# Constant-delay Enumeration for Lorem Ipsum

## arlos Olguin ⊠

ontificia Universidad Católica de Chile

## cristian Riveros ⊠

ontificia Universidad Católica de Chile

#### — Abstract

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112 ACM Subject Classification Theory of computation → Database theory

eywords and phrases Streams, query evaluation, enumeration algorithms.

#### Introduction

Cristian: Here a comment from Cristian.

El siguiente paper abordara como se puede relacion el Strahler number con diversas aplicaciones en el undo, tal que, la centralidad planteada en un paper anterior tendra un papel de suma importancia para antear todo.

### **Preliminaries**

**raphs**. A graph is a pair G = (V, E) where V is a finite set and  $E \subseteq V \times V$  is a finite relation. Each par of extex let be  $(v_1, v_2)$ ,  $v_1, v_2 \in V$  this set of vertex its called edges and can be directed or not, so the edges E. A path in a graph is a sequence of non-repeated nodes connected through edges present in a graph, if were exist a path between two vertex, this vertex are called connected. An example, let be  $x, y \in V$  a path on be expressed so  $\{x, x_1, x_2, \dots, y_1, y_2, \dots, y_n\}$  with  $x, x_i, y_i, y \in V$ 

rees. A tree is an undirected graph in which any two vertices are connected by only and only one path. A oted tree is referred as a tree with a vertex who serves as the "root" of the tree, being a references to the hers vertices in the tree.

plicacions.

## Main results

The present here the data structure, called Enumerable Compact Sets with Shifts, to compactly store the outputs of evaluating an annotated automaton over a straight-line program. This structure extends the numerable Compact Sets (ECS) introduced in [DurandG07] (we note that a similar data structure for instant-delay enumeration was previously proposed in [BaganDG07]). Indeed, people have also used CS extensions in [DurandG07, BucchiGQRV22]. This new version extends ECS by introducing a shift perator, which helps compactly move all outputs' positions with a single call. Although the shift nodes quire a revision of the complete ECS model, it simplifies the evaluation algorithm in Section ?? and achieves atput-linear delay for enumerating all outputs. For completeness of presentation, this section goes through I main details as in [BaganDG07].

**Lemma 1.** Given an SLP S, we can compute the values of |str(A)| for all non-terminals A in S in time (|S|).

From now on, we assume that all SLPs are in Chomsky normal form, due to the following result:

**Theorem 2** (SLP Balancing theorem). There is a  $c \in \mathbb{N}$  such that any given  $SLP \ S$  for string w can be ansformed in time  $\mathcal{O}(|S|)$  into a  $SLP \ S'$  for w in Chomsky normal form with  $|S'| \le c \cdot |S|$ .

**Algorithm 1** The enumeration algorithm of an unambiguous  $\mathcal{A} = (Q, \Sigma, \Omega, \Delta, q_0, F)$  over a SLP-compressed exament  $S = (N, \Sigma, R, S_0)$ .

```
: procedure Evaluation(\mathcal{A}, S)
                                                                       14: procedure NonTerminal(X)
                                                                                 M_X \leftarrow \{[p,q] \rightarrow \bot \mid p,q \in Q, p \neq q\} \cup
      Initialize \mathcal{D} as an empty \perp.
                                                                                              \{[p,q] \rightarrow \epsilon \mid p,q \in Q, p = q\}
      NonTerminal(S_0)
                                                                                 \mathsf{len}_X \leftarrow 0
      v \leftarrow \bot
                                                                       16:
      for each q \in F do
                                                                       17:
                                                                                 for i = 1 to |R(X)| do
           v \leftarrow \text{UNION}(v, M_{S_0}[q_0, q])
                                                                                     Y \leftarrow R(X)[i]
                                                                       18:
                                                                                     if M_Y is not defined then
                                                                       19:
      Enumerate(v, \mathcal{D})
                                                                                          if Y \in \Sigma then
                                                                       20:
: procedure TERMINAL(a)
                                                                                              TERMINAL(Y)
                                                                       21:
       M_a \leftarrow \{[p,q] \rightarrow \bot \mid p,q \in Q\}
                                                                                          else
                                                                       22:
      for each (p, a, o, q) \in \Delta do
                                                                                              NonTerminal(Y)
                                                                       23:
           M_a[p,q] \leftarrow \text{UNION}(M_a[p,q], \text{ADD}(o))
                                                                                      M_X \leftarrow M_X \otimes \operatorname{SHIFT}(M_Y, \operatorname{len}_X)
                                                                       24:
      for each (p, a, q) \in \Delta do
                                                                       25:
                                                                                      len_X \leftarrow len_X + len_Y
           M_a[p,q] \leftarrow \text{UNION}(M_a[p,q], \epsilon)
```

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**Proposition 3.** Given an SLP S, we can compute the values of |str(A)| for all non-terminals A in S in  $ne \mathcal{O}(|S|)$ .

roof Sketch. This is a short paragraph that gives an idea of the full proof to the statement above. ◀

The proposition above is Proposition??. The complete proof can be found in the full version of the paper.

#### Conclusions

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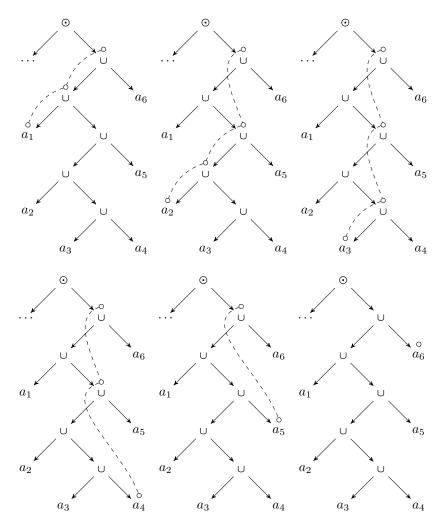


Figure 1 An example iteration of trav and move. The sequences of nodes joined by dashed lines represent a stack, where the first one was obtained after calling trav over the topmost union node, and the following five are obtained repeated applications of move(St).

## **Proofs from Section ??**

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## **Proofs of Section ??**

## **Proof of Lemma** ??

.1

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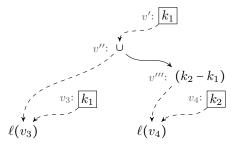


Figure 2 Gadget used in Theorem ??.

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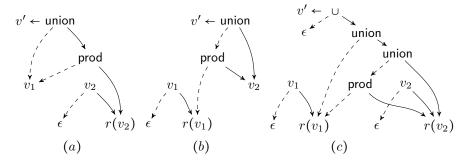
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#### .2 Proof of Theorem ??

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**Figure 3** Gadgets for product as defined for an  $\mathcal{D}$  with the  $\epsilon$ -node.

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## .3 Proof of Proposition ??

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Claim 4. Fix  $k \in \mathbb{N}$ . Let  $C_k$  be the class of all duplicate-free and k-bounded D that satisfy the  $\epsilon$  condition. hen one can solve the problem  $\mathtt{Enum}[C_k]$  with output-linear delay and without preprocessing (i.e. constant reprocessing time).

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