

```

NEdistW[n_, p_, q_: 1, t_, opts___] :=
Module[{d, pr1, pr2, pr3, adn, func, st, v, rj, a, xr, prd},
Options[NEdistW] = {dist → 1, prcm → 300,
prcpa → 200, prcf → 16, ad → 0, function → 1, stat → 1};
d = dist /. {opts} /. Options[NEdistW];
pr1 = prcm /. {opts} /. Options[NEdistW];
pr2 = prcf /. {opts} /. Options[NEdistW];
pr3 = prcpa /. {opts} /. Options[NEdistW];
adn = ad /. {opts} /. Options[NEdistW];
func = function /. {opts} /. Options[NEdistW];
st = stat /. {opts} /. Options[NEdistW];
v = IntModule[n, p, q, st, d, pr1, pr3, adn];
rj = If[st == 1, Rj1[n, p],
If[st == 2, Rj1[n, p - {0, 1}], If[st == 3, Rj3[n, p], Rj4[n, p, q]]];
g = If[st == 1, g = Total[p], If[st == 2, g = Total[p] - 1, g = p]];
a = Table[(n - j) / n, {j, 2, g}];
xr = Rationalize[t, 0];
If[func == 3,
prd = Product[a[[j]]^rj[[j]] * (a[[j]] - I * xr)^(-rj[[j]]), {j, 1, g - 1}];
If[d == 2, (v[[1]] * v[[4]]^v[[2]] * (v[[4]] - I * xr)^(-v[[2]])) +
(1 - v[[1]]) * v[[4]]^v[[3]] * (v[[4]] - I * xr)^(-v[[3]])) * prd,
If[d == 3, (v[[1]] * v[[6]]^v[[3]] * (v[[6]] - I * xr)^(-v[[3]]) +
v[[2]] * v[[6]]^v[[4]] * (v[[6]] - I * xr)^(-v[[4]]) +
(1 - v[[1]] - v[[2]]) * v[[6]]^v[[5]] * (v[[6]] - I * xr)^(-v[[5]])) *
prd, v[[2]]^v[[1]] * (v[[2]] - I * xr)^(-v[[1]]) * prd]],
If[func == 2, GNIG[r_, b_, l_, a_, w_] := GNIGpdf[r, b, l, a, w],
GNIG[r_, b_, l_, a_, w_] := GNIGcdf[r, b, l, a, w]];
If[d == 2, SetPrecision[v[[1]] * GNIG[rj, v[[2]], a, v[[4]], xr] +
(1 - v[[1]]) * GNIG[rj, v[[3]], a, v[[4]], xr], pr2],
If[d == 3, SetPrecision[v[[1]] * GNIG[rj, v[[3]], a, v[[6]], xr] +
v[[2]] * GNIG[rj, v[[4]], a, v[[6]], xr] +
(1 - v[[1]] - v[[2]]) * GNIG[rj, v[[5]], a, v[[6]], xr], pr2],
SetPrecision[GNIG[rj, v[[1]], a, v[[2]], xr], pr2]]]

IntModule[n_, p_, q_: 1, st_, d_, pr1_: 300, pr3_, adn_] := Module[{mm},
mm = Table[SetPrecision[
If[st == 1, MomPhi21[n, p, h], If[st == 2, MomPhi21[n, p - {0, 1}, h], If[st == 3,
MomPhi23[n, p, h], MomPhi24[n, p, q, h]]], pr1], {h, 1, 2 * d}];
If[d == 1, Module1[mm], If[d == 2, Module2[mm],
Module3[mm, pr3, adn]]]

MomPhi21[n_, p_, h_] := I^(-h) * D[Phi21[n, p, t], {t, h}] /. t → 0

Phi21[n_, pk_, t_] := Module[{p, kstar},
p = Total[pk];
kstar = Floor[Count[pk, _?OddQ] / 2];
(Gamma[(n - 1) / 2] * Gamma[n / 2 - 1 - n / 2 * I * t] /
(Gamma[n / 2 - 1] * Gamma[(n - 1) / 2 - n / 2 * I * t]))^kstar

MomPhi23[n_, p_, h_] := I^(-h) * D[Phi23[n, p, t], {t, h}] /. t → 0

```

```

Phi23[n_, p_, t_] :=
  Product[Gamma[(n - 1) / 2 + (j - 1) / p] * Gamma[(n - 1) / 2 - n / 2 * I * t] /
    (Gamma[(n - 1) / 2 + (j - 1) / p - n / 2 * I * t] * Gamma[(n - 1) / 2]),
    {j, 1, p - Floor[p / 2]}] * Product[Gamma[(n - 1) / 2 + (j - 1) / p] *
    Gamma[n / 2 - n / 2 * I * t] / (Gamma[(n - 1) / 2 + (j - 1) / p - n / 2 * I * t] *
    Gamma[n / 2]), {j, 1 + p - Floor[p / 2], p}]

MomPhi24[n_, p_, q_, h_] := I^(-h) * D[Phi24[n, p, q, t], {t, h}] /. t -> 0

Phi24[n_, p_, q_, t_] := Module[{aj, bjk, bjks, bpks},
  aj = Table[n - 1, {j, 1, Floor[p / 2]}];
  bjk = Table[Table[(k - 2 * j) / q, {k, 1, q}], {j, 1, Floor[p / 2]}];
  bjks = Floor[bjk];
  ap = (n - 1) / 2;
  bpk = Table[(2 * k - p - 1) / (2 * q), {k, 1, q}];
  bpks = Floor[bpk];
  Product[Product[
    Gamma[aj[[j]] + bjk[[j, k]]] * Gamma[aj[[j]] + bjks[[j, k]] - n * I * t] /
    (Gamma[aj[[j]] + bjks[[j, k]]] * Gamma[aj[[j]] + bjk[[j, k]] - n * I * t]),
    {k, 1, q}], {j, 1, Floor[p / 2]}] * (Product[Gamma[ap + bpk[[k]]] *
    Gamma[ap + bpks[[k]] - n / 2 * I * t] / (Gamma[ap + bpks[[k]]] *
    Gamma[ap + bpk[[k]] - n / 2 * I * t]), {k, 1, q})^Mod[p, 2]
]

Module1[mm_] :=
  {mm[[1]]^2 / (mm[[2]] - mm[[1]]^2), mm[[1]] / (mm[[2]] - mm[[1]]^2)}

Module2[mm_] := Module[{},
  Sort[Cases[{p1, r1, r2, m} /.
    NSolve[Table[mm[[h]] == MomMixGam[{p1}, {r1, r2}], {m, m}, h], {h, 1, 4}],
    {p1, r1, r2, m}], {_Real, _Real, _Real, _Real}][[2]]
]

Module3[mm_, prcpar_: 200, ad_: 0] := Module[{vecn},
  vecn = Module2[p, q, n, prcm];
  {p1, p2, r1, r2, r3, m} /. FindRoot[
    Table[mm[[h]] == MomMixGam[{p1, p2}, {r1, r2, r3}, {m, m, m}, h], {h, 1, 6}],
    {p1, vecn[[1]]}, {p2, .99 * (1 - vecn[[1]])}, {r1, vecn[[2]]},
    {r2, vecn[[3]]}, {r3, ad + 2 * vecn[[3]] - vecn[[2]]},
    {m, vecn[[4]]}, WorkingPrecision -> prcpar]
]

Rj1[n_, pk_] := Module[{p, kstar, hj},
  p = Total[pk];
  kstar = Floor[Count[pk, _?OddQ] / 2];
  hj = Table[Count[pk - (j - 1), _?Positive], {j, 1, p - 2}] - 1;
  rj = Table[0, {j, 1, p}];
  rj[[3]] = hj[[1]] - kstar; rj[[4]] = hj[[2]] + kstar;
  Do[rj[[j]] = rj[[j - 2]] + hj[[j - 2]], {j, 5, p}];
  Drop[rj, 1]
]

```

```
Rj3[n_, p_] := Table[Floor[(p - j + 2) / 2], {j, 2, p}]
```

```
Rj4[n_, p_, q_] := Module[{a, a1, a2, p2, q2},
  a = Floor[(p - 1) / q];
  a1 = Floor[(q - 1) / q * (p - 1) / 2];
  a2 = Floor[(q - 1) / q * (p + 1) / 2];
  p2 = Floor[p / 2]; q2 = Floor[q / 2];
  rj = Table[0, {j, 1, p - 1}];
  Do[rj[[j]] =
    q2 * ((j - 1) * q - 2 * Mod[q + 1, 2] * Floor[j / 2] + Floor[(q + Mod[j, 2]) / 2]), {j,
    1, a}];
  rj[[a + 1]] = - (p2 - a * q2) ^ 2 + q * (p2 - Floor[(a + 1) / 2]) +
    Mod[q, 2] * (a * p2 + Mod[a, 2] / 4 - a^2 / 4 - a^2 * q2);
  Do[rj[[j]] = q * (p2 - Floor[j / 2]), {j, a + 2, Min[p - 2 * a1, p - 1]}];
  Do[rj[[j]] = q * (p2 - Floor[j / 2]), {j, 2 + p - 2 * a1, 2 * p2 - 1, 2}];
  Do[rj[[j]] = q * (Floor[(p + 1) / 2] - Floor[j / 2]), {j, 1 + p - 2 * a1, p - 1, 2}];
  rj[[p - 1 - 2 * a1]] = rj[[p - 1 - 2 * a1]] +
    Mod[p, 2] * (a2 - a1) * (q - (p - 1) / 2 + q * Floor[p / (2 * q)]);
  rj
]
```

```
GNIGpdf[r_, b_, l_, a_, w_] := Module[{g, c},
  If[
    Count[r, _Integer] == Length[r] && And@@Positive[r] && And@@Positive[l],
    g = Length[r];
    c = Makeec[r, l, g];
    Product[l[[j]]^r[[j]], {j, 1, g}] *
      a^b * Sum[Exp[-l[[j]] * w] * Sum[c[[j]][[k]] *
        Gamma[k] / Gamma[k + b] * w^(k + b - 1) *
          Hypergeometric1F1[b, k + b, - (a - l[[j]]) * w],
        {k, 1, r[[j]]}], {j, 1, g}]
  ] ]
```

```
GNIGcdf[r_, b_, l_, a_, w_] := Module[{g, c},
  g = Length[r];
  c = Makeec[r, l, g];
  a^b * w^b / Gamma[b + 1] * Hypergeometric1F1[b, b + 1, -a w] -
    Product[l[[j]]^r[[j]], {j, 1, g}] * a^b *
      Sum[Exp[-l[[j]] * w] * Sum[c[[j]][[k]] / l[[j]]^k * Gamma[k] *
        Sum[w^(b + i) * l[[j]]^i / Gamma[b + 1 + i] *
          Hypergeometric1F1[b, b + 1 + i, - (a - l[[j]]) w], {i, 0, k - 1}],
        {k, 1, r[[j]]}],
    {j, 1, g}]
]
```

```
Makeec[r_, l_, p_] := Module[{c},
  c = Table[Table[1, {j, 1, Max[r]}], {i, 1, p}];
  Table[
    c = ReplacePart[c, (Product[(l[[j]] - l[[i]])^(-r[[j]]), {j, 1, i - 1}] *
      Product[(l[[j]] - l[[i]])^(-r[[j]]), {j, i + 1, p}]) /
      (r[[i]] - 1)!, {i, r[[i]]}], {i, 1, p}];
  Table[Table[c = ReplacePart[c, Sum[(r[[i]] - k + j - 1)! *
```

```

      (Sum[r[[h]] / (l[[i]] - l[[h]])^j, {h, 1, i - 1}] +
      Sum[r[[h]] / (l[[i]] - l[[h]])^j, {h, i + 1, p}]) *
      c[[i]] [(r[[i]] - (k - j))] / (r[[i]] - k - 1)!, {j, 1, k} / k,
      {i, r[[i]] - k}, {k, 1, r[[i]] - 1}, {i, 1, p}];
    c
  ]

```