

## Task2 (2)

August 23, 2022

Task 2: Input encoding

```
[1]: import numpy as np
      from qiskit.algorithms.linear_solvers.numpy_linear_solver import NumPyLinearSolver
```

<frozen importlib.\_bootstrap>:219: RuntimeWarning: scipy.\_lib.messagestream.MessageStream size changed, may indicate binary incompatibility. Expected 56 from C header, got 64 from PyObject

Make a quantum circuit that prepares the input state

```
[2]: #
      # Function that randomly pick a 2 dimentional state to simulate position of
      # satellite
      #
      from random import randrange
      def random_quantum_state():
          # quantum state
          quantum_state=[0,0]
          random_number1 = randrange(-100,101)
          #print("the first number is",random_number1)
          random_number2 = randrange(-100,101)
          #print("the second number is",random_number2)
          #probability=random_number1**2+random_number2**2
          # print("probability is",probability)
          #amplitude1=random_number1/(probability**0.5)
          # print("amplitude 1 is",amplitude1)
          #amplitude2=random_number2/(probability**0.5)
          # print("amplitude 2 is",amplitude2)
          quantum_state[0]=random_number1
          quantum_state[1]=random_number2
          #sum=amplitude1**2+amplitude2**2
          #print("sum=",sum)
          return quantum_state
```

We make a function that normalizes the state we made in the function above

```
[3]: #
# Function that normalizes a 2 dimensional state to simulate quantum state of
# the position of satellite
#
def normal_quantum_state(quantum_state):
    probability=quantum_state[0]**2+quantum_state[1]**2
    amplitude1=quantum_state[0]/(probability**0.5)
    amplitude2=quantum_state[1]/(probability**0.5)
    quantum_state[0]=amplitude1
    quantum_state[1]=amplitude2
    return quantum_state
```

We can make sure our functions work properly with the following 2 cells.

```
[4]: #
# check randomly pick function
#
rs = random_quantum_state()
rs
```

```
[4]: [38, -85]
```

```
[5]: #check function that normilizes the state
n_quantum_state = normal_quantum_state(rs)
n_quantum_state
```

```
[5]: [0.4081305412501237, -0.9129235791121187]
```

We define a fuction that checks whether the picked quantum state is valid

```
[6]: # Function that checks whether the picked quantum state is valid
from random import randrange
def check_random_quantum_state(quantum_state):
    value=0
    for i in range(len(quantum_state)):
        value+=quantum_state[i]**2
    if (value - 1)**2 < 0.00000001:
        return True
    else:
        return False
```

We can make sure our function work properly with the following cell

```
[7]: #
# check function that states if the quantum state is valid
#
check_random_quantum_state(n_quantum_state)
```

[7]: True

Finally we make a quantum circuit that prepares the input state, here we consider 10 satellites.

```
[8]: #Function to prepare the quantum state of N satellites
quantum_satellites=[] #this will be our quantum state for the N satellites
N=10 #Number of satellites
for i in range(N):
    picked_quantum_state=random_quantum_state() #call function that randomly
    ↪pick a 2 dimensional state to simulate position of satellite
    n_state = normal_quantum_state(picked_quantum_state) # Function that
    ↪normalizes a 2 dimensional state to simulate quantum state of the position
    ↪of satellite
    print(n_state,"this is randomly picked quantum state for satellite",i)
    print("Is it valid?",check_random_quantum_state(n_state)) #check if it is a
    ↪valid quantum state
    if check_random_quantum_state(n_state)==True: #if it is a quantum valid
    ↪quantum state then save it to our quantum state for N satellites
        x= n_state[0] #define x component
        y = n_state[1] #define y component
        quantum_satellites.append(x) #save x position of satellite on our
        ↪quantum state
        quantum_satellites.append(y) #save y position of satellite on our
        ↪quantum state
        print() # print an empty line
print("The input quantum state for the",N,"satellites is given by the following
↪state")
print()
print("x=",quantum_satellites) #print the quantum state for the N satellites
```

```
[0.9449860734402582, 0.3271105638831663] this is randomly picked quantum state
for satellite 0
Is it valid? True
```

```
[0.8372705045624257, -0.546788900938727] this is randomly picked quantum state
for satellite 1
Is it valid? True
```

```
[-0.5985256885300932, 0.8011036138787402] this is randomly picked quantum state
for satellite 2
Is it valid? True
```

```
[-0.9496887635303413, -0.3131952305259636] this is randomly picked quantum state
for satellite 3
Is it valid? True
```

`[-0.696785684263249, 0.7172793808592269]` this is randomly picked quantum state  
for satellite 4  
Is it valid? True

`[0.7022134834058589, 0.7119664484531625]` this is randomly picked quantum state  
for satellite 5  
Is it valid? True

`[-0.973417168333576, -0.2290393337255473]` this is randomly picked quantum state  
for satellite 6  
Is it valid? True

`[-0.4948386187009886, -0.8689848913773458]` this is randomly picked quantum state  
for satellite 7  
Is it valid? True

`[-0.9989685402102997, 0.045407660918649985]` this is randomly picked quantum  
state for satellite 8  
Is it valid? True

`[0.7196931822512745, 0.6942922464071118]` this is randomly picked quantum state  
for satellite 9  
Is it valid? True

The input quantum state for the 10 satellites is given by the following state

```
x= [0.9449860734402582, 0.3271105638831663, 0.8372705045624257,  
-0.546788900938727, -0.5985256885300932, 0.8011036138787402,  
-0.9496887635303413, -0.3131952305259636, -0.696785684263249,  
0.7172793808592269, 0.7022134834058589, 0.7119664484531625, -0.973417168333576,  
-0.2290393337255473, -0.4948386187009886, -0.8689848913773458,  
-0.9989685402102997, 0.045407660918649985, 0.7196931822512745,  
0.6942922464071118]
```

We see that our quantum state can make a quantum circuit that prepares the input state for  $N$  satellites. We choose that it made smaller quantum states in each iteration, rather than performing the measurement of positions of the  $N$  satellites and then preparing the quantum state, the introduction of another for cycle would increase the complexity of the system.

[ ]: