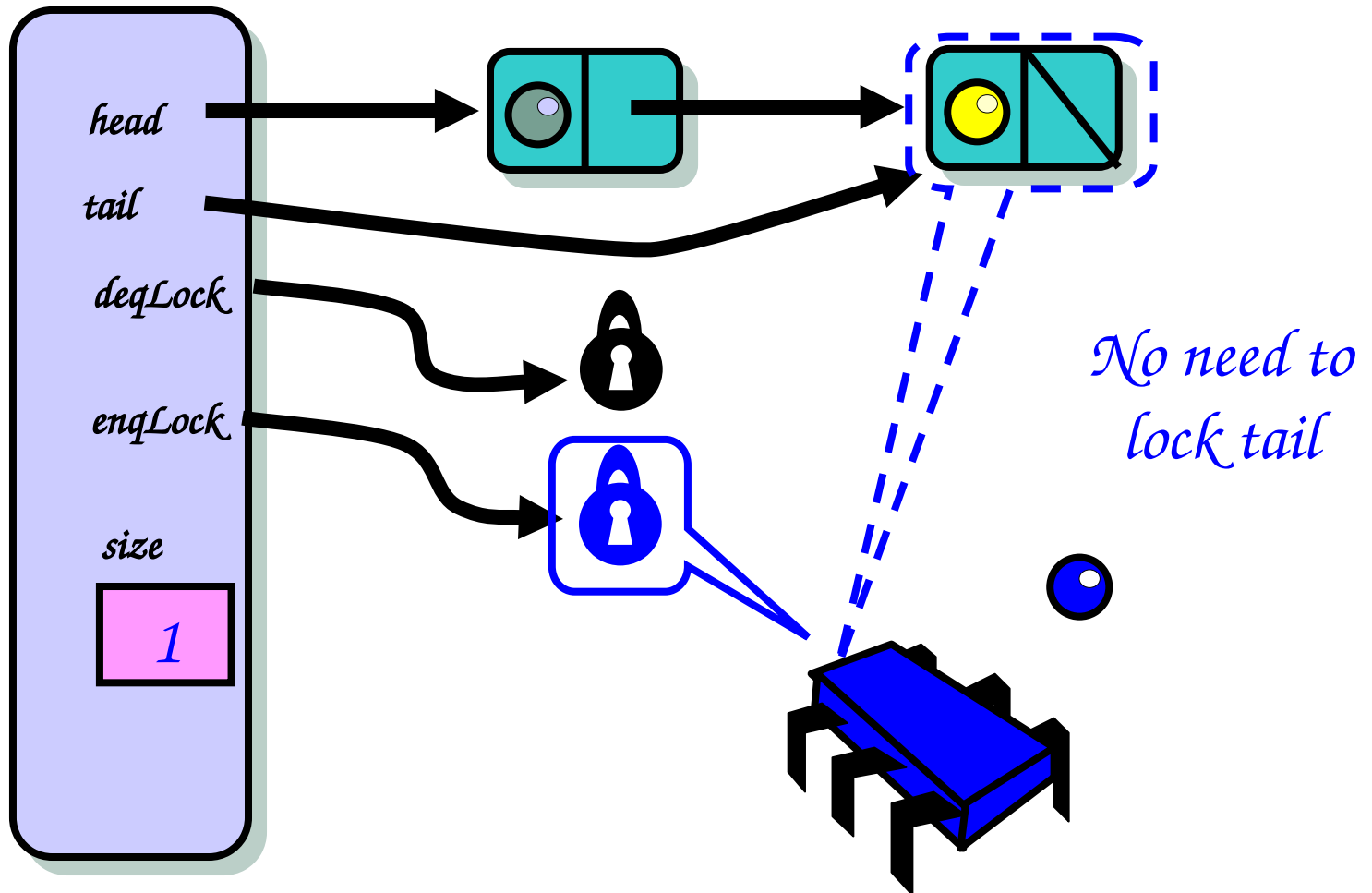
# Enqueuer



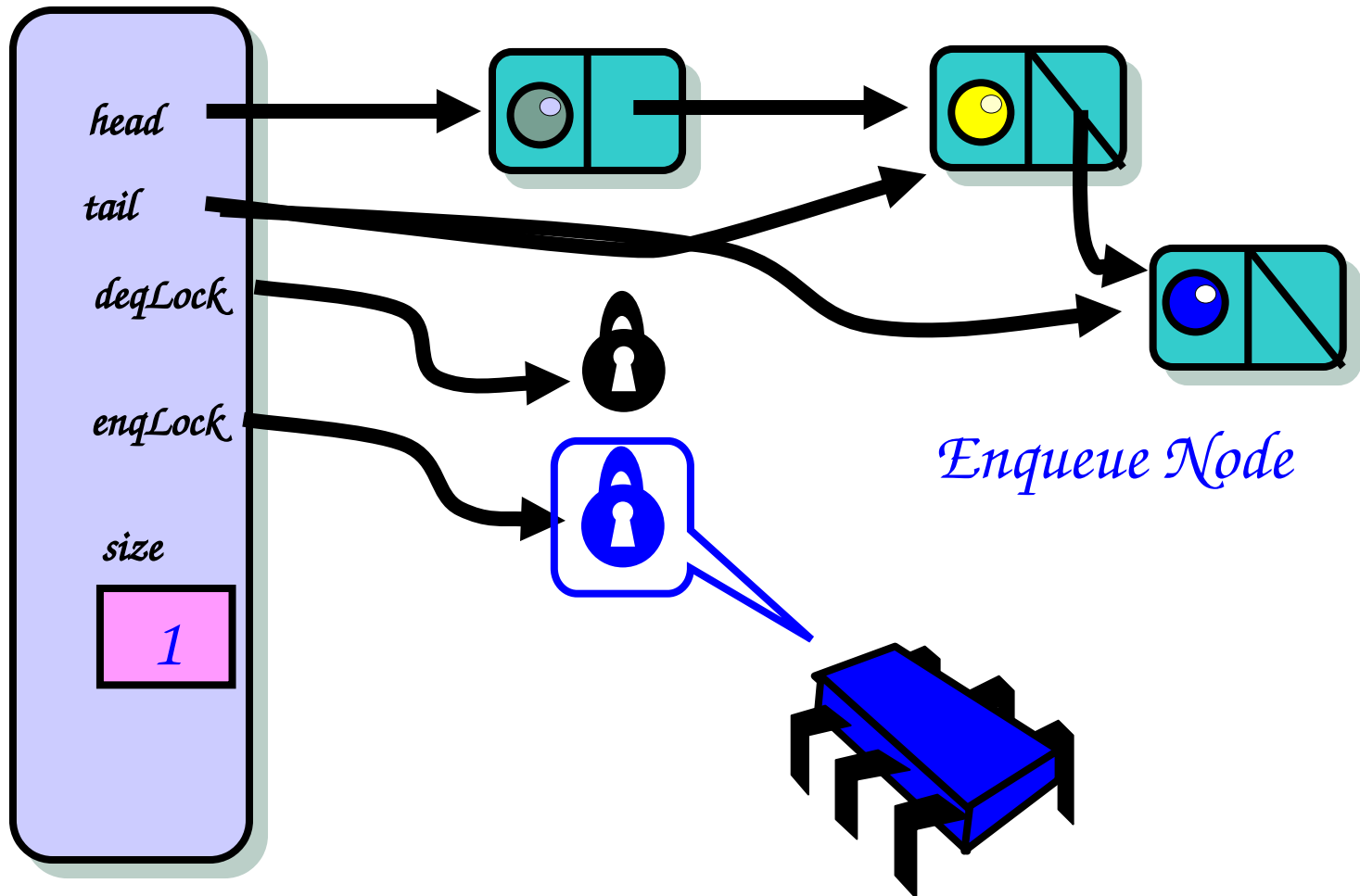
# Enqueuer



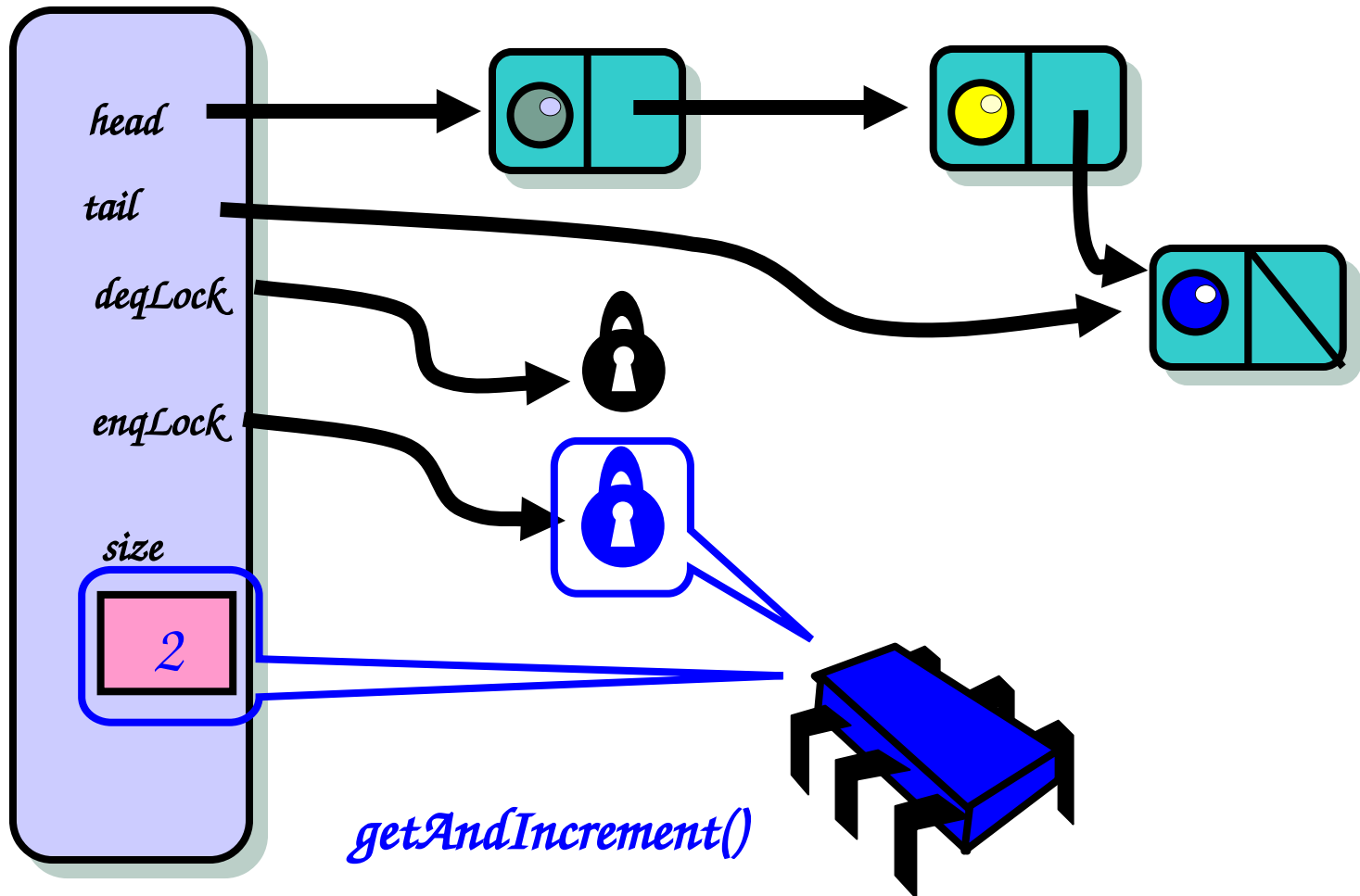
# Enqueuer



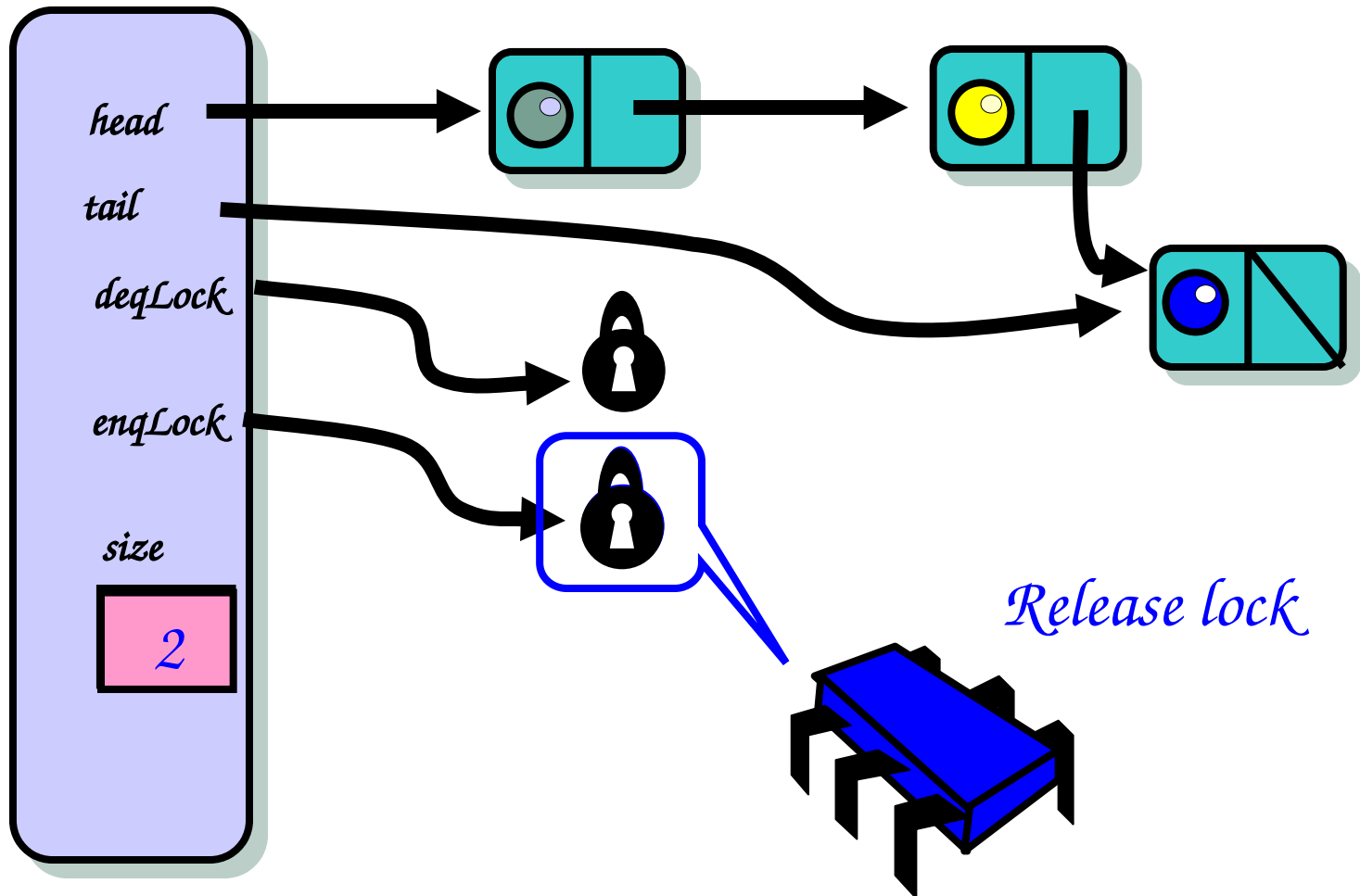
# Enqueuer



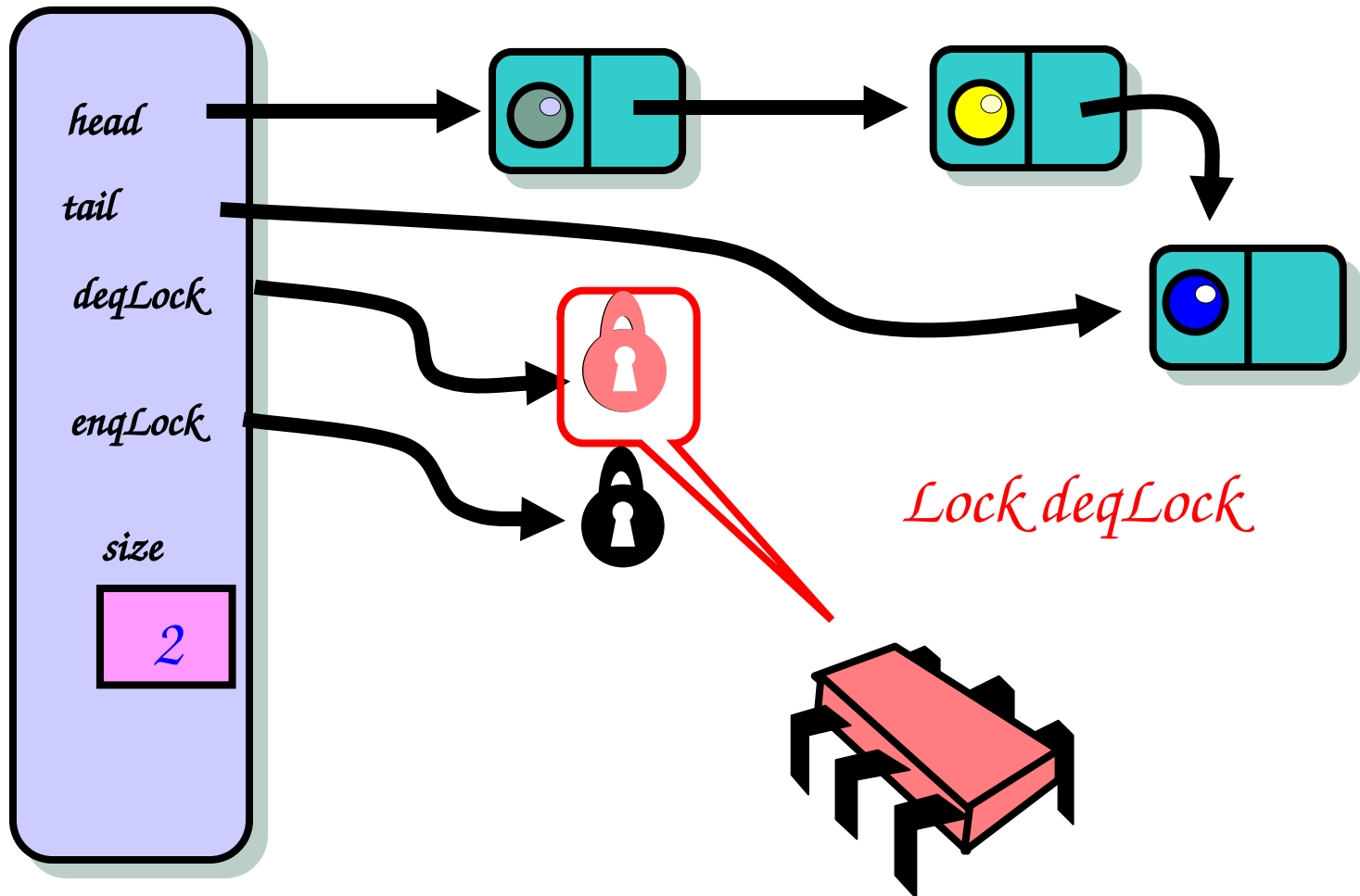
# Enqueuer



# Enqueuer

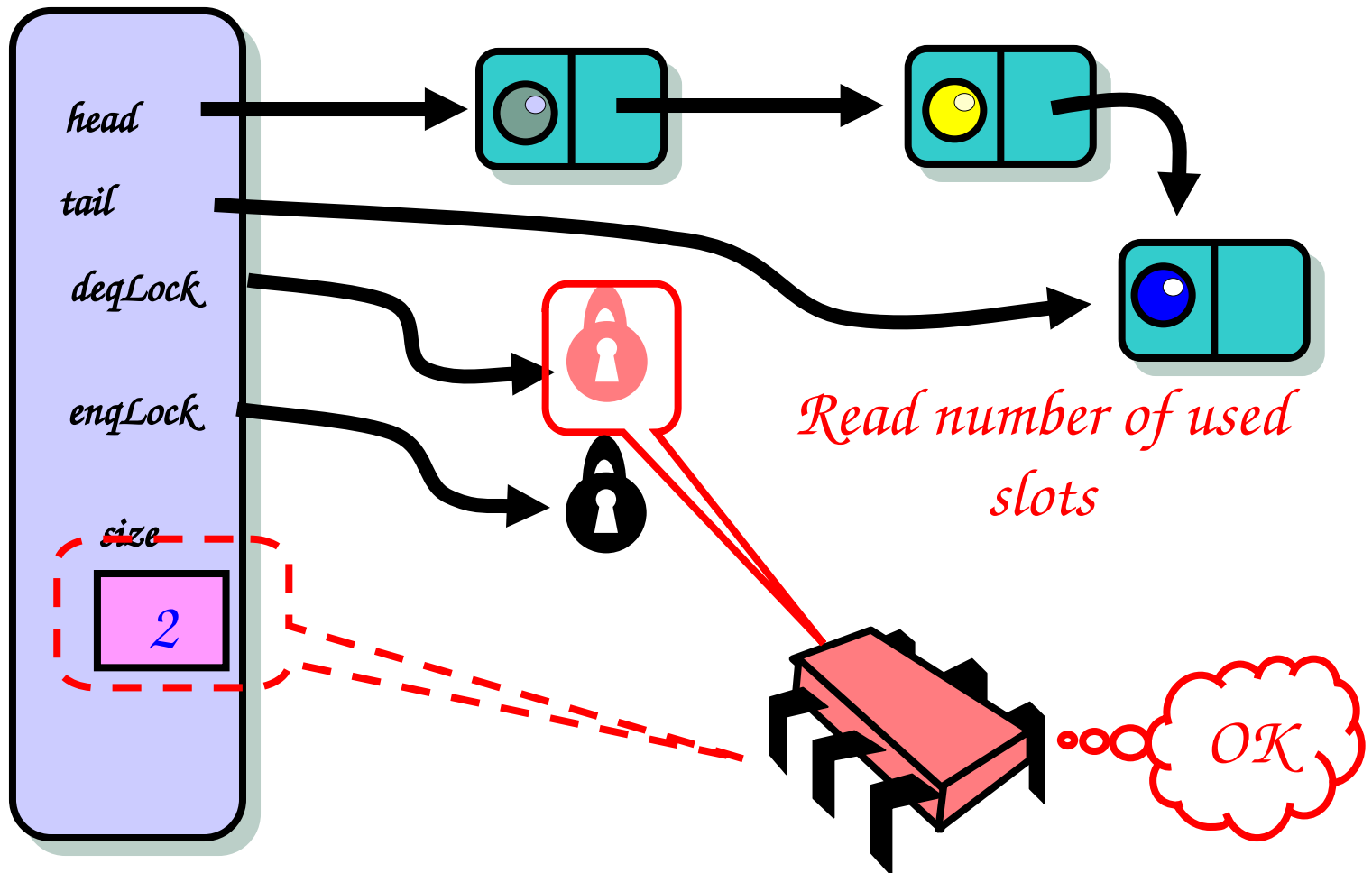


# Dequeuer

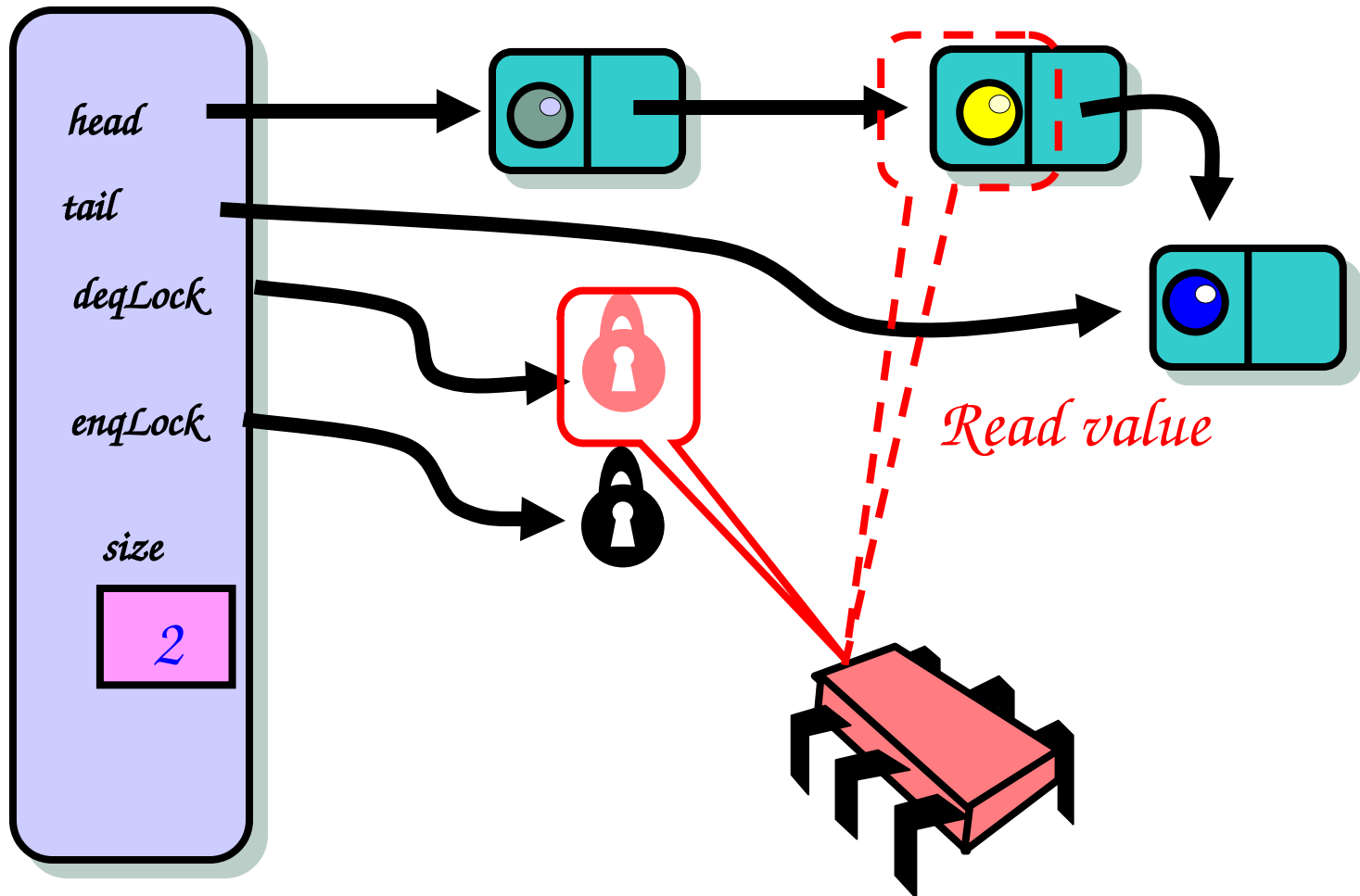




# Dequeuer

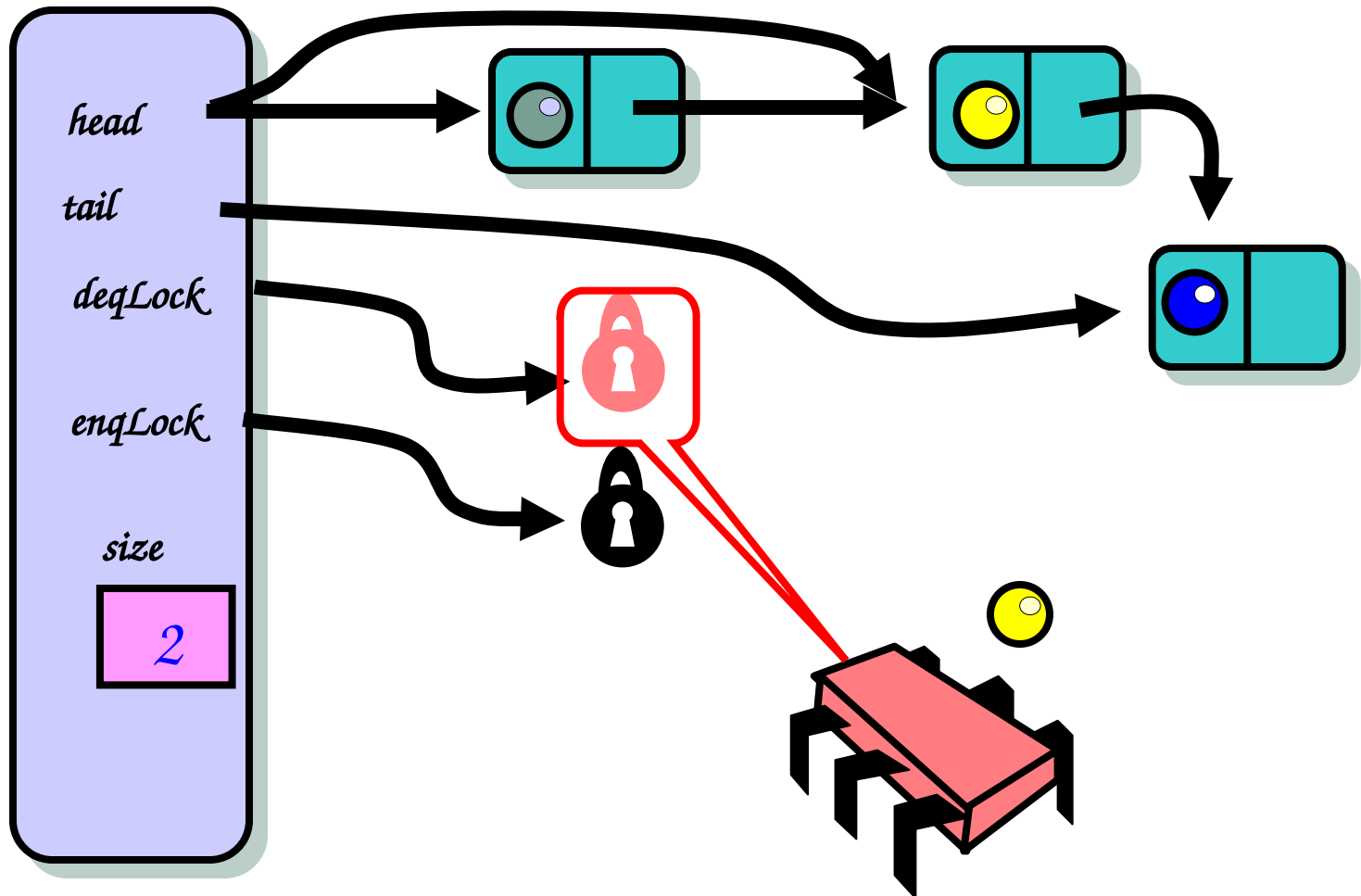


# Dequeuer

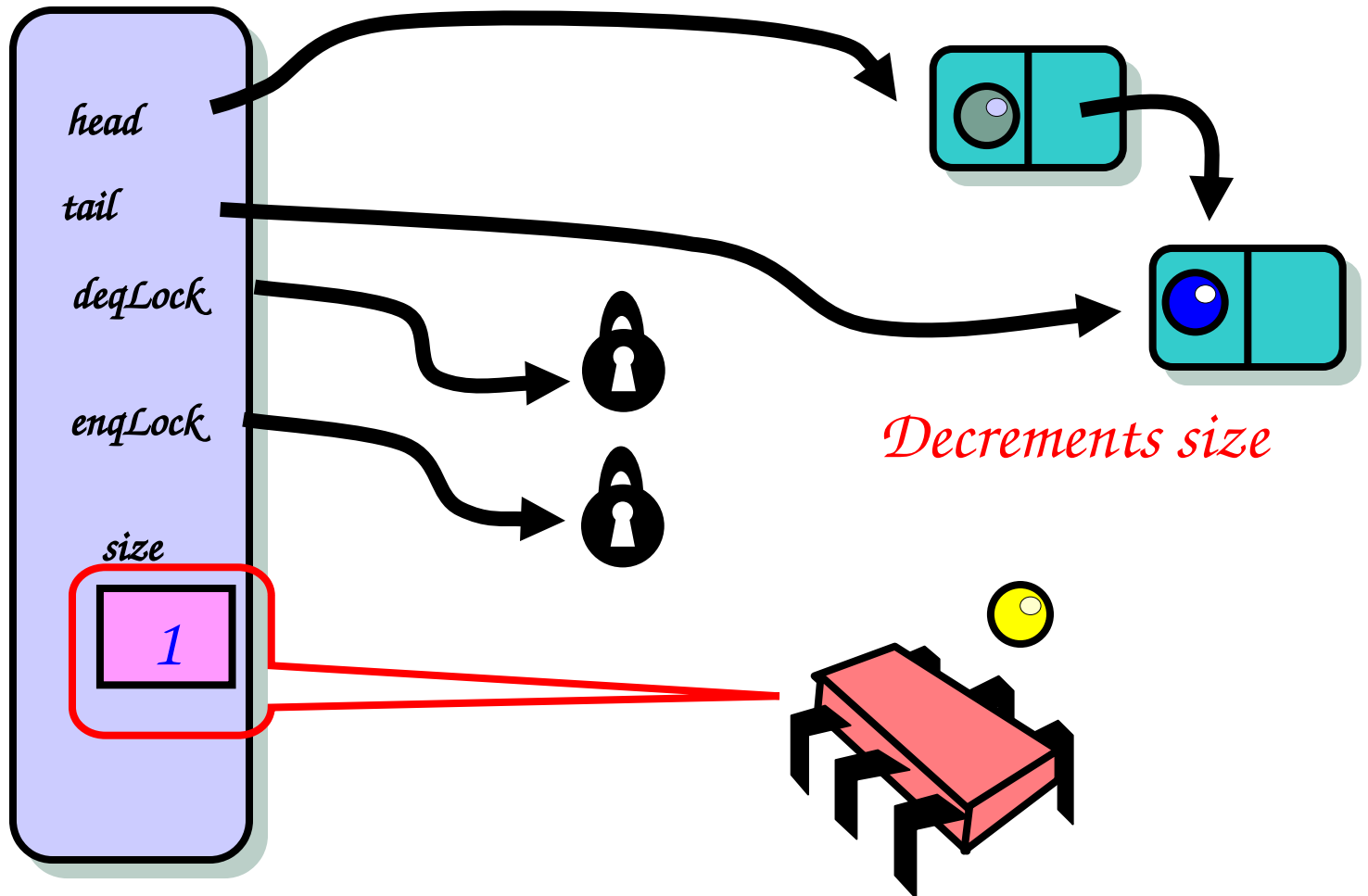


# Dequeuer

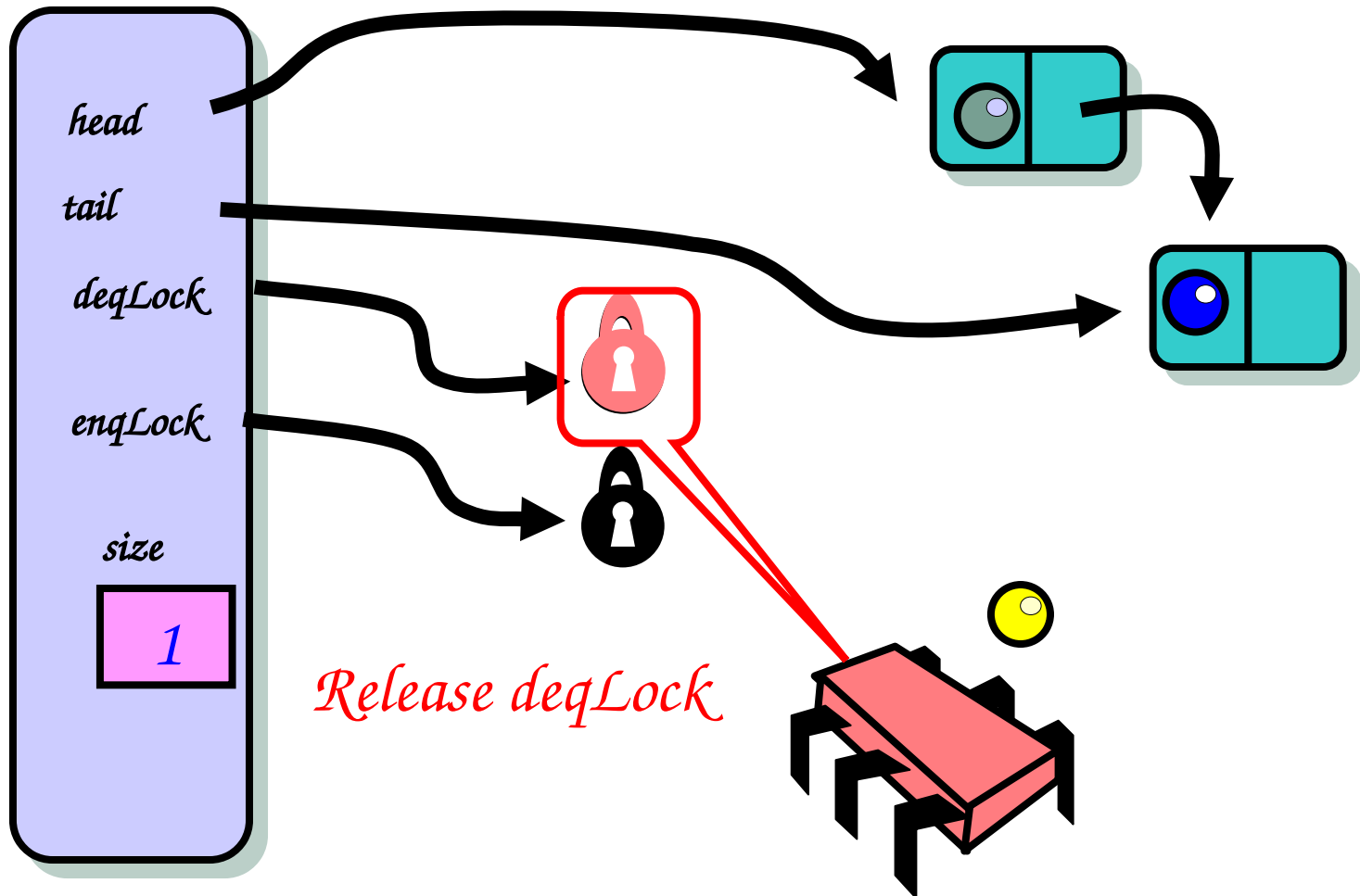
*Make first Node new  
sentinel*



# Dequeuer



# Dequeuer





# Bounded Queue

```
public class BoundedQueue<T> {  
    ReentrantLock enqLock, deqLock;  
    Condition notEmptyCondition, notFullCondition;  
    AtomicInteger size;  
    Node head;  
    Node tail;  
    int capacity;  
    enqLock = new ReentrantLock();  
    notFullCondition = enqLock.newCondition();  
    deqLock = new ReentrantLock();  
    notEmptyCondition = deqLock.newCondition();  
}
```

# Bounded Queue

```
public class BoundedQueue<T> {  
    ReentrantLock enqLock, deqLock;  
    Condition notEmptyCondition, notFullCondition;  
    AtomicInteger size;  
    Node head;  
    Node tail;  
    int capacity;  
    enqLock = new ReentrantLock();  
    notFullCondition = enqLock.newCondition();  
    deqLock = new ReentrantLock();  
    notEmptyCondition = deqLock.newCondition();  
}
```

*Enq & deq locks*

# Bounded Queue

```
public class BoundedQueue<T> {  
    ReentrantLock enqLock, deqLock;  
    Condition notEmptyCondition, notFullCondition;  
    AtomicInteger size;  
    Node head;  
    Node tail;  
    int capacity;  
    enqLock = new ReentrantLock();  
    notFullCondition = enqLock.newCondition();  
    deqLock = new ReentrantLock();  
    notEmptyCondition = deqLock.newCondition();  
}
```

*Conditions*



# Bounded Queue

```
public class BoundedQueue<T> {  
    ReentrantLock enqLock, deqLock;  
    Condition notEmptyCondition, notFullCondition;  
    AtomicInteger size;  
    Node head;  
    Node tail;  
    int capacity;  
    enqLock = new ReentrantLock();  
    notFullCondition = enqLock.newCondition();  
    deqLock = new ReentrantLock();  
    notEmptyCondition = deqLock.newCondition();  
}
```

*Associate conditions with locks*

# Enq Method Part One

```
public void enq(T x) {
    boolean mustWakeDequeuers = false;
    enqLock.lock();
    try {
        while (size.get() == capacity)
            notFullCondition.await();
        Node e = new Node(x);
        tail.next = e;
        tail = tail.next;
        if (size.getAndIncrement() == 0)
            mustWakeDequeuers = true;
    } finally {
        enqLock.unlock();
    }
    ...
}
```

# Enq Method Part One

```
public void enq(T x) {  
    boolean mustWakeDequeueurs = false;  
    enqLock.lock();  
    try {  
        while (size.get() == capacity)  
            notFullCondition.await();  
        Node e = new Node(x);  
        tail.next = e;  
        tail = tail.next;  
        if (size.getAndIncrement() == 0)  
            mustWakeDequeueurs = true;  
    } finally {  
        enqLock.unlock();  
    }  
    ...  
}
```

*Lock and unlock enq  
lock*

# Enq Method Part One

```
public void enq(T x) {  
    boolean mustWakeDequeuers = false;  
    enqLock.lock();  
    try {  
        while (size.get() == capacity)  
            notFullCondition.await();  
        Node e = new Node(x);  
        tail.next = e;  
        tail = tail.next;  
        if (size.getAndIncrement() == 0)  
            mustWakeDequeuers = true;  
    } finally {  
        enqLock.unlock();  
    }  
    ...  
}
```

*If queue is full, patiently await further instructions ...*

# Enq Method Part One

```
public void enq(T x) {  
    boolean mustWakeDequeueurs = false;  
    enqLock.lock();  
    try {  
        while (size.get() == capacity)  
            notFullCondition.await();  
        Node e = new Node(x);  
        tail.next = e;  
        tail = tail.next;  
        if (size.getAndIncrement() == 0)  
            mustWakeDequeueurs = true;  
    } finally {  
        enqLock.unlock();  
    }  
    ...  
}
```

*Add new node*

# Enq Method Part One

```
public void enq(T x) {  
    boolean mustWakeDequeuers = false;  
    enqLock.lock();  
    try {  
        while (size.get() == capacity)  
            notFullCondition.await();  
        Node e = new Node(x);  
        tail.next = e;  
        tail = tail.next;  
        if (size.getAndIncrement() == 0)  
            mustWakeDequeuers = true;  
    } finally {  
        enqLock.unlock();  
    }  
    ...  
}
```

*If queue was empty, allows dequeuers to be woken*

# Enq Method Part Deux

```
public void enq(T x) {  
    ...  
    if (mustWakeDequeuers)  
notEmptyCondition.signalAll();  
}  
}
```

# Enq Method Part Deux

```
public void enq(T x) {  
    ...  
    if (mustWakeDequeuers) {  
        notEmptyCondition.signalAll();  
    }  
}
```

*Are there dequeuers to be signaled?*



# Enq Method Part Deux

```
public void enq(T x) {  
    ...  
    if (mustWakeDequeuers) {  
        notEmptyCondition.signalAll();  
    }  
}
```

*Signal dequeuers that queue no  
longer empty*

# Deq Method Part One

```
public T deq() {  
    T result;  
    boolean mustWakeEnqueuers = false;  
    deqLock.lock();  
    try {  
        while (size.get() == 0)  
            notEmptyCondition.await();  
        result = head.next.value;  
        head = head.next;  
        if (size.getAndDecrement() == capacity)  
            mustWakeEnqueuers = true;  
    } finally {  
        deqLock.unlock();  
    }  
    ...  
}
```

# Deq Method Part Deux

```
public T deq() {  
    ...  
    if (mustWakeEnqueuers) {  
        notFullCondition.signalAll();  
    }  
    return result;  
}
```



# The Enq() & Deq() Methods

- Share no locks
  - That's good
- But do share an atomic counter
  - Accessed on every method call
  - That's not so good
- Can we alleviate this bottleneck?



# Split the Counter into two counters

- enqSideSize
  - Decremented by deq()
- deqSideSize
  - Incremented by enq()



# Two counters

- The `enq()` method:

- ☐ Checks `enqSideSize` and proceeds as long as less than capacity
- ☐ Cares only if value is capacity

- The `deq()` method:

- ☐ Checks `deqSideSize` and proceeds as long as greater than zero
- ☐ Cares only if value is zero



# Unbounded Queues

- Queue can hold unbounded number of items:
  - `enq()` always enqueues its item
  - `deq()` throws an `EmptyException` if there is no item to dequeue
- Same representation as bounded queue, only no need to count number of items

# Unbounded queue enq()

```
public void enq(T x) {  
    enqLock.lock();  
    try {  
        Node e = new Node(x);  
        tail.next = e;  
        tail = tail.next;  
    } finally {  
        enqLock.unlock();  
    }  
}
```



# Unbounded queue deq()

```
public T deq() throws EmptyException {
    T result;
    deqLock.lock();
    try {
        if (head.next == null)
            throw new EmptyException();
        result = head.next.value;
        head = head.next;
    } finally {
        deqLock.unlock();
    }
    return result;
}
```

*Only need to check that queue  
is not empty*



# Now an unbounded lock-free queue

- Natural extension of the unbounded queue
- However it prevents method calls from starving by having quicker threads help slower threads



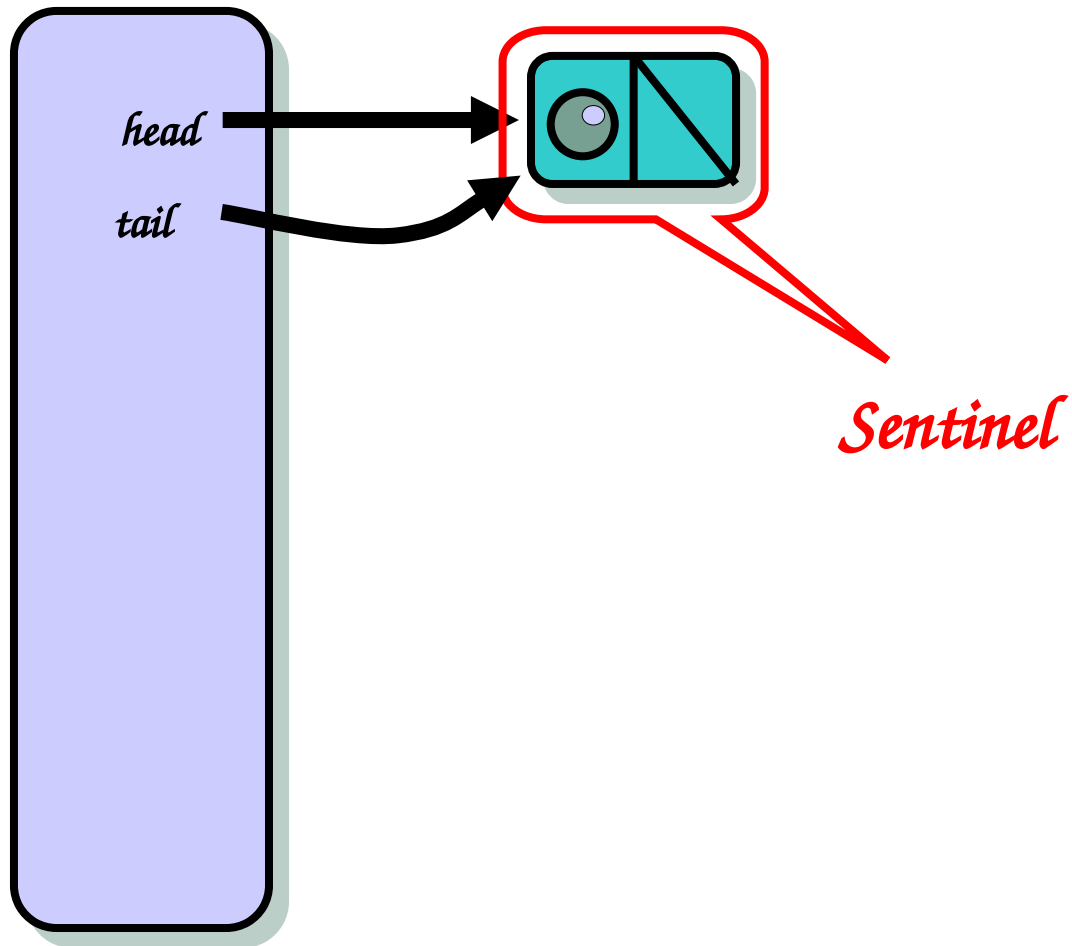
# Unbounded Lock-free Queue

- Again represented as a Linked List
- However each node's next field is now an AtomicReference (to facilitate lock-free operations)

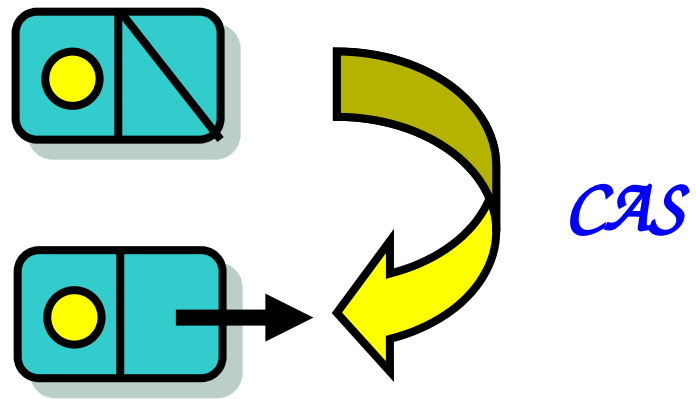
# Lock-free queue Node class

```
public class Node {  
    public T value;  
    public AtomicReference<Node> next;  
  
    public Node(T value) {  
        value = value;  
        next = new AtomicReference<Node>(null);  
    }  
}
```

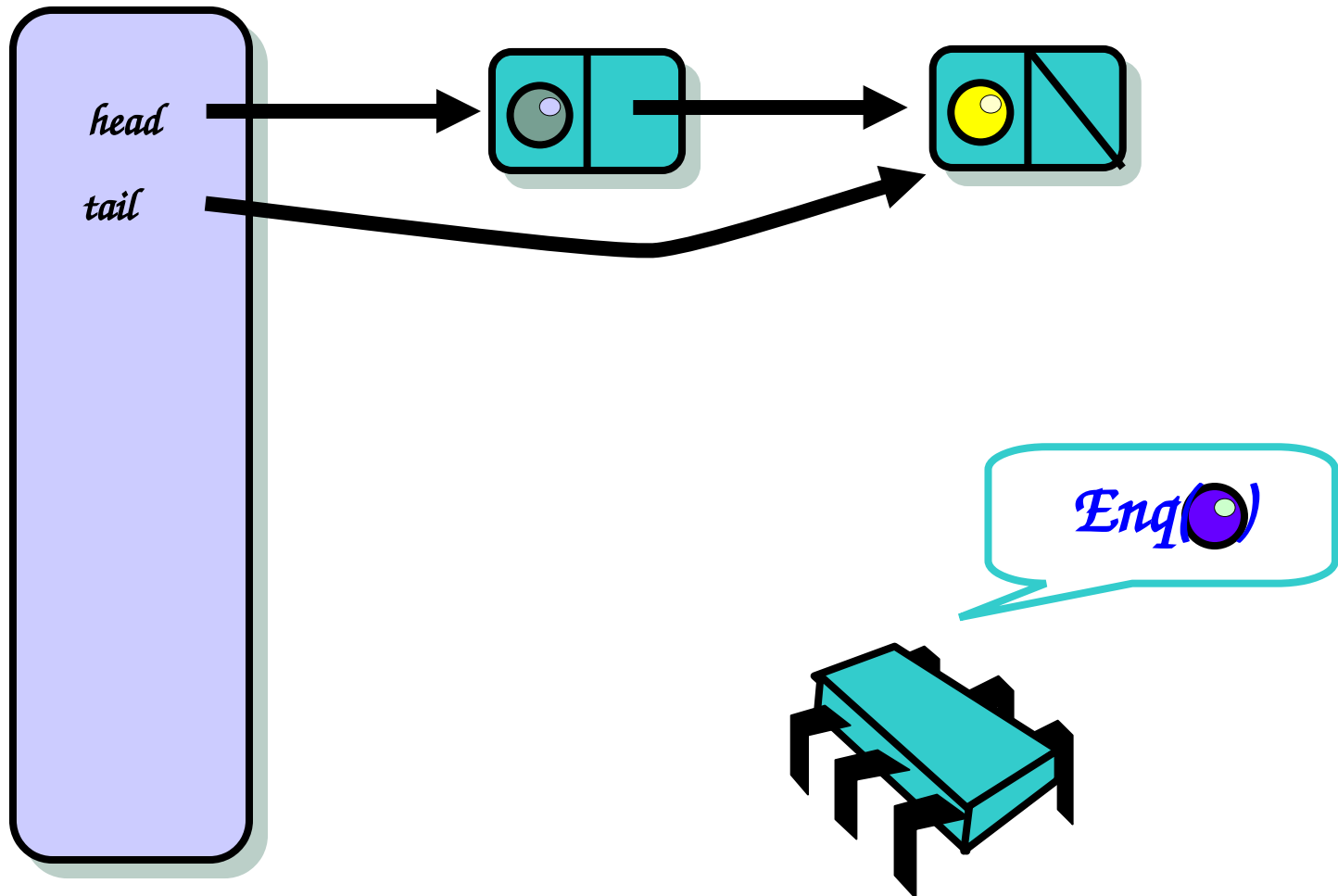
# A Lock-Free Queue



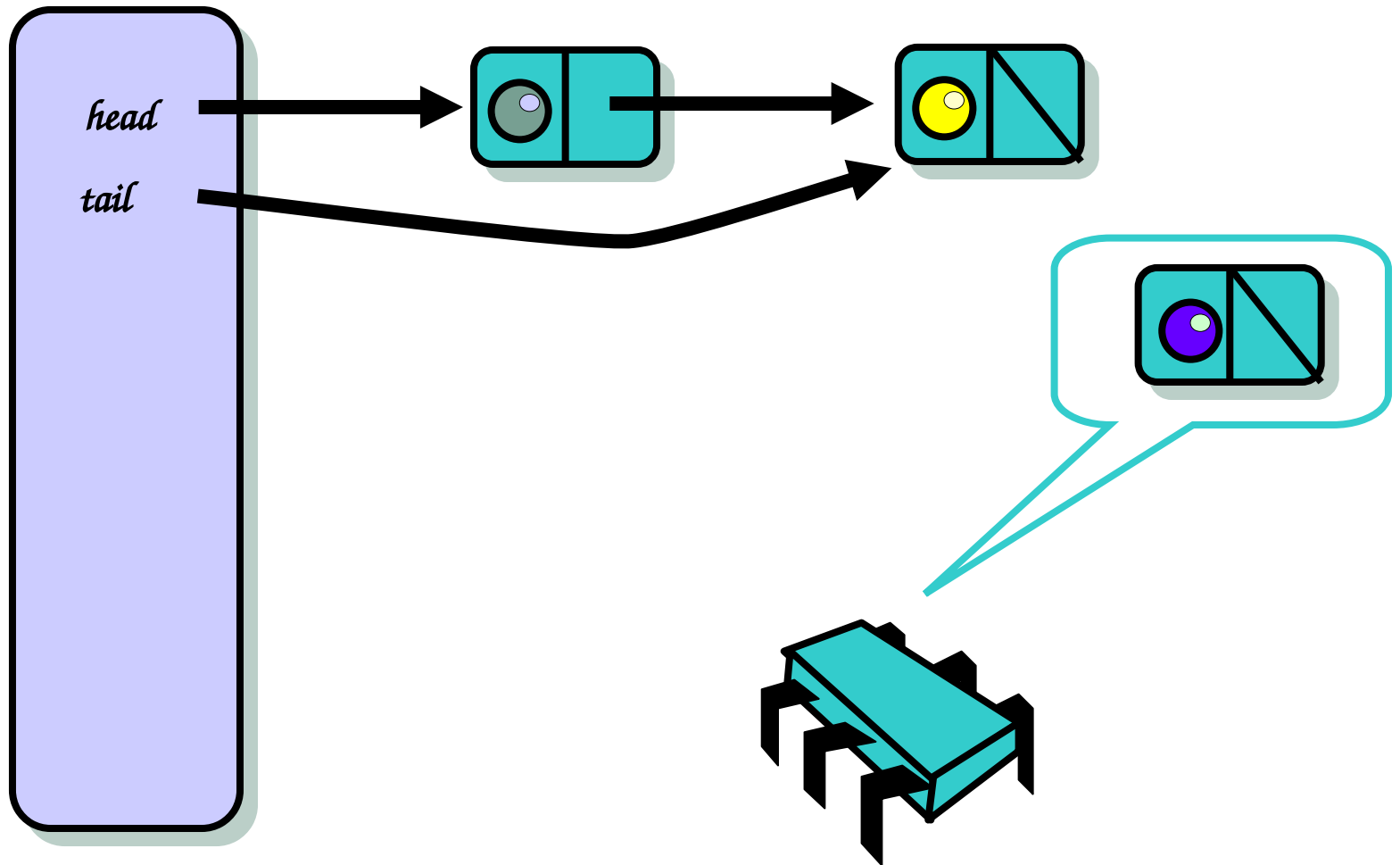
# Compare and Set



# Enqueue

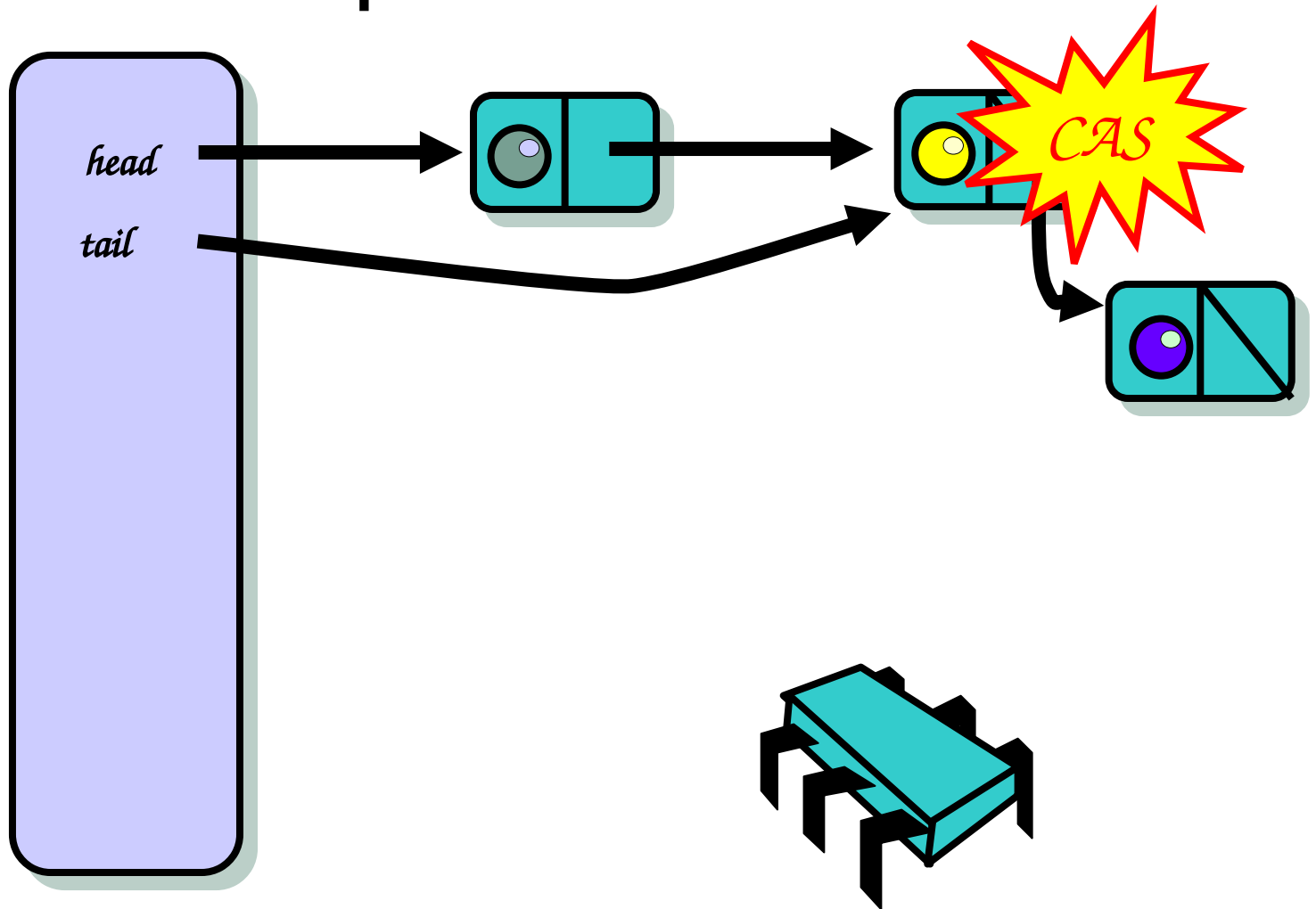


# Enqueue

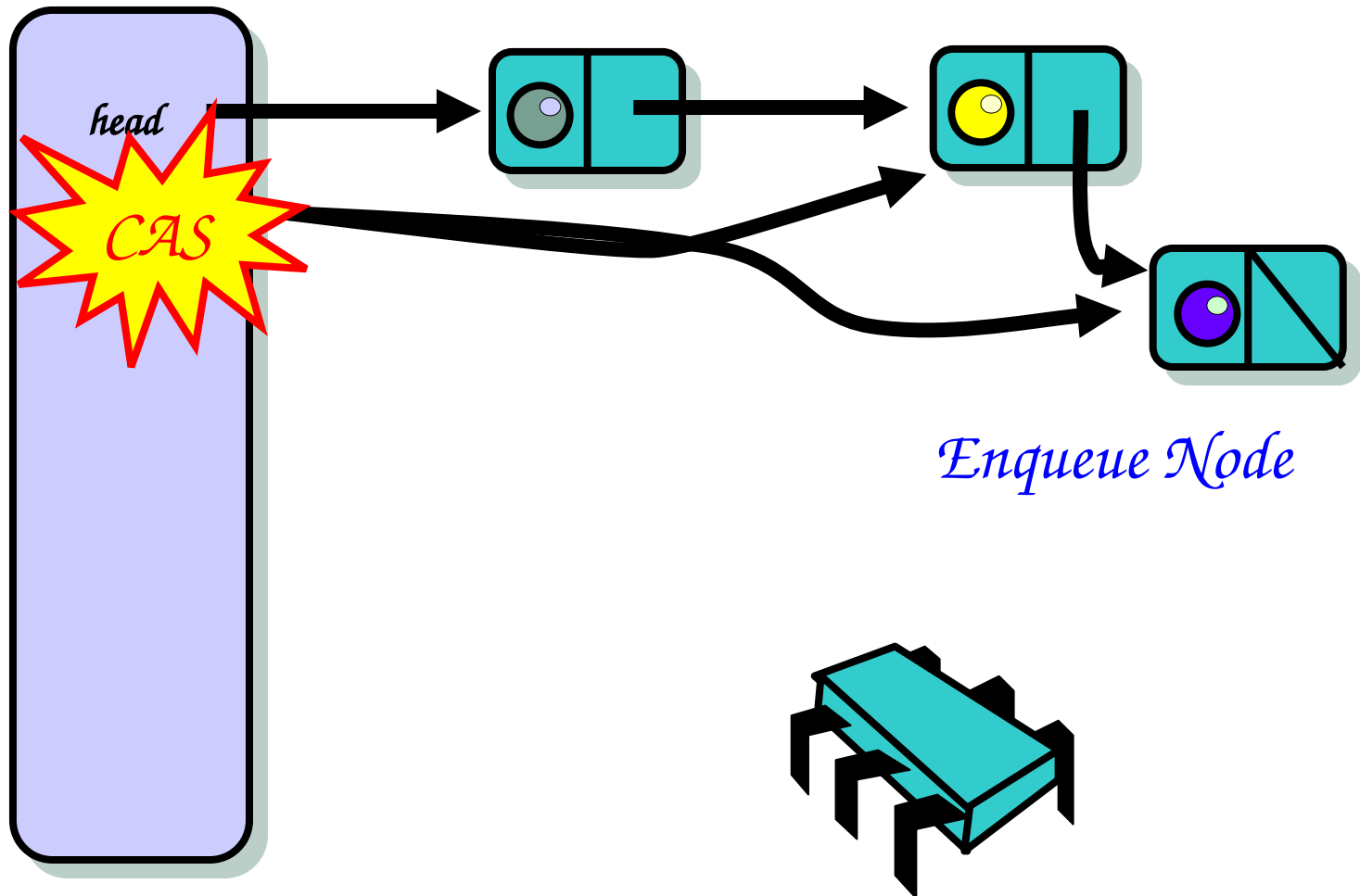




# Logical Enqueue



# Physical Enqueue





# Enqueue

- The enq() method is lazy
- Enqueue consists of two steps:
  - Logical enqueue – appends the node to the linked list
  - Physical enqueue – changes the tail field to point to the new node
- These two steps are not atomic



# Enqueue

- It is thus possible that a new item is reachable by other threads before it actually becomes the tail
- The tail field can thus refer to either
  - The actual last node or
  - The penultimate node



# Enqueue

- When enqueueing you have to make sure that you are adding an item to the actual end of the queue
- So check whether the tail you are working with has a successor



# Enqueue

- What do you do if you find
  - Tail pointing to the wrong value?
- Stop and help fix it
  - If **tail** node has non-*null* next field
  - CAS the queue's **tail** field to **tail.next**

# Lock-free enqueue method

```
public void enq(T value) {
    Node node = new Node(value);
    while (true) {
        Node last = tail.get();
        Node next = tail.next.get();
        if (last == tail.get()) {
            if (next == null) {
                if (last.next.compareAndSet(next, node)) {
                    tail.compareAndSet(last, node);
                    return;
                } else
                    tail.compareAndSet(last, last.next);
            }
        }
    }
}
```

# Lock-free enqueue method

```
public void enq(T value) {  
    Node node = new Node(value);  
    while (true) {  
        Node last = tail.get();  
        Node next = tail.next.get();  
        if (last == tail.get()) {  
            if (next == null) {  
                if (last.next.compareAndSet(next, node)) {  
                    tail.compareAndSet(last, node);  
                    return;  
                } else  
                    tail.compareAndSet(last, last.next);  
            }  
        }  
    }  
}
```

*What does tail point to*



# Lock-free enqueue method

```
public void enq(T value) {  
    Node node = new Node(value);  
    while (true) {  
        Node last = tail.get();  
        Node next = tail.next.get();  
        if (last == tail.get()) {  
            if (next == null) {  
                if (last.next.compareAndSet(next, node)) {  
                    tail.compareAndSet(last, node);  
                    return;  
                } else  
                    tail.compareAndSet(last, last.next);  
            }  
        }  
    }  
}
```

*What does tail's next point to*

# Lock-free enqueue method

```
public void enq(T value) {  
    Node node = new Node(value);  
    while (true) {  
        Node last = tail.get();  
        Node next = tail.next.get();  
        if (last == tail.get()) {  
            if (next == null) {  
                if (last.next.compareAndSet(next, node)) {  
                    tail.compareAndSet(last, node);  
                    return;  
                } else  
                    tail.compareAndSet(last, last.next);  
            }  
        }  
    }  
}
```

*If the value pointed to  
by tail has not  
changed...*

# Lock-free enqueue method

```
public void enq(T value) {  
    Node node = new Node(value);  
    while (true) {  
        Node last = tail.get();  
        Node next = tail.next.get();  
        if (last == tail.get()) {  
            if (next == null) {  
                if (last.next.compareAndSet(next, node)) {  
                    tail.compareAndSet(last, node);  
                    return;  
                } else  
                    tail.compareAndSet(last, last.next);  
            }  
        }  
    }  
}
```

*...and tail's next points to null...*

# Lock-free enqueue method

```
public void enq(T value) {  
    Node node = new Node(value);  
    while (true) {  
        Node last = tail.get();  
        Node next = tail.next.get();  
        if (last == tail.get()) {  
            if (next == null) {  
                if (last.next.compareAndSet(next, node)) {  
                    tail.compareAndSet(last, node);  
                    return;  
                } else  
                    tail.compareAndSet(last, last.next);  
            }  
        }  
    }  
}
```

*Logical enqueue*

# Lock-free enqueue method

```
public void enq(T value) {  
    Node node = new Node(value);  
    while (true) {  
        Node last = tail.get();  
        Node next = tail.next.get();  
        if (last == tail.get()) {  
            if (next == null) {  
                if (last.next.compareAndSet(next, node)) {  
                    tail.compareAndSet(last, node);  
                    return;  
                } else  
                    tail.compareAndSet(last, last.next);  
            }  
        }  
    }  
}
```

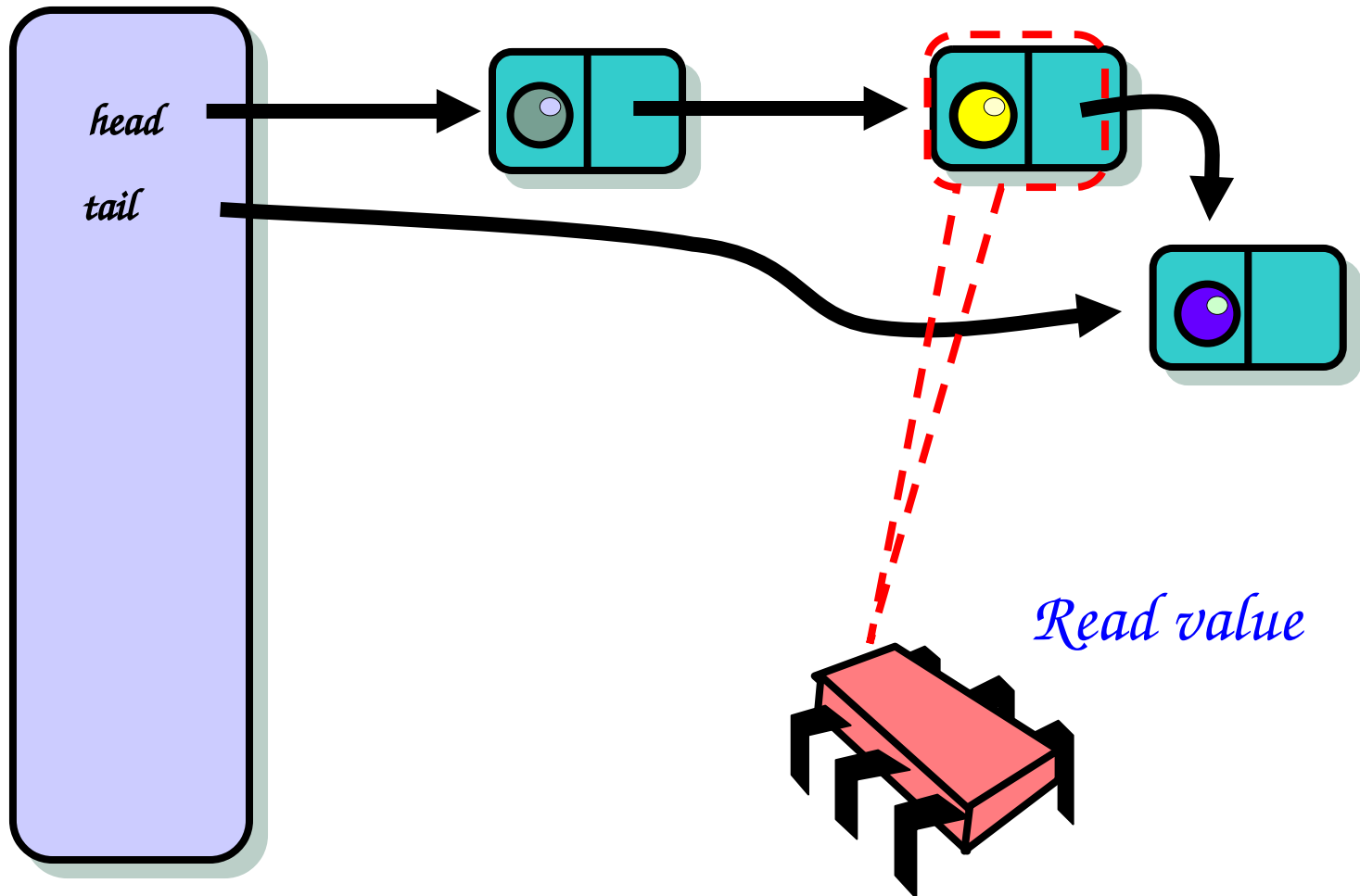
*Physical enqueue*

# Lock-free enqueue method

```
public void enq(T value) {  
    Node node = new Node(value);  
    while (true) {  
        Node last = tail.get();  
        Node next = tail.next.get();  
        if (last == tail.get()) {  
            if (next == null) {  
                if (last.next.compareAndSet(next, node)) {  
                    tail.compareAndSet(last, node);  
                    return;  
                } else  
                    tail.compareAndSet(last, last.next);  
            }  
        }  
    }  
}
```

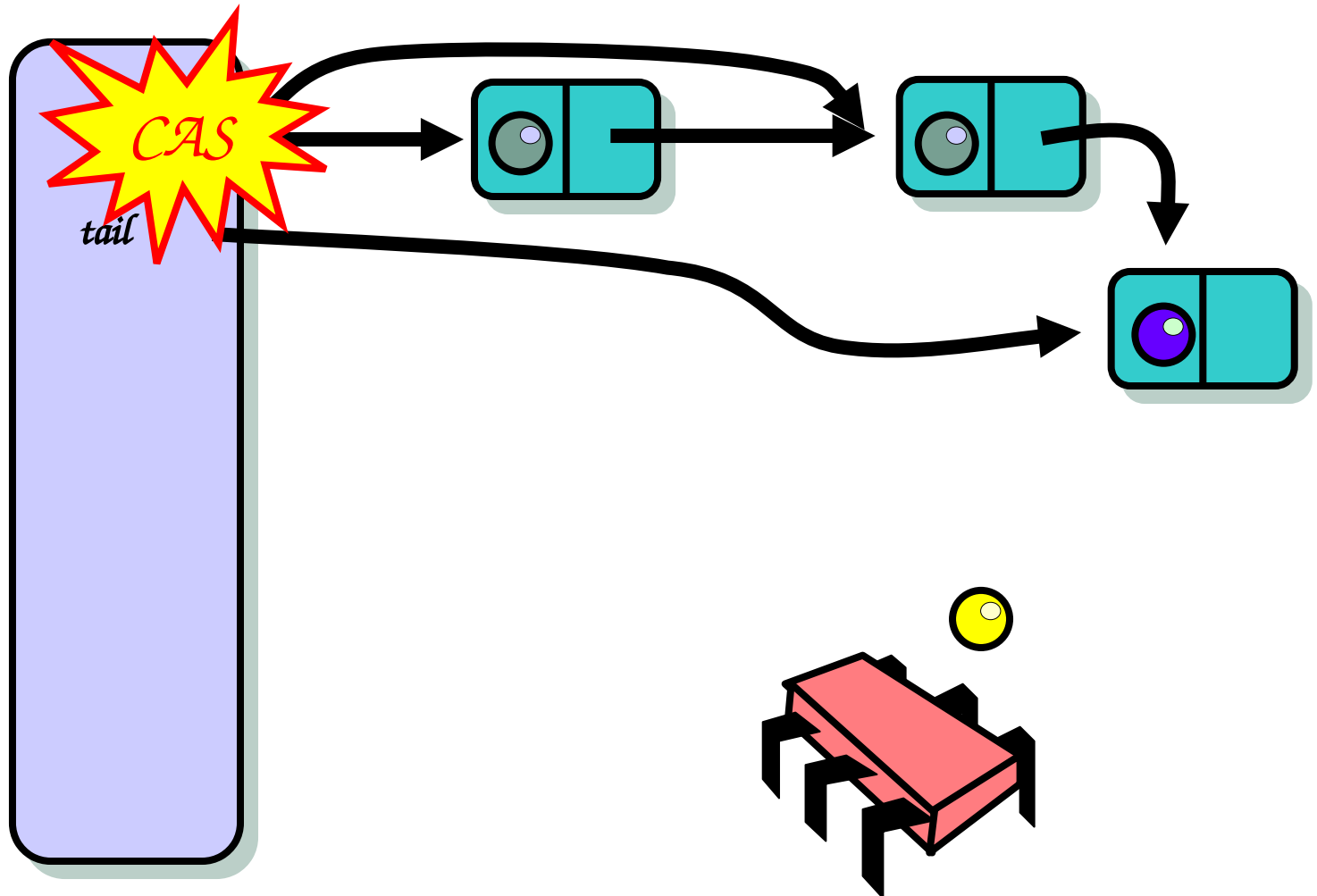
*If tail has a successor it 'helps' other nodes by advancing tail to refer to the successor*

# Dequeuer



# Dequeuer

*Make first Node new  
sentinel*







# Dequeuer

- Although queue is unbounded, you always have to check that queue is not empty
- Without counter, queue is empty when  $\text{head} = \text{tail} = \text{sentinel}$

# Lock-free dequeue method

```
public T deq() throws EmptyException {
    while (true) {
        Node first = head.get();
        Node last = tail.get();
        Node next = first.next.get();
        if (first == head.get()) {
            if (first == last) {
                if (next == null) {
                    throw new EmptyException();
                }
                tail.compareAndSet(last, next);
            } else {
                T value = next.value;
                if (head.compareAndSet(first, next))
                    return value;
            }
        }
    }
}
```

# Lock-free dequeue method

```
public T deq() throws EmptyException {  
    while (true) {  
        Node first = head.get();  
        Node last = tail.get();  
        Node next = first.next.get();  
        if (first == head.get()) {  
            if (first == last) {  
                if (next == null) {  
                    throw new EmptyException();  
                }  
                tail.compareAndSet(last, next);  
            } else {  
                T value = next.value;  
                if (head.compareAndSet(first, next))  
                    return value;  
            }  
        }  
    }  
}
```

*What does head point to*

}}}

# Lock-free dequeue method

```
public T deq() throws EmptyException {  
    while (true) {  
        Node first = head.get();  
        Node last = tail.get();  
        Node next = first.next.get();  
        if (first == head.get()) {  
            if (first == last) {  
                if (next == null) {  
                    throw new EmptyException();  
                }  
                tail.compareAndSet(last, next);  
            } else {  
                T value = next.value;  
                if (head.compareAndSet(first, next))  
                    return value;  
            }  
        }  
    }  
}
```

*What does tail point to*

}}}

# Lock-free dequeue method

```
public T deq() throws EmptyException {
    while (true) {
        Node first = head.get();
        Node last = tail.get();
        Node next = first.next.get();
        if (first == head.get()) {
            if (first == last) {
                if (next == null) {
                    throw new EmptyException();
                }
                tail.compareAndSet(last, next);
            } else {
                T value = next.value;
                if (head.compareAndSet(first, next))
                    return value;
            }
        }
    }
}
```

*Is there a node after head?*

# Lock-free dequeue method

```
public T deq() throws EmptyException {
    while (true) {
        Node first = head.get();
        Node last = tail.get();
        Node next = first.next.get();
        if (first == head.get()) {
            if (first == last) {
                if (next == null) {
                    throw new EmptyException();
                }
                tail.compareAndSet(last, next);
            } else {
                T value = next.value;
                if (head.compareAndSet(first, next))
                    return value;
            }
        }
    }
}
```

*Has the value of head changed?*

# Lock-free dequeue method

```
public T deq() throws EmptyException {  
    while (true) {  
        Node first = head.get();  
        Node last = tail.get();  
        Node next = first.next.get();  
        if (first == head.get()) {  
            if (first == last) {  
                if (next == null) {  
                    throw new EmptyException();  
                }  
                tail.compareAndSet(last, next);  
            } else {  
                T value = next.value;  
                if (head.compareAndSet(first, next))  
                    return value;  
            }  
        }  
    }  
}
```

*Is the queue empty?*

# Lock-free dequeue method

```
public T deq() throws EmptyException {  
    while (true) {  
        Node first = head.get();  
        Node last = tail.get();  
        Node next = first.next.get();  
        if (first == head.get()) {  
            if (first == last) {  
                if (next == null) {  
                    throw new EmptyException();  
                }  
                tail.compareAndSet(last, next);  
            } else {  
                T value = next.value;  
                if (head.compareAndSet(first, next))  
                    return value;  
            }  
        }  
    }  
}
```

*Is the queue still empty?*



# Lock-free dequeue method

```
public T deq() throws EmptyException {  
    while (true) {  
        Node first = head.get();  
        Node last = tail.get();  
        Node next = first.next.get();  
        if (first == head.get()) {  
            if (first == last) {  
                if (next == null) {  
                    throw new EmptyException();  
                }  
                tail.compareAndSet(last, next);  
            } else {  
                T value = next.value;  
                if (head.compareAndSet(first, next))  
                    return value;  
            }  
        }  
    }  
}
```

*If a new value node  
have arrived, 'help'  
others by advancing tail*

# Lock-free dequeue method

```
public T deq() throws EmptyException {
    while (true) {
        Node first = head.get();
        Node last = tail.get();
        Node next = first.next.get();
        if (first == head.get()) {
            if (first == last) {
                if (next == null) {
                    throw new EmptyException();
                }
                tail.compareAndSet(last, next);
            } else {
                T value = next.value;
                if (head.compareAndSet(first, next))
                    return value;
            }
        }
    }
}
```

*If the queue is not empty*

# Lock-free dequeue method

```
public T deq() throws EmptyException {  
    while (true) {  
        Node first = head.get();  
        Node last = tail.get();  
        Node next = first.next.get();  
        if (first == head.get()) {  
            if (first == last) {  
                if (next == null) {  
                    throw new EmptyException();  
                }  
                tail.compareAndSet(last, next);  
            } else {  
                T value = next.value;  
                if (head.compareAndSet(first, next))  
                    return value;  
            }  
        }  
    }  
}
```

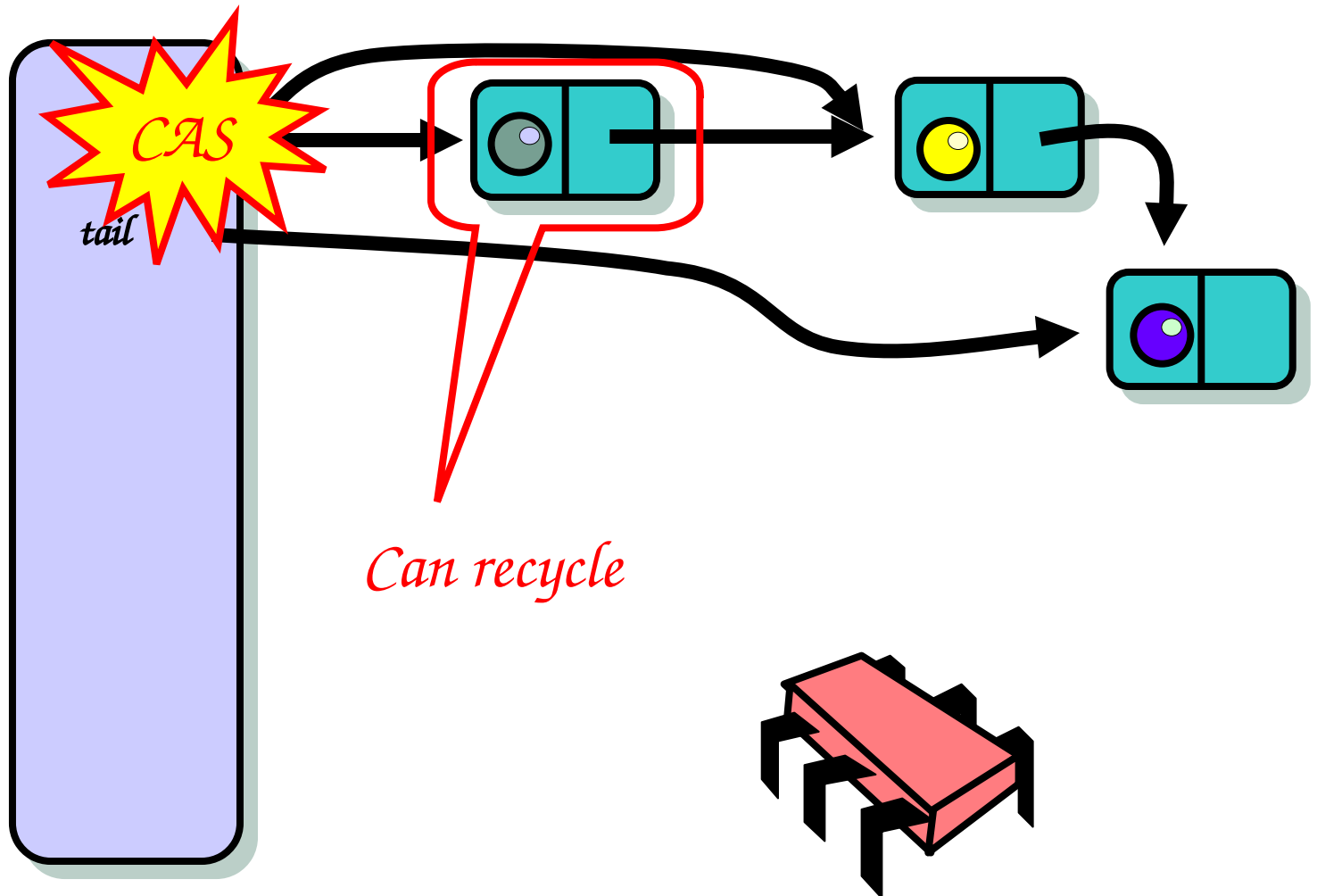
*Try to remove the first  
value from the queue*



# Memory reuse

- What do we do with nodes after we dequeue them?
- With current implementation nodes are unlinked from linked list, but we depend on built-in garbage collection to remove them from memory
- Suppose there is no garbage collector?

# Dequeuer

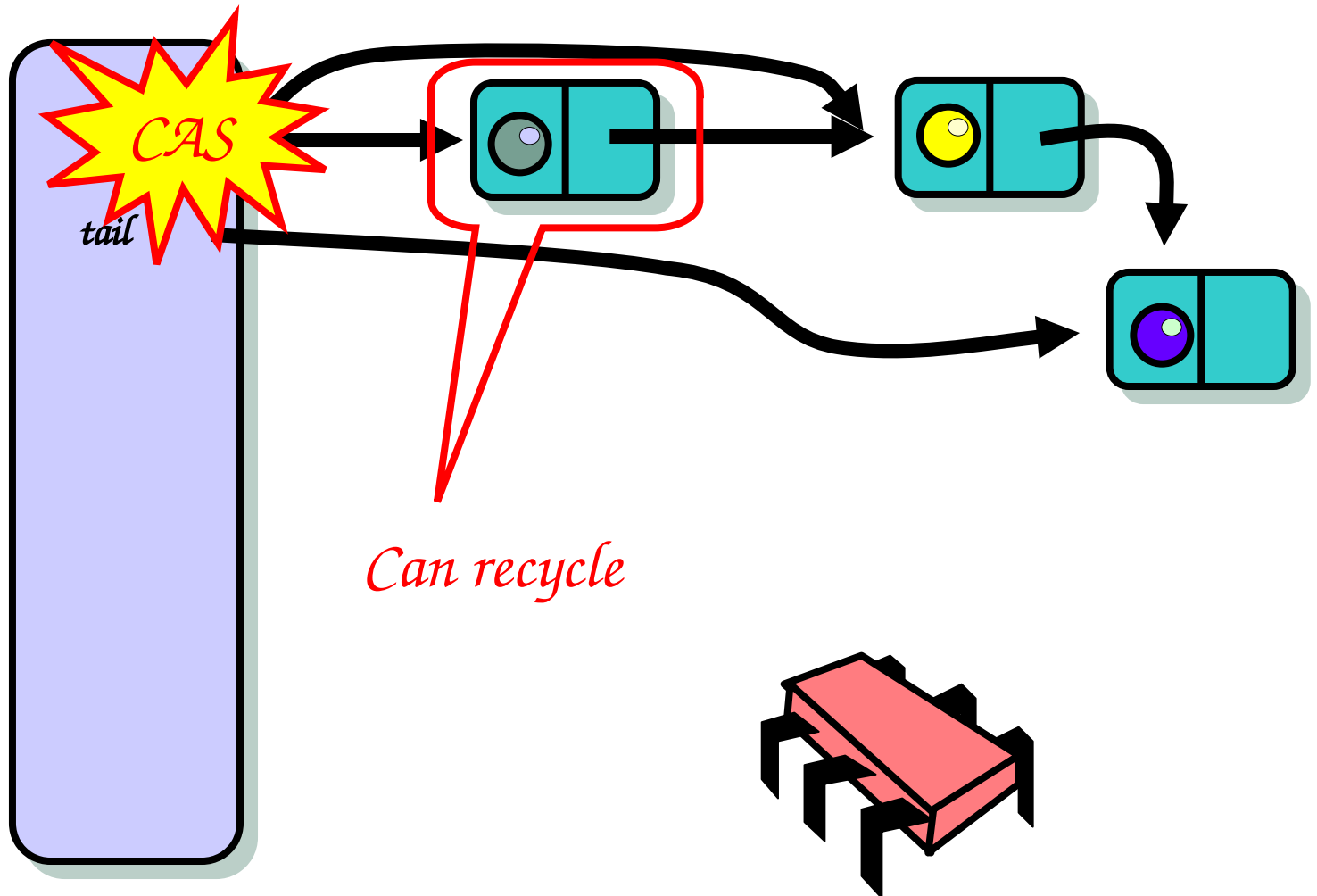




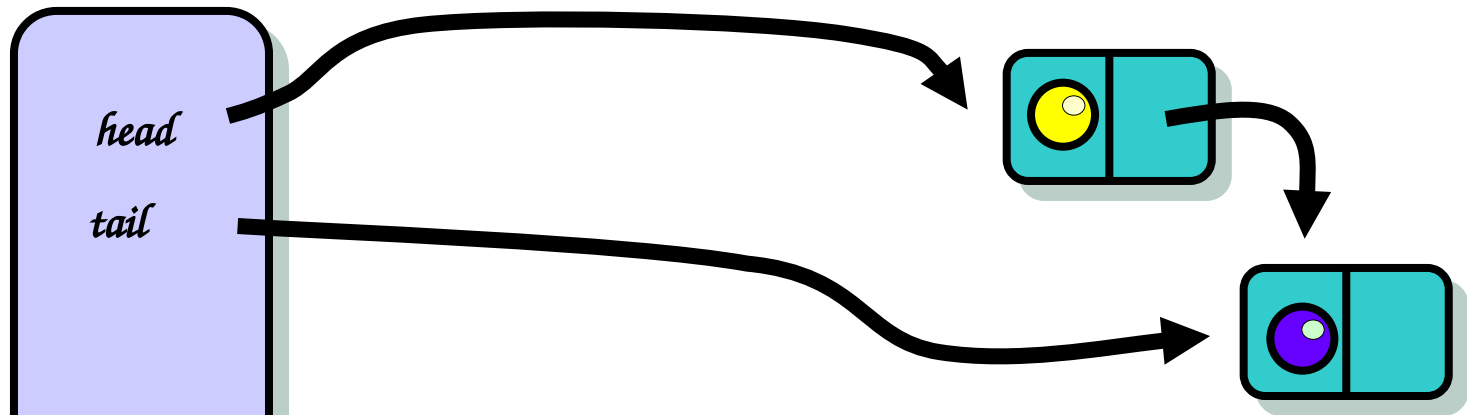
# Simple solution

- Each thread maintains its own private free-list of unused queue entries
  - When enqueue – get a node from the free-list
  - When dequeue – add removed node to free-list
- If free-list is empty, simply allocate new node through dynamic memory allocation

# Dequeuer



# Dequeuer



*Can recycle*



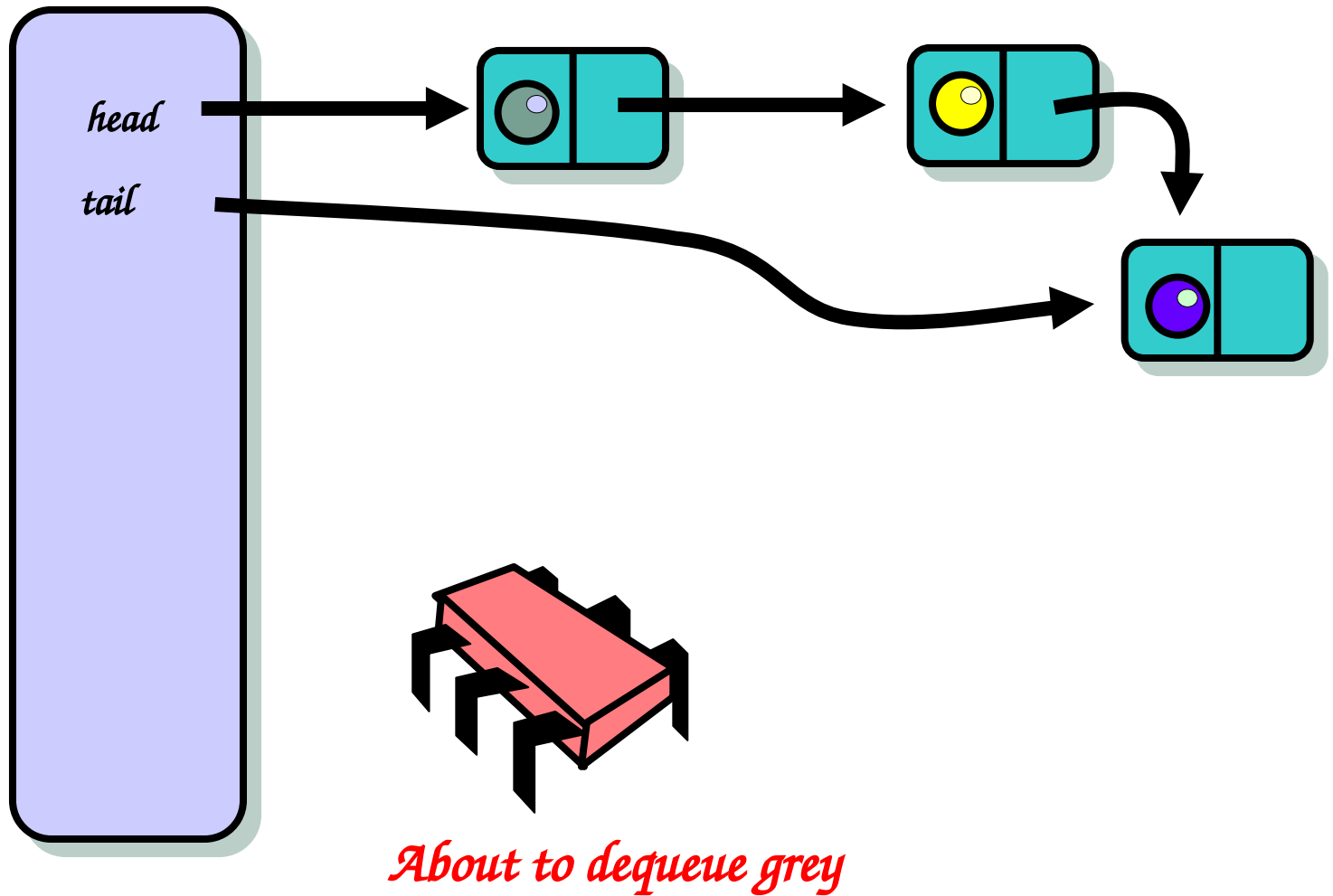




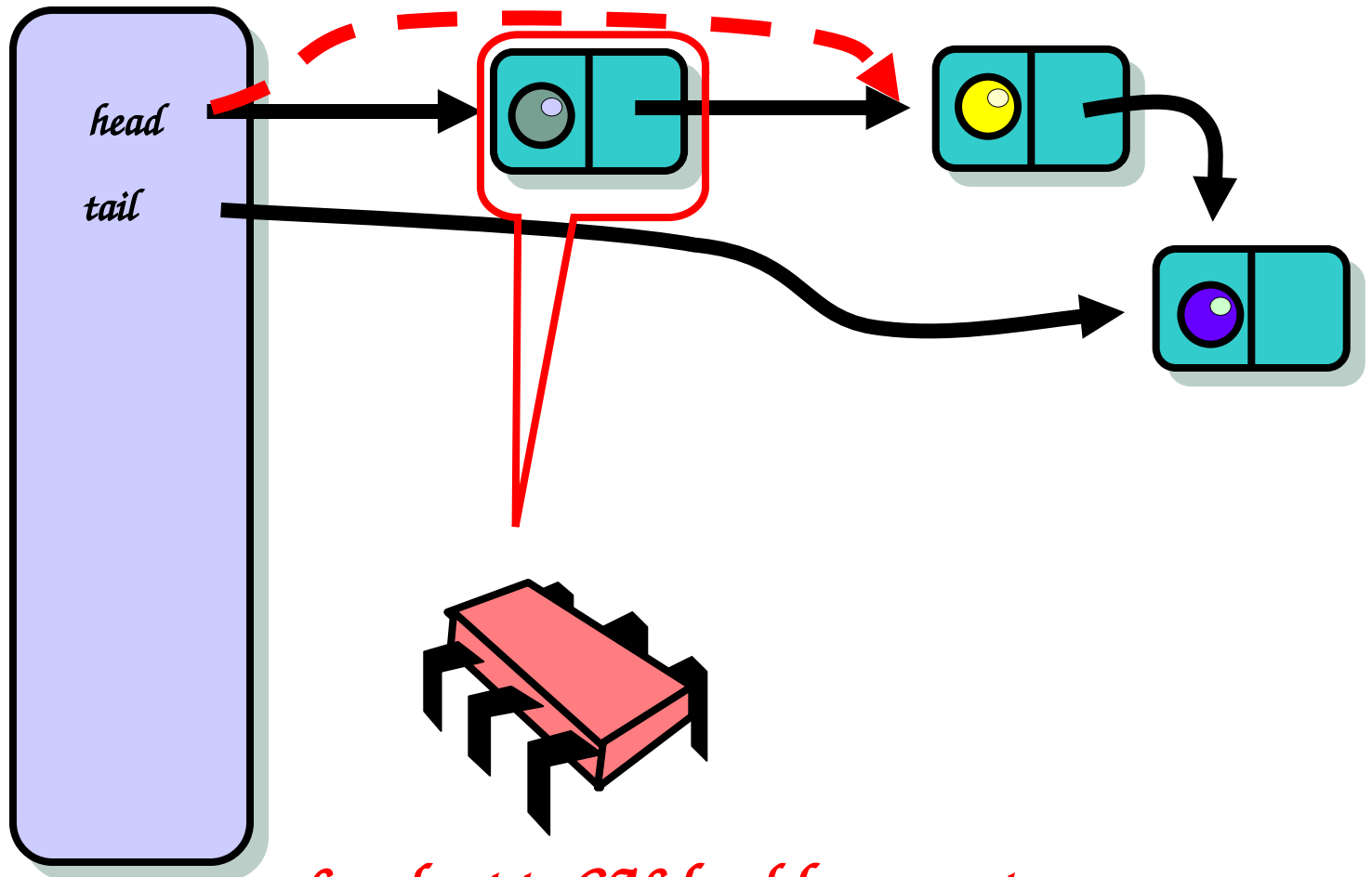
# Potential problem

- When nodes are recycled – removed from the queue and later added again
  - Dreaded ABA problem

# Dequeuer

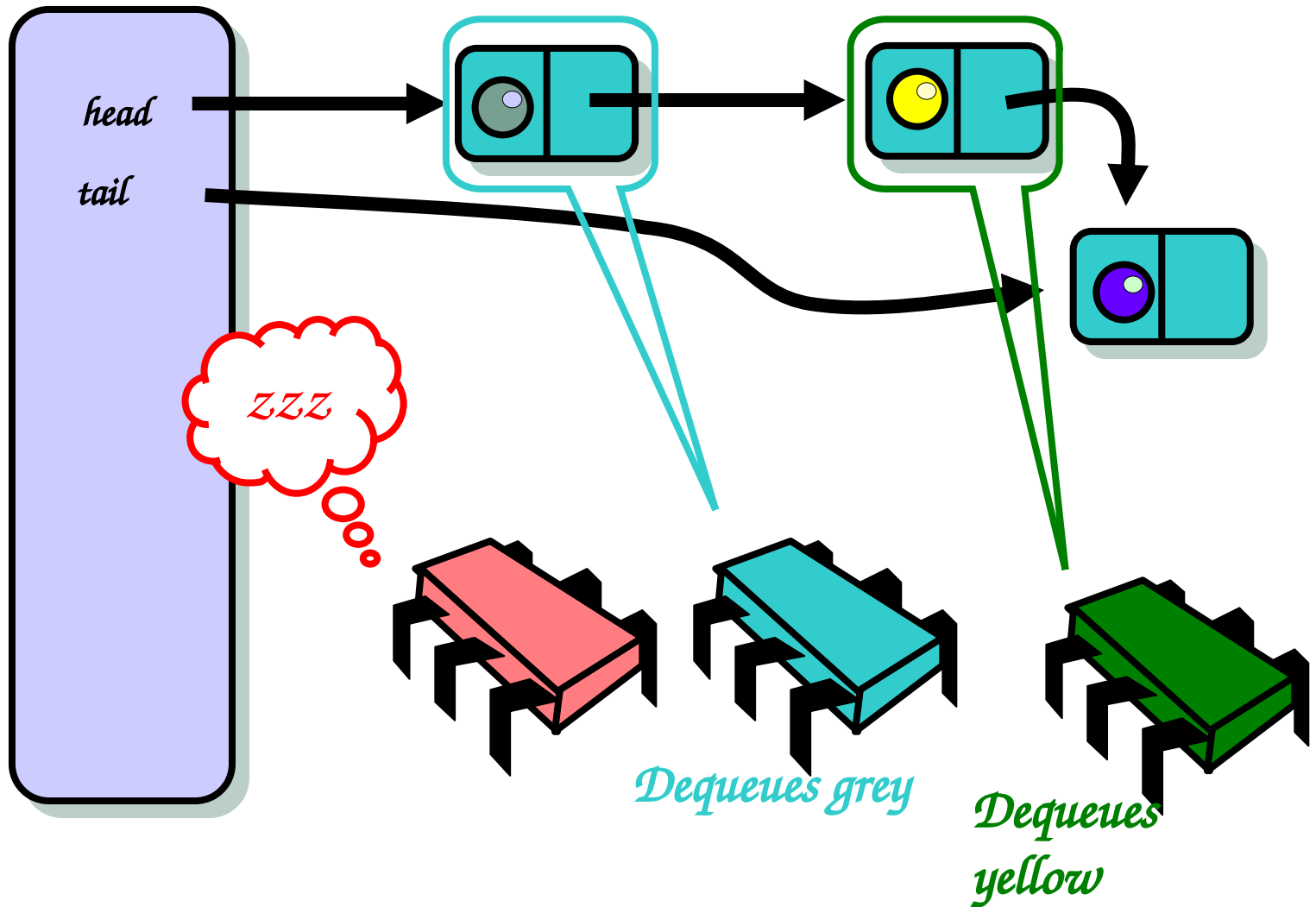


# Dequeuer

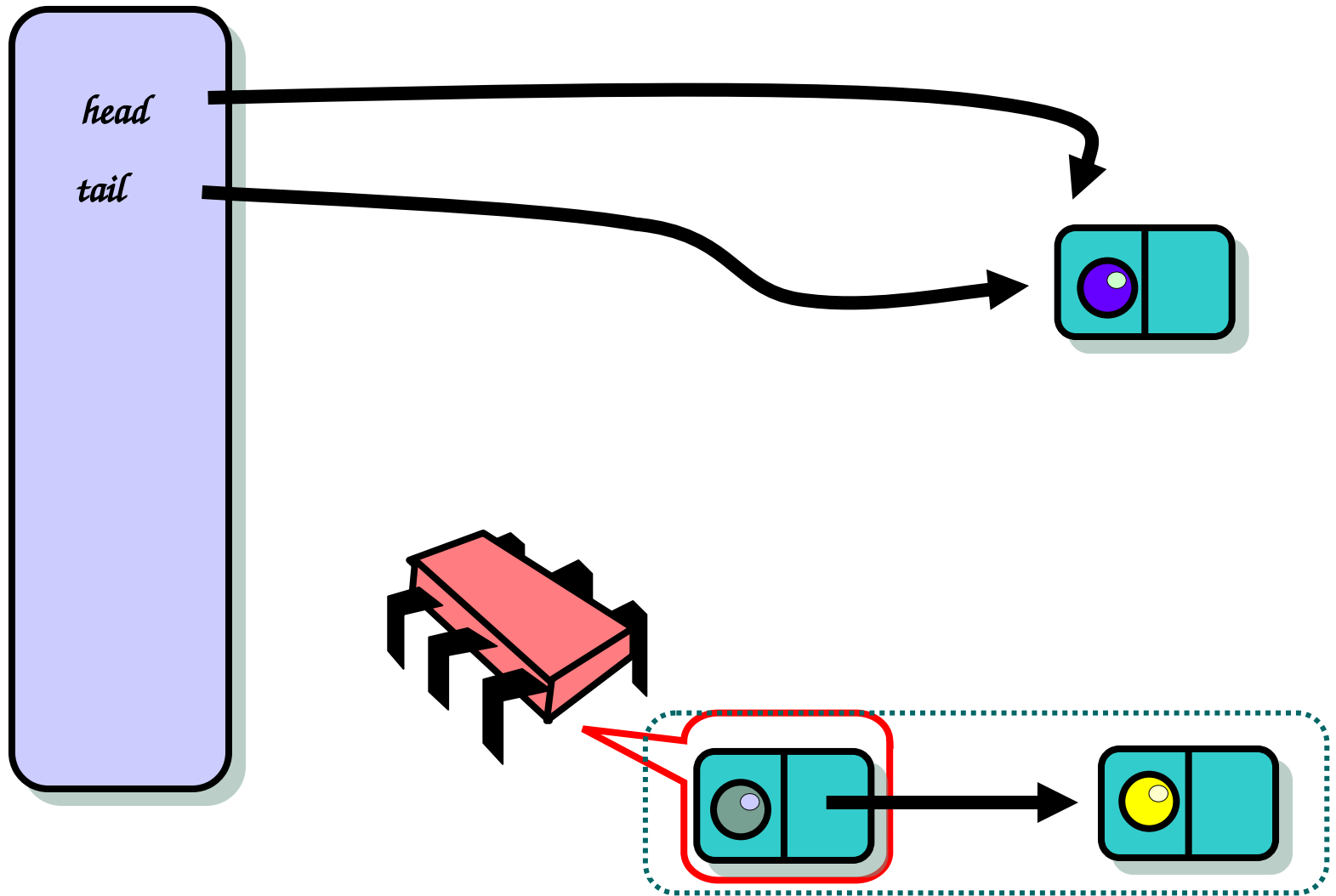


*So, about to CAS head from grey to yellow*

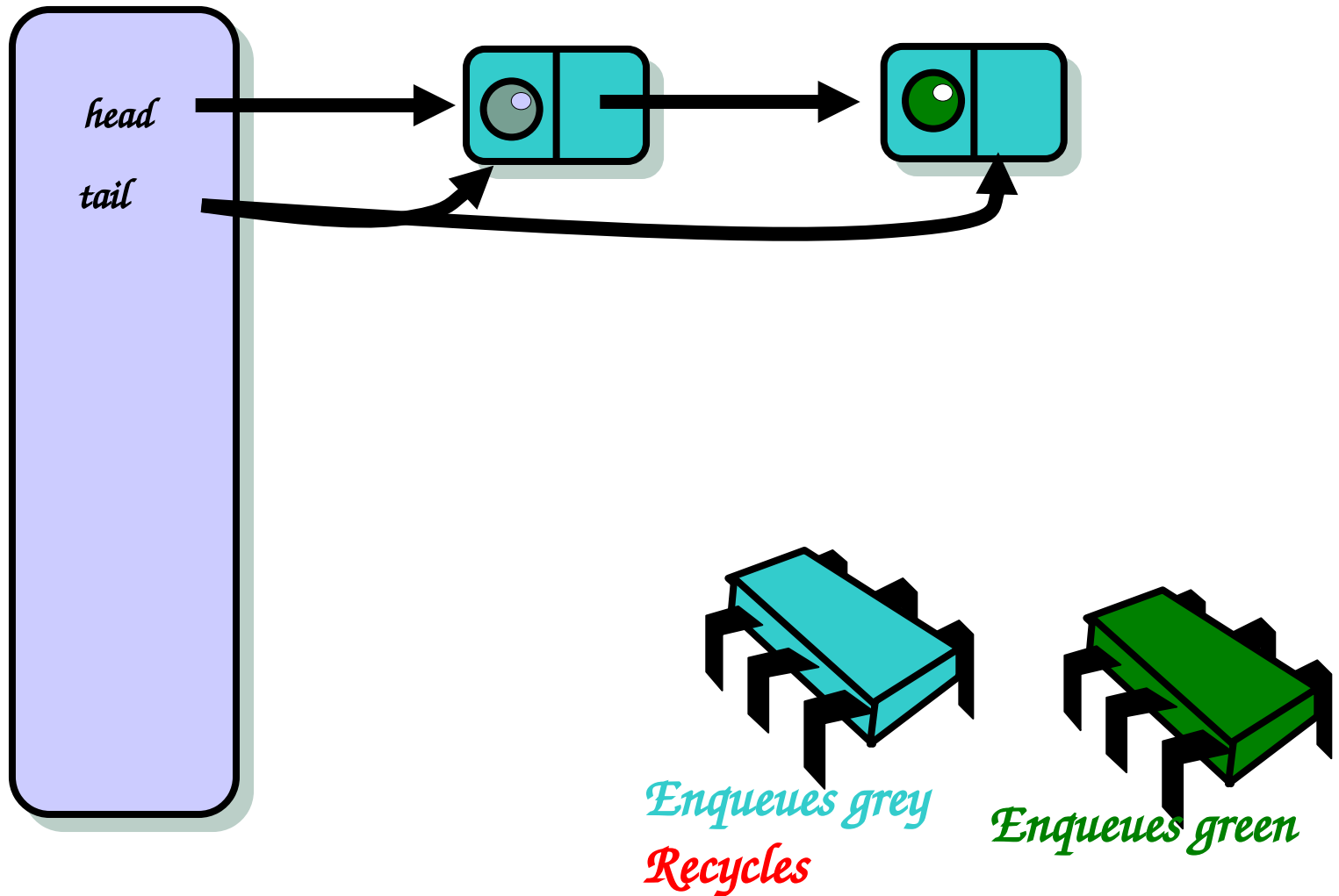
# Dequeuer

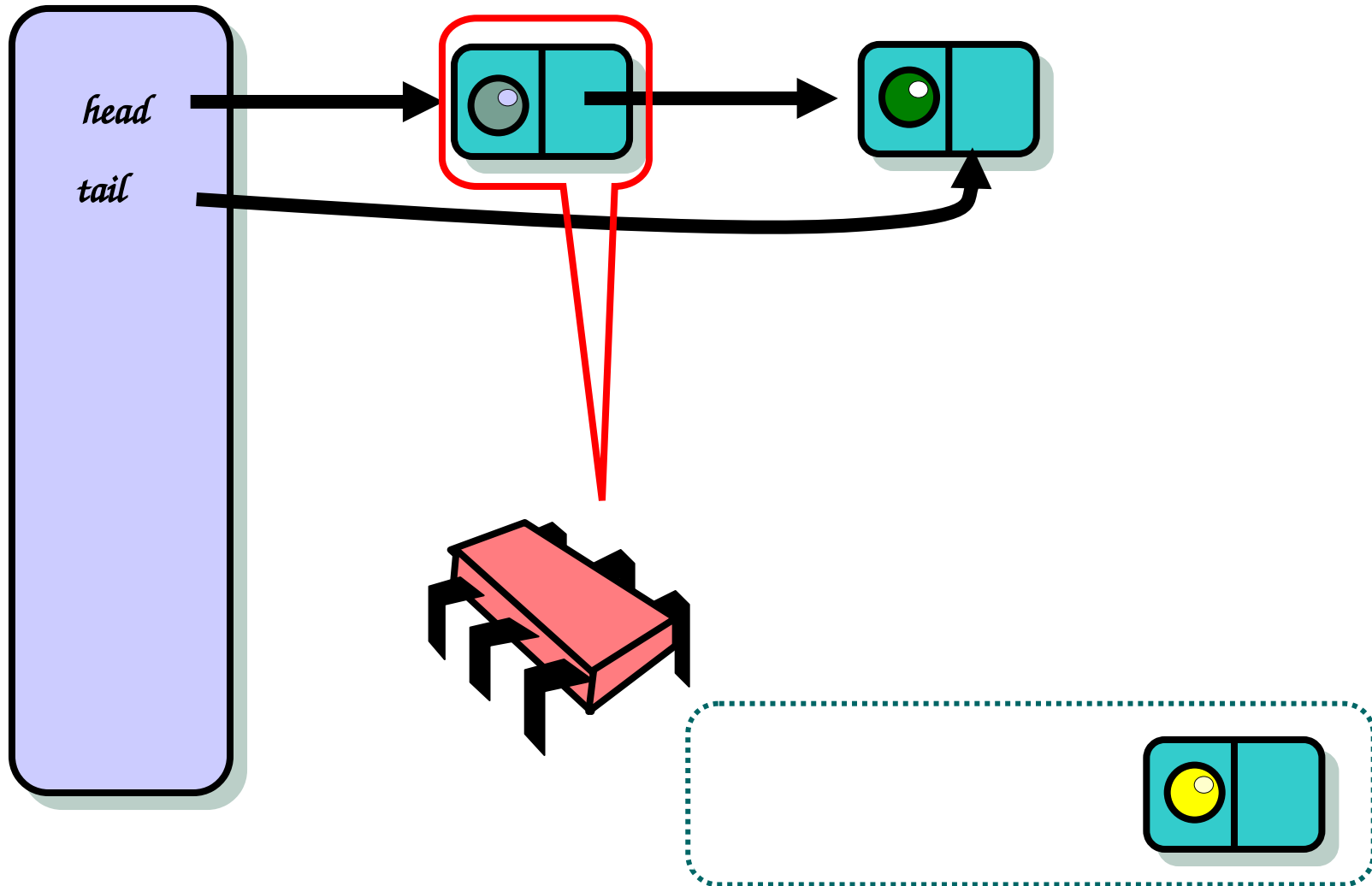


# Dequeuer

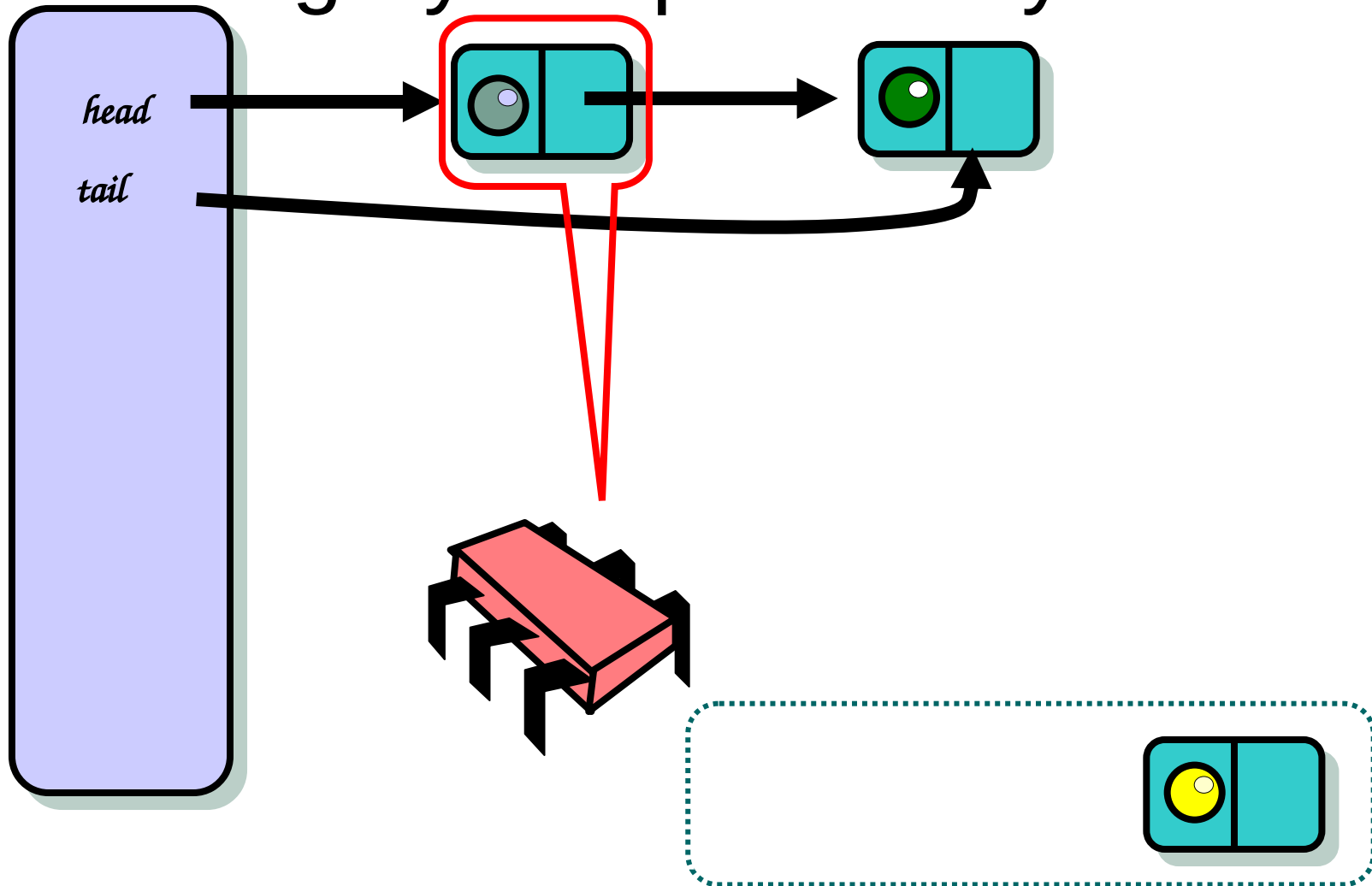


# Dequeuer



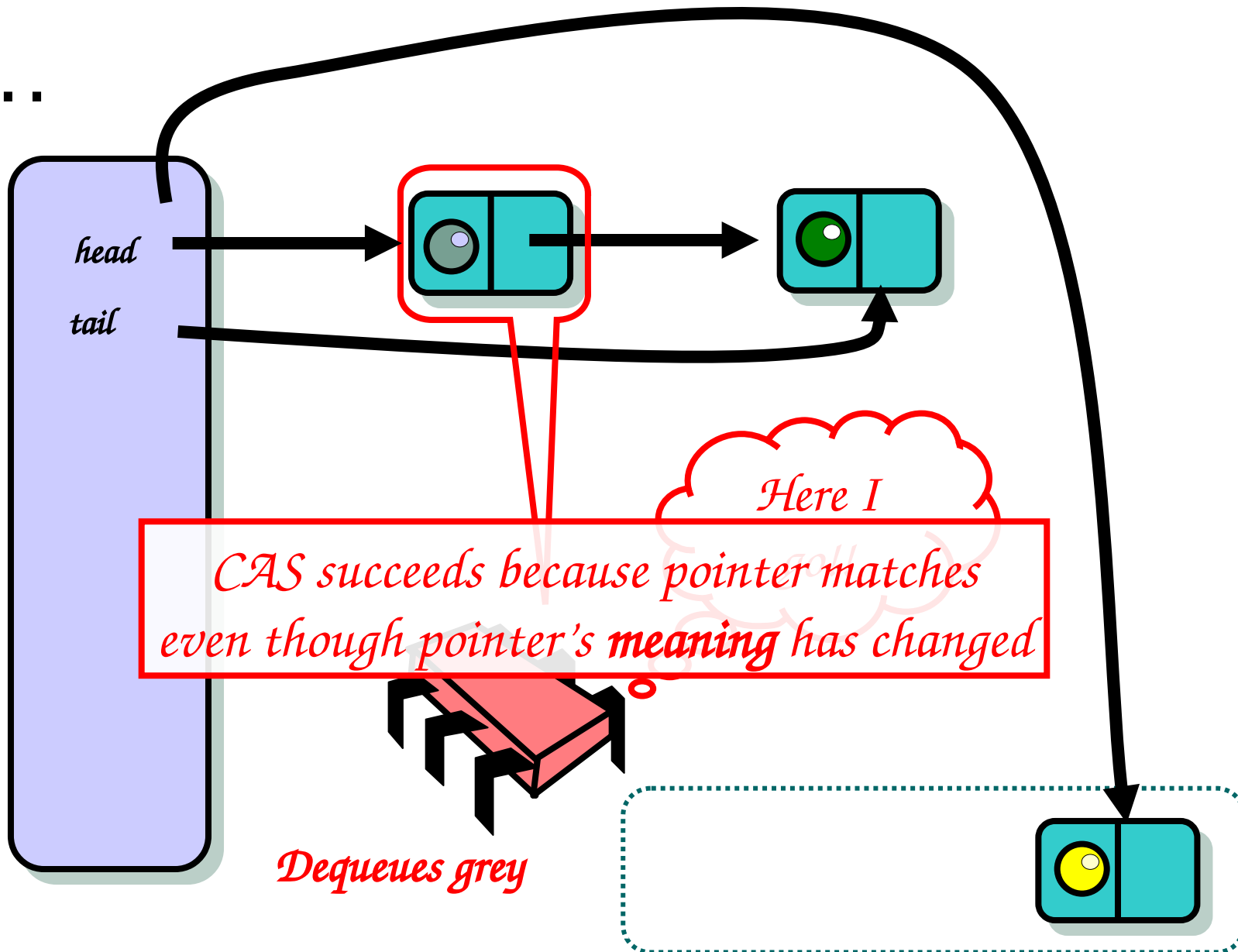


And according to its previous calculation grey still points to yellow





So...





# ABA problem

- Head ends up pointing to a node that is not in the queue anymore, but has been added to the free-list



# Dreaded ABA – A Solution

- Tag each pointer with a counter
- Unique over lifetime of node
- Pointer size vs word size issues
- Overflow?
  - ☐ Don't worry be happy?
  - ☐ Bounded tags?
- AtomicStampedReference class



# Dual Data Structures

- To reduce the synchronization overhead of the synchronous queue we split `enq()` and `deq()` into two steps



# deq() method

- If a dequeuer tries to remove an item from an empty queue:
  - It puts a reservation object in the queue to indicate that the deq() is waiting for an enq() to rendezvous with
  - deq() spins on flag in reservation



# enq() method

- When enq() sees reservation:
  - Fulfills the reservation by depositing an item
  - Notifies deq() by setting object's flag



# Dual Data Structure

- An enq() can also add its own reservation to the queue and spin on the flag waiting for a deq()
- At any time the queue contains either enq() reservations, deq() reservations or is empty



# Dual Data Structure

- Methods take effect in two stages:
  - Reservation and fulfillment





# Dual Data structures

- Good things:

- ☐ Waiting threads spin on a locally cached flag
- ☐ Ensures fairness
- ☐ Linearizable

# Node class

```
private enum NodeType {ITEM, RESERVATION};
private class Node {
    volatile NodeType type;
    volatile AtomicReference<T> item;
    volatile AtomicReference<Node> next;

    Node (T myItem, NodeType myType) {
        item = new AtomicReference<T> (myItem);
        next = new AtomicReference<Node>(null);
        type = myType;
    }
}
```

# enq()

```
public void enq(T e) {
    Node offer = new Node (e, ITEM);
    while (true) {
        Node t = tail.get(), h = head.get();
        if (h == t || t.type == ITEM) {
            Node n = t.next.get();
            if (t == tail.get()) {
                if (n != null) {
                    tail.compareAndSet(t, n);
                } else if (t.next.CAS(n, offer)) {
                    tail.compareAndSet(t, offer);
                    while (offer.item.get() == e) {}
                    h = head.get();
                    if (offer == h.next.get())
                        head.compareAndSet(h, offer);
                    return; }}
    }
```

# enq()

*Create new node*

```
public void enq(T e) {  
    Node offer = new Node (e, ITEM);  
    while (true) {  
        Node t = tail.get(), h = head.get();  
        if (h == t || t.type == ITEM) {  
            Node n = t.next.get();  
            if (t == tail.get()) {  
                if (n != null) {  
                    tail.compareAndSet(t, n);  
                } else if (t.next.CAS(n, offer)) {  
                    tail.compareAndSet(t, offer);  
                    while (offer.item.get() == e) {}  
                    h = head.get();  
                    if (offer == h.next.get())  
                        head.compareAndSet(h, offer);  
                    return; }}  
    }
```

# enq()

*If the queue is empty  
OR if it contains only  
ITEMS...*

```
public void enq(T e) {
    Node offer = new Node (e, ITEM);
    while (true) {
        Node t = tail.get(), h = head.get();
        if (h == t || t.type == ITEM) {
            Node n = t.next.get();
            if (t == tail.get()) {
                if (n != null) {
                    tail.compareAndSet(t, n);
                } else if (t.next.CAS(n, offer)) {
                    tail.compareAndSet(t, offer);
                    while (offer.item.get() == e) {}
                    h = head.get();
                    if (offer == h.next.get())
                        head.compareAndSet(h, offer);
                    return;
                }
            }
        }
    }
}
```

# enq()

*...then no reservations  
only add ITEM*

```
public void enq(T e) {
    Node offer = new Node (e, ITEM);
    while (true) {
        Node t = tail.get(), h = head.get();
        if (h == t || t.type == ITEM) {
            Node n = t.next.get();
            if (t == tail.get()) {
                if (n != null) {
                    tail.compareAndSet(t, n);
                } else if (t.next.CAS(n, offer)) {
                    tail.compareAndSet(t, offer);
                    while (offer.item.get() == e) {}
                    h = head.get();
                    if (offer == h.next.get())
                        head.compareAndSet(h, offer);
                    return; }}
    }
```

# enq()

*If tail not last value  
move it up*

```
public void enq(T e) {
    Node offer = new Node (e, ITEM);
    while (true) {
        Node t = tail.get(), h = head.get();
        if (h == t || t.type == ITEM) {
            Node n = t.next.get();
            if (t == tail.get()) {
                if (n != null) {
                    tail.compareAndSet(t, n);
                } else if (t.next.CAS(n, offer)) {
                    tail.compareAndSet(t, offer);
                    while (offer.item.get() == e) {}
                    h = head.get();
                    if (offer == h.next.get())
                        head.compareAndSet(h, offer);
                    return; }}
        }
```

# enq()

*Else add new ITEM  
node to queue*

```
public void enq(T e) {
    Node offer = new Node (e, ITEM);
    while (true) {
        Node t = tail.get(), h = head.get();
        if (h == t || t.type == ITEM) {
            Node n = t.next.get();
            if (t == tail.get()) {
                if (n != null) {
                    tail.compareAndSet(t, n);
                } else if (t.next.CAS(n, offer)) {
                    tail.compareAndSet(t, offer);
                } while (offer.item.get() == e) {}
                h = head.get();
                if (offer == h.next.get())
                    head.compareAndSet(h, offer);
            }
            return;
        }
    }
}
```



# enq()

*Now we wait until it  
gets dequeued*

```
public void enq(T e) {
    Node offer = new Node (e, ITEM);
    while (true) {
        Node t = tail.get(), h = head.get();
        if (h == t || t.type == ITEM) {
            Node n = t.next.get();
            if (t == tail.get()) {
                if (n != null) {
                    tail.compareAndSet(t, n);
                } else if (t.next.CAS(n, offer)) {
                    tail.compareAndSet(t, offer);
                    while (offer.item.get() == e) {}
                    h = head.get();
                    if (offer == h.next.get())
                        head.compareAndSet(h, offer);
                    return; }}
    }
```

# enq()

*After it is dequeued  
remove node from queue*

```
public void enq(T e) {
    Node offer = new Node (e, ITEM);
    while (true) {
        Node t = tail.get(), h = head.get();
        if (h == t || t.type == ITEM) {
            Node n = t.next.get();
            if (t == tail.get()) {
                if (n != null) {
                    tail.compareAndSet(t, n);
                } else if (t.next.CAS(n, offer)) {
                    tail.compareAndSet(t, offer);
                    while (offer.item.get() == e) {}
                    h = head.get();
                    if (offer == h.next.get())
                        head.compareAndSet(h, offer);
                    return;
                }
            }
        }
    }
}
```

# enq()

```
...  
    } else {  
        Node n = h.next.get();  
        if (t != tail.get() || h != head.get() || n ==  
            null) {  
            continue;  
        }  
        boolean success = n.item.compareAndSet(null,e);  
        head.compareAndSet(h, n);  
        if (success)  
            return;  
    }  
}
```

*Otherwise fulfill  
reservation*

# enq()

```
...  
    } else {  
        Node n = h.next.get();  
        if (t != tail.get() || h != head.get() || n ==  
            null) {  
            continue;  
        }  
        boolean success = n.item.compareAndSet(null, e);  
        head.compareAndSet(h, n);  
        if (success)  
            return;  
    }  
}}
```

# enq()

*Make sure nothing has  
changed*

```
...
    } else {
        Node n = h.next.get();
        if (t != tail.get() || h != head.get() || n ==
            null) {
            continue;
        }
        boolean success = n.item.compareAndSet(null,e);
        head.compareAndSet(h, n);
        if (success)
            return;
    }
}
```

# enq()

*Change item in  
reservation node to enq  
item*

```
...  
    } else {  
        Node n = h.next.get();  
        if (t != tail.get() || h != head.get() || n ==  
            null) {  
            continue;  
        }  
        boolean success = n.item.compareAndSet(null,e);  
        head.compareAndSet(h, n);  
        if (success)  
            return;  
    }  
}
```