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# Eletricidade CA - Lista 2 Carla Beatriz da Silva Teixeira - S2 em Telemática

1º) Resolva c/ números complexos, na forma polarizadora:

a)  $(2 + j3) + (5 - j2) = 7 + j$

b)  $(10 - j5) + (7 + j2) = 17 - j3$

c)  $(5 + j5) - (2 + j3) = 3 + j2$

d)  $(20 + j5) - (12 - j2) = 8 + j3$

2º) Resolva c/ números complexos, na forma polarizadora:

a)  $20 \angle 30^\circ + 20 \angle 45^\circ =$

$X_1 = 20 \cos(30) = 17,32$  }  $= 17,32 + j10$

$Y_1 = 20 \sin(30) = 10$  }

$X_2 = 20 \cos(45) = 14,14$  }  $= 14,14 + j14,14$

$Y_2 = 20 \sin(45) = 14,14$  }

Somando:  $31,46 + j24,14$

$Z = \sqrt{(31,46^2 + 24,14^2)}$  }  $Z = 39,65$

$\theta = \arctan\left(\frac{24,14}{31,46}\right)$  }  $\theta = 37,40^\circ$

b)  $15 \angle 20^\circ + 10 \angle 45^\circ =$

$X_1 = 15 \cos(20) = 14,09$  }  $= 14,09 + j5,13$

$Y_1 = 15 \sin(20) = 5,13$  }

$X_2 = 10 \cos(45) = 7,07$  }  $= 7,07 + j7,07$

$Y_2 = 10 \sin(45) = 7,07$  }

Somando:  $21,16 + j12,2$

$Z = \sqrt{(21,16^2 + 12,2^2)}$  }  $Z = 24,42$

$\theta = \arctan\left(\frac{12,2}{21,16}\right)$  }  $\theta = 29,96^\circ$

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c)  $30 < 40^\circ - 20 < 45^\circ =$

$X_1 = 30 \text{ cop } (40) = 22, 98 \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} = 22, 98 + g 19, 28$

$Y_1 = 30 \text{ pen } (40) = 19, 28$

$X_2 = 20 \text{ cop } (45) = 14, 14 \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} = 14, 14 + g 14, 14$

$Y_2 = 20 \text{ pen } (45) = 14, 14$

Subtraendo:  $8, 84 + g 5, 14$

$\rightarrow Z = \sqrt{(8, 84^2 + 5, 14^2)} \rightarrow Z = 10, 22$

$\phi = \text{arc tang } \left( \frac{5, 14}{8, 84} \right) \rightarrow \phi = 30, 57^\circ$

d)  $35 < 30^\circ - 20 < 15^\circ =$

$X_1 = 35 \text{ cop } (30) = 30, 31 \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} = 30, 31 + g 17, 5$

$Y_1 = 35 \text{ pen } (30) = 17, 5$

$X_2 = 20 \text{ cop } (15) = 19, 31 \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} = 19, 31 + g 5, 17$

$Y_2 = 20 \text{ pen } (15) = 5, 17$

Subtraendo:  $11 + g 12, 33$

$\rightarrow Z = \sqrt{(11^2 + 12, 33^2)} \rightarrow Z = 16, 52$

$\phi = \text{arc tang } \left( \frac{12, 33}{11} \right) \rightarrow \phi = 48, 26^\circ$

(3º) Regras:

a)  $(20 < 30^\circ) \cdot (20 < 45^\circ) =$

$\frac{(20) \cdot (20)}{30 + 45} = \frac{400}{75^\circ}$

b)  $(15 < 20^\circ) \cdot (10 < 45^\circ) =$

$\frac{(15) \cdot (10)}{20 + 45} = \frac{150}{65^\circ}$

c)  $(30 < 40^\circ) / (20 < 45^\circ) =$

$\frac{(30) \cdot (20)}{40 + 45} \rightarrow \frac{600}{85^\circ}$

d)  $(35 < 30^\circ) / (20 < 15^\circ) =$

$\frac{(35) \cdot (20)}{30 + 15} = \frac{700}{45^\circ}$



4º Regra:

$$a) (20 < 30^\circ) \cdot (2 + j5) =$$

$$Z = \sqrt{2^2 + 5^2} \rightarrow Z = 5,38$$

$$\phi = \arctan\left(\frac{5}{2}\right) \rightarrow \phi = 68,19^\circ$$

$$\therefore (20 / 30^\circ) \cdot (5,38 / 68,19^\circ)$$

$$\frac{(20) \cdot (5,38)}{30^\circ + 68,19^\circ} \rightarrow \frac{107,6}{98,19^\circ}$$

$$b) (15 < 20^\circ) \cdot (10 - j2) =$$

$$Z = \sqrt{10^2 + (-2)^2} \rightarrow Z = 10,19$$

$$\phi = \arctan\left(\frac{2}{10}\right) \rightarrow \phi = 11,3^\circ$$

$$\therefore (20 / 30^\circ) \cdot (10,19 / 11,3^\circ)$$

$$\frac{(20) \cdot (10,19)}{30^\circ + 11,3^\circ} \rightarrow \frac{226}{41,3^\circ}$$

$$c) (2 + j5) / (20 < 45^\circ) =$$

$$Z = \sqrt{2^2 + 5^2} \rightarrow Z = 5,38$$

$$\phi = \arctan\left(\frac{5}{2}\right) \rightarrow \phi = 68,19^\circ$$

$\therefore$

$$(5,38 / 68,19^\circ) / (20 / 45^\circ)$$

$$\frac{(5,38) / (68,19^\circ - 45^\circ)}{(20) / (5,38)} \rightarrow \frac{3,71}{23,19^\circ}$$

$$d) (10 - j2) / (20 < 35^\circ) =$$

$$Z = \sqrt{10^2 + (-2)^2} \rightarrow Z = 10,19$$

$$\phi = \arctan\left(\frac{2}{10}\right) \rightarrow \phi = 11,3^\circ$$

$$(10,19 / 11,3^\circ) / (20 / 35^\circ) \rightarrow \frac{0,51}{-3,7^\circ}$$